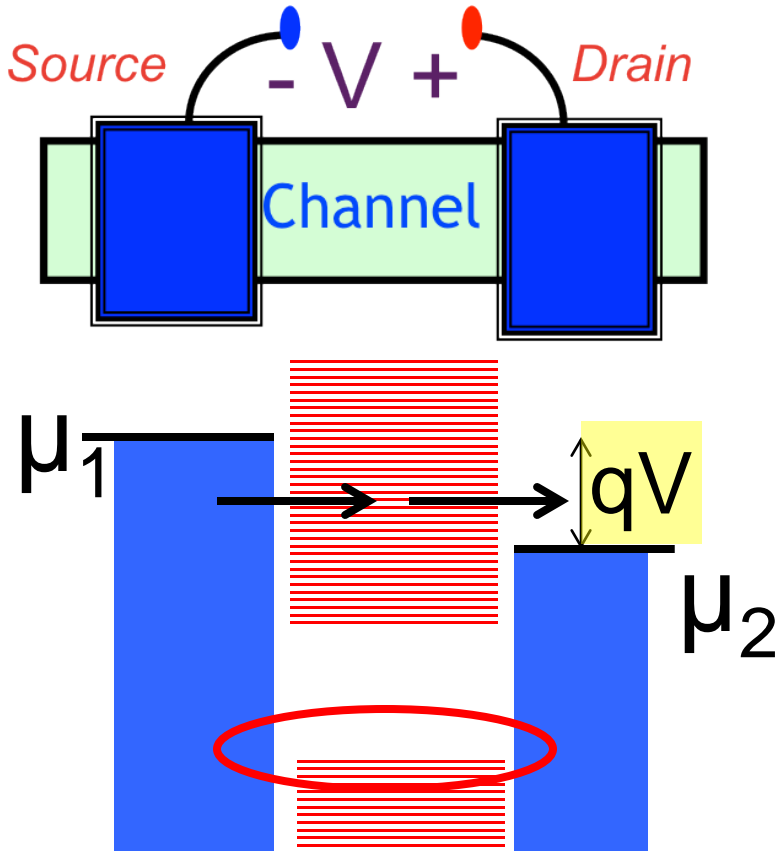


# FUNDAMENTALS OF NANOEELECTRONICS



$$G = \frac{q^2 D}{2t}$$

D: Density of states  
t : transfer time

## A. Basic Concepts:

### Semiclassical (SC) Model

1. The new perspective
2. Energy band model
3. What and where is the voltage?
4. Heat & electricity:  
Second law & information

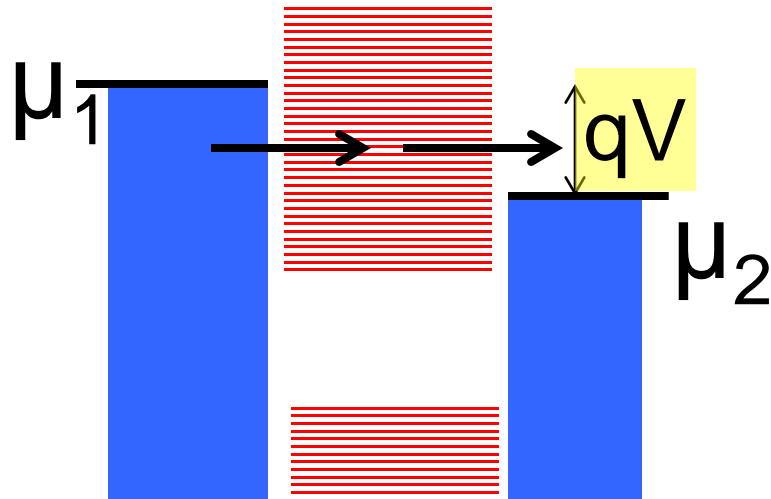
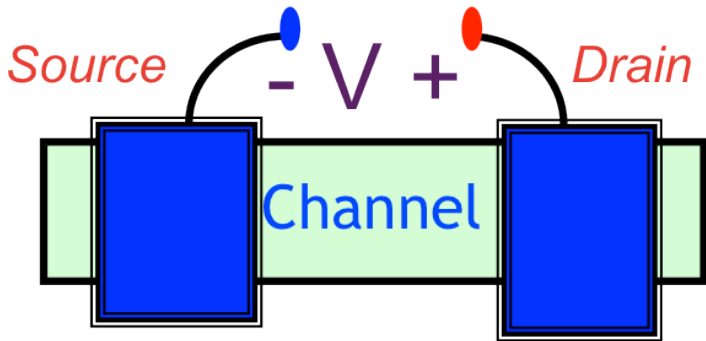
## From SC to Q

