

## Section 23 Schottky Diode

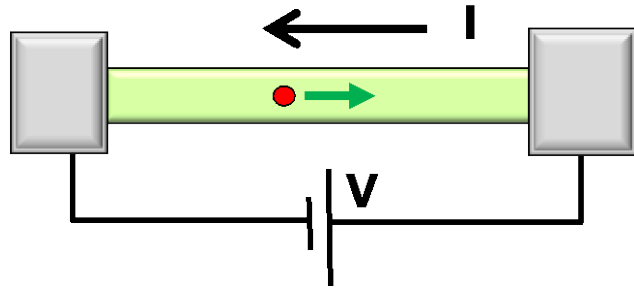
### 23.2 Physical Processes

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School of Electrical and  
Computer Engineering

# Section 23 Schottky Diode



$$I = G \times V$$

$$= q \times n \times v \times A$$

↑ charge density   
 ↑ velocity   
 area

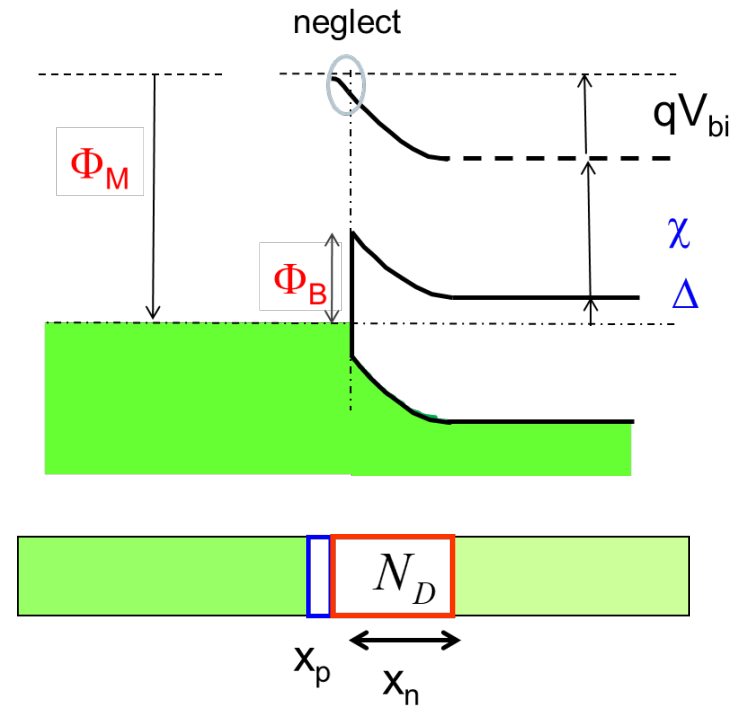
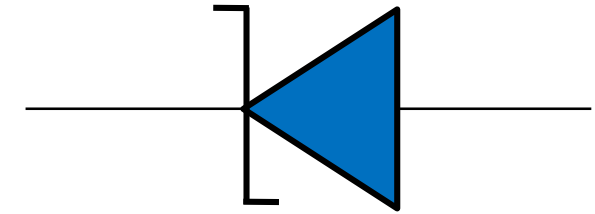
## • 23.1 Basics

- » Equilibrium band-diagram
- » DC Thermionic current (simple derivation)

## • 23.2 Physical Processes

- » DC Thermionic current (detailed derivation)
- » Recombination/Generation/Ionization
- » AC and Large Signal Response

## • 23.4 Practical Issues



$$J_T = J_{s \rightarrow m}(0) - J_{s \rightarrow m}(V_A) = \frac{q n_m v_{th}}{2} N_D e^{\frac{-q \Phi_B}{kT}} \left[ e^{\frac{q V_A}{kT}} - 1 \right]$$

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# Energy Resolved Thermionic Flux

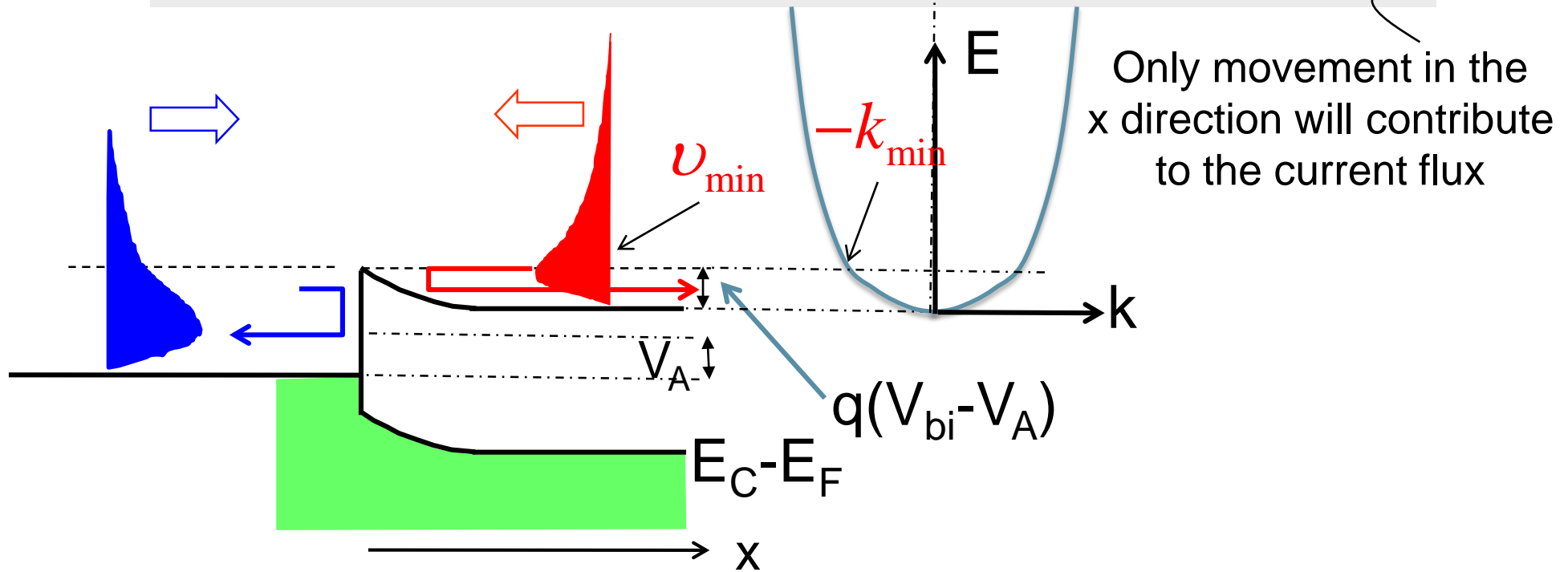
Energy  $< \frac{1}{2} m^* v_{\min}^2$

will be bounced back

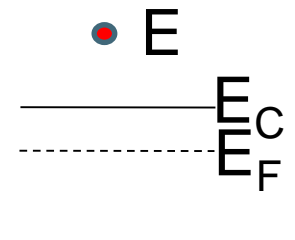
**~ DOS**

Occupation (non-degenerate)

$$J_{s \rightarrow m} = -q \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{-k_{\min}} \frac{\Omega}{4\pi^3} dk_x dk_y dk_z e^{-(E-E_F)\beta} v_x$$



