

## Section 32 Modern MOSFET

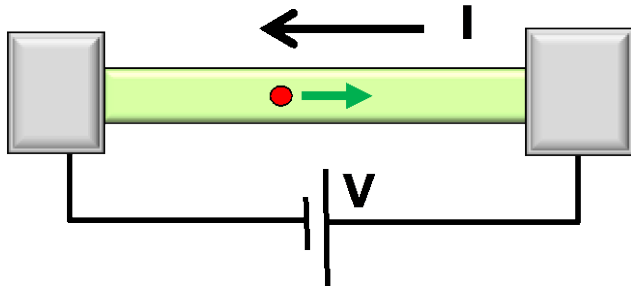
### 32.3 Control of threshold voltage

Gerhard Klimeck  
[gekco@purdue.edu](mailto:gekco@purdue.edu)



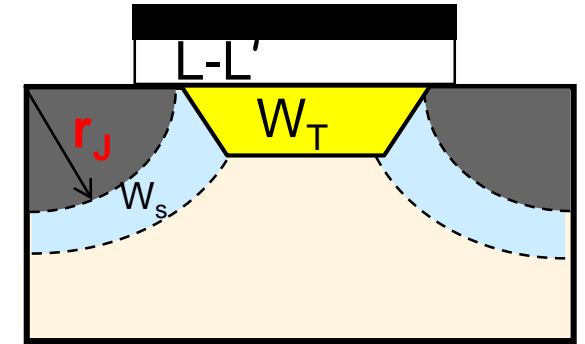
School of Electrical and  
Computer Engineering

# Section 32 Modern MOSFET

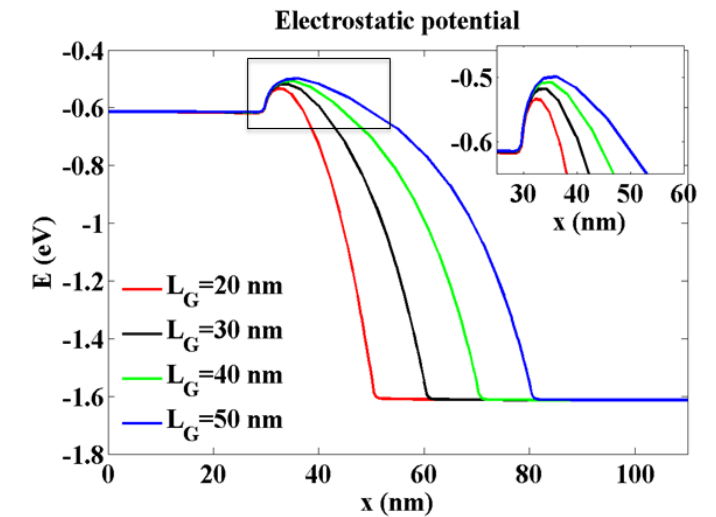


$$I = G \times V$$
$$= q \times n \times v \times A$$

charge density    velocity    area

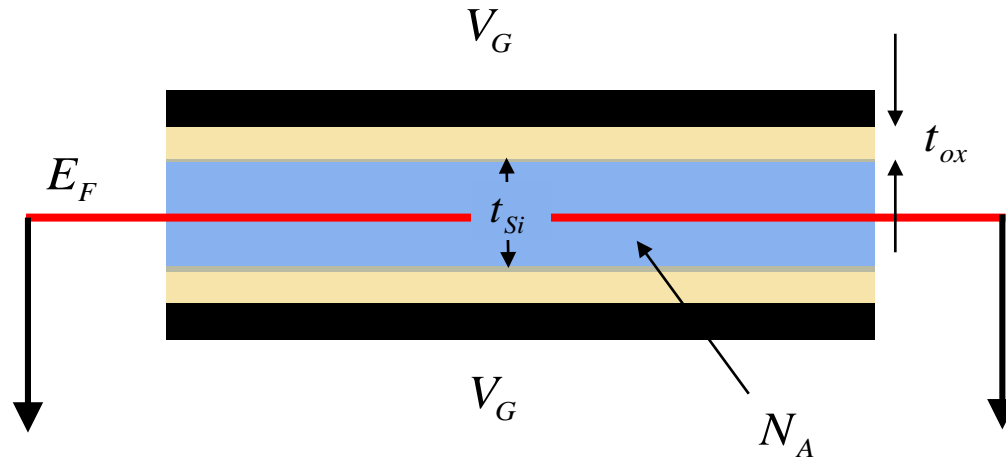


- 1 • 32.1 Some of Moore's Law Challenges
- 2 • 32.2 Short channel effect
- 3 • 32.3 Control of threshold voltage
- 4 • 32.4 Mobility enhancement

