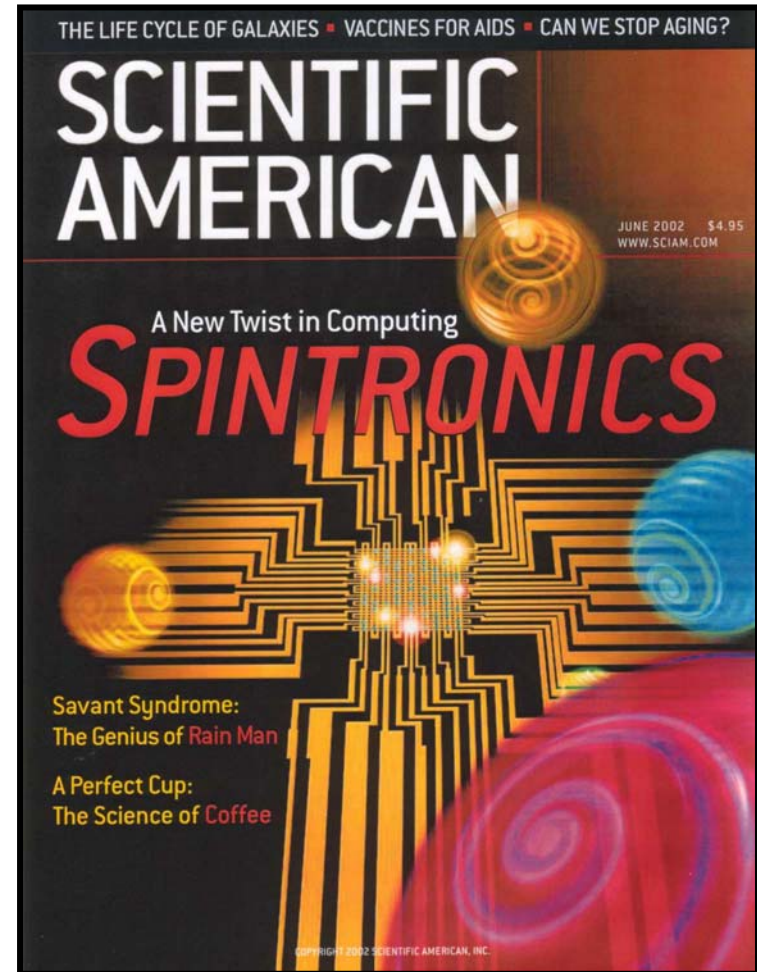
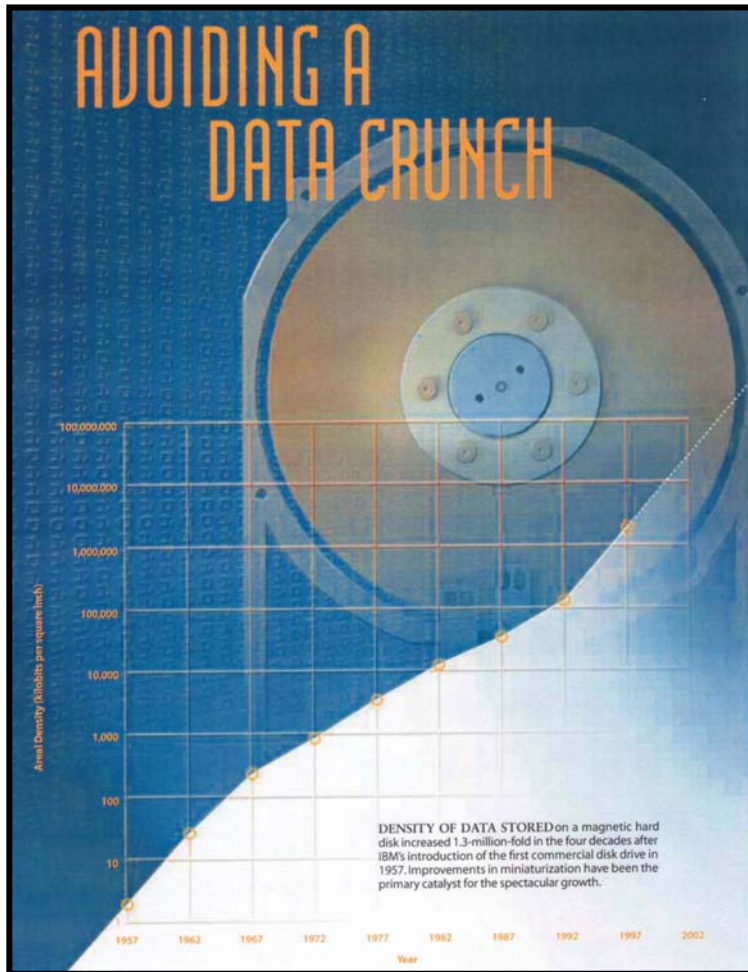


