

## Section 27

# Heterojunction Bipolar Transistor

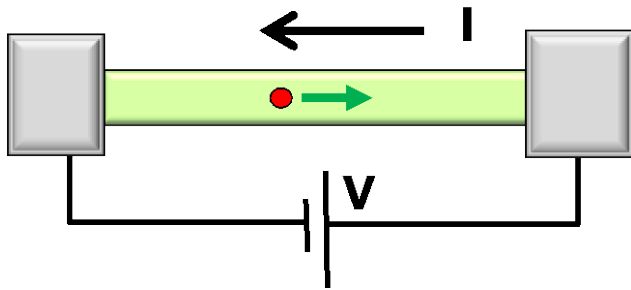
### 27.5 Graded Junction HBTs

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School of Electrical and  
Computer Engineering

# Section 27 Heterojunction Bipolar Transistor



$$I = G \times V$$

$$= q \times n \times v \times A$$

↑ charge density    ↑ density    ↑ velocity    ↑ area

$$\beta_{poly,ballistic} \rightarrow \frac{n_{i,B}^2}{n_{i,E}^2} \times \frac{N_E}{N_B} \times \frac{v_{th}}{v_s}$$

$$\frac{n_{i,B}^2}{n_{i,E}^2} = \frac{N_{C,B} N_{V,B} e^{-E_{g,B}\beta}}{N_{C,E} N_{V,E} e^{-E_{g,E}\beta}} \approx e^{(E_{g,E} - E_{g,B})\beta}$$

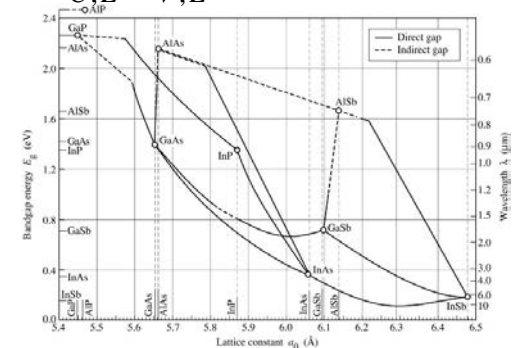
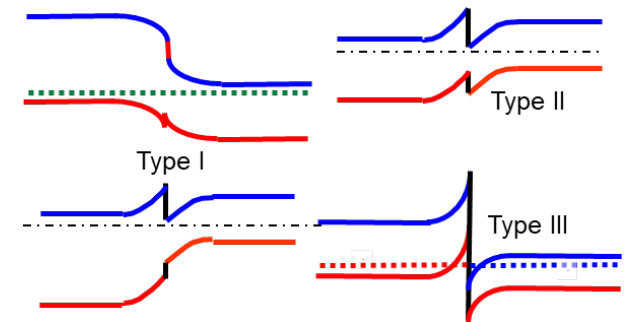
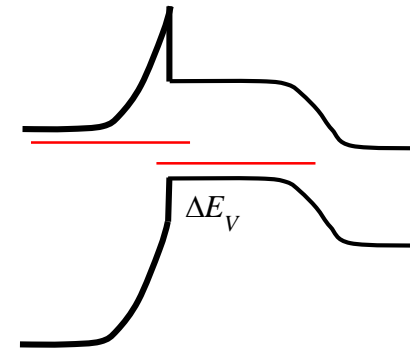


Fig. 7.6. Bandgap energy and lattice constant of various III-V semiconductors at room temperature (adopted from Tien, 1988).