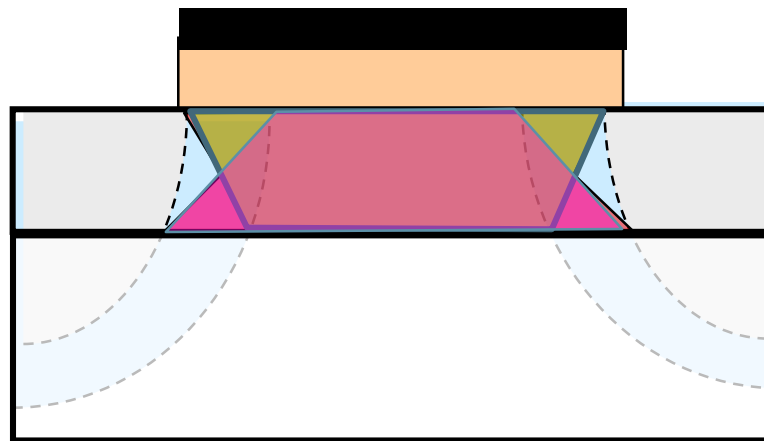


# Solution: Ultra-thin Body SOI

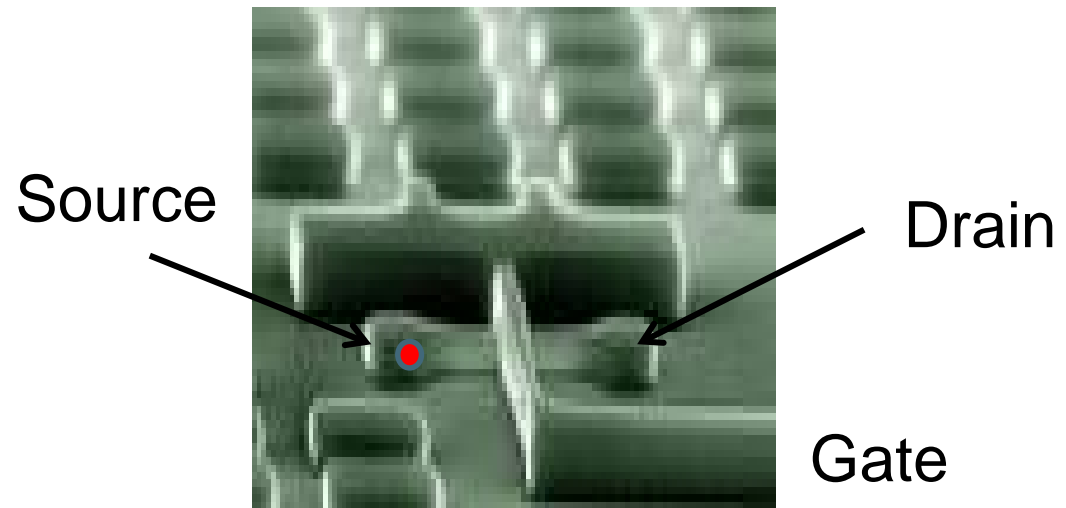
Two Gates →  
better channel  
control



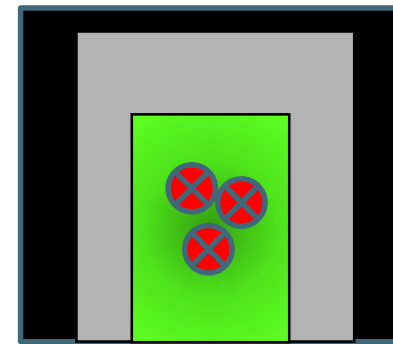
SOI: Silicon On  
Insulator



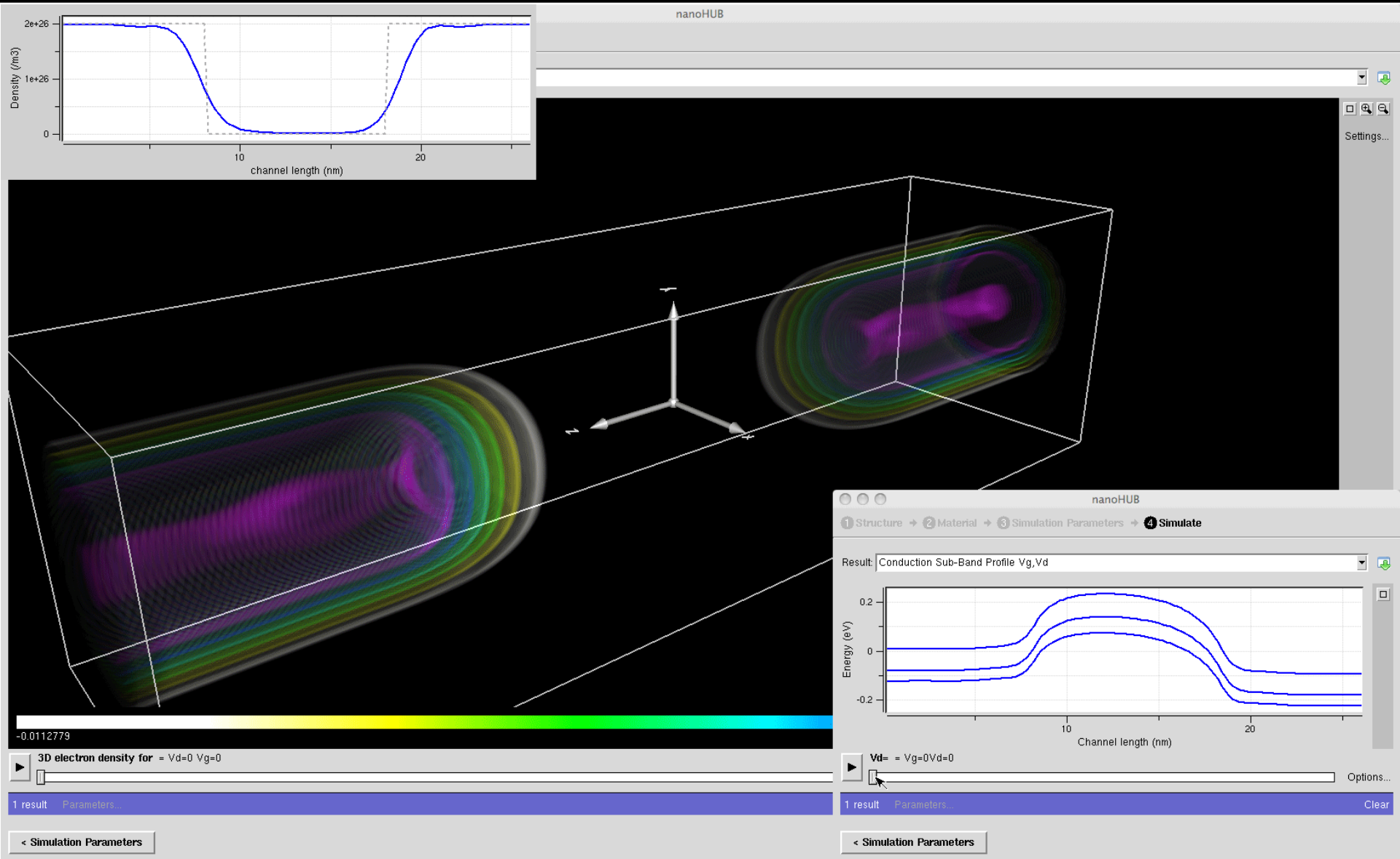
# Example: FINFET, OmegaFET, X-FET



## Cross-section

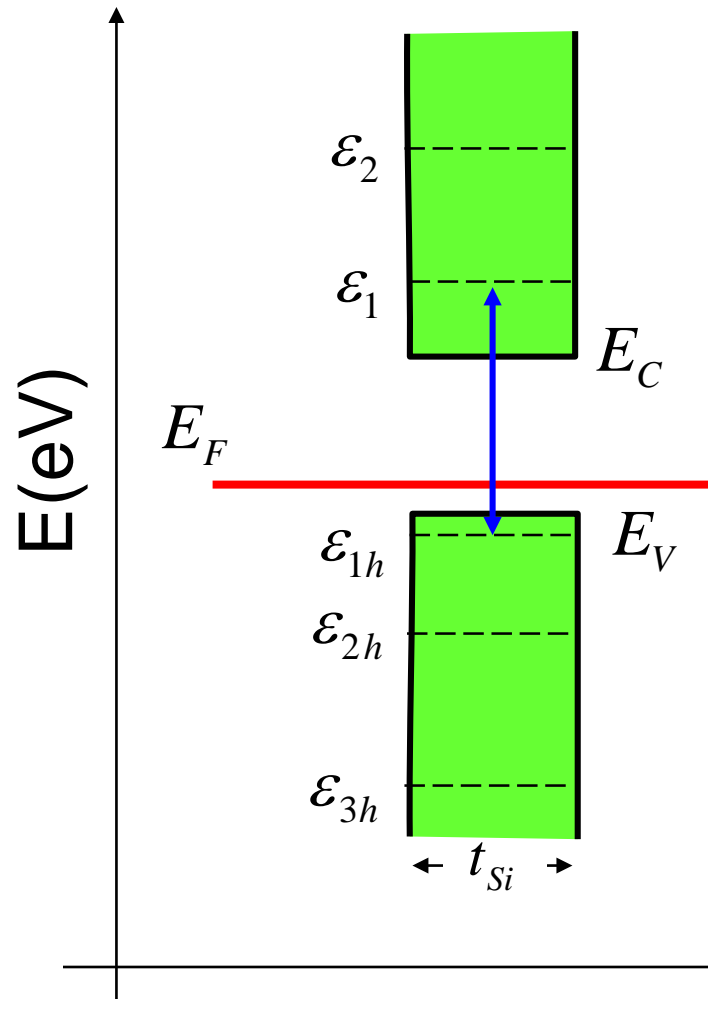


# Electro-Static Control in a GAA Nanowire nanowire tool on nanoHUB.org



- <https://nanohub.org/tools/omenwire>

# Quantization and Control of Fin-width

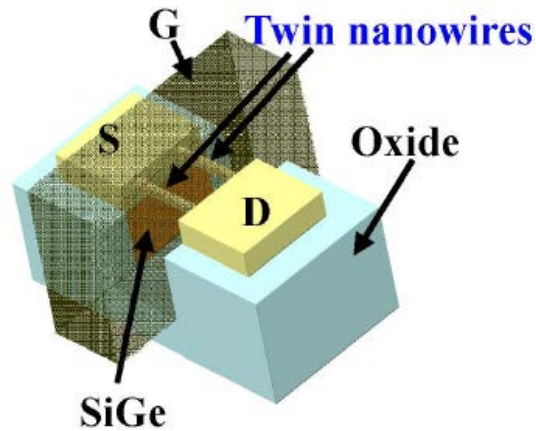


$$\epsilon_n = \frac{\hbar^2 n^2 \pi^2}{2m^* t_{Si}^2}$$

$$E'_G = E_G + \epsilon_1 + \epsilon_{1h}$$

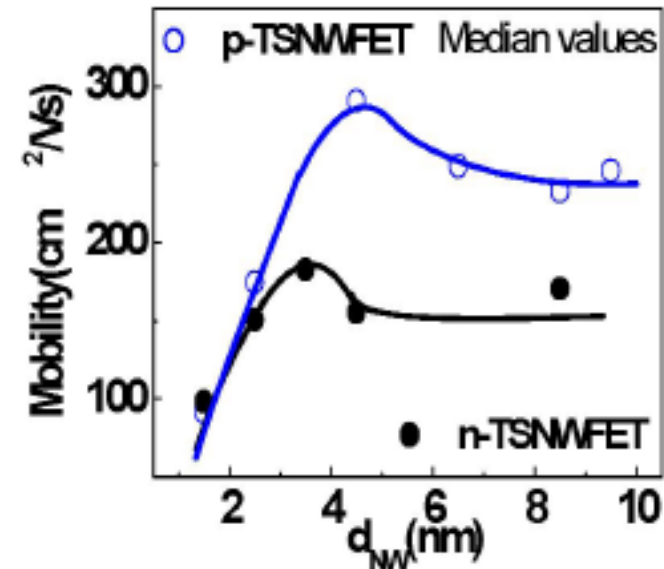
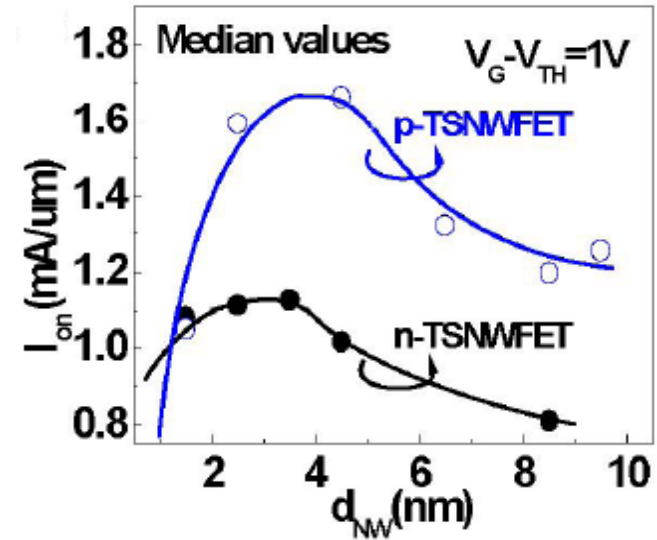
Band-gap widening  
Fluctuation in thickness