# Thermionic Flux from Semi to Metal ..

$$J_{s \rightarrow m} = -q \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{-k_{\min}} \frac{\Omega}{4\pi^3} dk_x dk_y dk_z e^{-(E-E_F)\beta} v_x$$


$$E - E_F = (E - E_C) + (E_C - E_F) = \frac{1}{2} m^* v_x^2 + \frac{1}{2} m^* v_y^2 + \frac{1}{2} m^* v_z^2 + (E_C - E_F)$$

$$= q e^{-(E_C - E_F)\beta} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{-v_{\min}} \frac{\Omega}{4\pi^3} \frac{d(m^* v_x)}{\hbar} \frac{d(m^* v_y)}{\hbar} \frac{d(m^* v_z)}{\hbar} e^{-\frac{(m v_x^2 + m v_y^2 + m v_z^2)}{2} \beta} v_x$$

$$J_{s \rightarrow m} = \frac{q\Omega (m^*)^3}{4\pi^3 \hbar^3} e^{-(E_C - E_F)\beta} \left[ \int_{-\infty}^{\infty} e^{-\left(\frac{m^* v_y^2}{2}\right)\beta} dv_y \right] \left[ \int_{-\infty}^{\infty} e^{-\left(\frac{m^* v_z^2}{2}\right)\beta} dv_z \right] \left[ \int_{-\infty}^{-v_{\min}} dv_x e^{-\left(\frac{m^* v_x^2}{2}\right)\beta} v_x \right]$$

# Thermionic Current ...

$$v_{\min} = \sqrt{\frac{2q}{m^*} (V_{bi} - V_A)}$$

$$J_{s \rightarrow m} = \frac{q\Omega(m^*)^3}{4\pi^3\hbar^3} e^{-(E_c - E_F)\beta} \left[ \int_{-\infty}^{\infty} e^{-\left(\frac{m^*v_y^2}{2}\right)\beta} dv_y \right] \left[ \int_{-\infty}^{\infty} e^{-\left(\frac{m^*v_z^2}{2}\right)\beta} dv_z \right] \left[ \int_{-\infty}^{-v_{\min}} dv_x e^{-\left(\frac{m^*v_x^2}{2}\right)\beta} v_x \right]$$

$\downarrow$   $\sqrt{\pi}$        $\downarrow$   $\sqrt{\pi}$        $\downarrow$   $\frac{1}{2} e^{-q(V_{bi} - V_A)\beta}$

$$J_{s \rightarrow m} = \frac{4\pi q m^* k^2}{h^3} T^2 e^{(E_F - E_C - qV_{bi})\beta} e^{qV_A\beta} = A_0 e^{qV_A\beta}$$

$$J_T = J_{s \rightarrow m} - J_{m \rightarrow s} = A_0 \left( e^{qV_A\beta} - 1 \right)$$

# Some insight of the Thermionic Current ...

Compare to the current of p-n diodes...

$$J_T = J_{s \rightarrow m} - J_{m \rightarrow s} = A_0 \left( e^{qV_A \beta} - 1 \right) \quad \text{Schottky diode}$$

$$J_T = -q \left[ \frac{D_n}{W_p} \frac{n_i^2}{N_A} + \frac{D_p}{W_n} \frac{n_i^2}{N_D} \right] \left( e^{qV_A \beta} - 1 \right) \quad \text{p-n diode}$$

Both of them depends exponentially on  $V_A$ , however current of p-n diodes depends more on temperature (since  $n_i$  depends strongly on  $E_g$ ), where the Schottky diode doesn't have that dependence.

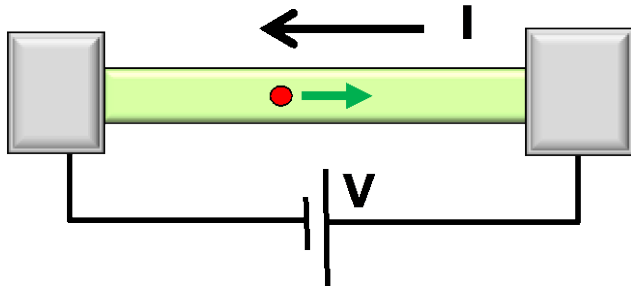
However,  $E_g$  hides in...

$$J_{s \rightarrow m} = \frac{4\pi q m^* k^2}{h^3} T^2 e^{(E_F - E_C - qV_{bi})\beta} e^{qV_A \beta} = A_0 e^{qV_A \beta}$$

The information of material hides in  $m^*$

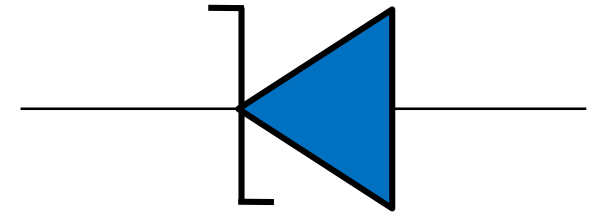
The information of doping concentration hides in  $E_F - E_C$

# Section 23 Schottky Diode

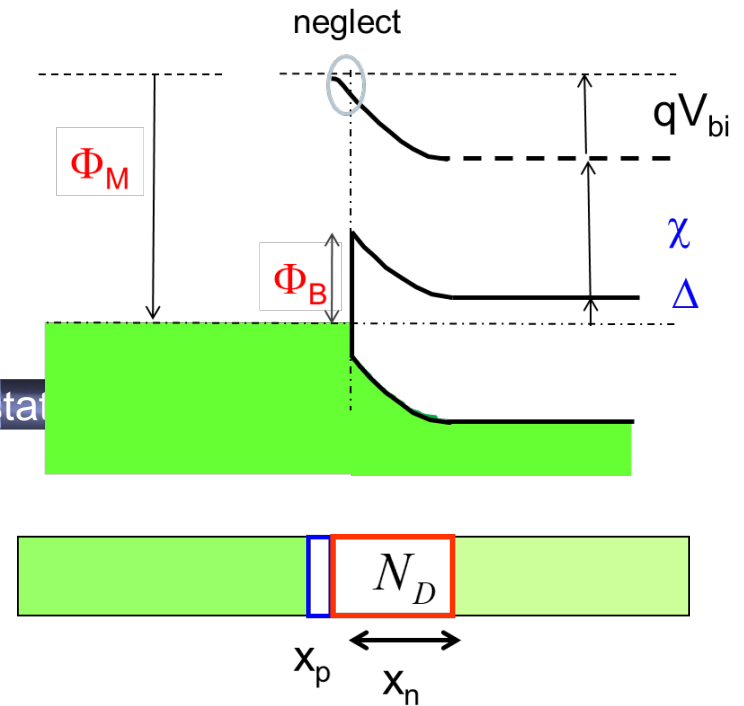


$$I = G \times V$$

$$= \underset{\substack{\uparrow \\ \text{charge density}}}{q} \times \underset{\substack{\uparrow \\ \text{density}}}{n} \times \underset{\substack{\uparrow \\ \text{velocity}}}{v} \times \underset{\substack{\uparrow \\ \text{area}}}{A}$$



