

*Spring 2019 Purdue University*

# **ECE 255: L26**

# **Multi-stage Amplifiers**

School of ECE  
Purdue University  
West Lafayette, IN USA

# Announcements

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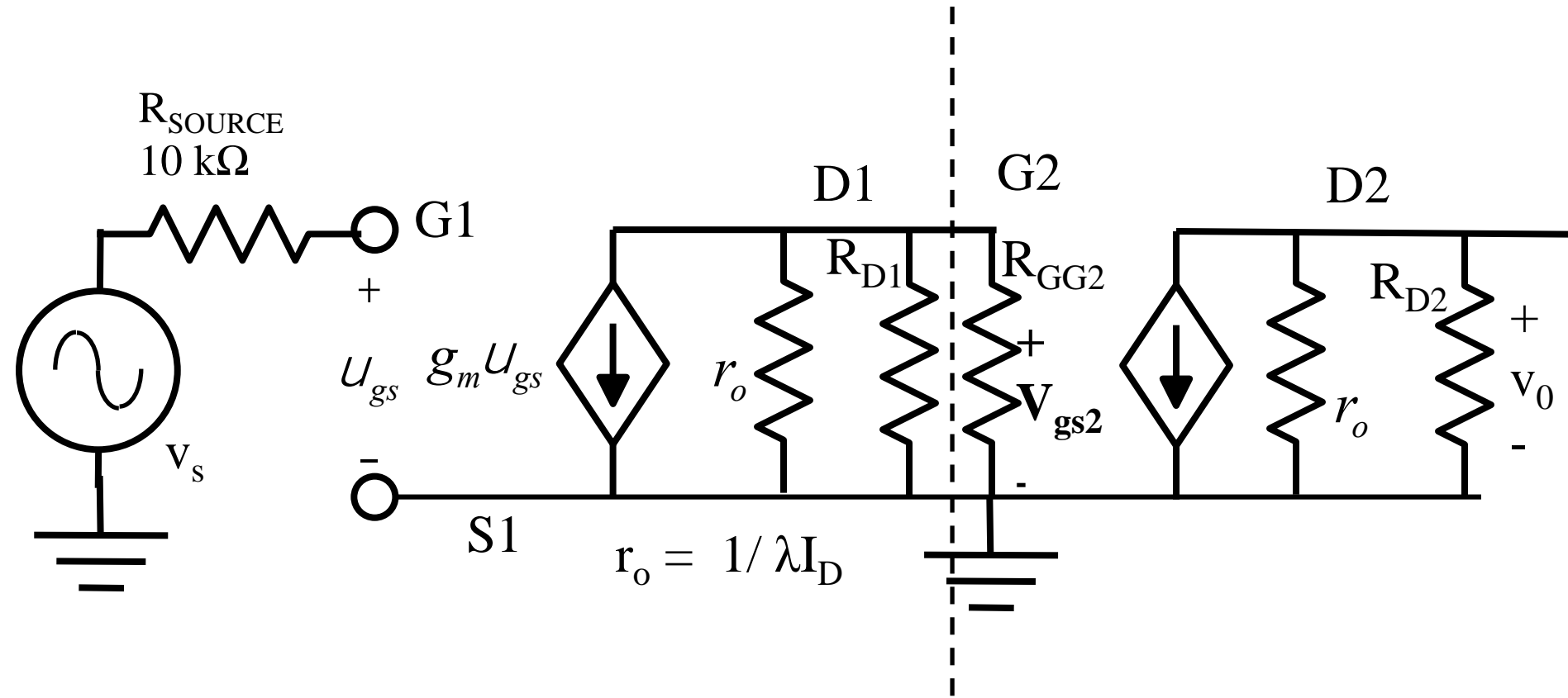
**A1:**