### B. Quantum (Q) Model

1. Schrodinger Equation
2. Contact-ing Schrodinger
3. NEGF Method
4. Spin Transport

# The New Perspective

# Drude Formula



*M*: Number of “modes”

**NEW**

$$G = \frac{q^2 D}{2t} \rightarrow G_B = \frac{q^2 D \bar{u}}{2L} \rightarrow G = \frac{G_B}{1 + \frac{L}{\lambda}}$$

$$\sigma = \frac{q^2 n \tau}{m}$$

$$\sigma = \frac{G_B}{A} \lambda$$

$$\frac{G_B \lambda}{L + \lambda}$$

$$\frac{G_B}{1 + \frac{L}{\lambda}}$$

# Where is the Resistance?

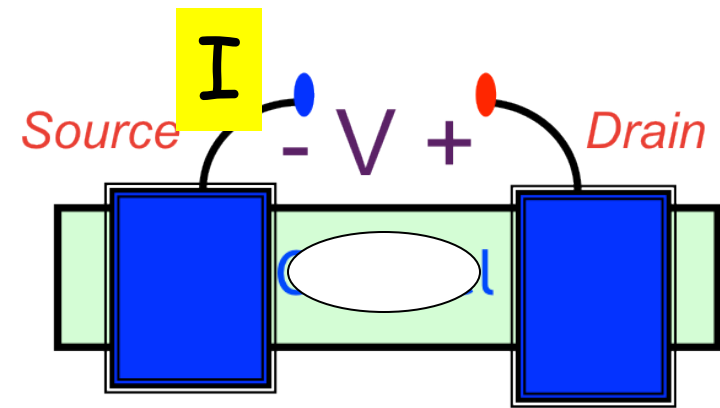
1. The new perspective
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Resistance is associated with