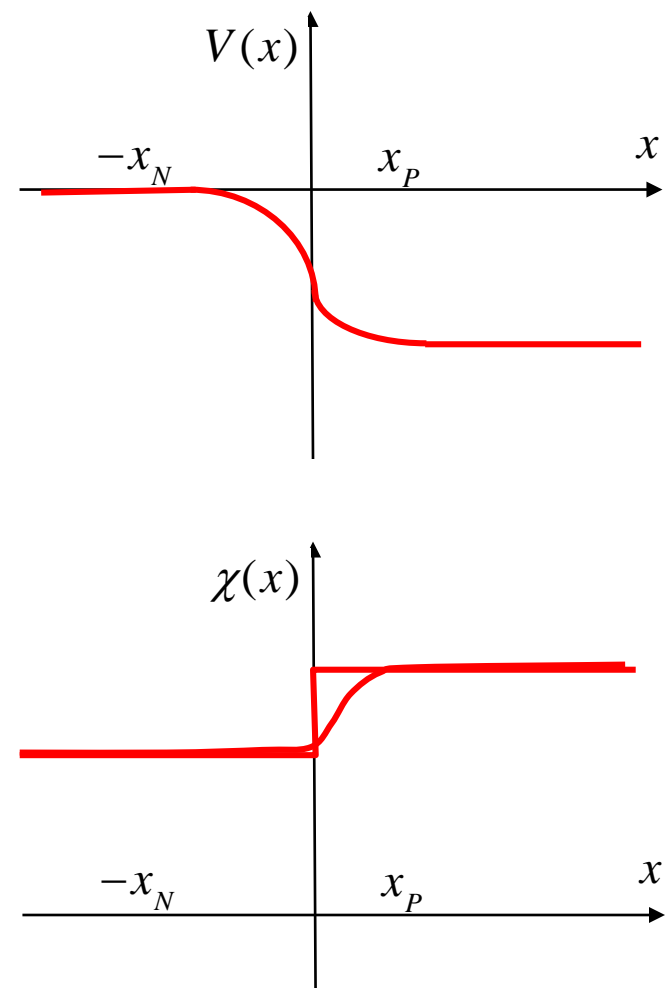
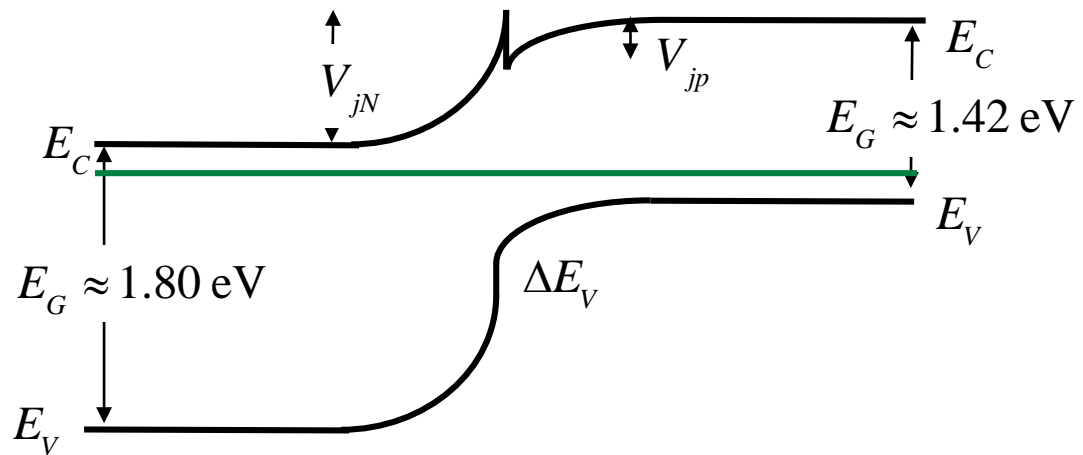
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- 4 • 27.4 Abrupt junction HBTs
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- 8 • 27.8 Modern Designs