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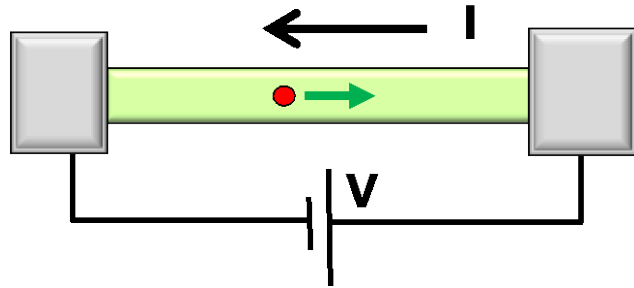
$$J_{s \rightarrow m} = \frac{4\pi q m^* k^2}{h^3} T^2 e^{(E_F - E_C - qV_{bi})/\beta} e^{qV_A/\beta} = A_0 e^{qV_A/\beta}$$

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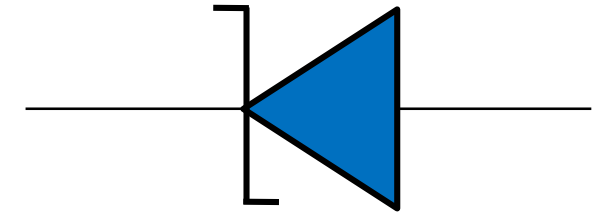
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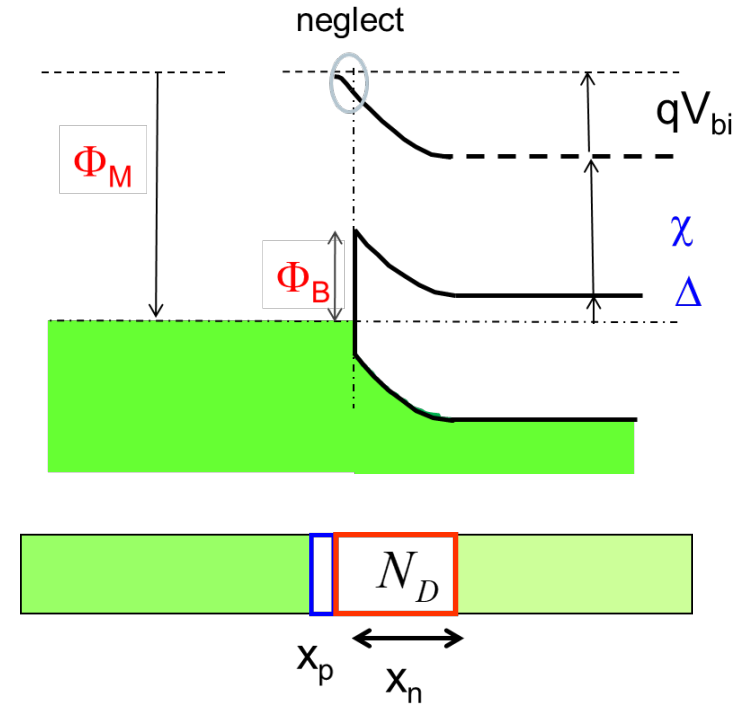
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$$J_{s \rightarrow m} = \frac{4\pi q m^* k^2}{h^3} T^2 e^{(E_F - E_C - qV_{bi})/\beta} e^{qV_A/\beta} = A_0 e^{qV_A/\beta}$$