~~➤ Joule Heating:  $T^2R$~~

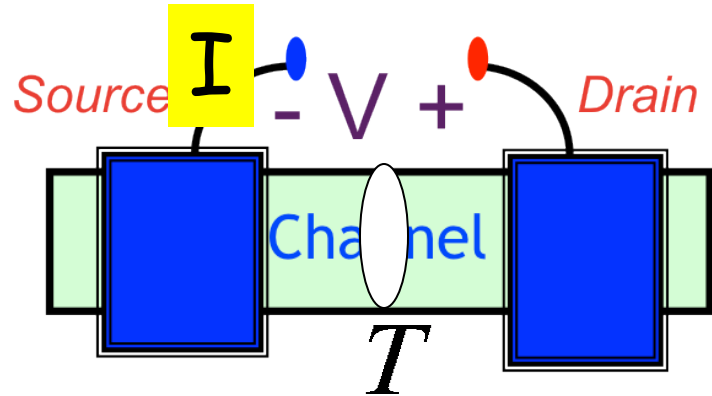
➤ Voltage drop:  $IR$



$$\frac{R_B}{2} \quad R_B \quad \frac{L}{\lambda} \quad \frac{R_B}{2}$$

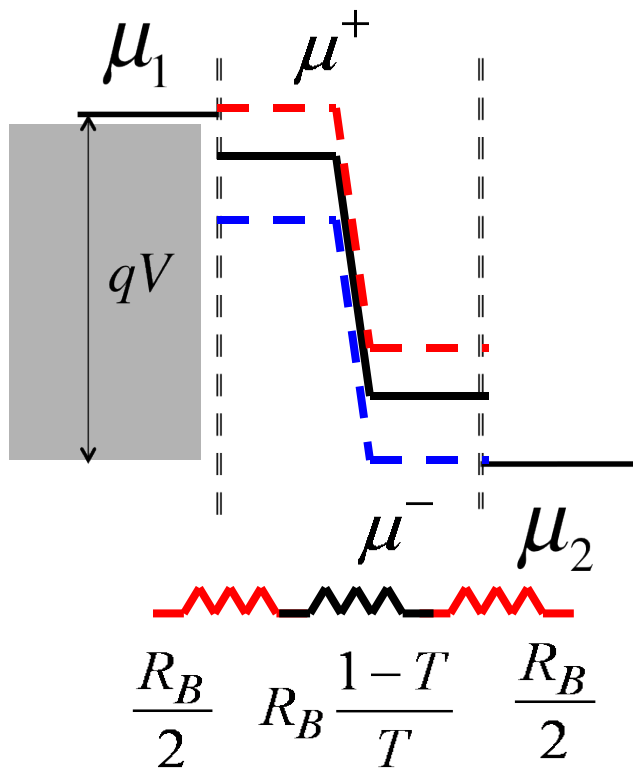
$$R_B + R_B \frac{L}{\lambda}$$

$$R = R_B \left( 1 + \frac{L}{\lambda} \right) \quad G = \frac{G_B}{1 + \frac{L}{\lambda}}$$



## What & where is the voltage?

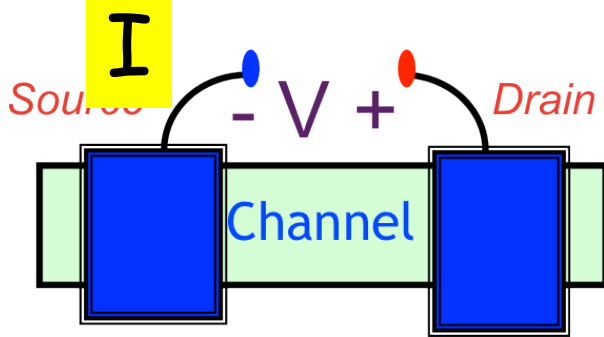
1. The new perspective
2. Energy band model
3. What and where is the voltage?
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Second law & information



➤ Voltage drop:  $IR$

➤ Quasi-Fermi Levels (QFL)

# "Elastic Resistor"



$$\frac{R_B}{2}$$

$$\frac{R_B}{2}$$

1. The new perspective
2. Energy band model
3. What and where is the voltage?
4. Heat & electricity:  
Second law & information

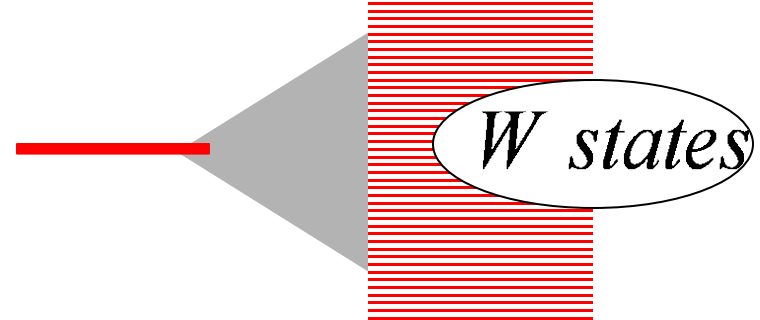
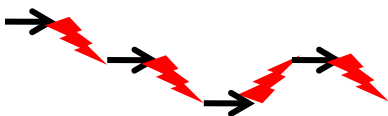
*Mechanics:  
Force driven*



*Thermodynamics:  
Entropy driven*

$$I \sim G(E) \times$$

$$(f_1(E) - f_2(E))$$



$$S = k \ln W$$

Usually all mixed up !!