status

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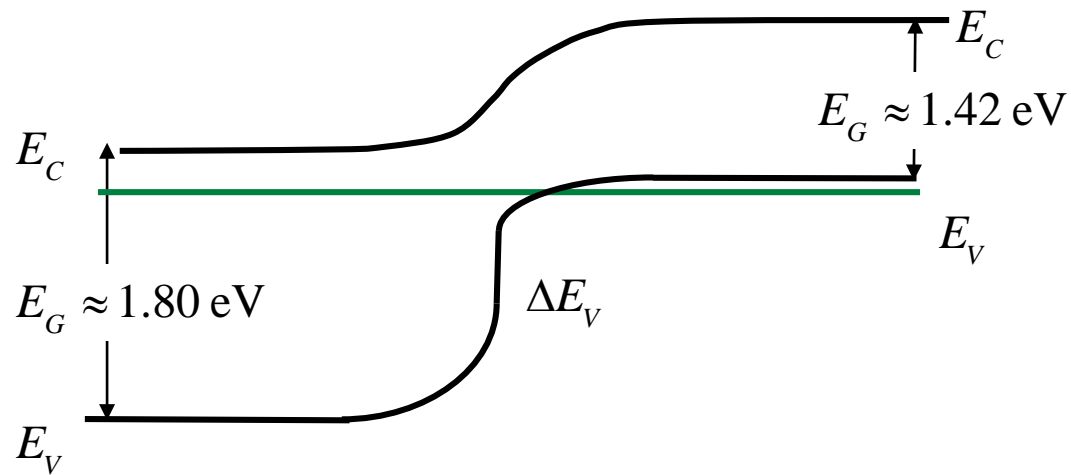
# Abrupt Junction