# Nanomaterials

## Lecture 15: Nanomagnetism

# Nanomagnetism



# Review “Macro” Magnetism

At thermal equilibrium, define:

(1) Magnetization density: 
$$M = -\frac{1}{V} \frac{\partial F}{\partial H}$$

$V$  = volume,  $H$  = magnetic field,  
 $F$  = magnetic Helmholtz free energy

(2) Susceptibility: 
$$\chi = \frac{\partial M}{\partial H} = -\frac{1}{V} \frac{\partial^2 F}{\partial H^2}$$

# Review “Macro” Magnetism

NOTE: Force per unit volume ( $f$ ) exerted on a specimen by an inhomogeneous magnetic field is:

$$f = -\frac{1}{V} \frac{\partial F}{\partial x} = -\frac{1}{V} \frac{\partial F}{\partial H} \frac{\partial H}{\partial x} = M \frac{\partial H}{\partial x}$$

To determine  $M$  and  $\chi$ , quantum mechanics is required; in particular, we need to consider the modification to the Hamiltonian by spin.

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# Review “Macro” Magnetism

- (1) Diamagnetism: negative susceptibility
  - induced moment opposes applied field (similar to Lenz’s Law)
  - common for noble gas atoms and alkali halide ions (e.g., He, Ne, F<sup>-</sup>, Cl<sup>-</sup>, Li<sup>+</sup>, Na<sup>+</sup>, ....)
  
- (2) Paramagnetism: positive susceptibility
  - induced moment is favored by applied field (but is opposed by thermal disorder)
  - magnetization is immediately lost upon removal of field
  - common for isolated rare earth ions, iron (group 3d) ions (e.g., Sm<sup>+</sup>, Er<sup>+</sup>, Fe<sup>3+</sup>, Co<sup>2+</sup>, Ni<sup>2+</sup>, ....)

# Magnetic Ordering

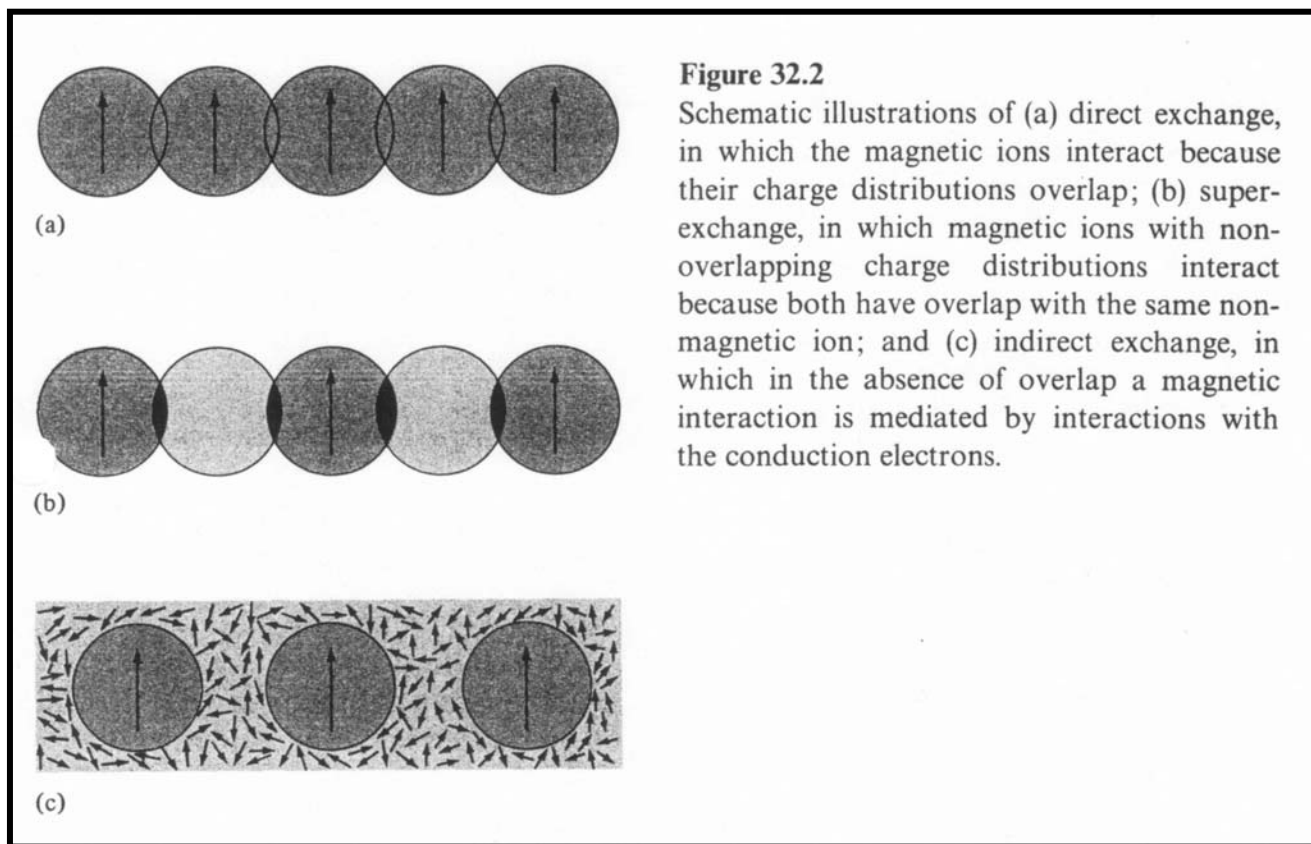
In solids, electron-electron interactions lead to magnetic ordering (one of the less well-developed theories in solid state physics)