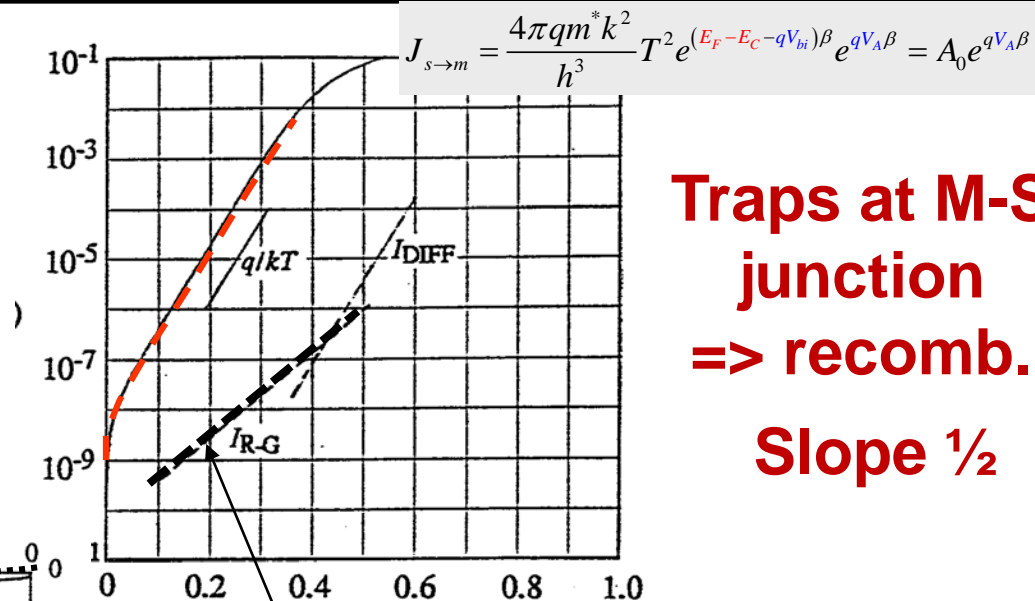
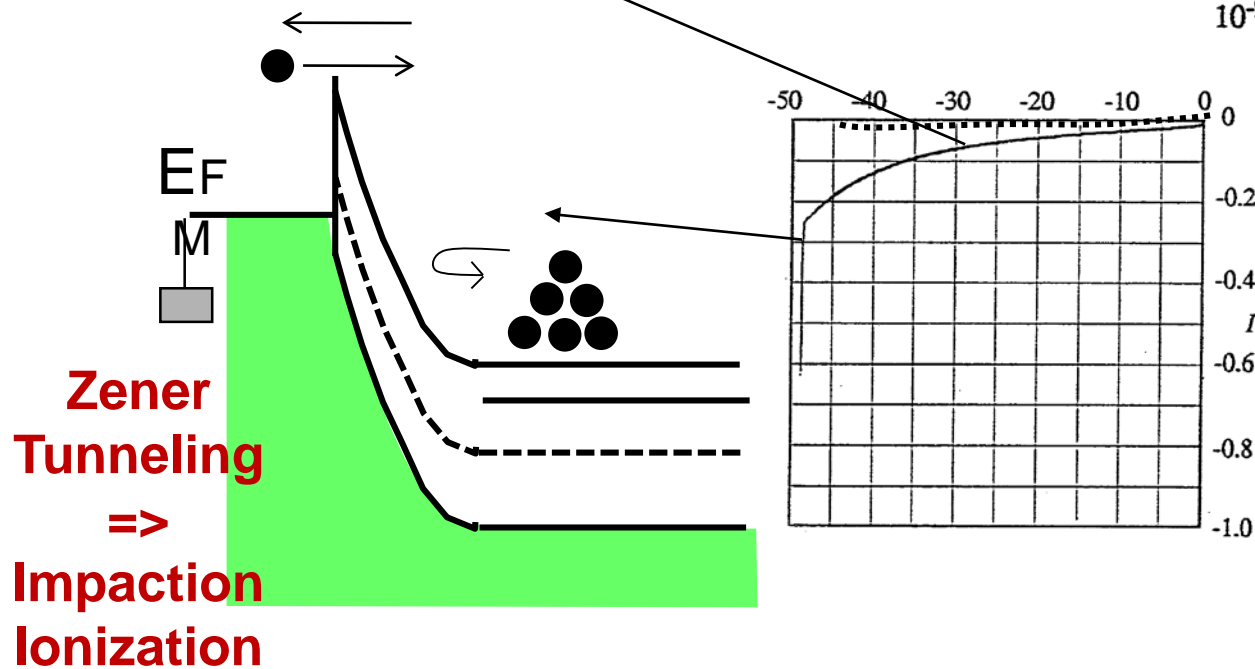
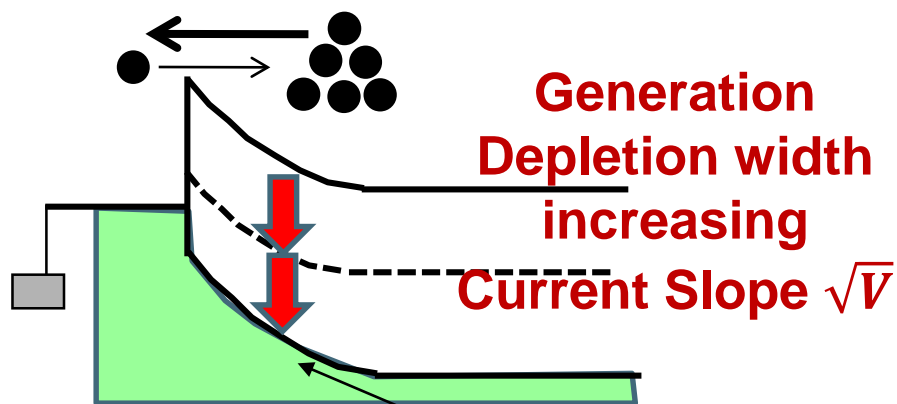
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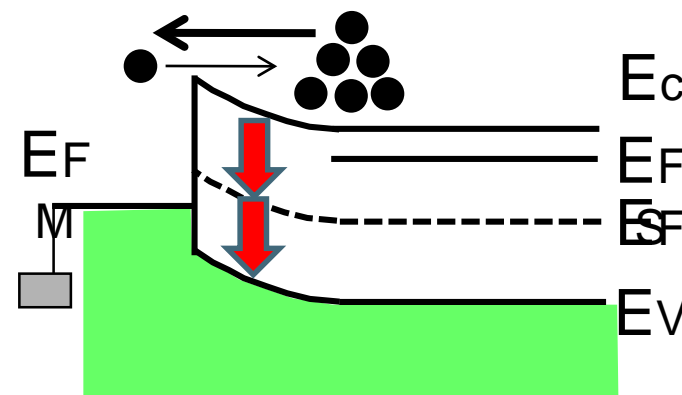
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# Recombination/Generation/Impact-ionization



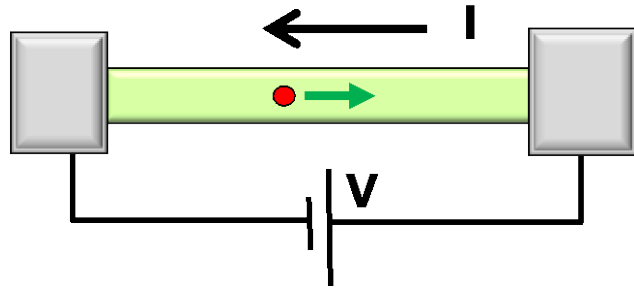
**Traps at M-S junction**  
**=> recomb.**  
**Slope  $1/2$**



$$I = I_o \left( e^{q(V_A - R_S I)\beta / m} - 1 \right)$$

**SAME technique as in p-n junction except integrate to  $x_p$  only**  
**=> ONE sided junction**

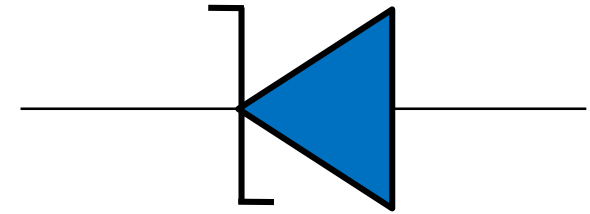
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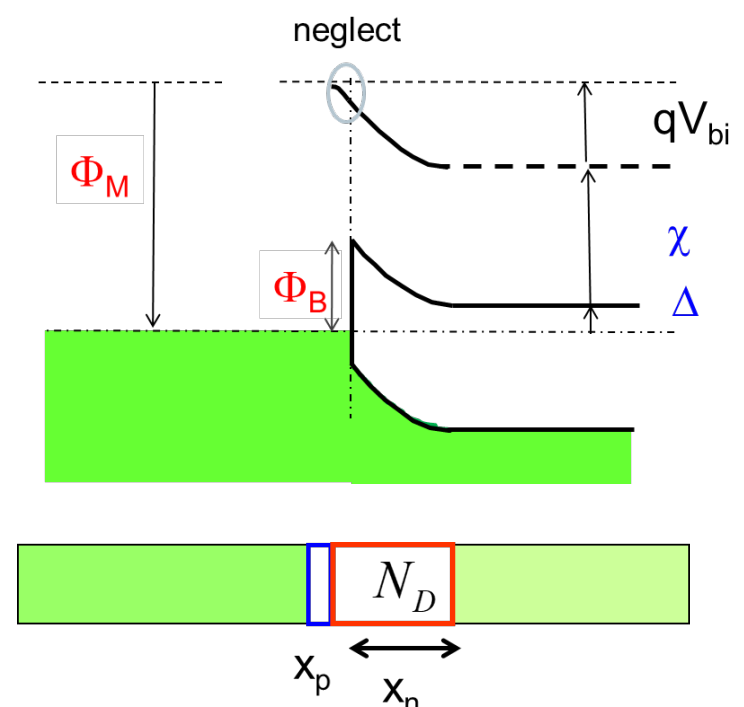
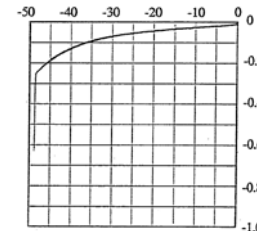
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$$J_{s \rightarrow m} = \frac{4\pi q m^* k^2}{h^3} T^2 e^{(E_F - E_C - qV_{bi})/\beta} e^{qV_A/\beta} = A_0 e^{qV_A/\beta}$$