# Motivation

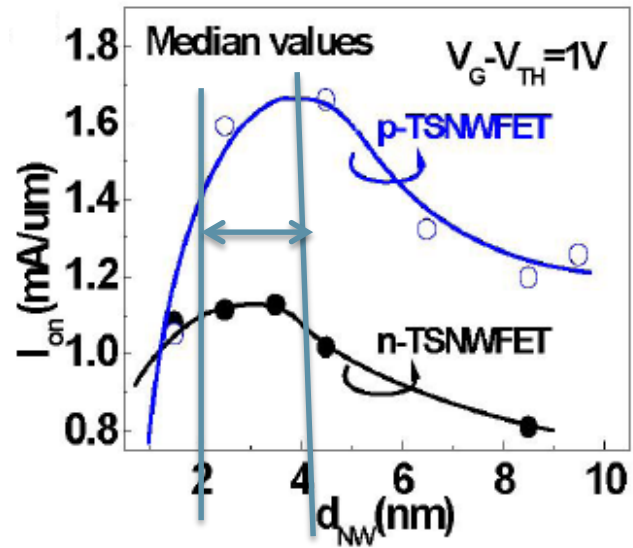


[1] S. D. Suk, IEDM, 2007

- Significant reduction of ON-current/mobility in NW with diameter less than 3 nm.
- What causes this?

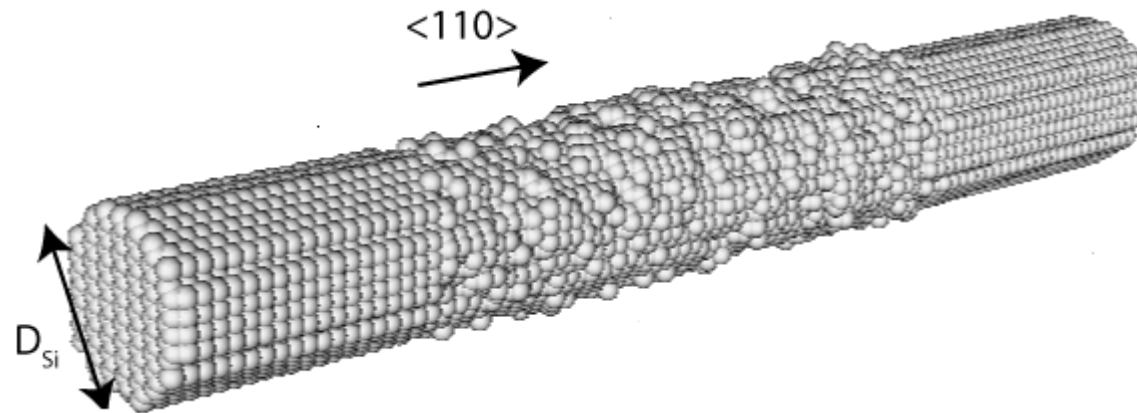


# Interface roughness scattering



- Bandstructure: tight-binding/full-band
- 3D-atomistic interface roughness
- SiO<sub>2</sub> included in transport
- Low/High-drain bias

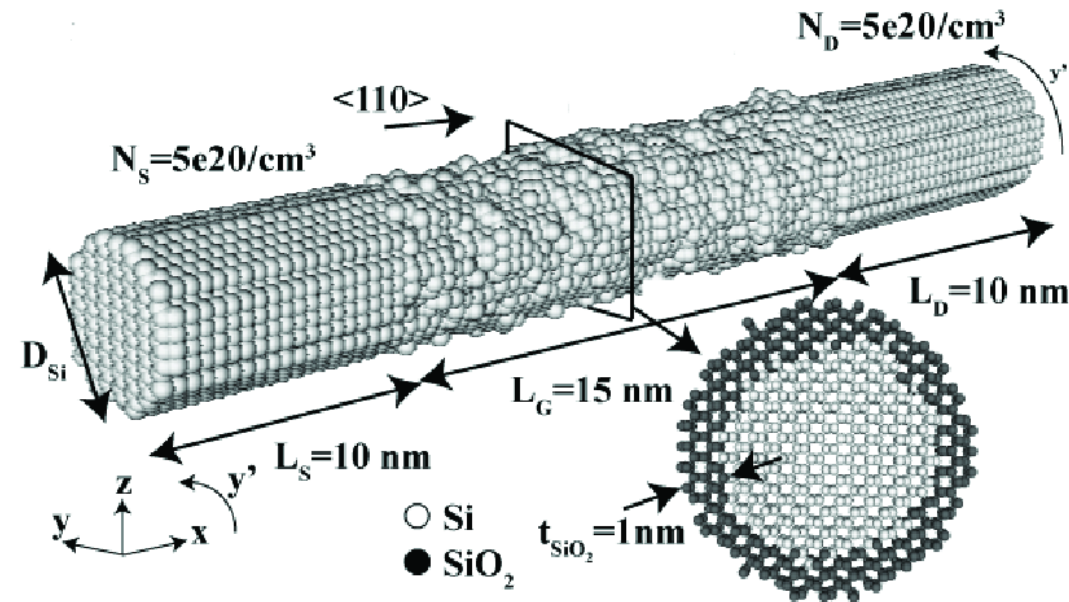
Comparison with experiments





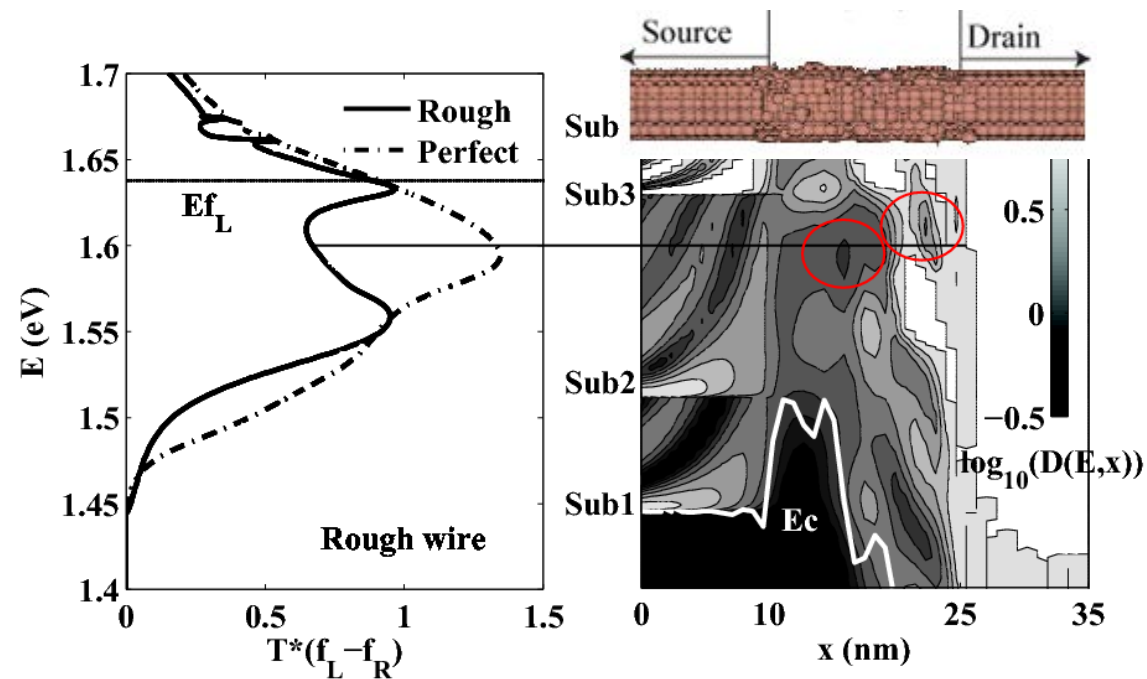
# Difficulties: Interface roughness scattering

- Realistic/atomistic rough interface between Si/SiO<sub>2</sub>
  - » Adapt experimentally generated statistical function: How do we know the generated interface roughness is correct?
  - » Many statistical samples needed: computational cost high
  - » Electrons may penetrate into the SiO<sub>2</sub> region. How do we count it?
  - » Computational cost increases as we take into account SiO<sub>2</sub> in tight-binding approximation.