$$E_C(x) = E_0 - \chi(x) - qV(x)$$

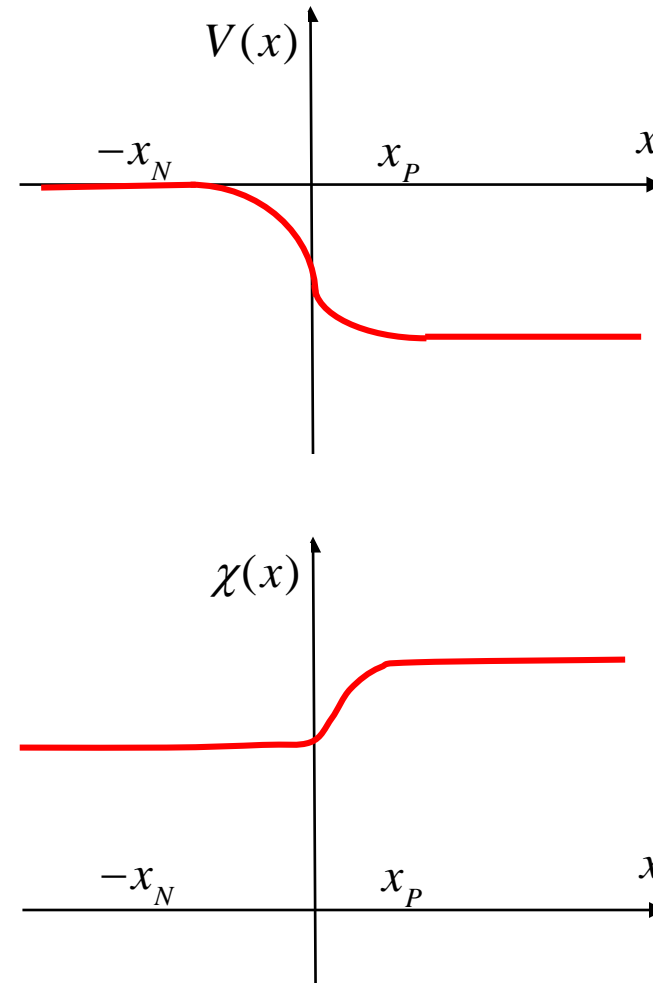
$$E_V(x) = E_C(x) - E_G(x)$$

# Graded Base-Emitter Junction



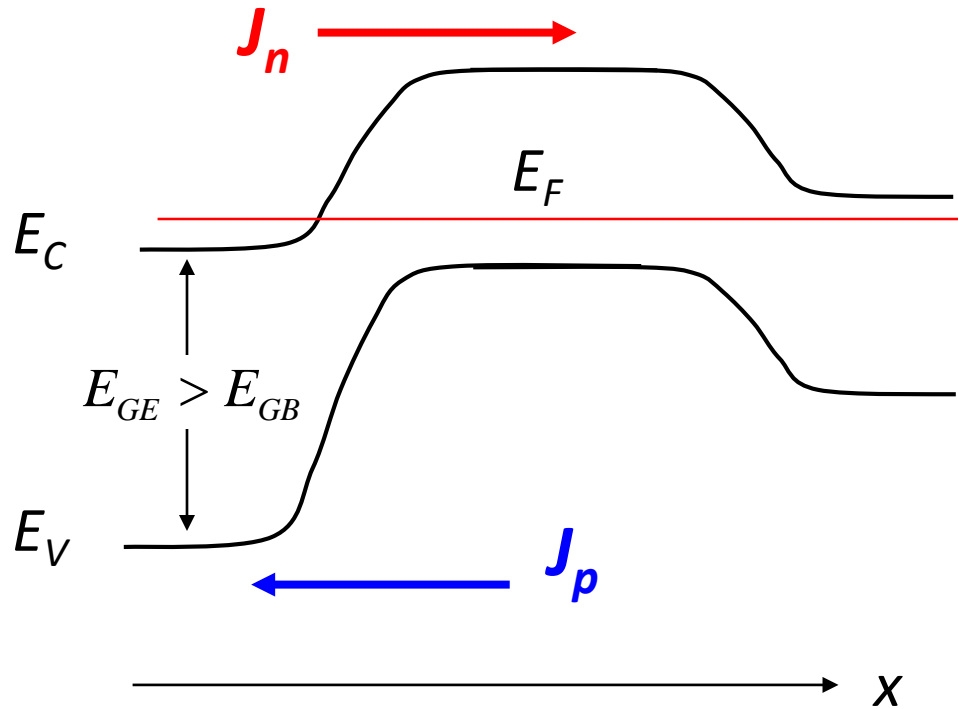
$$E_C(x) = E_0 - \chi(x) - qV(x)$$

$$E_V(x) = E_C(x) - E_G(x)$$



# Current Gain

No exponential Suppression!



$$J_n = q \left( \frac{n_{iB}^2}{N_{AB}} \right) \frac{D_n}{W_B} e^{qV_{BE}/k_B T}$$

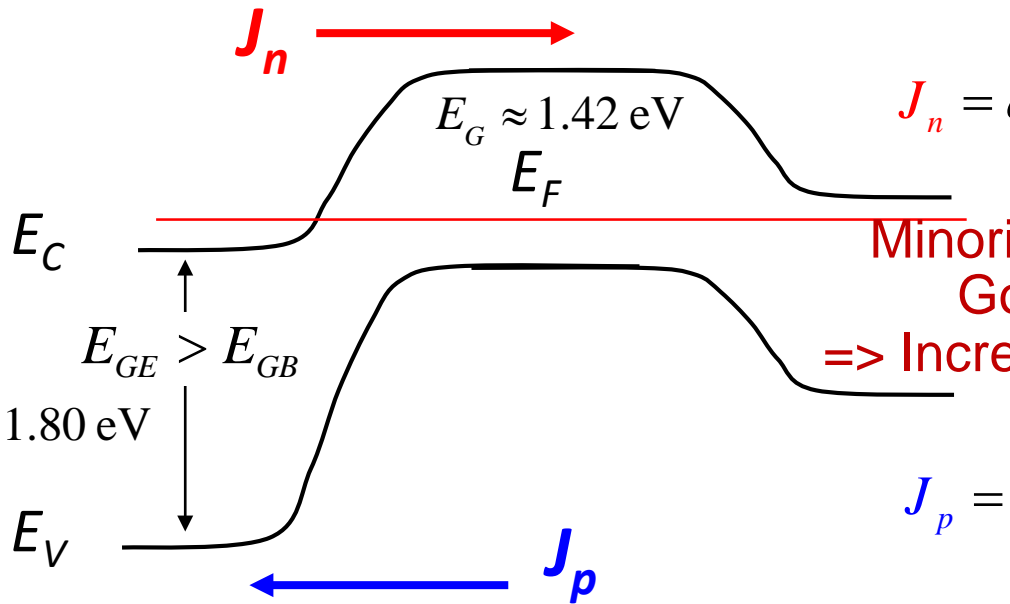
$$J_p = q \left( \frac{n_{iE}^2}{N_{DE}} \right) \frac{D_p}{W_E} e^{qV_{BE}/k_B T}$$