# Outline

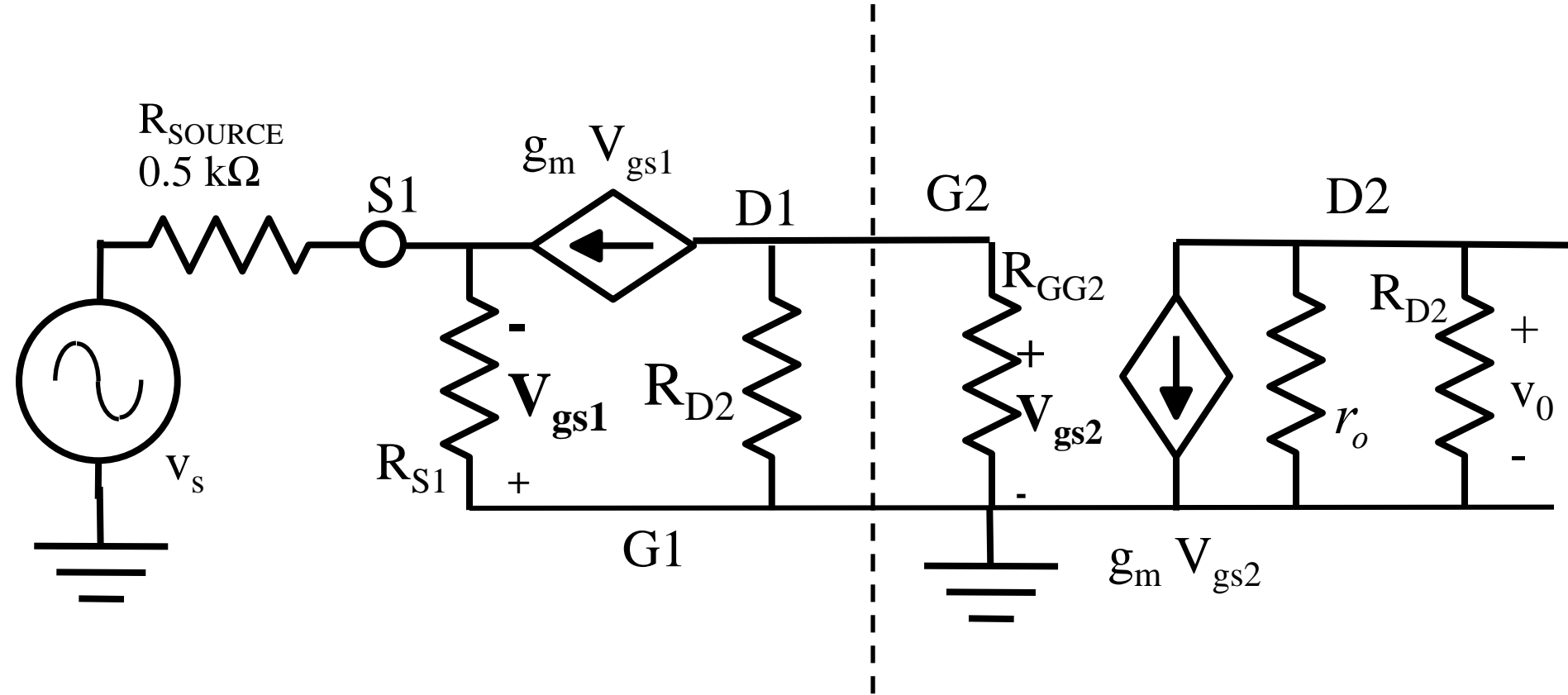
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- 1) Cascaded amplifier stages – small signal
- 2) Discussion/alternate stage gain approach

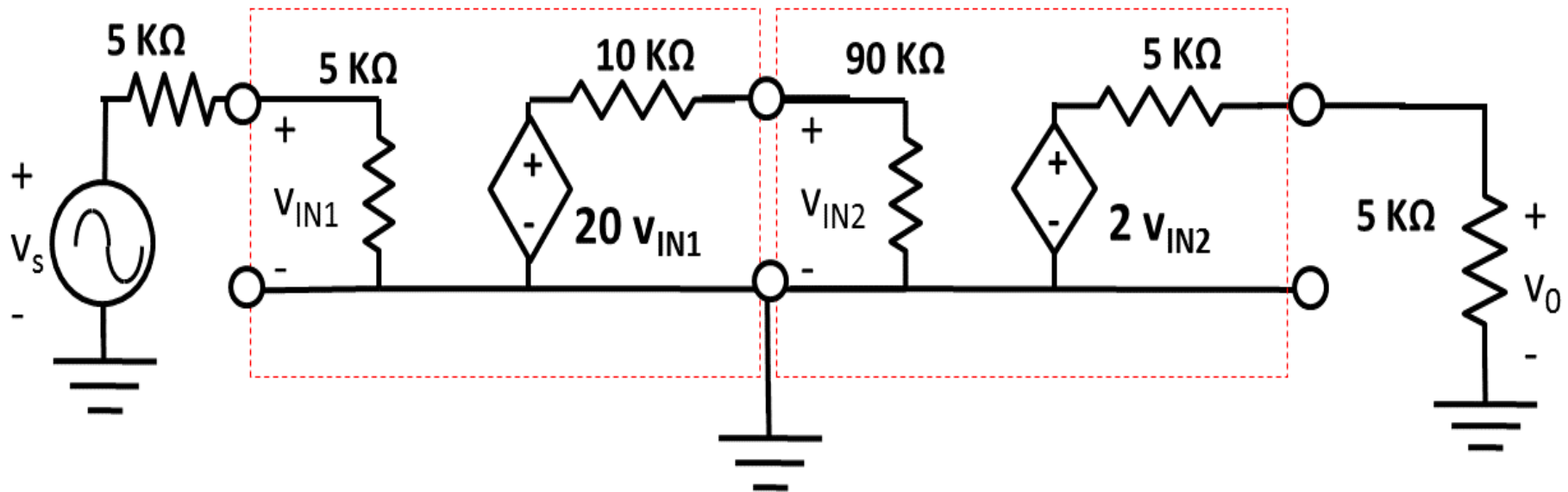
# Multi-stage (cascaded) amp



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# $A_{vo}/R_{in}/R_{out}$ Representation

