

Section 14 Doping

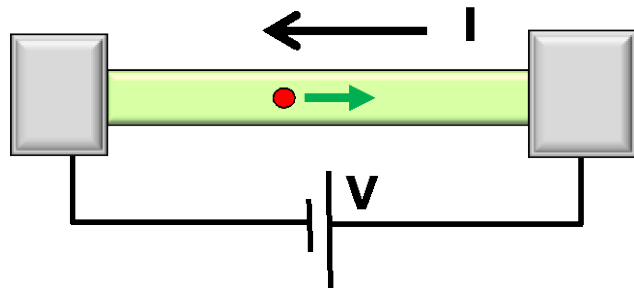
14.4 Multiple doping, co-doping, and heavy-doping

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School of Electrical and
Computer Engineering

Section 14 Doping

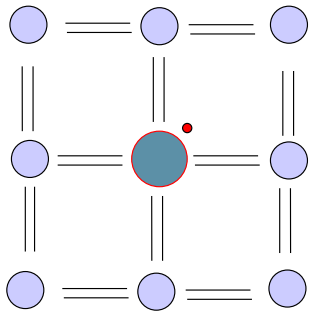


$$I = G \times V$$

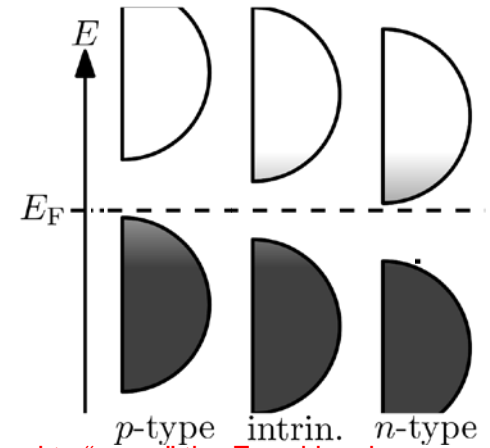
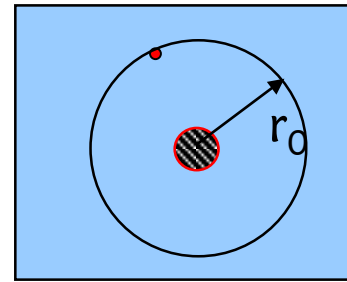
$$= q \times n \times v \times A$$

↑ charge density ↑ velocity area

• 14.1 Basic concepts of donors and acceptors

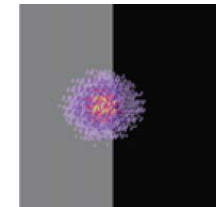
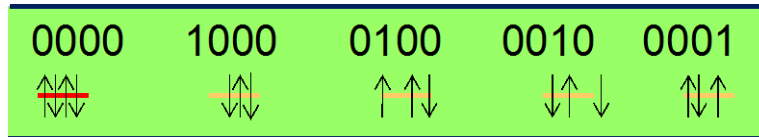


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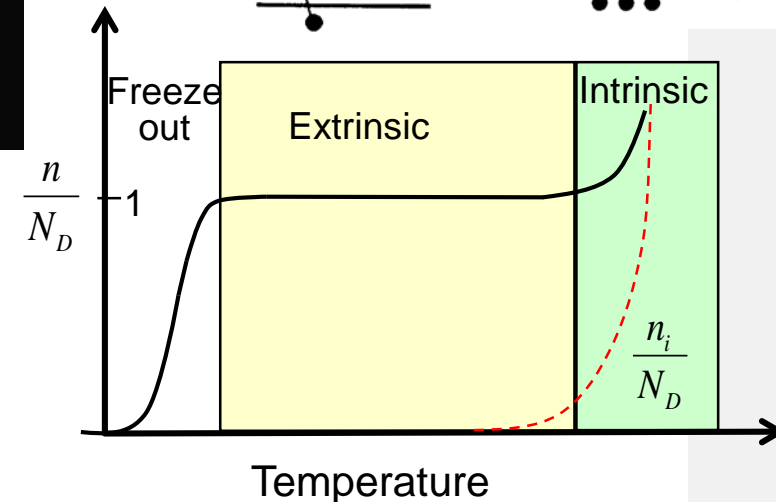
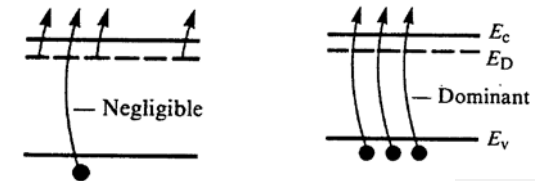