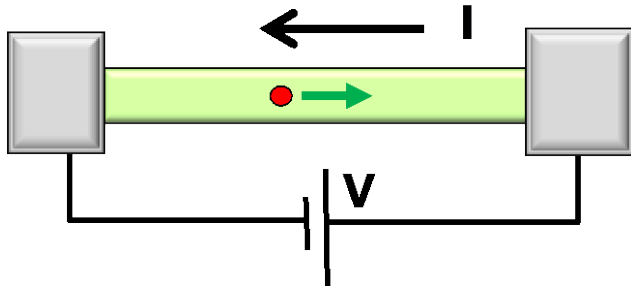
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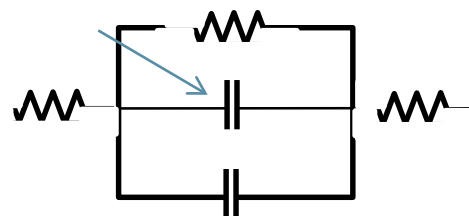
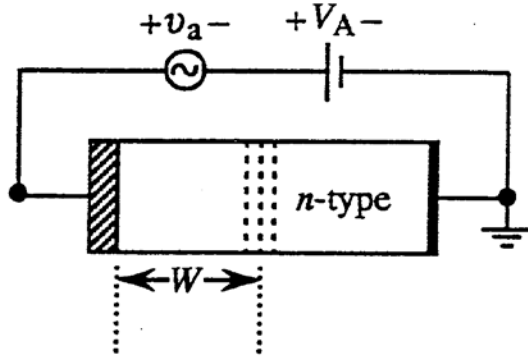
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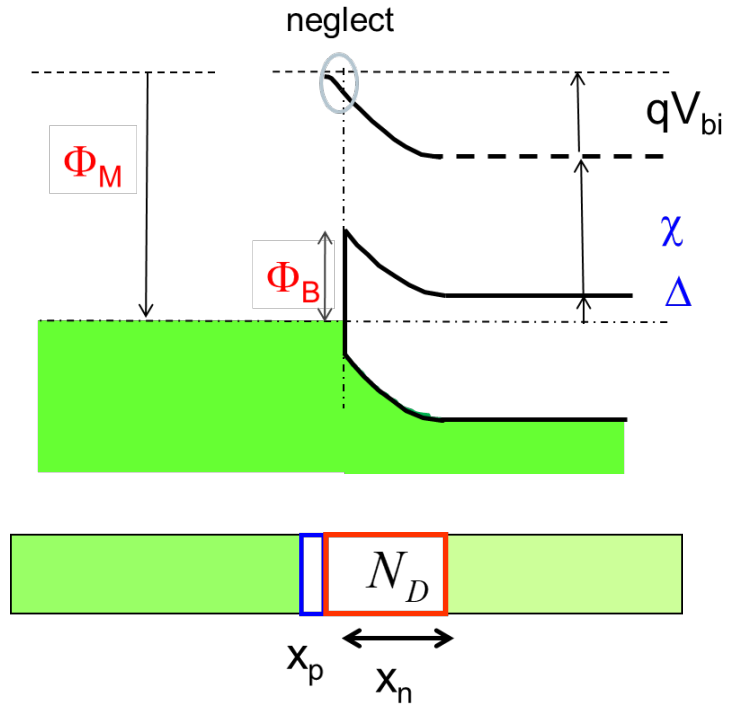
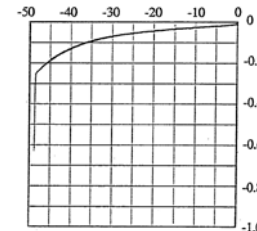
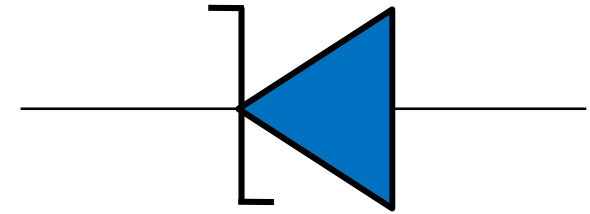
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$$I = I_o \left( e^{q(V_A - R_S I)\beta / m} - 1 \right)$$



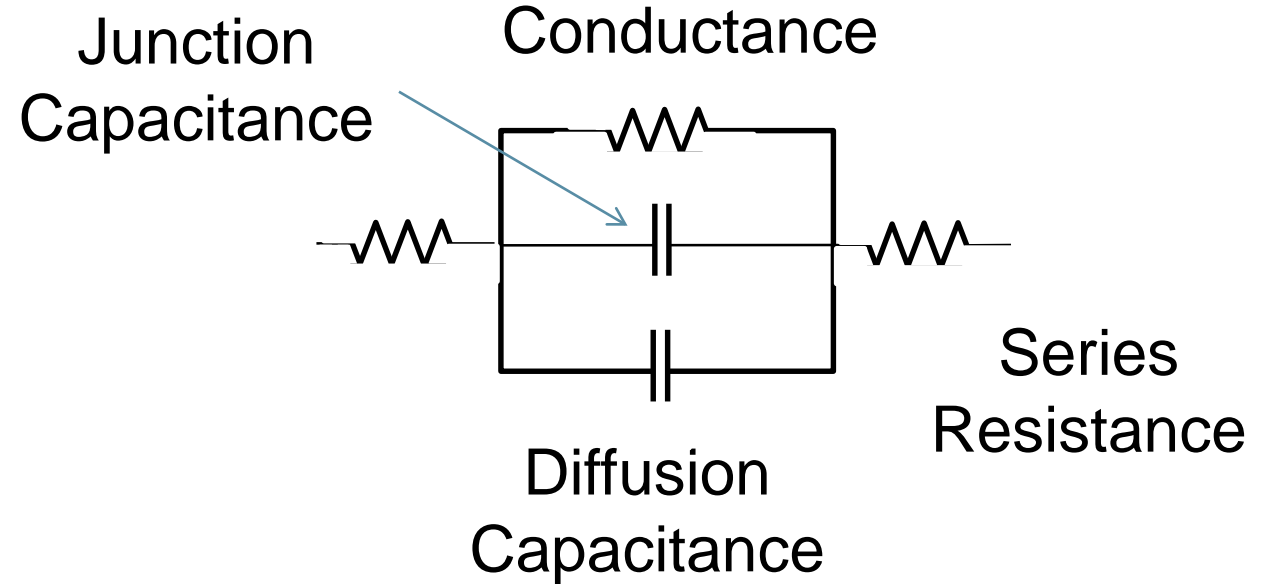
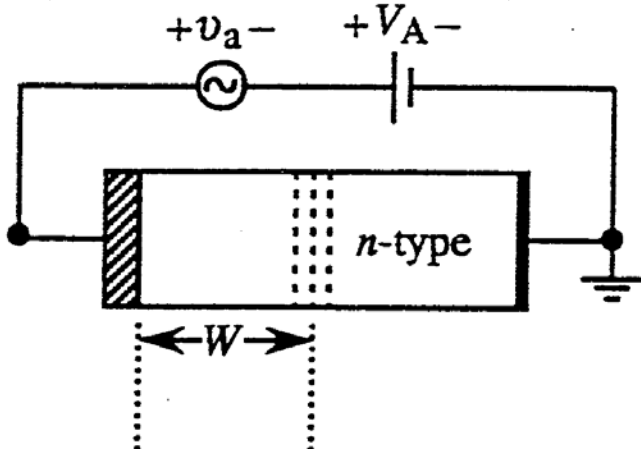
Video

