

Introduction to Semiconductor Devices
(Purdue University EE 305/606)
Supplemental Homework Exercises

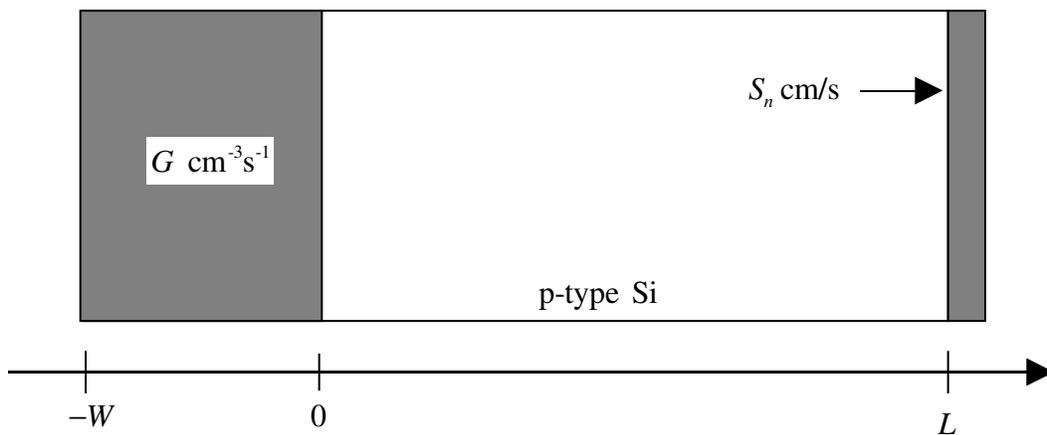
Tutorial questions based on Drift-Diffusion Lab v1.0 available online at <http://www.nanohub.org>.

Reference book: Semiconductor Device Fundamentals by Robert E. Pierret (Chapter 3)

Concept: Diffusion and Ambipolar Diffusion in Uniform Semiconductor

The purpose of these exercises is to familiarize you with minority carrier diffusion in semiconductors. Recall that for a uniformly doped, p-type semiconductor with a uniform electron-hole generation rate of G electron-hole pairs /cm³.s, the excess minority carrier (electron) density is, $\Delta n = G\tau_n$, where τ_n is the minority carrier lifetime.

Now consider a semiconductor as shown below.



Assume that the electron-hole generation rate is G for $x \leq 0$ and that the contact at $x = L$ is specified by a minority carrier surface recombination velocity, S_n . Our objective is to determine the $\Delta n(x)$ profile for $x > 0$. We will do this with the computer simulation tool, Drift-Diffusion Lab, on www.nanoHUB.org, but before doing a computer simulation, we should always know what to expect, so we begin with an analytical calculation.

- 1) Assume that $\Delta n = G\tau_n$ for $x \leq 0$ (this is an approximation that ignores edge effects near $x = 0$). Also assume that the diffusion length, $L_n = \sqrt{D_n\tau_n} \ll L$ and that $S_n \rightarrow \infty$. Derive an expression for $\Delta n(x)$ for $x > 0$. Make a sketch of the result.

- 2) Repeat problem 1) but this time assume that the diffusion length, $L_n = \sqrt{D_n \tau_n} \gg L$ and that $S_n \rightarrow \infty$. Derive an expression for $\Delta n(x)$ for $x > 0$. Make a sketch of the result.
- 3) Repeat problem 2) but this time assume that that $S_n = 0$. Derive an expression for $\Delta n(x)$ for $x > 0$. Make a sketch of the result.

Now that we know what to expect, we are ready to do a numerical simulation with the simulation tool, Drift-Diffusion Lab, on the nanoHUB.

(Turn ON *Surface Recombination* to set S_n)

For the exercises below, assume:

$$N_A = 1 \times 10^{15} \text{ cm}^{-3} \text{ for the bulk doping}$$

$$G = 2e20 \text{ cm}^{-3} \text{ s}^{-1}$$

$$L+W = 10 \mu\text{m}$$

$$W = 1 \mu\text{m}$$

$$T = 300 \text{ K}$$

$$\mu_p \sim 1300 \text{ cm}^2/\text{V.s}$$

$$\mu_n \sim 460 \text{ cm}^2/\text{V.s}$$

- 4) Choose the minority carrier lifetime, τ_n , so that $L_n = 2 \mu\text{m}$. (Also set $\tau_n = \tau_p$ and $S_n = 10^7$ in the simulation.) Run the simulation and examine $\Delta n(x)$. Compare the numerical result to the analytical result and discuss the similarities and differences.
- 5) For the simulation of problem 4), examine the minority carrier current density, $J_n(x)$. Explain why the plots have the shape that it does.
- 6) Choose the minority carrier lifetime, τ_n , so that $L_n = 50 \mu\text{m}$. (Also set $\tau_n = \tau_p$ and $S_n = 10^7$ in the simulation in the simulation.) Run the simulation and examine $\Delta n(x)$. Compare the numerical result to the analytical result and discuss the similarities and differences.
- 7) For the simulation of problem 6), examine the minority carrier current density, $J_n(x)$. Explain why the plots have the shape that it does.
- 8) Excess electrons, $\Delta n(x)$, should attract excess holes, $\Delta p(x)$. We expect that the attraction of opposite charges should lead to a semiconductor that is approximately neutral, $\Delta n(x) \approx \Delta p(x)$. Rerun problem 4) and examine $\Delta n(x)$ and $\Delta p(x)$. You will note that they are a little different. Explain the difference. HINT: you may also want to examine the electric field profile and the space charge density and think about the consequences of the fact that electrons and holes have different mobilities.