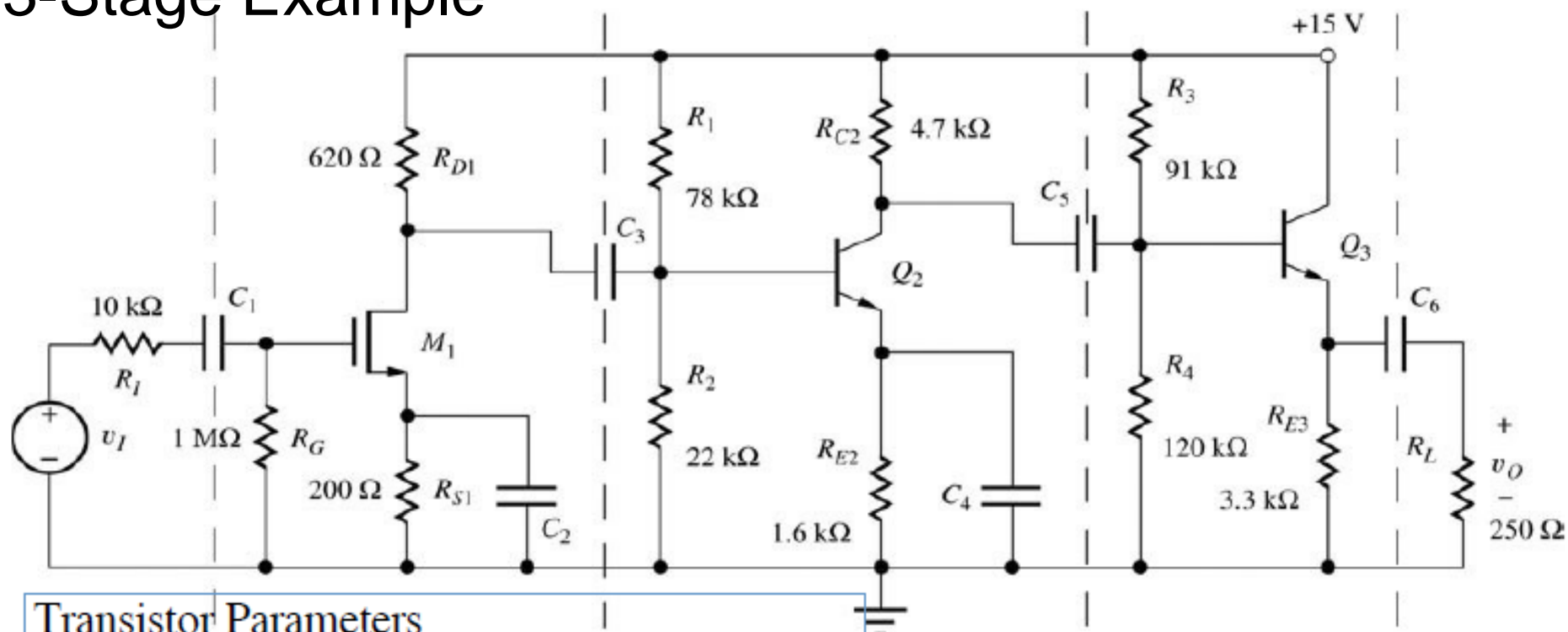


$$A_v = v_o/v_s = v_{in1}/v_s \times v_{in2}/v_{in1} \times v_o/v_{in2}$$

$$A_v = 5k/(5k+5k) \times (-20) (90k/90k+10k) \times 2 (5k/(5k+5k))$$

$$= 0.5 \times -18 \times 1 = -9$$

# 3-Stage Example



## Transistor Parameters

$$M_1: K_n = 10 \text{ mA/V}^2, V_{TN} = -2 \text{ V}, \lambda = 0.02 \text{ V}^{-1}$$