## Part A: Semiclassical Transport

Newton +  =



$$E\psi = H\psi$$

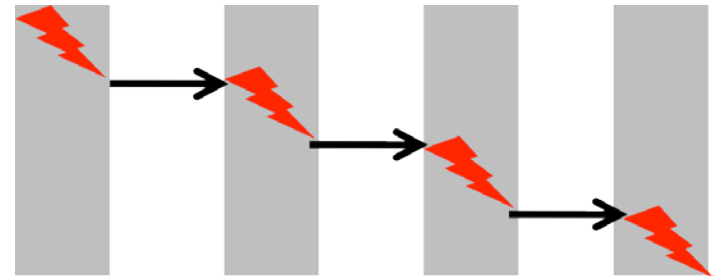
Schrodinger +  = NEGF

## Part B: Quantum Transport

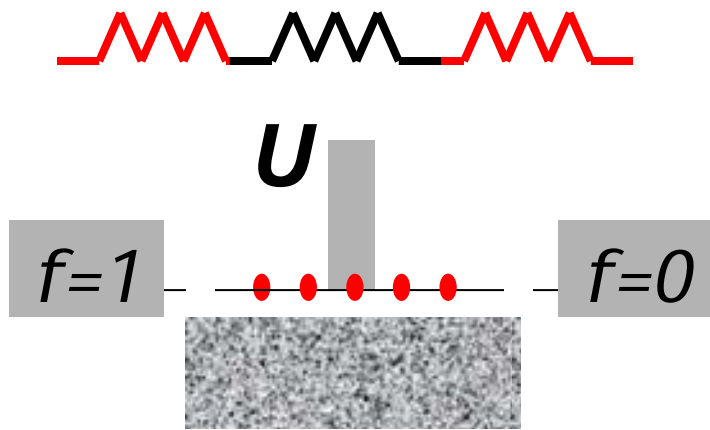
➤ Provides approximate physical picture in general