# Difficulties: Full band Tight-binding simulation

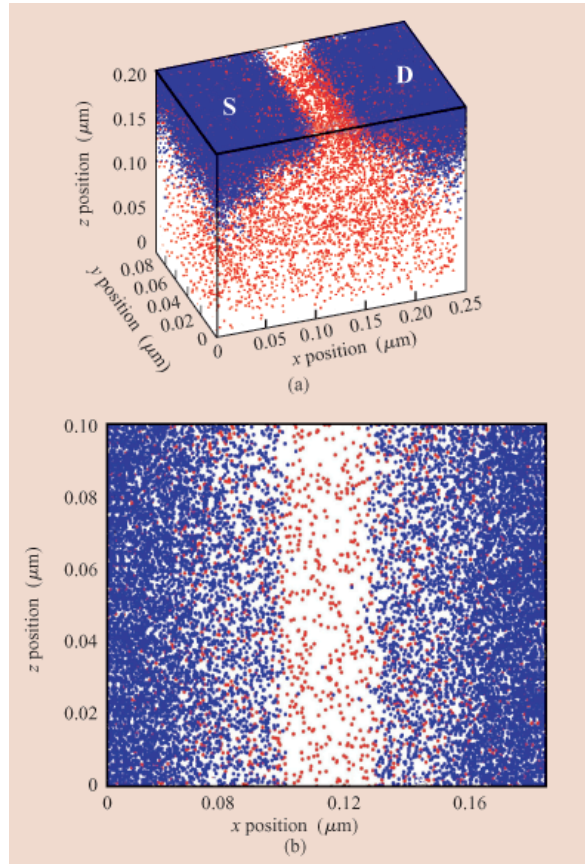
- To correctly include scattering mechanisms (interface roughness/phonon scattering)  $\langle 110 \rangle$  NW
  - » Beyond the effective mass approximation, full band tight-binding simulation is needed: computational cost is higher
    - ✓ Effective mass cannot understand non-parabolicity/anisotropy in the bandstructure of  $\langle 110 \rangle$  oriented NW
    - ✓ At high drain/gate bias drain side of the channel, higher subbands are mixing and influence the scattering



# Variability in $V_{th}$ at Low Doping

$$V_{th} = 2\phi_F - \frac{Q_B}{C_{ox}} = 2\phi_F - \frac{qN_D W_T}{C_{ox}}$$

$$\sigma_{V_T} = 3.19 \times 10^{-8} \left( \frac{t_{ox} N_A^{0.4}}{\sqrt{L_{eff} W_{eff}}} [V] \right),$$



Variation of  $V_T$  in short channel devices

Stronger effect of dopant number fluctuations on  $V_T$

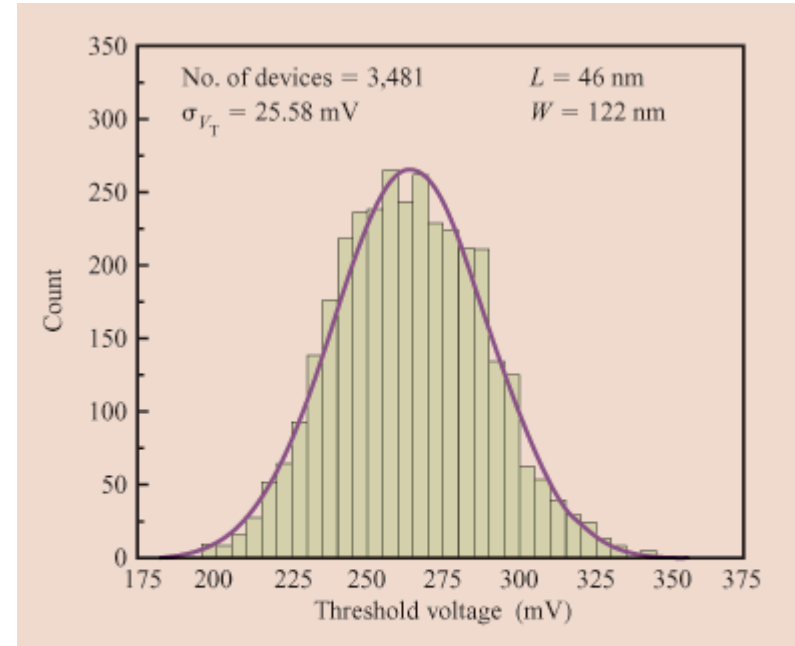


Figure 2

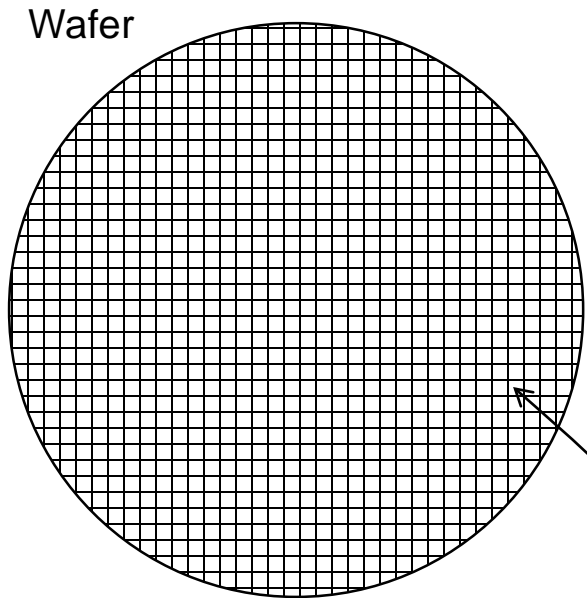
Threshold voltage histogram for FETs in the 90-nm-technology node.

IBM Journal of Res. And Tech. 2003.

# Variability in Threshold Voltage

$$V_{th} = 2\phi_F - \frac{Q_B}{C_{ox}} = 2\phi_F - \frac{qN_A W_T}{C_{ox}}$$

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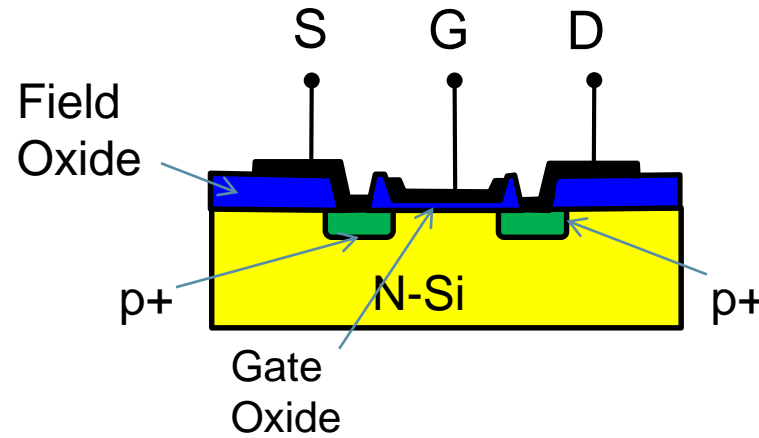
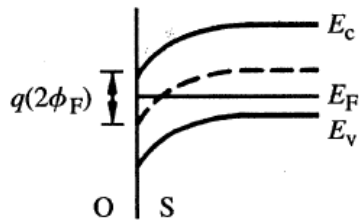


$$I_D = \frac{\mu C_{ox}}{L_{ch}} (V_G - V_{th}^*)^2$$

If every transistor has different  $V_{th}$  and therefore different current, circuit design becomes difficult