$$Q_2: \beta_F = 150, V_A = 80 \text{ V}, V_{BE} = 0.7 \text{ V}$$

$$Q_3: \beta_F = 80, V_A = 60 \text{ V}, V_{BE} = 0.7 \text{ V}$$

## Q-Points

$$M_1: (5.00 \text{ mA}, 10.9 \text{ V})$$

$$Q_2: (1.57 \text{ mA}, 5.09 \text{ V})$$

$$Q_3: (1.99 \text{ mA}, 8.36 \text{ V})$$

## Small-Signal Parameters

$$M_1: g_{m1} = 10.0 \text{ mS}, r_{o1} = 12.2 \text{ k}\Omega$$

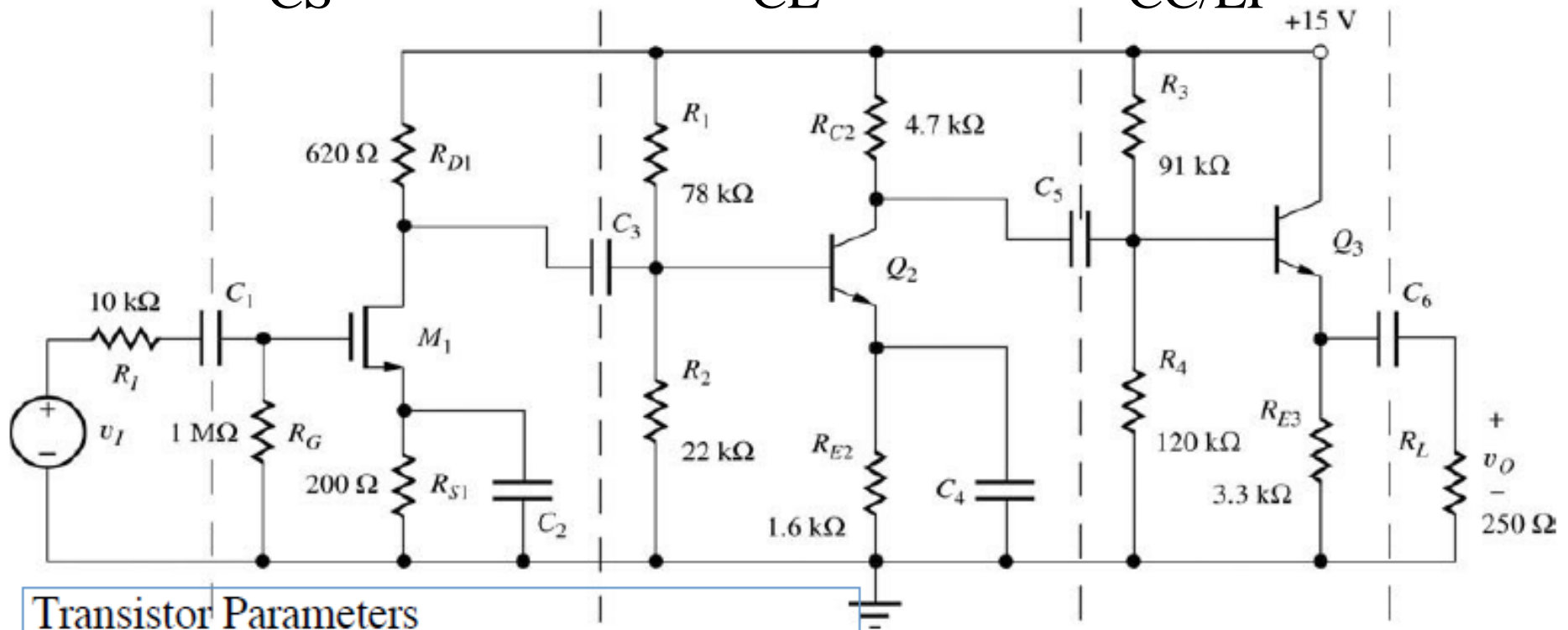
$$Q_2: g_{m2} = 62.8 \text{ mS}, r_{\pi 2} = 2.39 \text{ k}\Omega, \\ r_{o2} = 54.2 \text{ k}\Omega$$

$$Q_3: g_{m3} = 79.6 \text{ mS}, r_{\pi 3} = 1.00 \text{ k}\Omega, \\ r_{o3} = 34.4 \text{ k}\Omega$$

CS

CE

CC/EF



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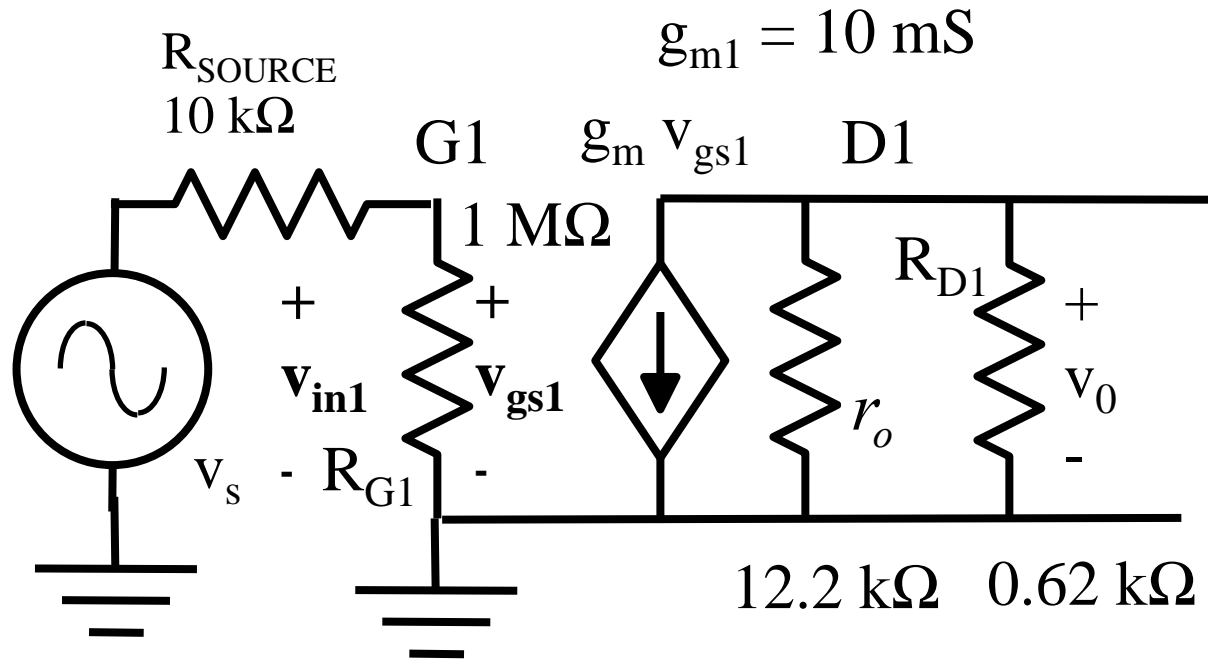
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# Stage 1 -- CS