Types of interactions:

- (1) Exchange interaction (electrostatic)
- (2) Dipolar interaction (spin-spin coupling)
- (3) Anisotropy interaction (spin-orbit coupling)



# Exchange Interactions



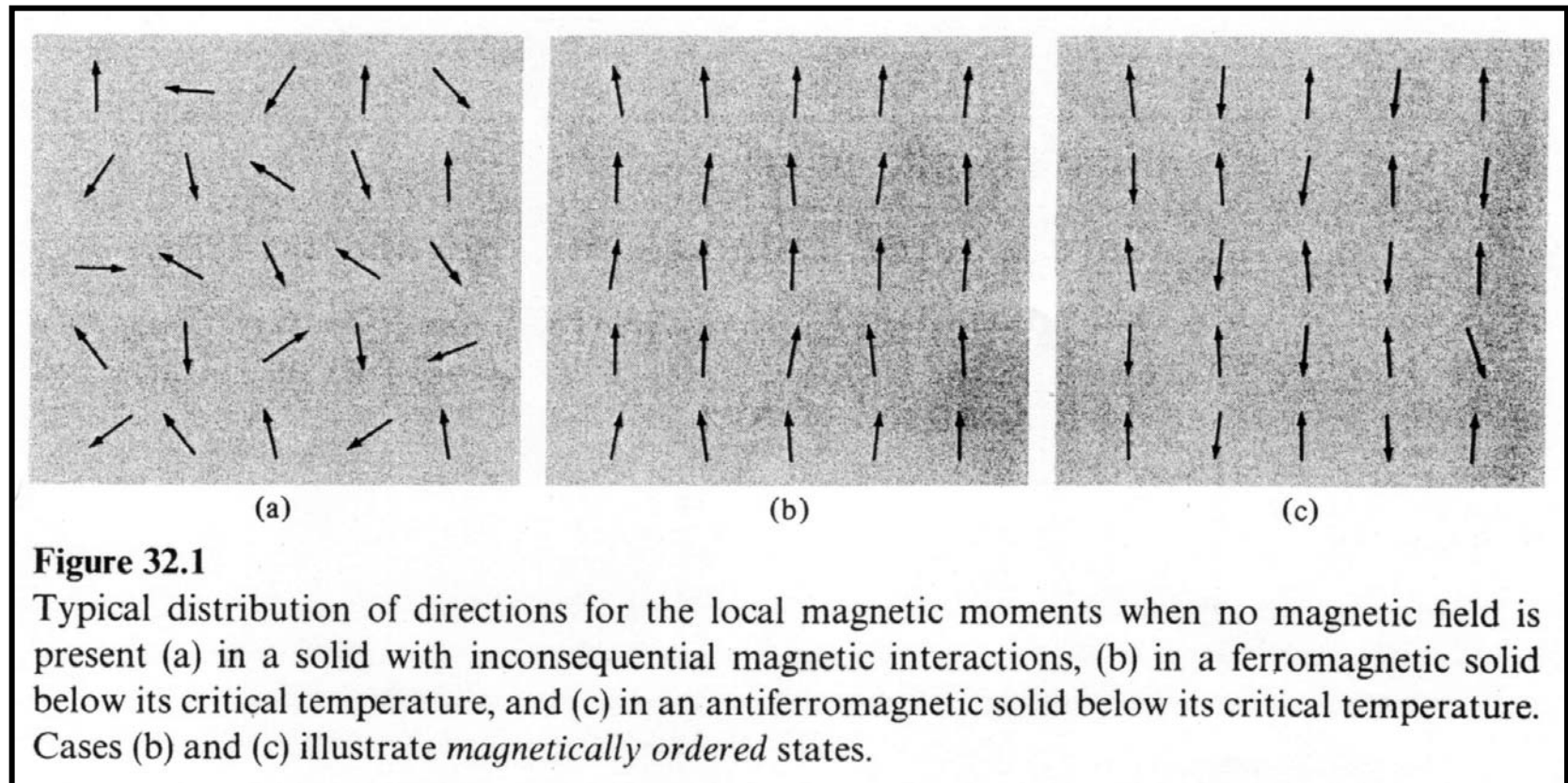
N. W. Ashcroft and N. D. Mermin, *Solid State Physics*, Harcourt, 1976.

