

2.2. E(p) or E(k) relations

2.2a. The velocity $v(E)$ is *always* related to the momentum $p(E)$ by the relation

$$(a) v = \frac{p}{m}$$

$$(b) v = \frac{p^2}{2m}$$

$$(c) v = v_0 \quad (\text{constant independent of } p)$$

$$(d) v = \sqrt{\frac{2p}{m}}$$

(e) None of the above

$v = \frac{dE}{dp}$, actual relation between velocity and momentum depends on energy-momentum relation. Parabolic

E(p) gives choice (a).

2.2b. A material with an energy momentum relation $E(p) = E_c + K p^a$, has a velocity $v(E)$ (d: number of dimensions, K: positive constant)

$$(a) v(E) \sim (E - E_c)^{1+(d/a)}$$

$$(b) v(E) \sim (E - E_c)^{1+(1/a)}$$

$$(c) v(E) \sim (E - E_c)^{1-(1/a)}$$

$$(d) v(E) \sim (E - E_c)^{1-(d/a)}$$

(e) none of the above

$$v(E) = \frac{dE}{dp} = aK p^{a-1} \sim (E - E_c)^{(a-1)/a}$$