- » Need to "move" the Fermi level
- » "add" electrons – n-type doping – E_F close to E_C
- » "add" holes – p-type doping – E_F close to E_V

• 14.2 Statistics of donor and acceptor levels



$$N_V e^{-(E_F - E_V)/k_B T} - N_C e^{-(E_C - E_F)/k_B T} + \frac{N_D}{1 + 2e^{(E_F - E_D)/k_B T}} - \frac{N_A}{1 + 4e^{(E_A - E_F)/k_B T}} = 0$$



• 14.3 Temperature dependence of carrier concentration

• 14.4 Multiple doping, co-doping, and heavy-doping

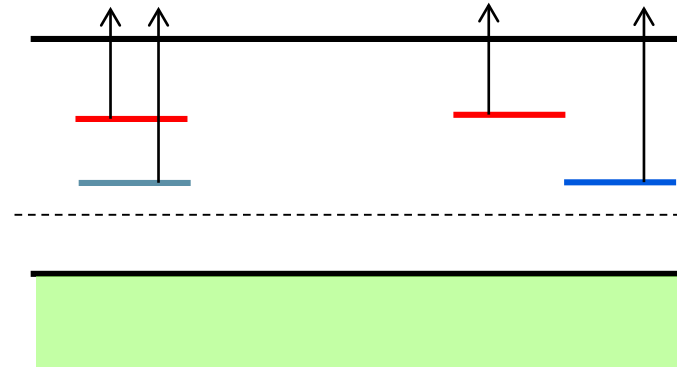
Video

Video

Video

Video

Multiple Donor Levels



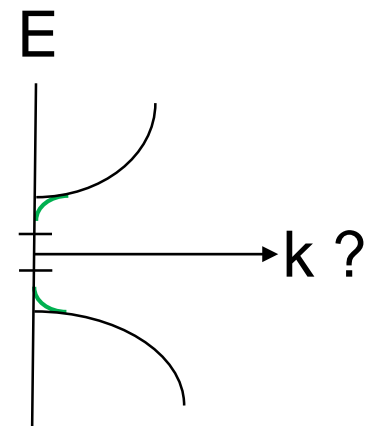
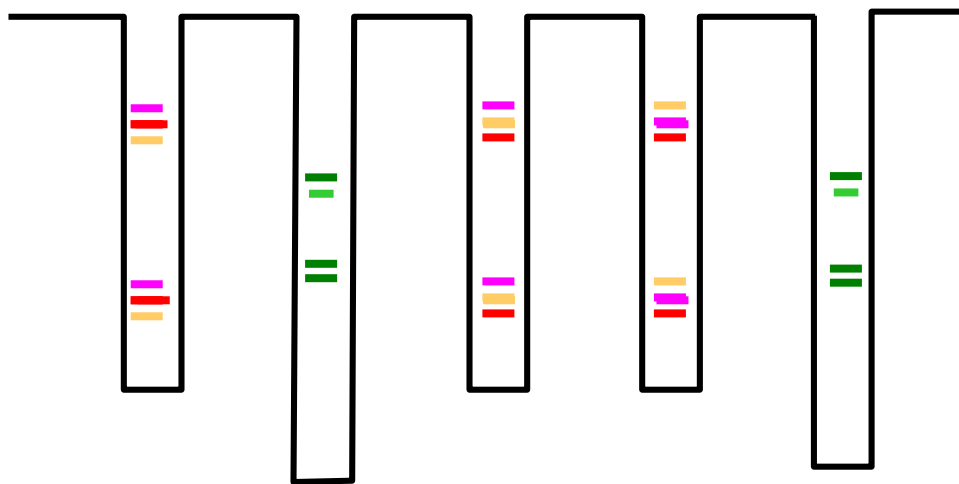
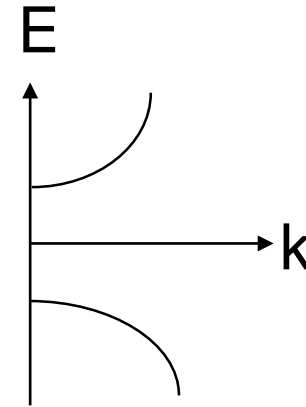
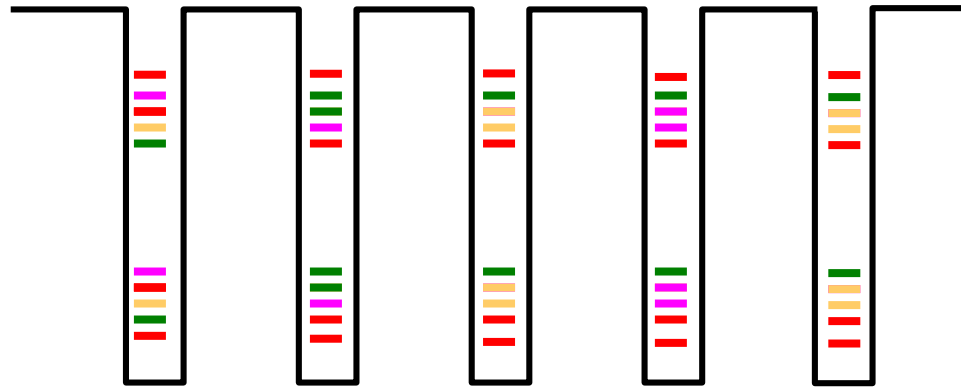
Multiple levels of same donor ...