# Types of Magnetic Ordering

If magnetic interactions are consequential and the temperature is below  $T_c$ , a solid can exist in the following magnetically ordered states even with no applied field:

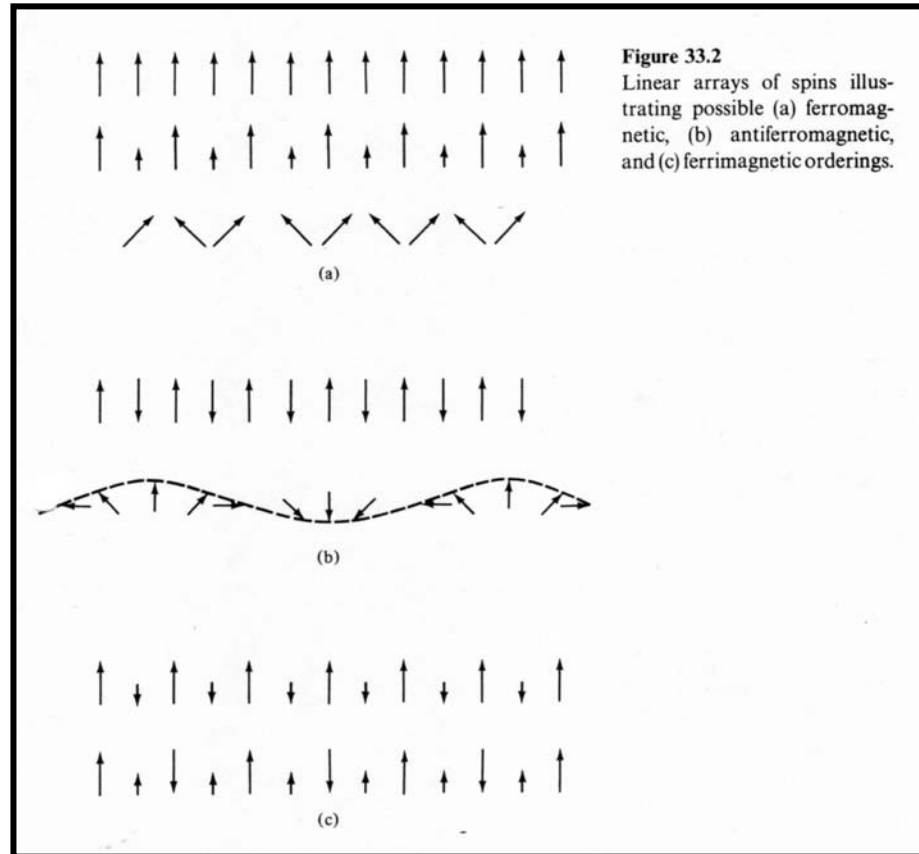
- (1) Ferromagnetic: all local moments have a positive component along the direction of the spontaneous magnetization
- (2) Antiferromagnetic: individual local moments sum to zero total moment (no spontaneous magnetization)
- (3) Ferrimagnetic: local moments are not all oriented in the same direction, but there is a non-zero spontaneous magnetization

# Types of Magnetic Ordering



N. W. Ashcroft and N. D. Mermin, *Solid State Physics*, Harcourt, 1976.

# Types of Magnetic Ordering



N. W. Ashcroft and N. D. Mermin, *Solid State Physics*, Harcourt, 1976.

# “Unusual” Behavior of Iron

Even though  $T_c$  for iron is  $>1000$  K, iron is normally “unmagnetized” at room temperature

However,

- (1) Iron is more strongly attracted by magnetic field than a paramagnetic material
- (2) Iron can be “magnetized” by stroking it with a permanent magnet

Why? We need to consider “weak” interactions besides electrostatic exchange coupling