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# AC response

$$I = I_o \left( e^{q(V_A - R_S I) \beta / m} - 1 \right)$$



We will not have Diffusion Capacitance here...

# Forward Bias Conductance

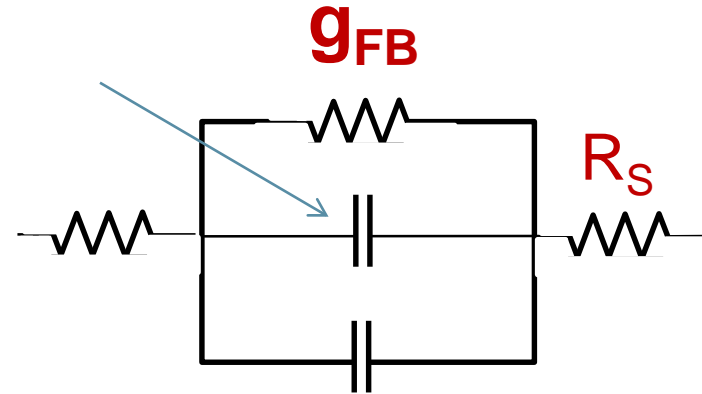
$m$  depends on which operation regime you are

$$I = I_o \left( e^{q(V_A - R_S I)\beta / m} - 1 \right)$$

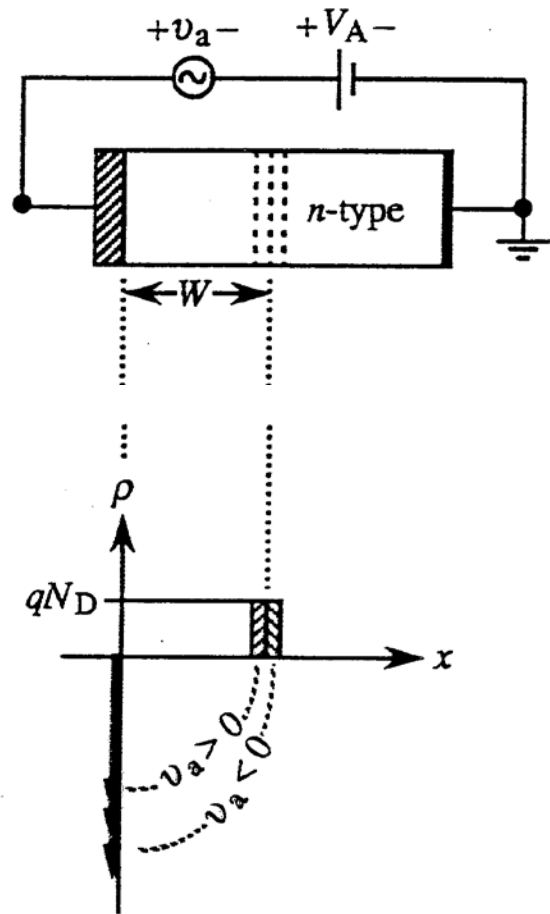
$$\ln \frac{I + I_o}{I_o} = q(V_A - R_S I)\beta / m$$

$$\frac{m}{q\beta(I + I_o)} = \frac{dV_A}{dI} - R_S$$

$$\frac{1}{g_{FB}} = R_S + \frac{m}{q\beta(I + I_o)}$$

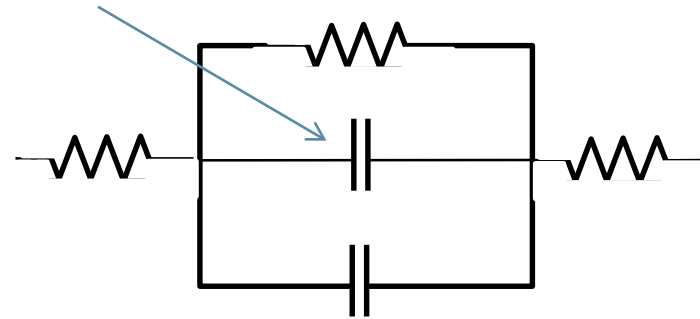


# Junction Capacitance (Majority Carriers)



Response time – dielectric  
Very fast propagation

Junction  
Capacitance

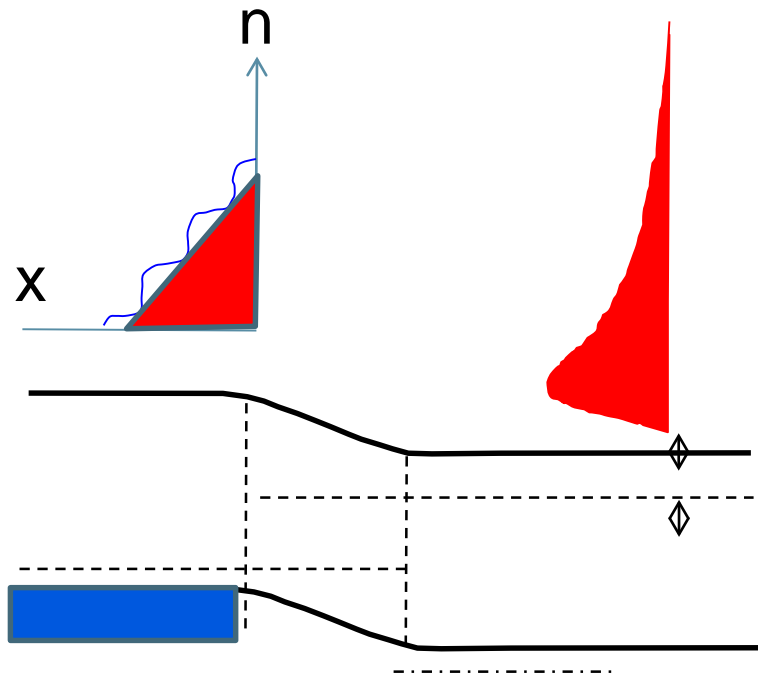


$$C_J = \frac{\kappa_s \epsilon_0 A}{W}$$

$$C_J = \frac{\kappa_s \epsilon_0 A}{\sqrt{\frac{2\kappa_s \epsilon_0}{qN_D} (V_{bi} - V_A)}}$$