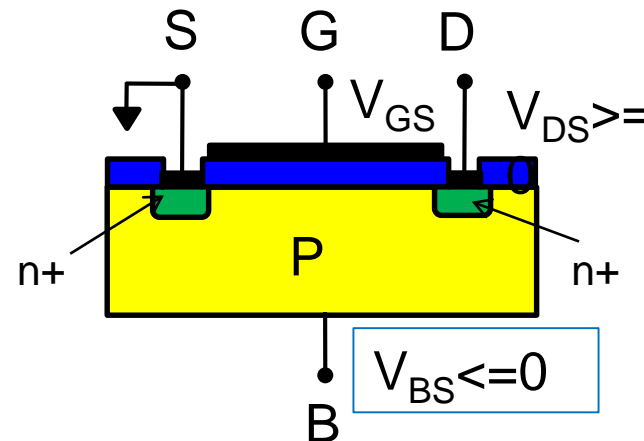
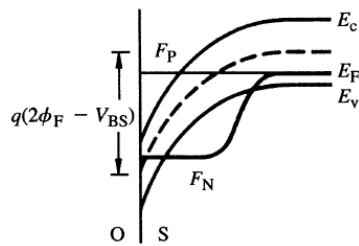
# $V_{th}$ control by Substrate Bias

$$V_{th} = \psi_s - \frac{Q_B}{C_{ox}} = \psi_s + B\sqrt{\psi_s}$$



$$\psi_s = 2\phi_F$$

Control channel inversion voltage through back gate bias

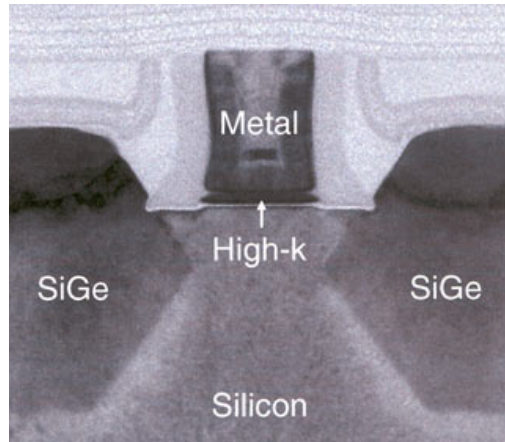


$$\psi_s = 2\phi_F - V_{BS}$$

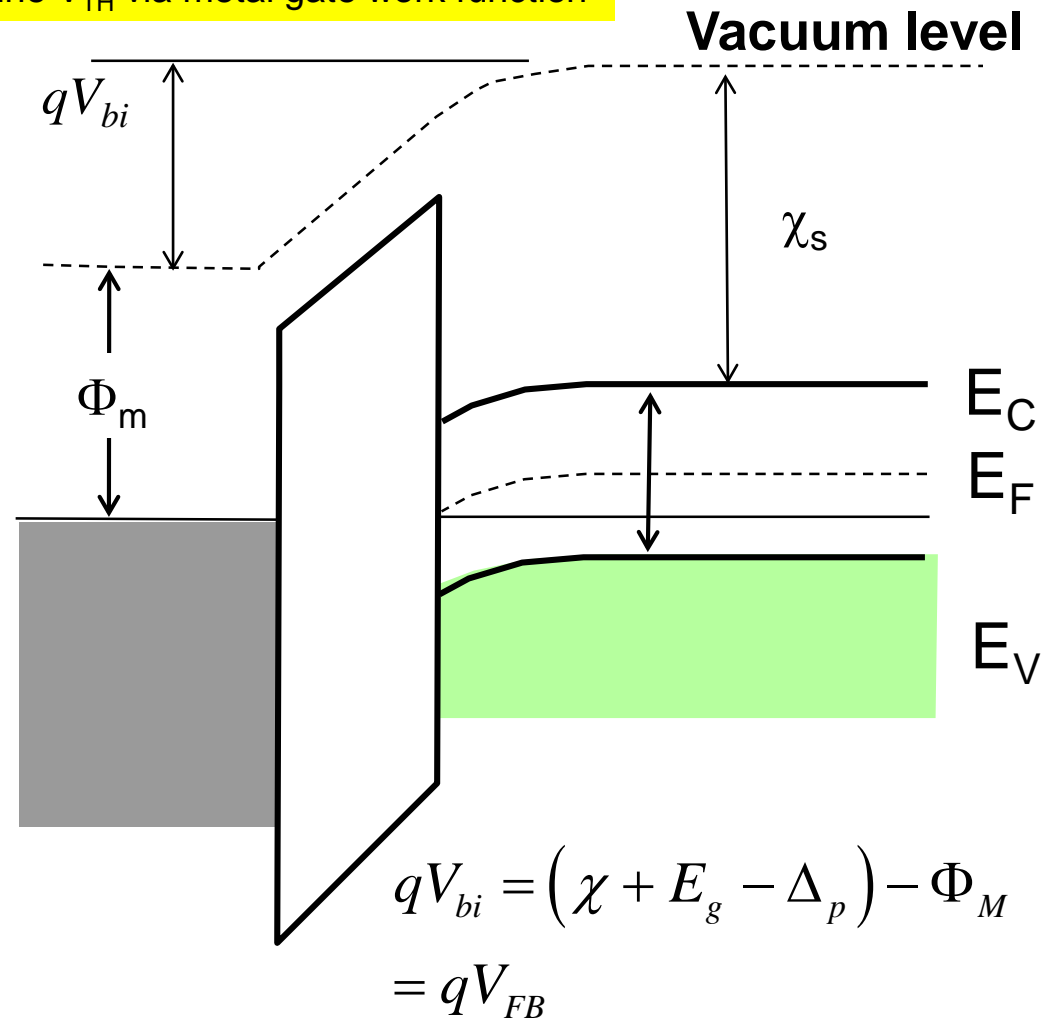
Tune  $V_T$  through back gate bias  $V_{BS}$

# $V_{th}$ control by Metal Work-function

## High-k/metal gate MOSFET



Tune  $V_{TH}$  via metal gate work function

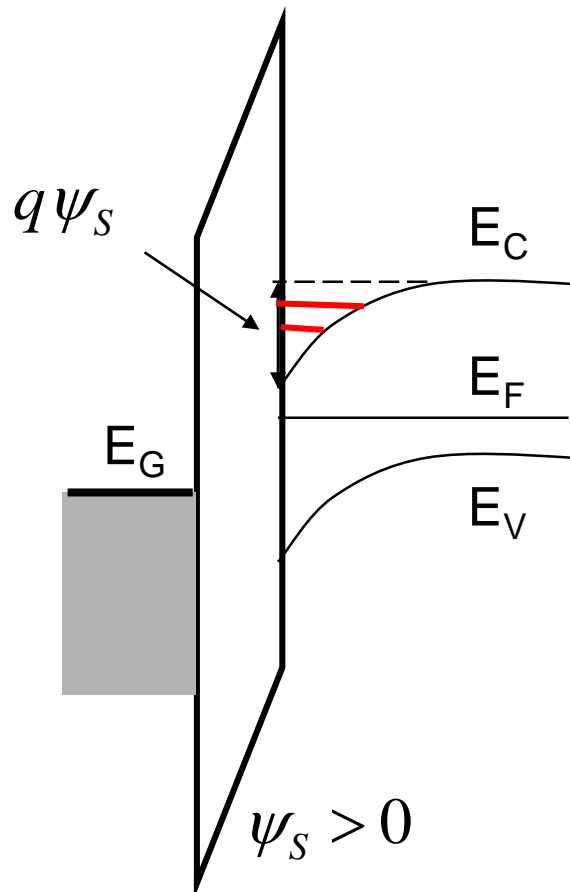


$$Q_i = C_{ox} (V_G - V_{th})$$

$$V_{th} = -V_{FB} + \psi_s - \frac{Q_B}{C_{ox}}$$

# Quantization in Inversion

## "Exact" solution is not really exact ...



$$\left. \frac{d^2\psi}{dx^2} \right| = \frac{-q}{\varepsilon} \left[ p(x) - n(x) |\psi(x)|^2 + N_D^+ - N_A^- \right]$$

↓  
wavefunction, not potential !

Wave function should be accounted for

Bandgap widening near the interface must also be accounted for.