$$p - n + \frac{N_D}{1 + 2e^{(E_F - E_{D1})/k_B T}} + \frac{N_D}{1 + 2e^{(E_F - E_{D2})/k_B T}} - \frac{N_A}{1 + 4e^{(E_A - E_F)/k_B T}} = 0$$

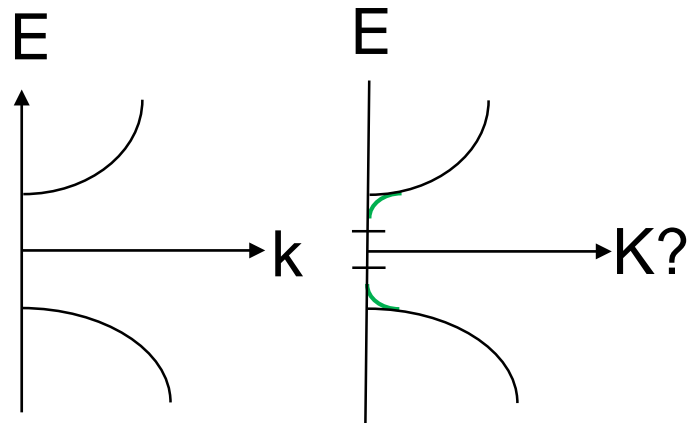
Codoping...

$$p - n + \frac{N_{D1}}{1 + 2e^{(E_F - E_{D1})/k_B T}} + \frac{N_{D2}}{1 + 2e^{(E_F - E_{D2})/k_B T}} - \frac{N_A}{1 + 4e^{(E_A - E_F)/k_B T}} = 0$$

Heavy Doping Effects: Bandtail States



Heavy Doping Effects: Hopping Conduction



Bandgap narrowing

$$p \times n = N_C N_V e^{-\beta E_G^*}$$

e.g. Base of HBTs



Band transport
vs.
hopping-transport

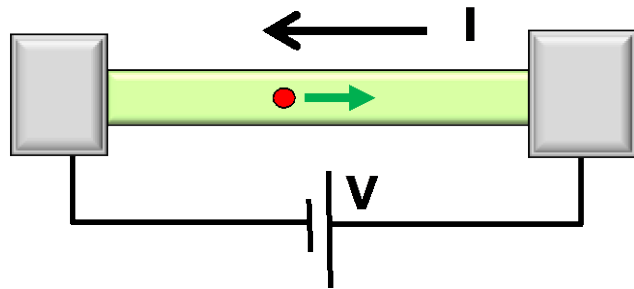
e.g. a-silicon, OLED

Conclusions

$$N_V e^{-(E_F - E_V)/k_B T} - N_A e^{-(E_C - E_F)/k_B T} + \frac{N_D}{1 + 2e^{(E_F - E_D)/k_B T}} - \frac{N_A}{1 + 4e^{(E_A - E_F)/k_B T}} = 0$$

1. Charge neutrality condition and law of mass-action allows calculation of Fermi-level and all carrier concentration.
2. For semiconductors with field, charge neutrality will not hold and we will need to use Poisson equation.
3. Heaving doping effects play an important role in carrier transport.