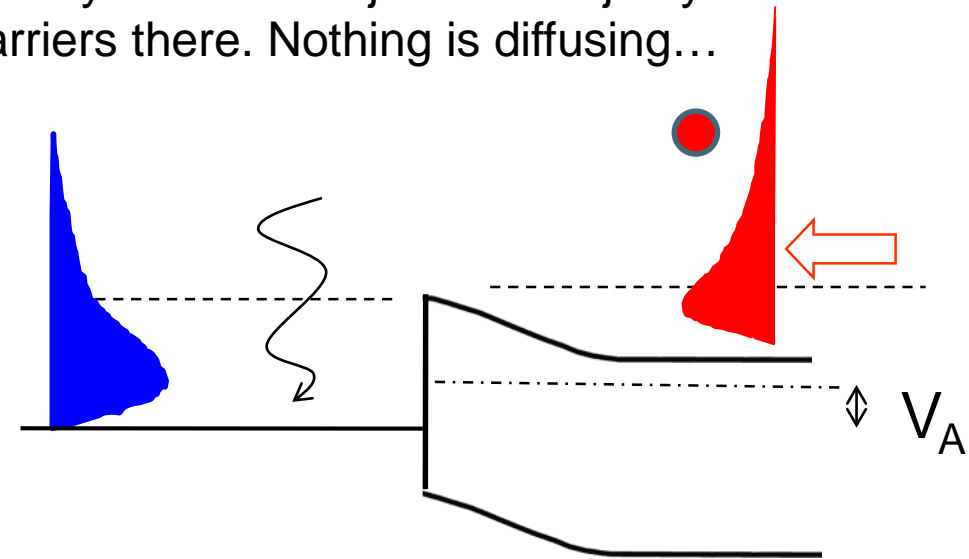
# No Diffusion Capacitance in Schottky Diode

## p-n Diode



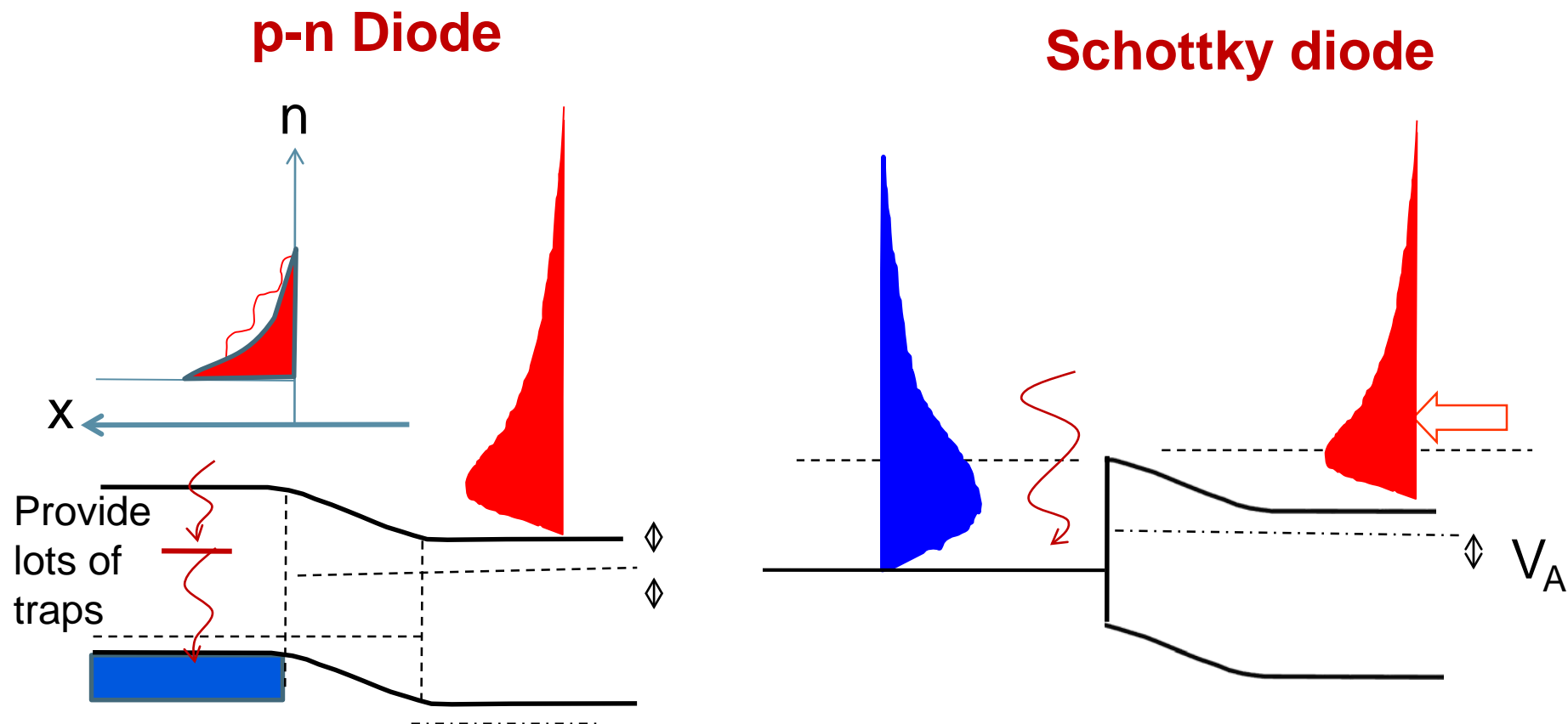
## Schottky diode

When electrons reach the metal side, they quickly scatter and join the majority carriers there. Nothing is diffusing...



No minority carrier transport and therefore no diffusion capacitance ..