# Ferromagnetic Domains

Note: (1) Exchange coupling is 1000X greater than dipolar coupling for nearest neighbors

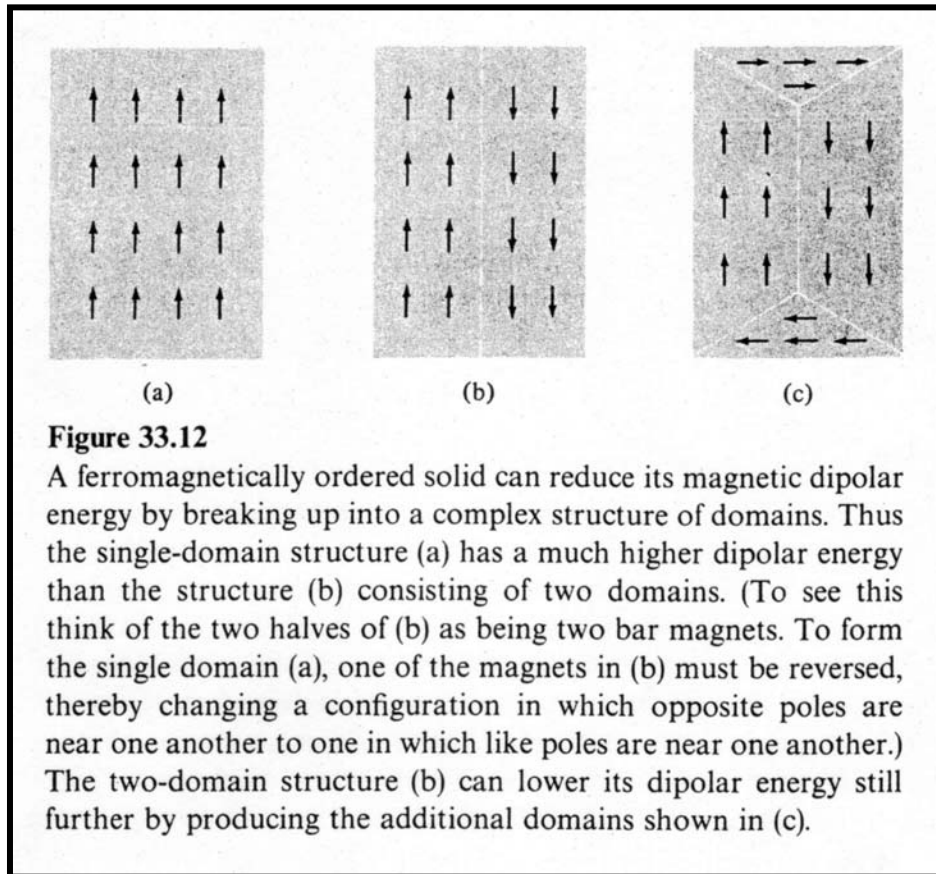
(2) But, exchange coupling is short ranged (falls off exponentially) compared to dipolar coupling ( $1/r^3$ )

→ In large samples, dipolar coupling can alter spin configurations favored by short range exchange coupling