Assumption of nondegeneracy may not always be valid

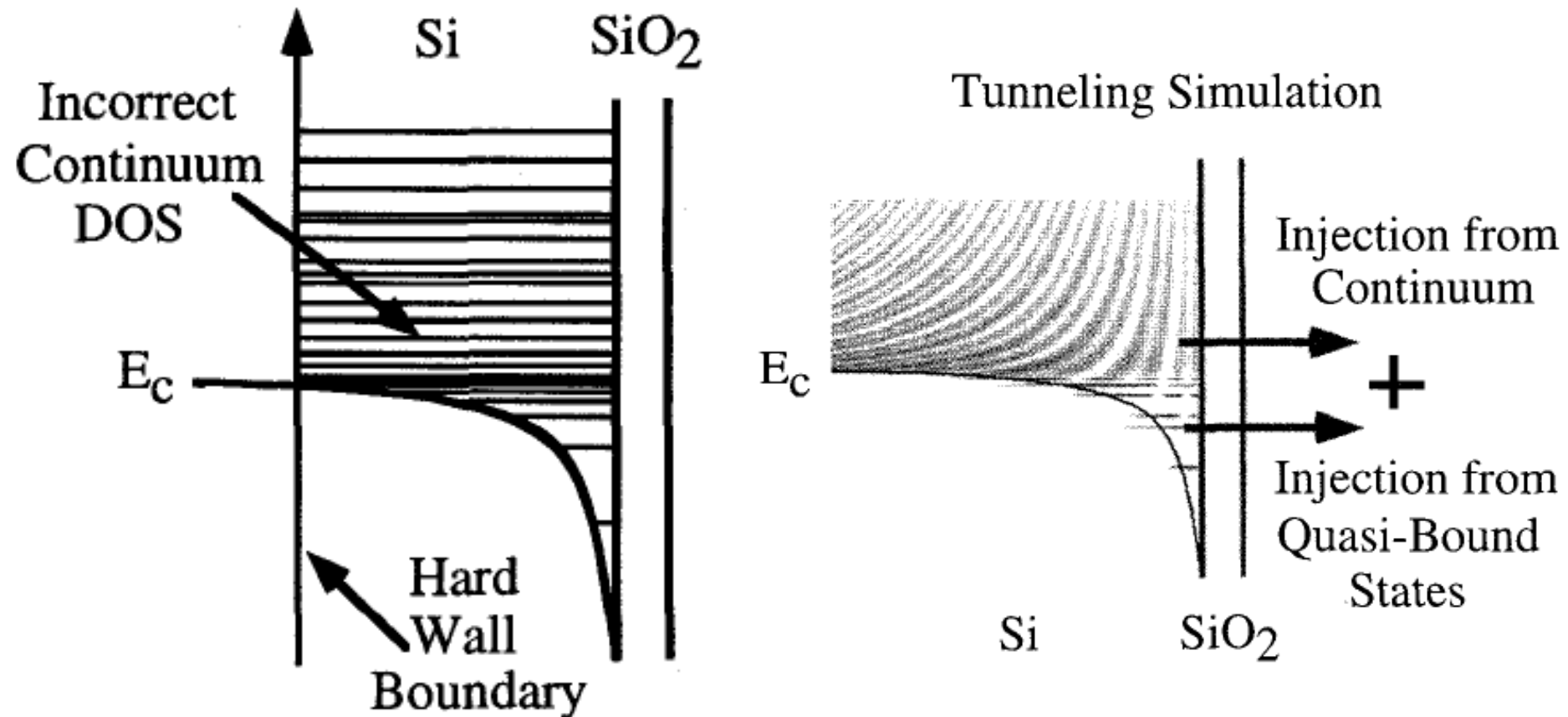


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**"Physical Oxide Extraction and Versification using Quantum Mechanical Simulation"**

Proceedings of IEDM 1997, IEEE, 869 (1997); [doi : 10.1109/IEDM.1997.650518](https://doi.org/10.1109/IEDM.1997.650518), [Cited by 42](#)



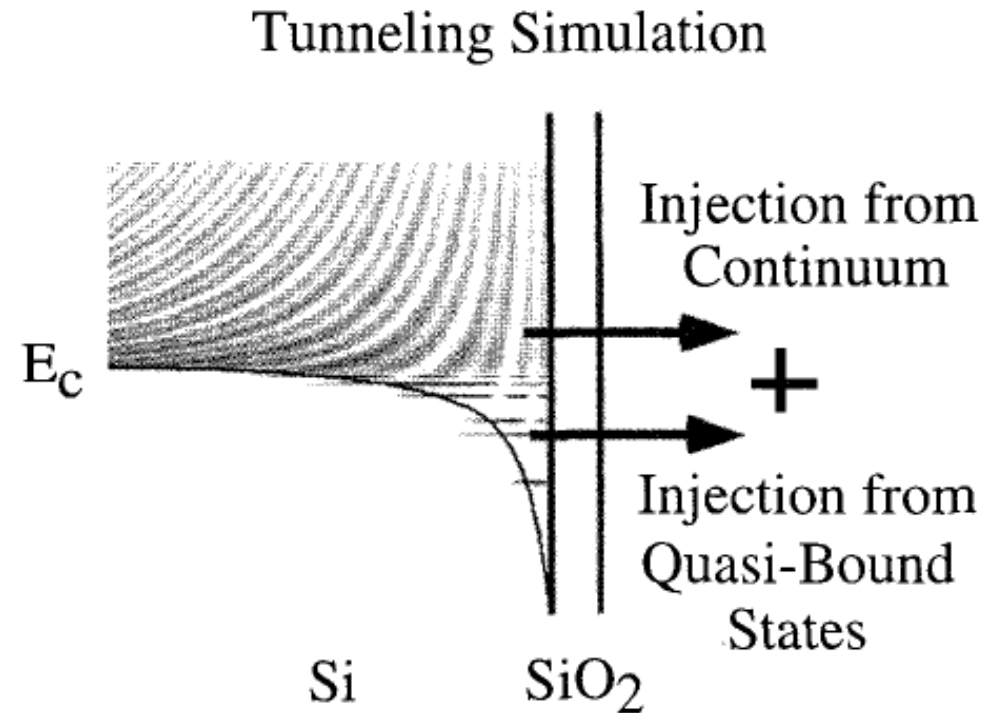
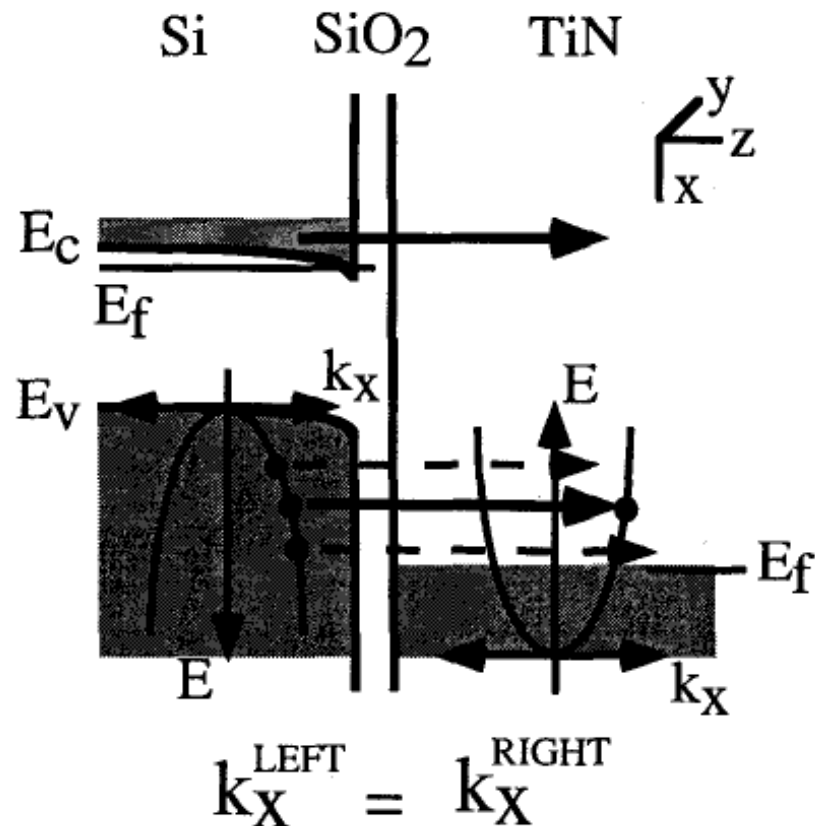