$$\beta = \frac{N_{DE}}{N_{AB}} \frac{D_n}{D_p} \frac{W_E}{W_B} \frac{n_{iB}^2}{n_{iE}^2}$$

$$n_i = \sqrt{N_C N_V} e^{-E_G/k_B T}$$

$$\beta_{DC} \approx \frac{N_{DE}}{N_{AB}} \frac{D_n}{D_p} \frac{W_E}{W_B} e^{\Delta E_G / k_B T}$$

# HBT Opportunities



$E_G \approx 1.80 \text{ eV}$

$E_G \approx 1.42 \text{ eV}$   
 $E_F$

$E_{GE} > E_{GB}$

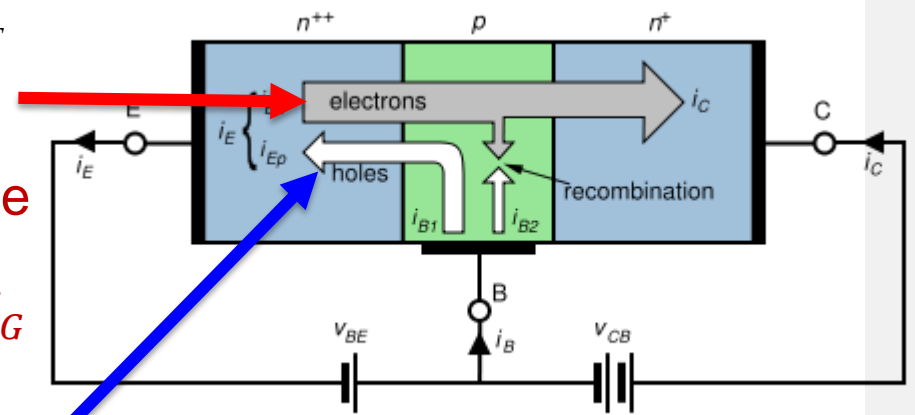
$E_C$   
 $E_V$

$J_p$

$$J_n = q \left( \frac{n_{iB}^2}{N_{AB}} \right) \frac{D_n}{W_B} e^{qV_{BE}/k_B T}$$

Minority electrons in base  
Goal: Increase  $I_C$   
 $\Rightarrow$  Increase  $n_i$  decrease  $E_G$

$$J_p = q \left( \frac{n_{iE}^2}{N_{DE}} \right) \frac{D_p}{W_E} e^{qV_{BE}/k_B T}$$



Minority holes in base

Goal: Decrease  $I_C$

$\Rightarrow$  Decrease  $n_i$  increase  $E_G$

Emitter bandgap > Base Bandgap

$$\beta_{DC} \approx \frac{N_{DE}}{N_{AB}} \frac{D_n}{D_p} \frac{W_E}{W_B} e^{\Delta E_G / k_B T}$$