→ Overall magnetic energy is minimized by formation of domains



# Ferromagnetic Domains



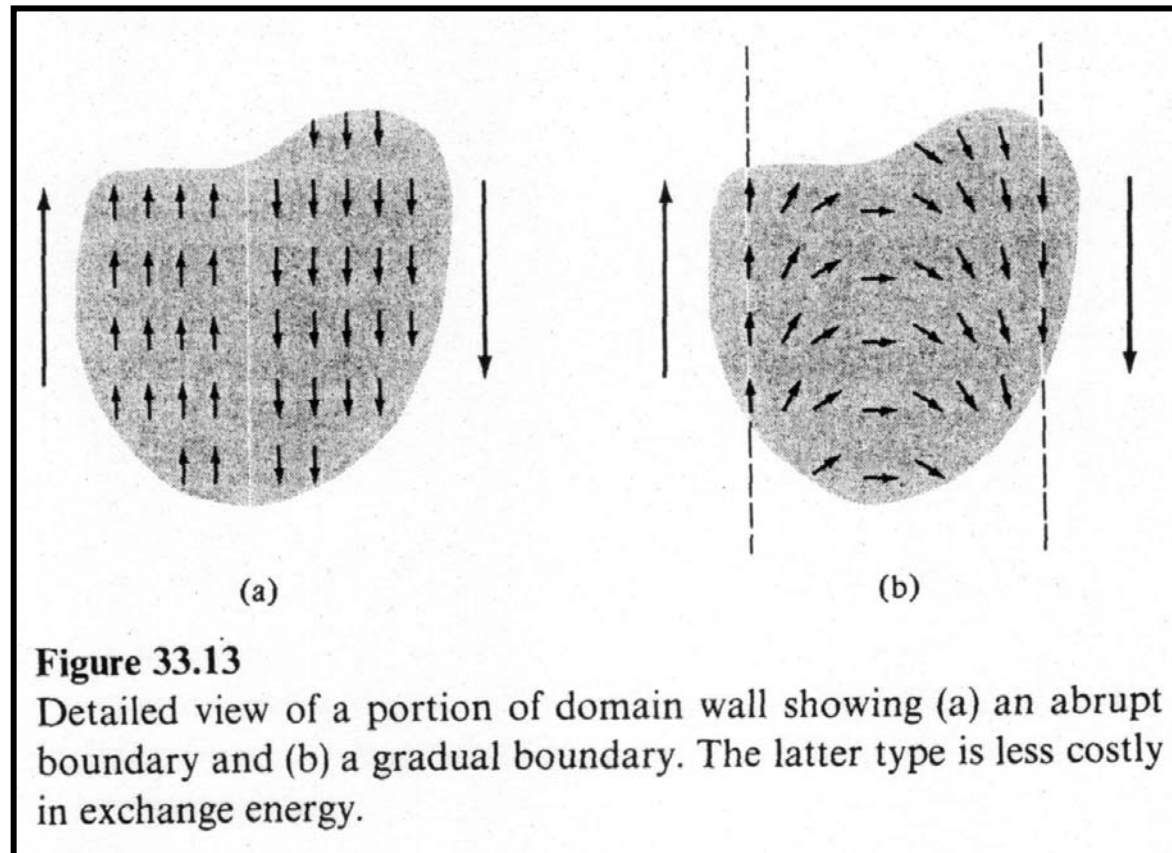
N. W. Ashcroft and N. D. Mermin, *Solid State Physics*, Harcourt, 1976.

# Domain Boundaries

- Upon domain formation, dipolar energy (bulk effect) is minimized and exchange energy is only raised for a small number of sites at the domain boundary → domain boundaries are gradual
- Domain boundaries are not infinitely large due to spin-orbit coupling
- Overall spin energy depends on angle of spin with respect to crystal axes → anisotropy energy
- Domain wall thickness is dictated by a competition between exchange and anisotropy energies