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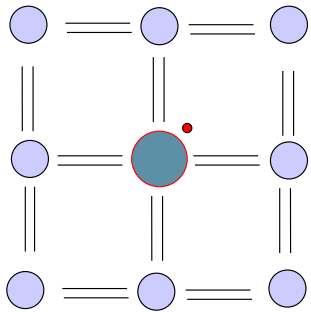


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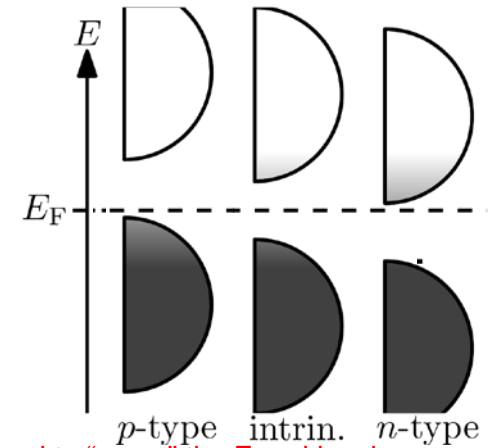
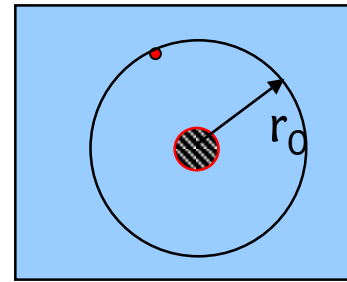
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 ↑ velocity
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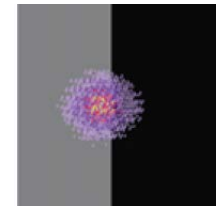
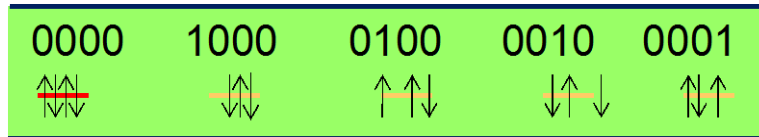


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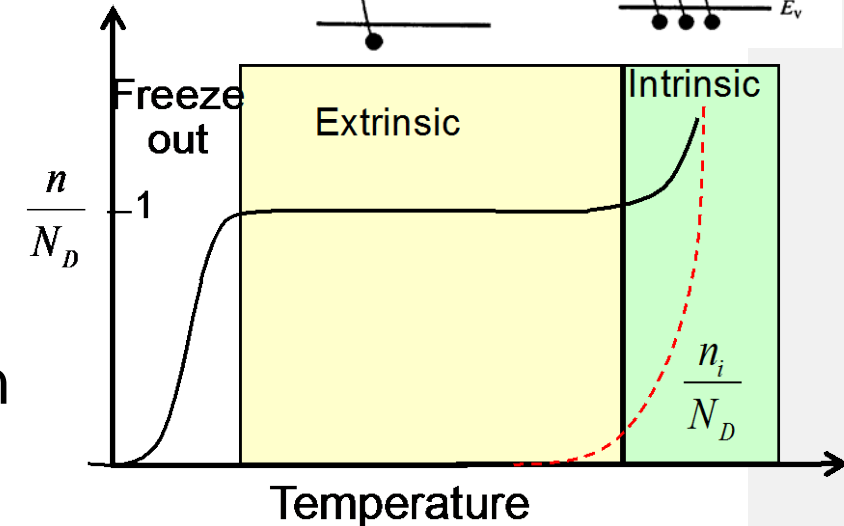
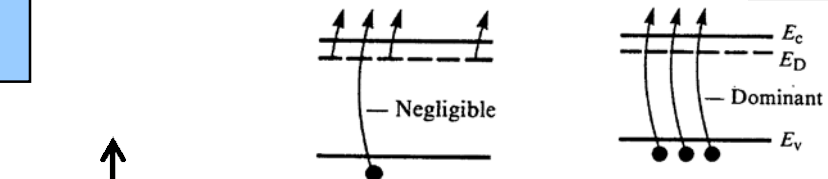


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