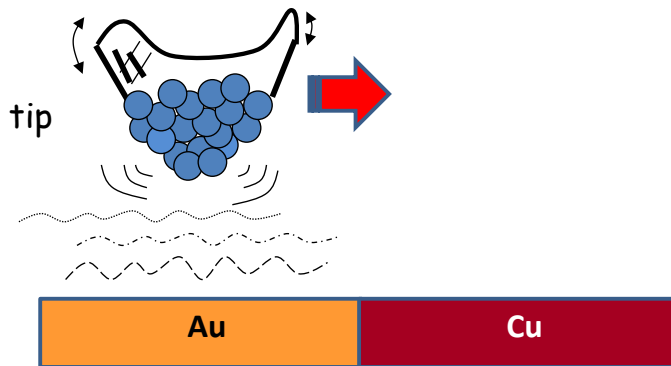


Homework No. 2

Fundamentals of AFM: Part I

Lectures: P1_Wk2_L1 - P1_Wk2_L6

Problem 1: A tip of radius 5 nm is sequentially positioned 1 nm above a flat substrate that has two different regions. One region of the substrate is made from Au, the other from Cu.



Q1.1. Assuming the vdW interaction dominates the tip-substrate interaction, and assuming the vdW interaction between a tip atom and a Au atom is the same as the interaction between a tip atom and a Cu atom, which of the following statements is likely to be true?

- a) The force acting on the tip when it is over the Au region will be the same as when the tip is over the Cu region
- b) The force acting on the tip when it is over the Au region will be about 2 times greater than when the tip is over the Cu region
- c) The force acting on the tip when it is over the Au region will be about 70% of the force when the tip is over the Cu region
- d) The force acting on the tip when it is over the Au region will be about 25% of the force when the tip is over the Cu region

Problem 2: Highly oriented pyrolytic graphite (HOPG) is a layered form of C that is commonly used as a substrate material used in many AFM studies. It is well documented that most materials deposited on HOPG do not strongly adhere to this substrate. This must imply that

- a) HOPG has a very high surface energy
- b) HOPG has the remarkable ability to adjust its surface energy depending on the deposited material
- c) HOPG must be an amorphous solid
- d) HOPG has a very low surface energy

Problem 3: The Derjaguin approximation states that

$$F_{plane-sphere}(d) = 2\pi R_{tip} \left(\frac{U_{plane-plane}(d)}{A} \right)$$

If the sphere comes into **contact** with the plane, then $d=a_0$ and we have

$$F_{plane-sphere}(a_0) = 2\pi R_{tip} (2\gamma)$$

where γ is the surface energy of the tip and substrate (assumed in this case to be of identical materials).

Q3.1 Suppose a Si tip contacts a Si wafer. It is well known that both the tip and wafer are coated with an amorphous, native oxide layer (SiO_2 , silica). What would be a good estimate for the surface energy of the tip and wafer?

- a) 3 mJ/m²
- b) 30 mJ/m²
- c) 300 mJ/m²
- d) 3000 mJ/m²

Q3.2 If the tip has a radius of 50 nm, using the value of κ from Q3.1, estimate the adhesive force between the tip and the substrate when they come into contact?

- a) 1.9 nN
- b) 19 nN
- c) 190 nN
- d) 1900 nN

Problem 4: Consider the same Si tip (50 nm radius) pressed against the same flat Si wafer discussed in **problem 3** above.

Q4.1 What is the approximate Young's modulus for silica that we should use to describe the contact mechanics in this situation?

- a) 0.066 GPa
- b) 0.66 GPa
- c) 6.6 GPa
- d) 66 GPa

Q4.2 From the Hertz model, what is the contact radius when a force of 10 nN is applied to the tip? Assume the Poisson ratio of silica is 0.17.

- a) 0.22 nm
- b) 2.2 nm
- c) 22 nm
- d) 220 nm

Q4.3 From the Hertz model, estimate the deformation (indentation) that will result when 10 nN is applied.

- a) 9.7 nm
- b) 0.97 nm
- c) 0.097 nm
- d) 0.0097 nm

Q4.4 Typically, the thickness of native SiO₂ layer on Si is about 1 nm. At what applied force will the tip/substrate indentation equal this amount? Use the Hertz model.

- a) 320 nN
- b) 32 nN
- c) 3.2 nN
- d) 0.32 nN