# Domain Boundaries

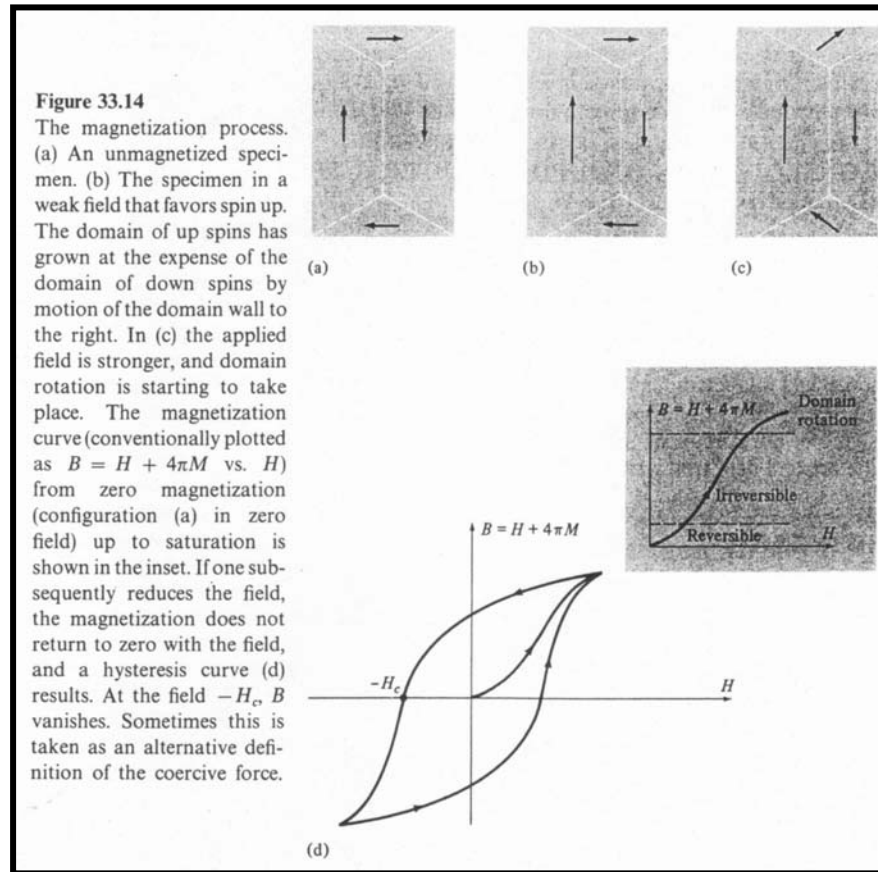


N. W. Ashcroft and N. D. Mermin, *Solid State Physics*, Harcourt, 1976.

# Magnetization of “Unmagnetized” Iron

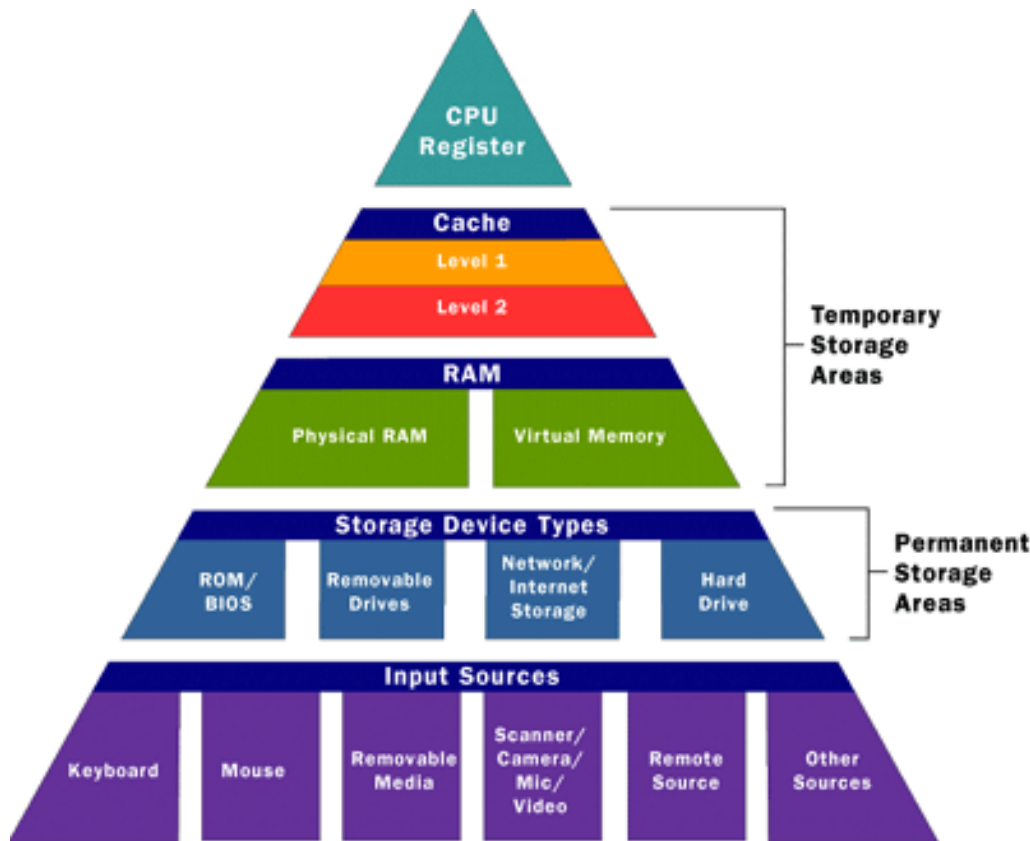
- (1) In small fields, domains reversibly align with fields by smooth motion of domain walls
  - (2) At high fields, domains irreversibly align with fields → defect mediated process → defects can prevent domain walls from returning to original zero bulk magnetization
- Magnetization of iron (non-zero bulk magnetization at zero field)
  - A reverse field is required to return to zero bulk magnetization (coercive force)
  - Hysteresis in  $B = H + 4\pi M$  vs.  $H$  curves