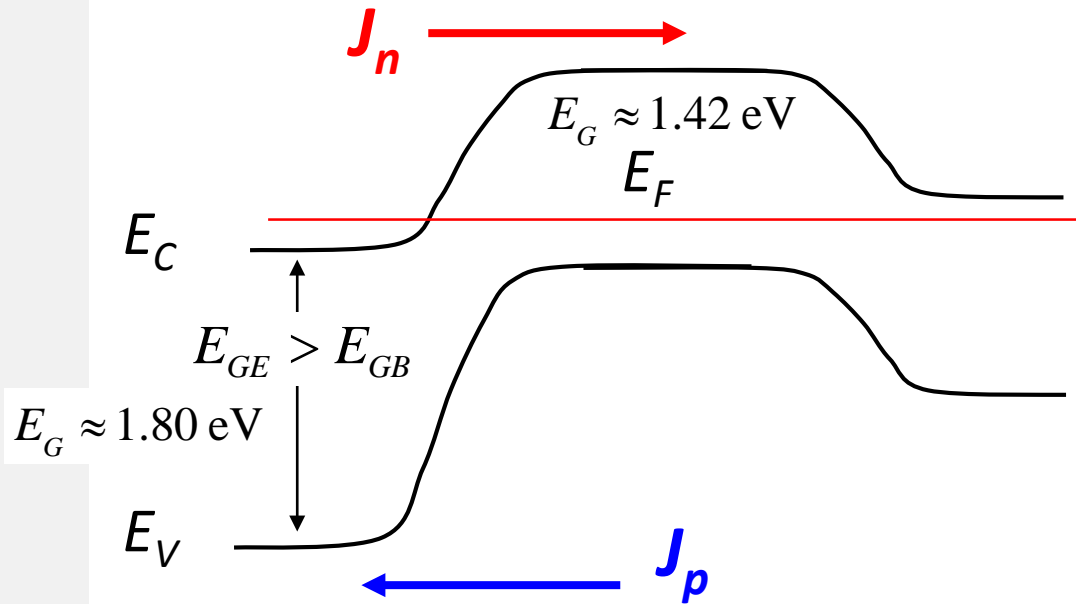
$$\Delta E_G = 1.8 \text{ eV} - 1.42 \text{ eV} = 380 \text{ meV}$$

$$k_B T \approx 25 \text{ meV}$$

$$e^{380/25} = e^{15.5} \approx 4 \times 10^6$$

$\Rightarrow$  Opportunity for alternative thinking!

# Advantages of HBT: Inverted Base Doping



$$\beta_{DC} \approx \frac{N_{DE}}{N_{AB}} \frac{D_n W_E}{D_p W_B} e^{\Delta E_G / k_B T}$$

$$\Delta E_G = 1.8eV - 1.42eV = 380meV$$

$$k_B T \approx 25meV$$

$$e^{380/25} = e^{15.5} \approx 4 \times 10^6$$

=> Opportunity for alternative thinking!

Thin base desired for speed and gain, but thin base was a problem (Early, Punch Through)

Increasing base doping was not an option since it lowered  $\beta_{DC}$

Now this is possible! => Very heavily doped base

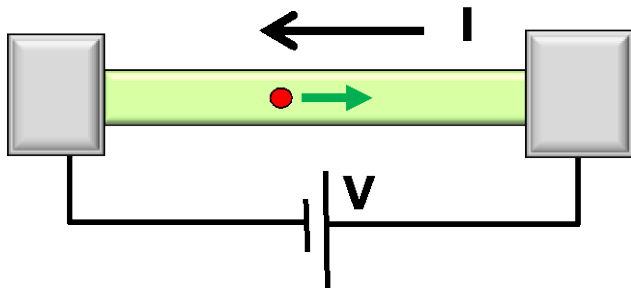
=> prevent Punch Through, reduce Early effect, and to lower  $R_{ex}$

Moderately doped Emitter (lower  $C_{j,BE}$ )