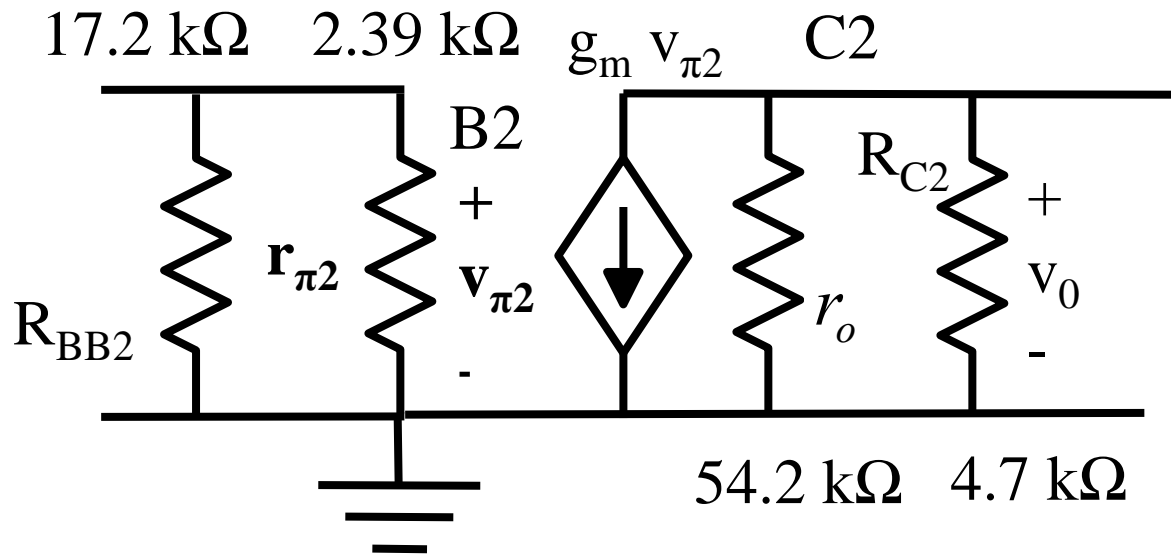
$$R_{o1} = (r_o \parallel R_{D1}) = 0.59 \text{ k}\Omega$$