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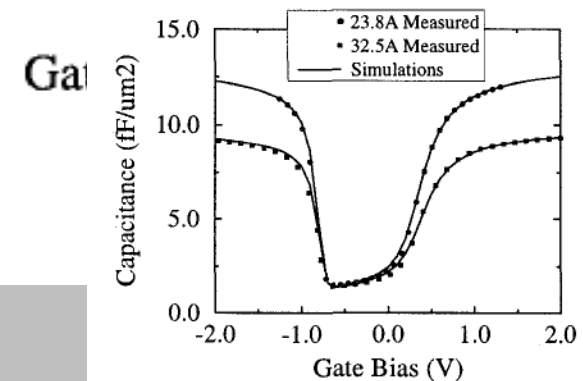
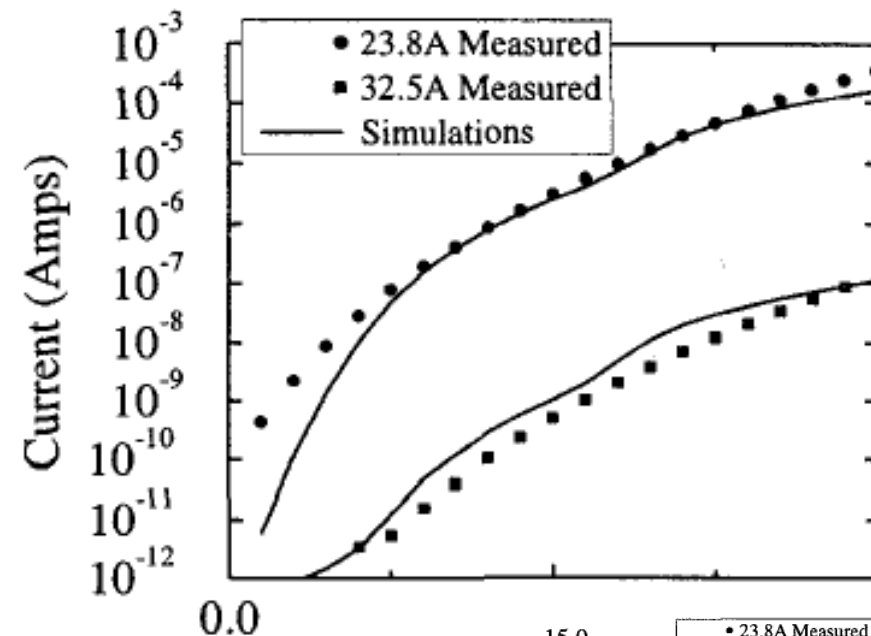
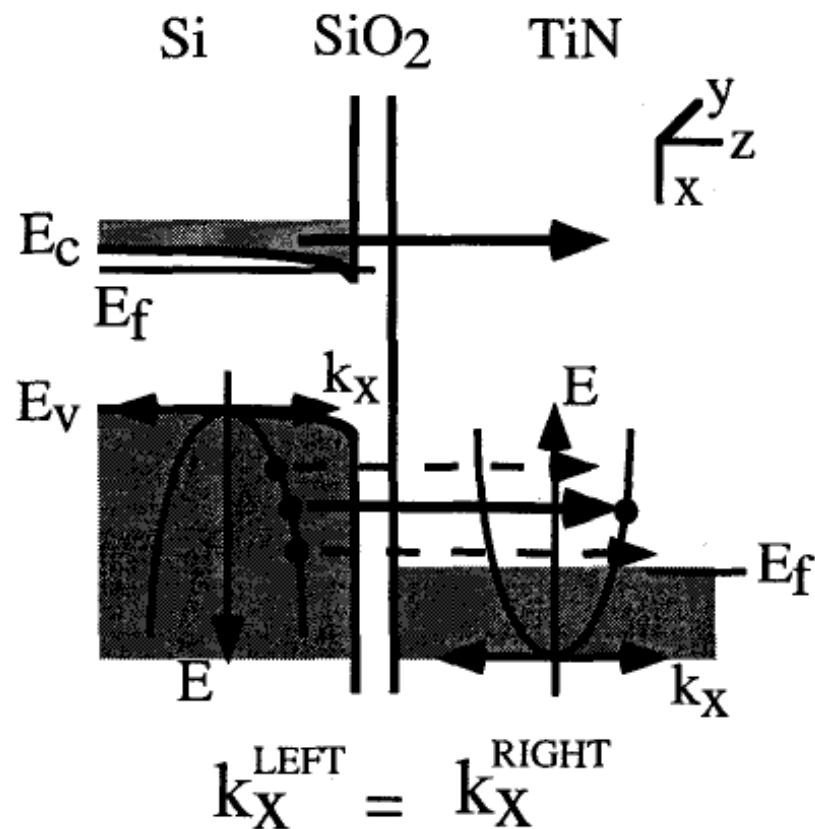


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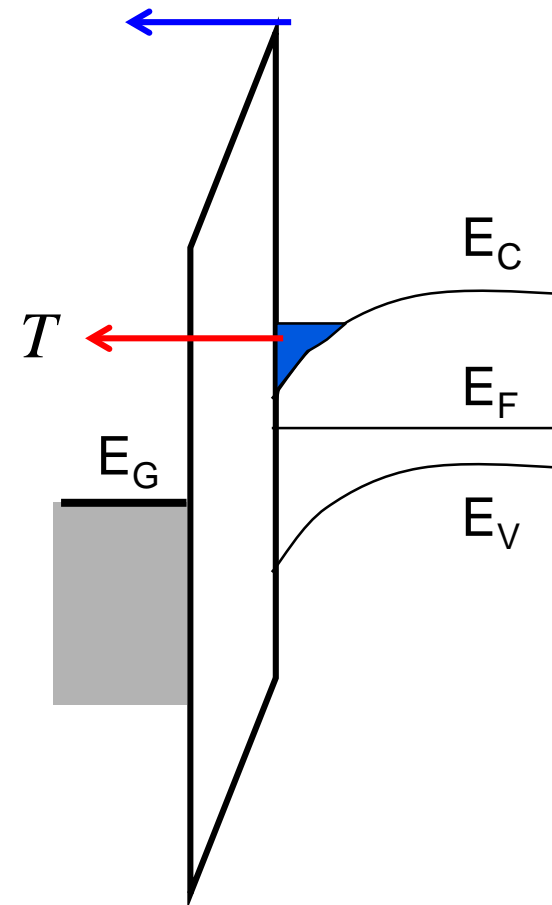
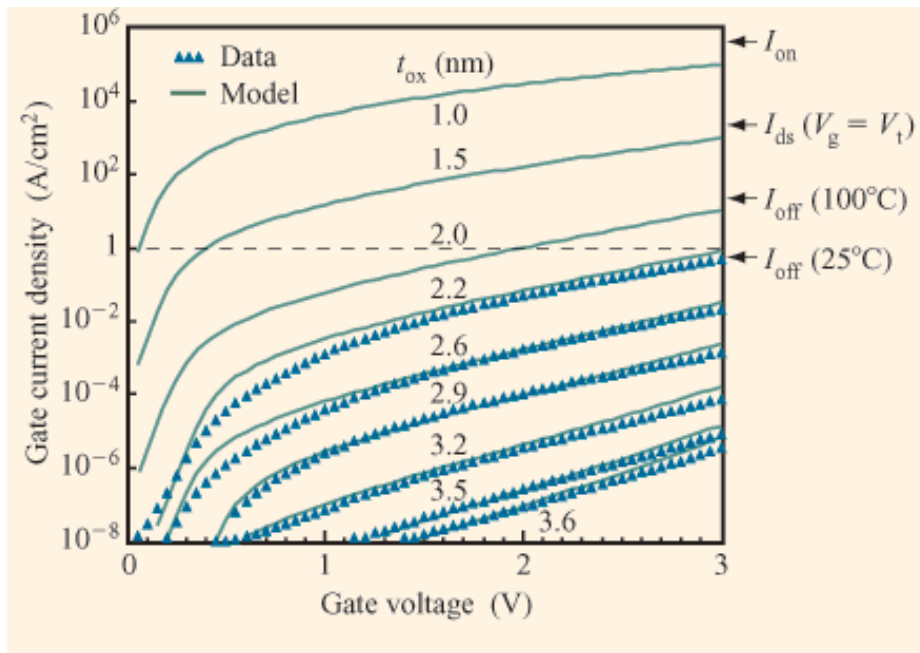
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# Tunneling Current

Don't make oxides too thin → tunneling!

$$J_T = \left[ Q_i(V_G) - \frac{n_i^2}{N_A} e^{-qV_G\beta} \right] v_{th} \langle T(E) \rangle$$

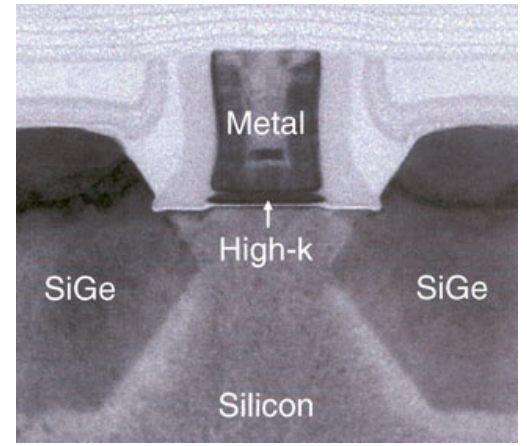


# How to make $V_{th}$ Roll-off small ...

$$L_{\min} = \frac{qN_A W_T}{\kappa_{ox} \epsilon_0} \frac{r_J}{\alpha} \left( \sqrt{1 + \frac{2W_T}{r_J}} - 1 \right) x_0$$