➤ Agrees with rigorous theory for low bias

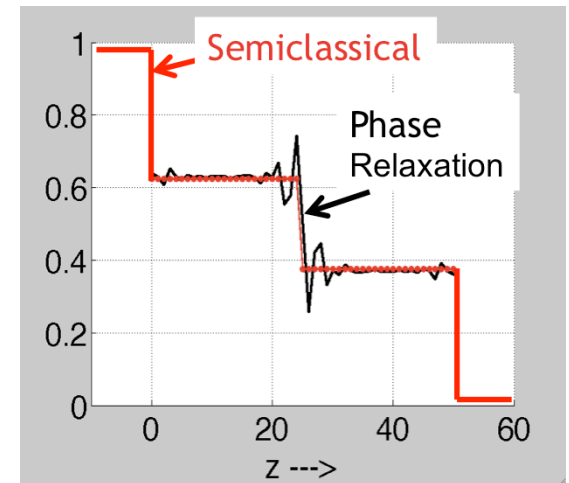
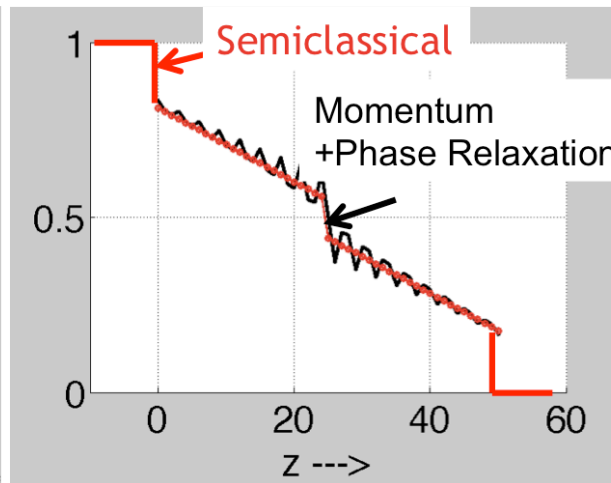
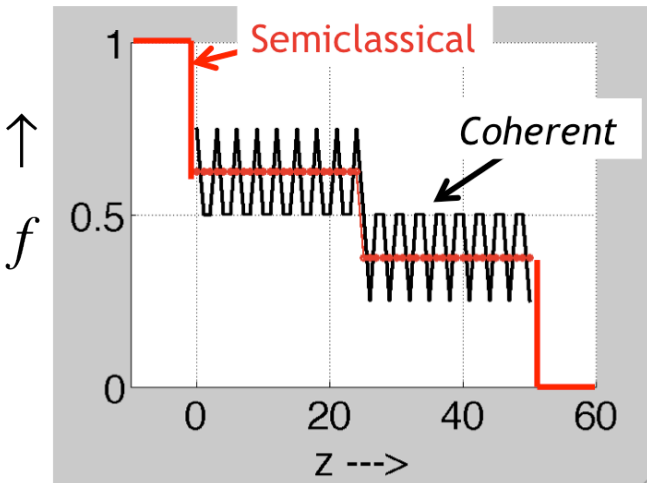