**“inverted base doping”**

$$N_{AB} \gg N_{DE}$$

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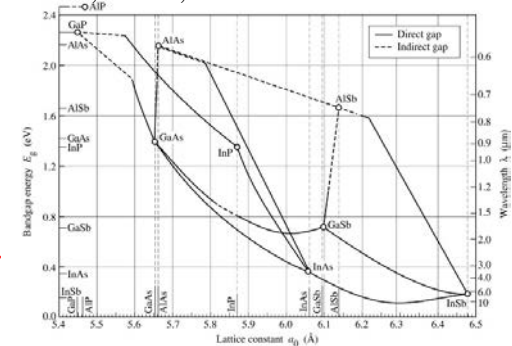
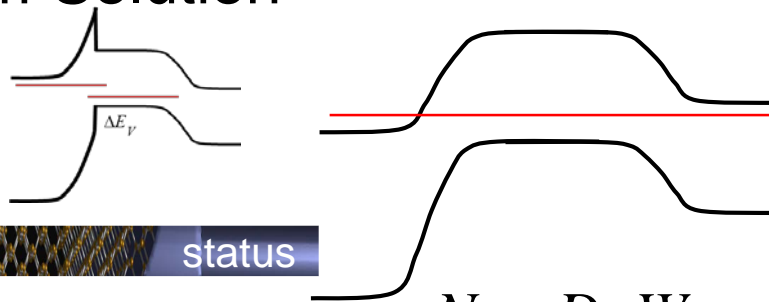
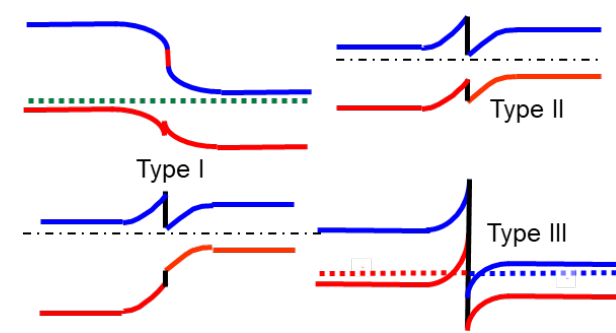


Fig. 7.6. Bandgap energy and lattice constant of various III-V semiconductors at room temperature (adopted from Tien, 1988).



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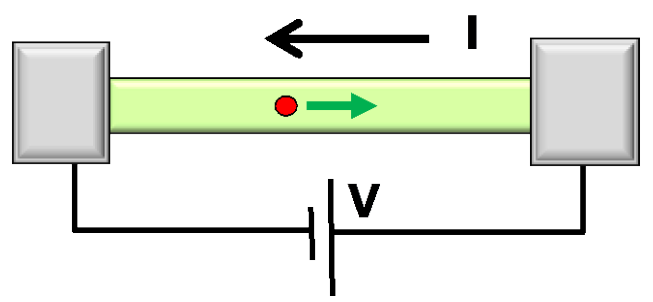
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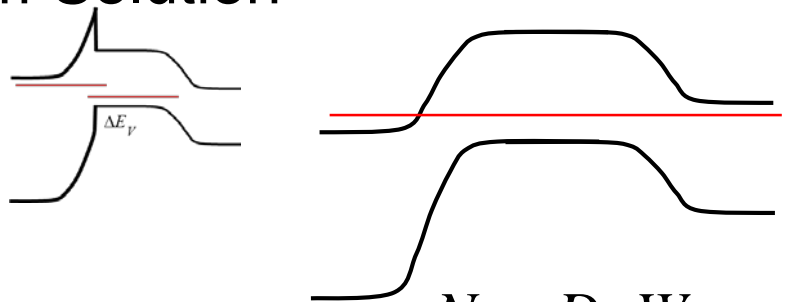
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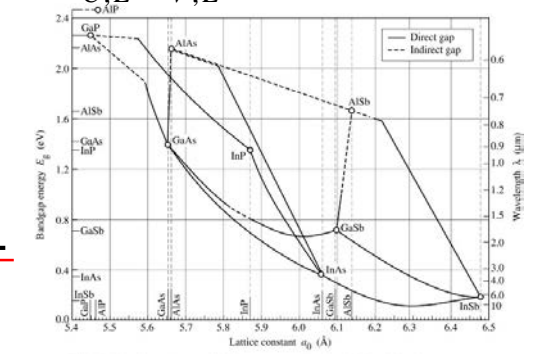
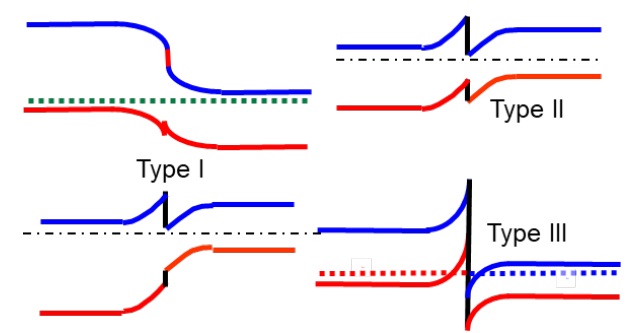


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