# Magnetic Hysteresis



N. W. Ashcroft and N. D. Mermin, *Solid State Physics*, Harcourt, 1976.

# Hierarchy of Computer Memory



## Issues:

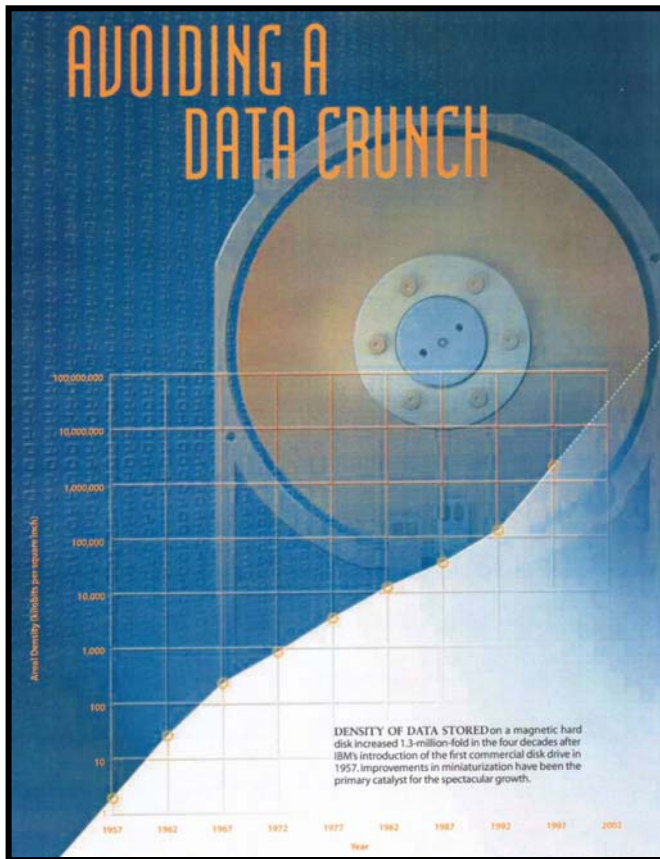
- (1) Cost
- (2) Data Storage Density
- (3) Access Time
- (4) Power Dissipation
- (5) Volatility



- What is the role of nanomagnetism?
- What are the alternatives?

<http://computer.howstuffworks.com/computer-memory1.htm>

# Magnetic Miniaturization

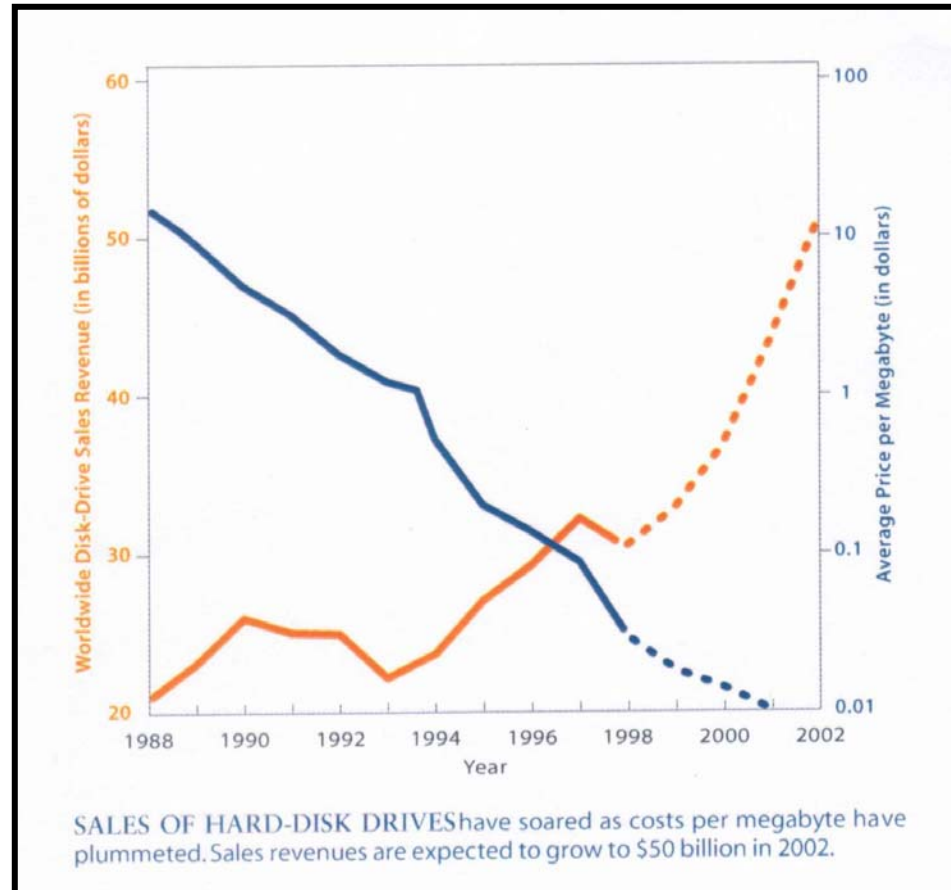


## Capacity of magnetic hard disks:

- 1980's: 30% growth per year
- early 1990's: 60% growth per year
- late 1990's: 130% growth per year
- disk capacity doubling every 9 months (twice the pace of Moore's Law)

J. W. Toigo, *Scientific American*, **282**, 58 (2000).

# Economics of Magnetic Storage



J. W. Toigo, *Scientific American*, **282**, 58 (2000).