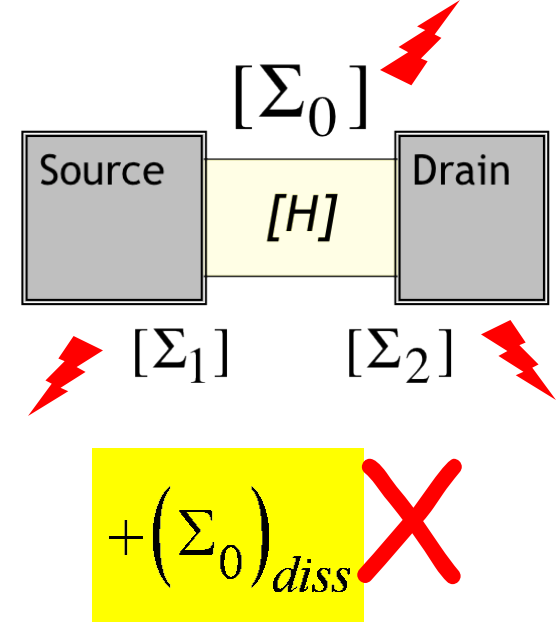
*Long Resistors*



# An Example

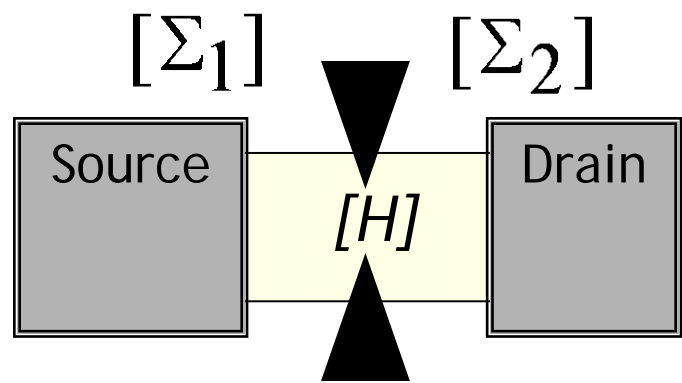
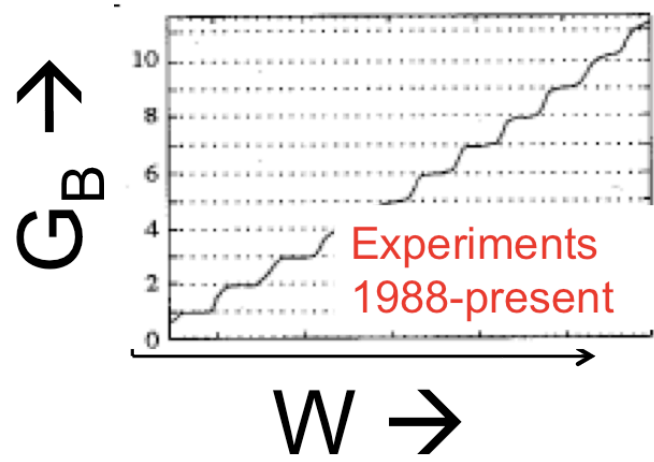
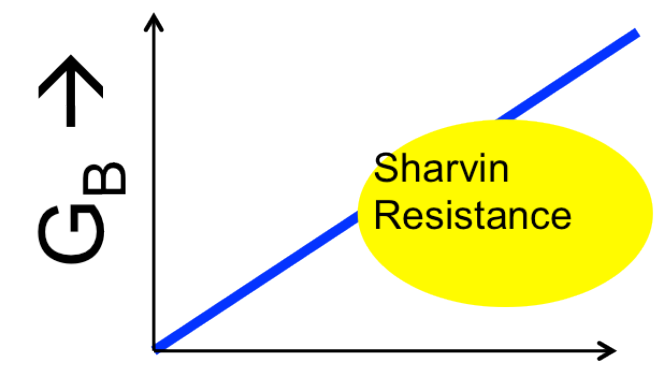