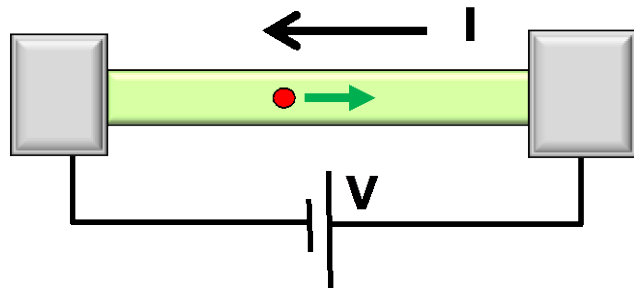
# Reducing diffusion capacitance in p-n diode



Short minority carrier lifetime in p-n junction diode equivalent to rapid energy relaxation in SB diode.



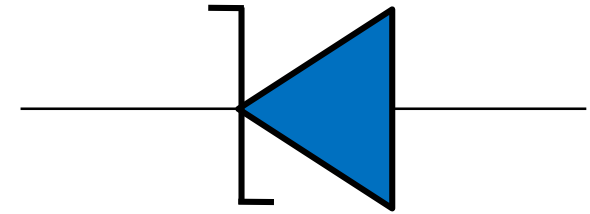
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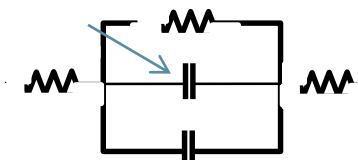
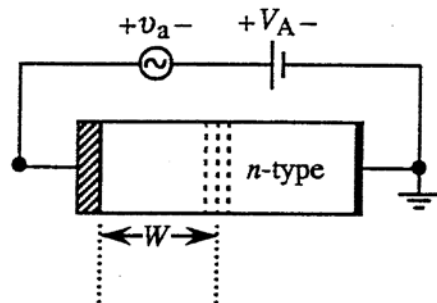
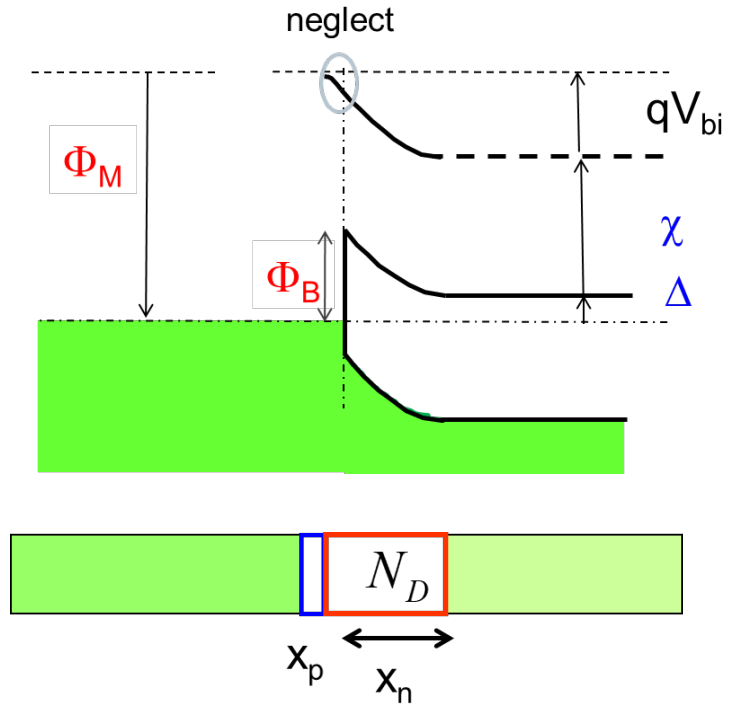
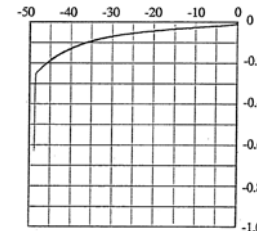
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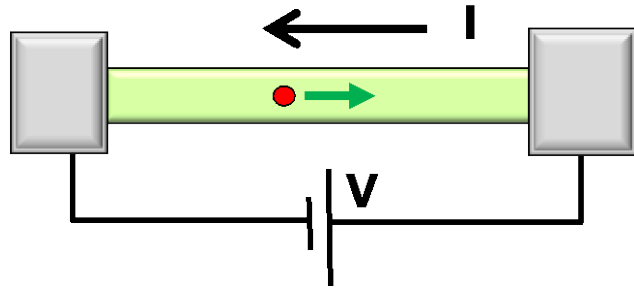
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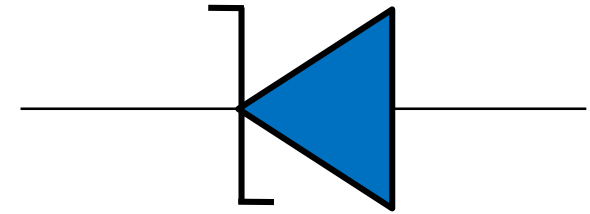
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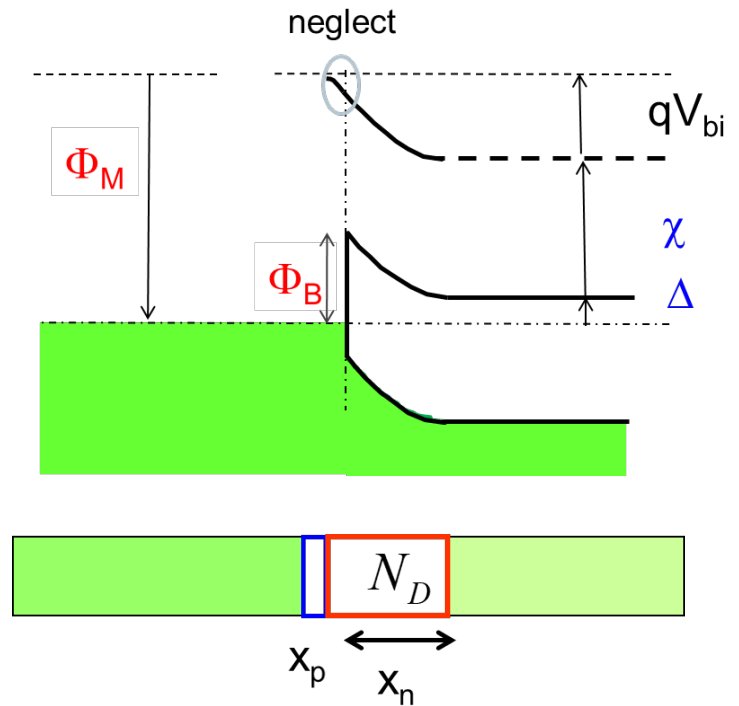
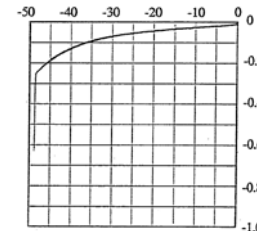
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  - » Schottky Barrier Lowering – Image Charges
  - » Fermi Level Pinning



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