$$A_{v_o} = -g_m (r_o \parallel R_{D1}) = -5.9$$

$$v_{in1} = v_s \left( \frac{R_{G1}}{R_{SOURCE} + R_{G1}} \right) = 0.99$$

# Stage 2 -- CE

$$g_m = 68.2 \text{ mS}$$



$$R_{o2} = (r_o \parallel R_{C2}) \\ = 4.3 \text{ k}\Omega$$

$$R_{in2} = (R_{BB2} \parallel r_{\pi2}) = 2.1 \text{ k}\Omega$$

$$A_{v_o} = -g_m (r_o \parallel R_{C2}) \\ = -293$$

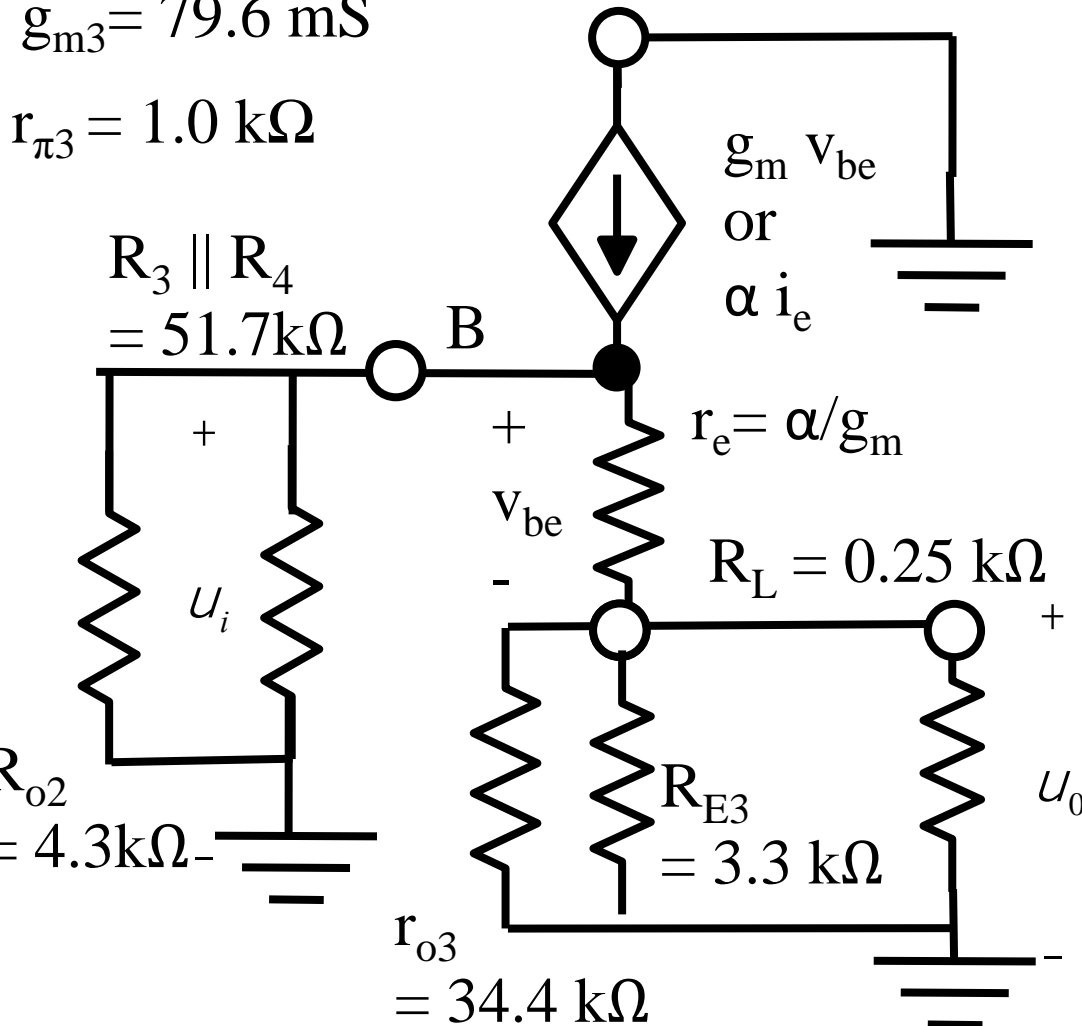
# Stage 3 -- EF

$$\beta = 80$$

$$g_{m3} = 79.6 \text{ mS}$$

$$r_{\pi3} = 1.0 \text{ k}\Omega$$

$$R_3 \parallel R_4 = 51.7 \text{ k}\Omega$$



$$R_E' = (r_{o3} \parallel R_{E3} \parallel R_L) = 0.23 \text{ k}\Omega$$

$$A_v = \frac{U_o}{U_i} = + \frac{(b+1)R_E}{r_{\rho} + (b+1)R_E} = 0.95$$

$$R_{in} = r_{\rho} + (b+1)R_E$$

$$R_{in3}' = 19.6 \text{ k}\Omega$$

$$R_{in3} = 19.6 \text{ k} \parallel 51.7 \text{ k} = 14.2 \text{ k}$$

$$R_o = R_E \parallel \left( \frac{r_{\rho} + R_{series}}{b+1} \right)$$

$$R_{series3} = R_3 \parallel R_4 \parallel R_{out2} = 4.0 \text{ k}\Omega$$

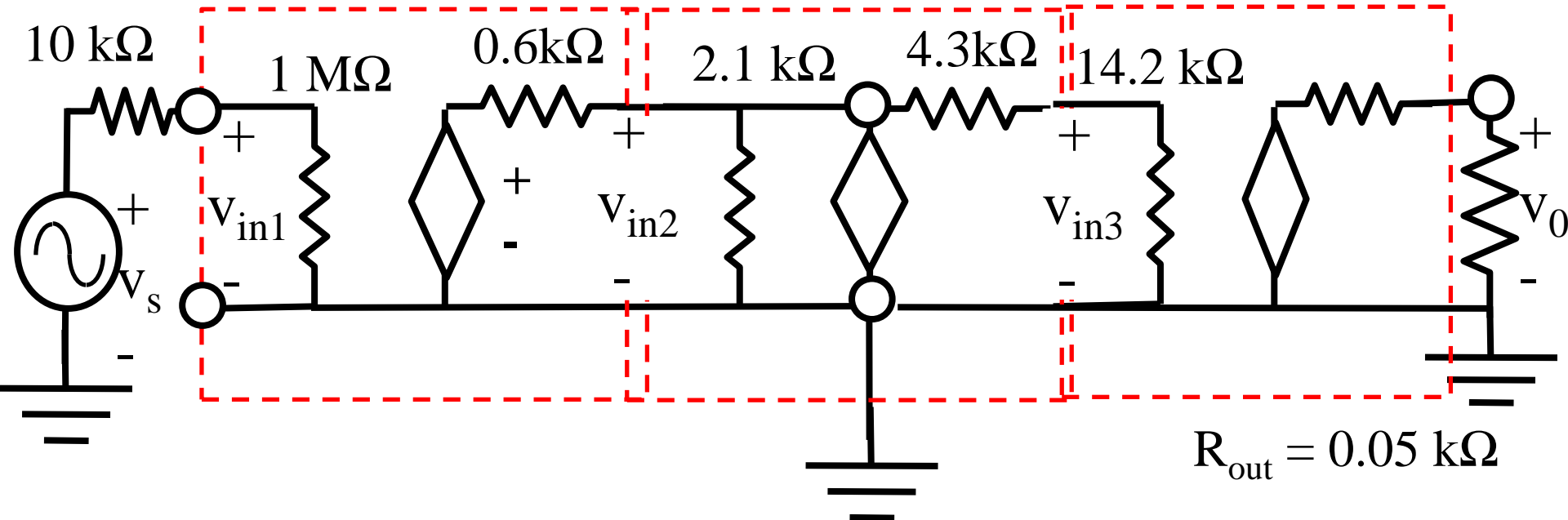
$$R_{out3} = 0.05 \text{ k}\Omega$$

# Combine 3 Stages

$$A_{v0} = -6$$

$$A_{v0} = -295$$

$$A_v \text{ (incl. } R_L\text{): } 0.95$$



$$A_v = v_o/v_s = v_{in1}/v_s \times v_{in2}/v_{in1} \times v_{in3}/v_{in2} \times v_o/v_{in3}$$

$$A_v = \frac{1\text{M}}{(10\text{k}+1\text{M})} (-5.9) \frac{2.1\text{k}}{(2.1\text{k}+0.6\text{k})} (-293) \frac{14.2\text{k}}{(14.2\text{k}+4.3\text{k})} (0.95)$$

