

Fundamentals of Nanoelectronics

ECE495 - Session 42, Dec 11, 2009

Thermoelectricity II

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$$I = 2 \frac{q}{h} \int dE \underbrace{\bar{T}(E)}_{M(E) \frac{\lambda}{L+\lambda}} \underbrace{(f_1 - f_2)}_{\left(-\frac{\partial f}{\partial E}\right) \left(qV + \frac{(E-\mu)\Delta T}{T}\right)} = G_{11}V + G_{12}\Delta T$$

100 μm

10 μm

1 μm

0.1 μm

←

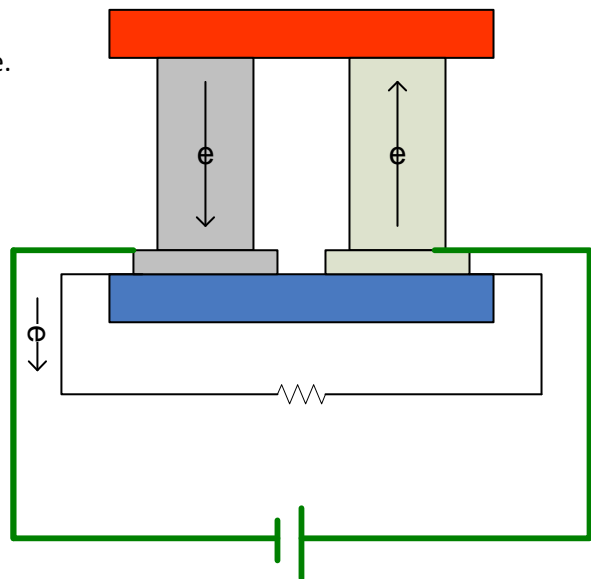
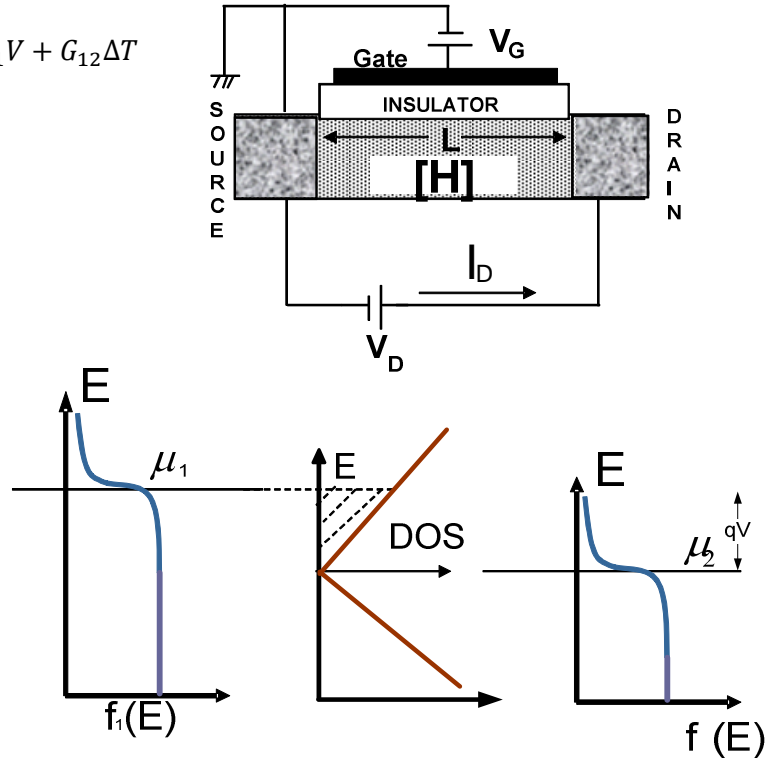
10 nm

1 nm

Heat current:

$$I_{Q_1} = \frac{2}{h} \int dE \bar{T}(E) (E - \mu_1) (f_1 - f_2) = G_{21}V + G_{22}\Delta T$$

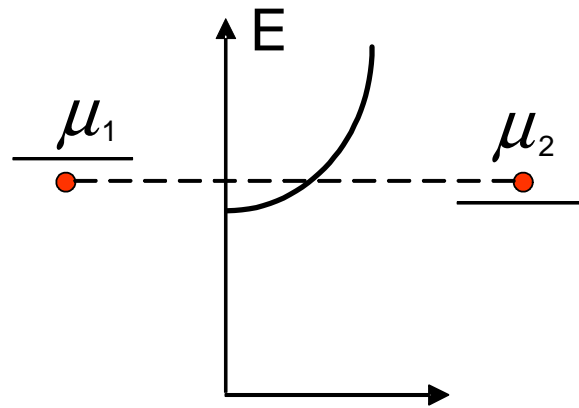
It carries $(E - \mu)$ energy before it was carry q charge.



$$G_{11} = \frac{2q^2}{h} \int dE \left(-\frac{\partial f}{\partial E} \right) \bar{T}(E)$$

$$G_{12} = \frac{2q}{h} \int dE \bar{T}(E) \frac{(E - \mu)}{T} \left(-\frac{\partial f}{\partial E} \right)$$

$$G_{21} = \frac{2q}{h} \int dE \bar{T}(E) (E - \mu) \left(-\frac{\partial f}{\partial E} \right)$$



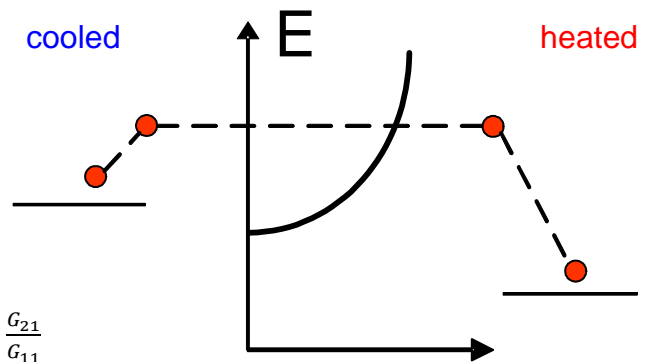
$$\Rightarrow TG_{12} = G_{21}$$

$$\begin{cases} I = G_{11}V + G_{12}\Delta T \\ I_Q = G_{21}V + G_{22}\Delta T \end{cases}$$

$$I = 0 \text{ then Seebeck coefficient: } S = \frac{V}{\Delta T} = \frac{G_{12}}{G_{11}}$$

$$f_1=f_2 \text{ and } \Delta T=0 \text{ then Peltier Coefficient: } \Pi = \frac{I_Q}{I} = \frac{G_{21}}{G_{11}}$$

$$\Rightarrow \Pi = TS \text{ Kelvin relation}$$



$$I = 2 \frac{q}{h} \int dE \bar{T}(E) (f_1 - f_2)$$

$$\bar{T}(E) = M(E) \frac{\lambda}{L + \lambda} \quad \text{Semi-classical view}$$

$$\bar{T}(E) = \text{Trace}[\Gamma_1 G \Gamma_2 G^+] \quad \text{Full quantum view}$$