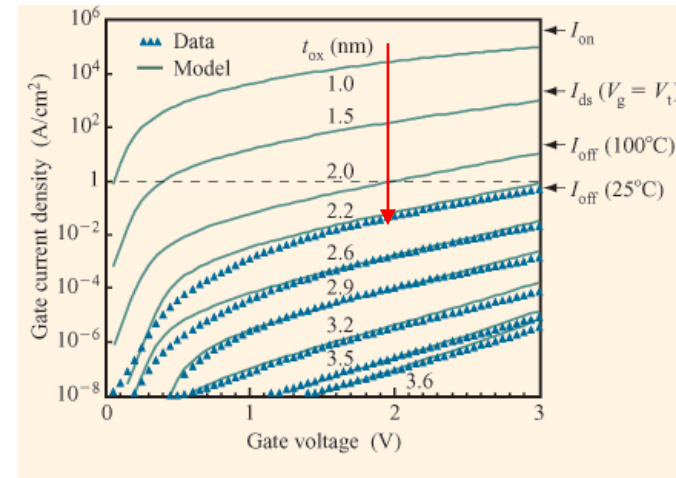
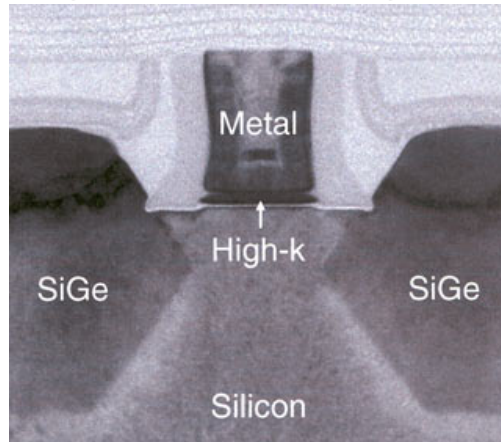
High k oxides allow for smaller  $L_{\min}$  but lot of defects

## High-k/metal gate MOSFET



- Shallow junction and geometry of transistors  
laser annealing of junctions, FINFET
- Substrate doping  $N_A$   
consider  $W_T$  and junction breakdown
- Thinner gate oxides  
consider tunneling current
- **Higher gate dielectric**  
consider bulk traps

## High-k/metal gate MOSFET



$$L_c = \frac{qN_A W_T}{\kappa_{ox} \epsilon_0} \frac{r_J}{\alpha} \left( \sqrt{1 + \frac{2W_T}{r_J}} - 1 \right)$$

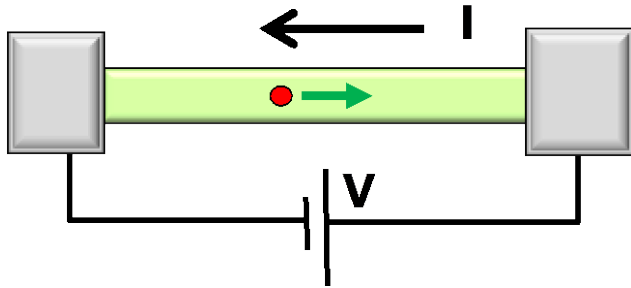
$x_0$

$$I_D = \frac{\mu C_{ox}}{L_{ch}} (V_G - V_{th}^*)^2$$

Thicker oxide ( $x_0$ ) for same capacitance ...

... ensures the drive-current is not reduced  
, but tunneling current is suppressed.

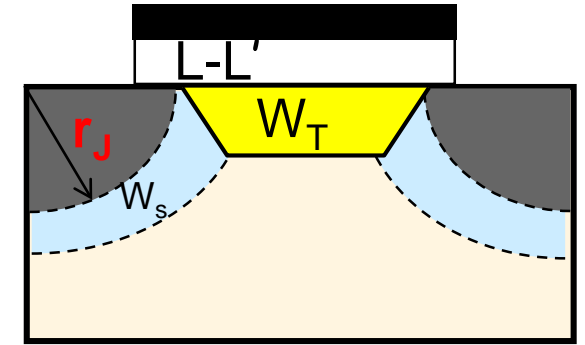
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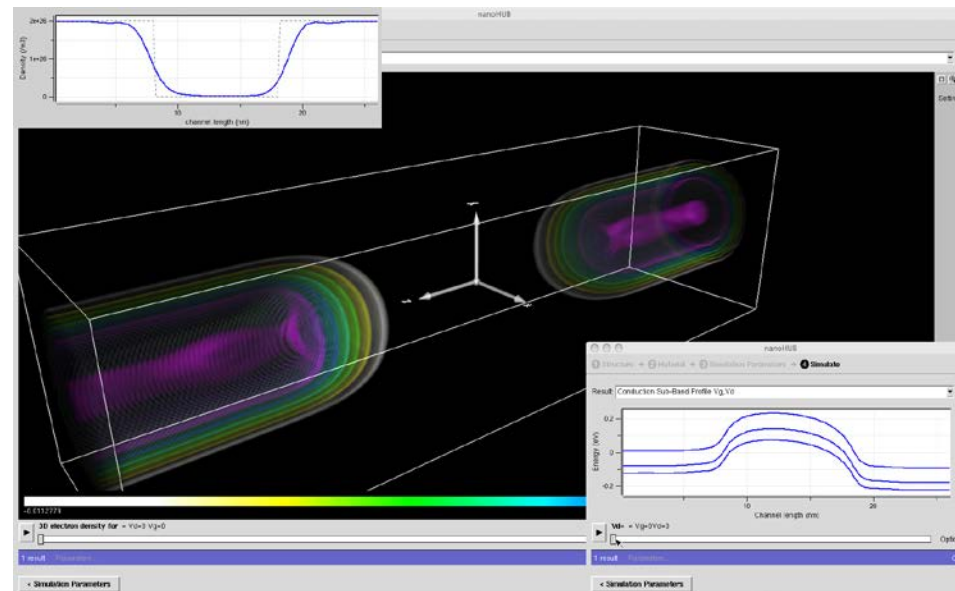
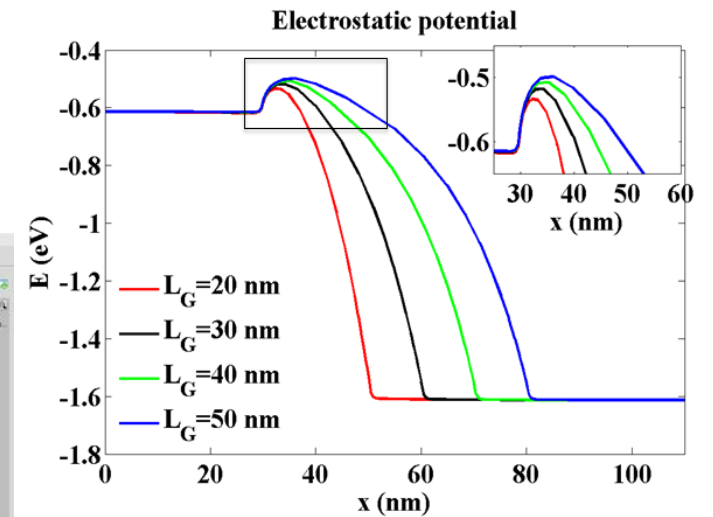
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$$= q \times n \times v \times A$$

↑ charge density   
 ↑ density   
 ↑ velocity   
 area

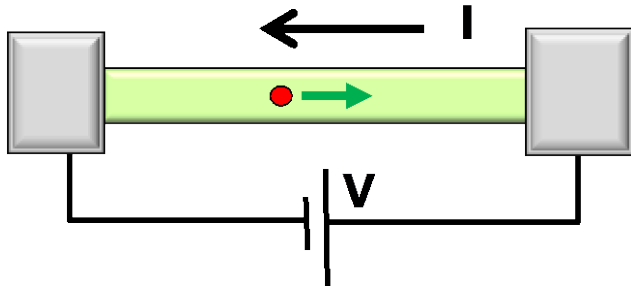


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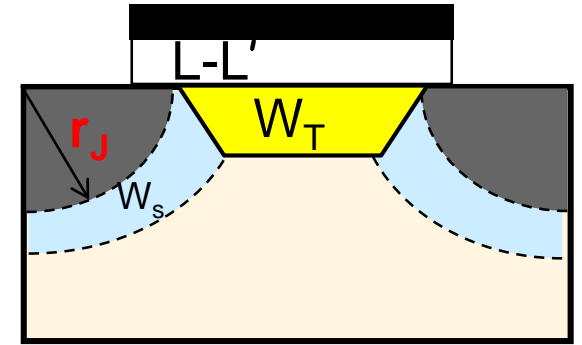
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