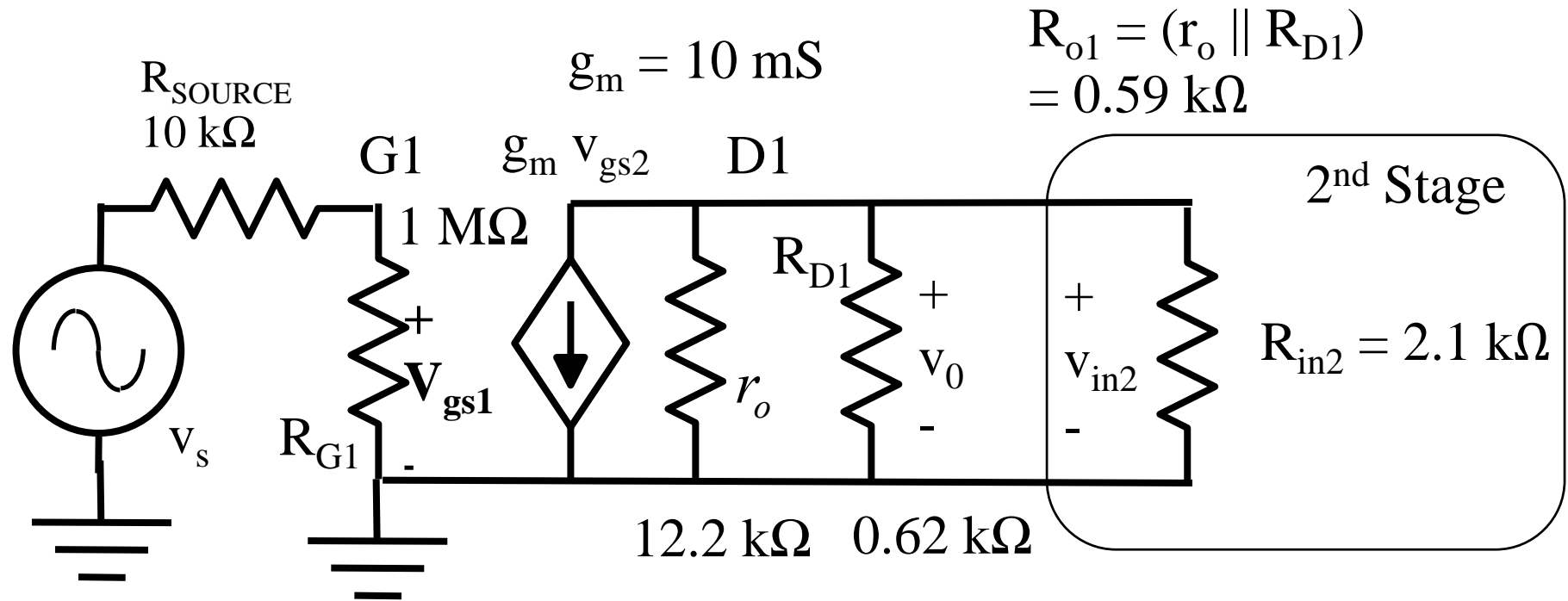
$$= 0.99 \times -4.6 \times -225 \times 0.95 = +973$$

# Perspective

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- 1) Analyze cascaded amplifier stages in terms of individual stage gain, input/output impedances.
- 2) Pay attention to cases in which  $R_{in,i}$  depends on subsequent stage, or  $R_{out,i}$  depends on previous stage (e.g.  $R_{series}$  of follower includes  $R_{out}$  of previous stage)
- 3) Example used  $A_{Vo}$  for each stage, then a voltage divider between  $R_{out,i}$  and  $R_{in,i+1}$ . You can also find overall  $A_V$  for a stage by considering  $R_{in,i+1}$  in calculation.