*NEGF*  
Non – Equilibrium  
Green's Function

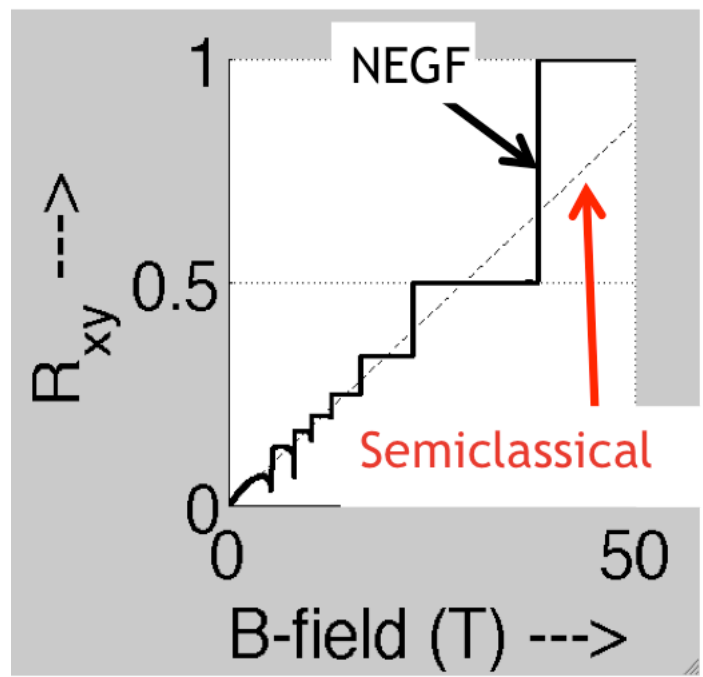


# More examples

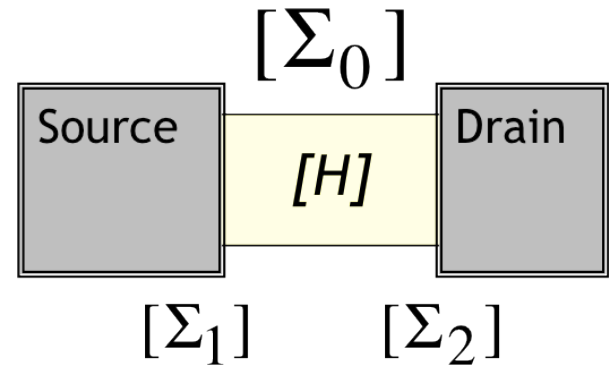
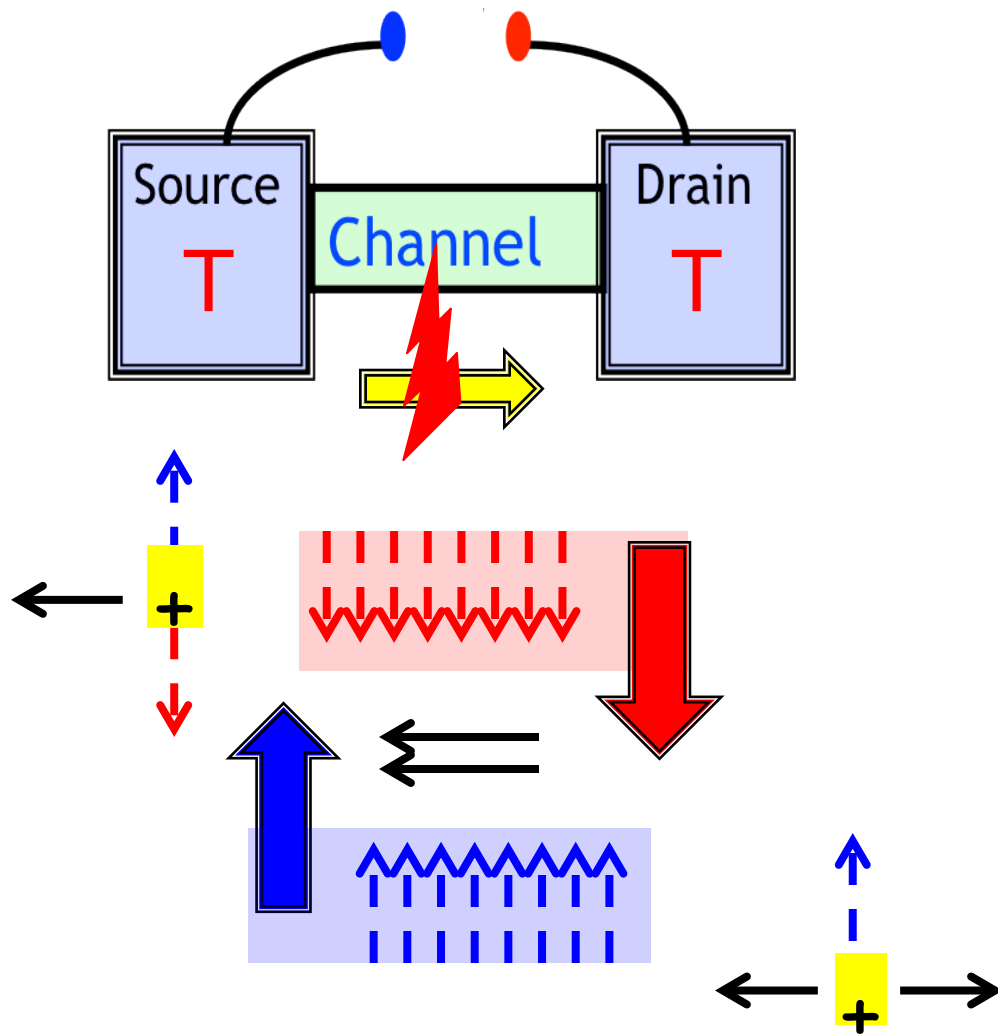
## Quantized conductance



## Quantum Hall Effect (1980)







## B. Quantum (Q) Model

1. Schrodinger Equation
2. Contact-ing Schrodinger
3. NEGF Method
4. Spin Transport

Similar to "Spin-flip Transistor"  
Bauer et al. 2001

# FUNDAMENTALS OF NANO ELECTRONICS

*Prerequisite: Calculus,  
Elementary Differential Equations*

*Part B requires Matrix Algebra*

*Text:*

*Lessons From Nanoelectronics:  
A New Perspective on Transport  
World Scientific (2012)*

*II Edition 2015:*

*Manuscript will be available  
to registered students*

*First offered on nanoHUB-U,  
Spring 2012*

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