# Alternate Stage 1 – CS with $R_{LOAD} = R_{in2}$

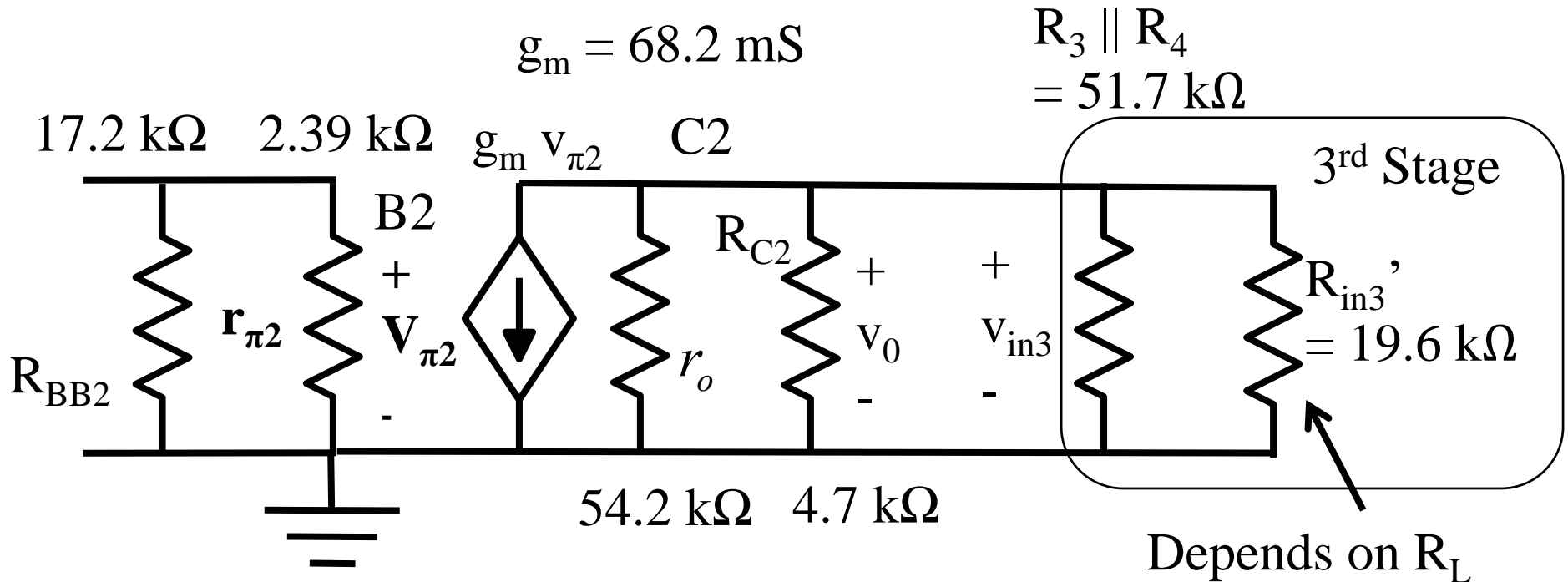


$$V_{in1} = V_s \left( \frac{R_{G1}}{R_{source} + R_{G1}} \right) = 0.99$$

$$A_{vtotal} = v_{in2}/v_{in1} = -g_m (r_o \parallel R_{D1} \parallel R_{in2}) = -4.6$$

Previously, had  $A_{v_o} = -5.9$ , then voltage divider.

# Alternate Stage 2 - CE with $R_{in3}$



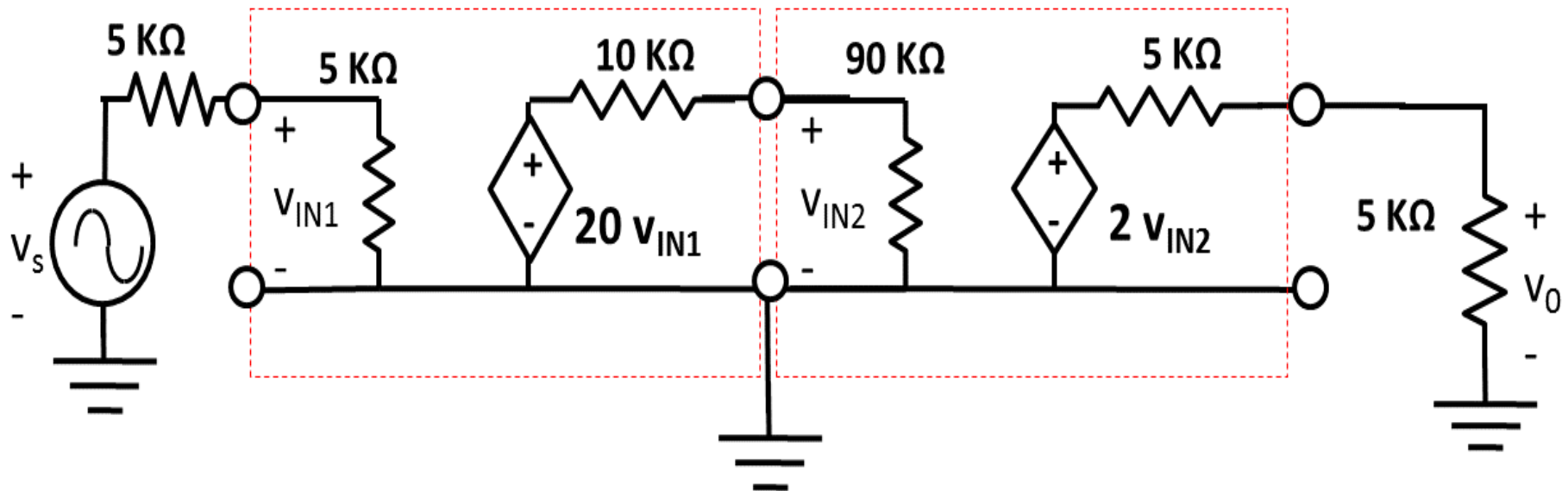
$$\begin{aligned}
 A_{vtotal} &= v_{in3}/v_{in2} = -g_m (r_{o2} \parallel R_{C2} \parallel R_3 \parallel R_4 \parallel R_{in3}') \\
 &= -68.2 \text{ ms} \times 3.3 \text{ k}\Omega = -226
 \end{aligned}$$

$$R_{in2} = (R_{BB2} \parallel r_{\pi 2}) = 2.1 \text{ k}\Omega$$

$$R_{o2} = (r_o \parallel R_{C2}) = 4.3 \text{ k}\Omega$$

vs  $A_{v0} = -293$ , then voltage divider.

# Summary



$$A_v = v_o/v_s = v_{in1}/v_s \times v_{in2}/v_{in1} \times v_o/v_{in2} \times \dots$$

- $A_{vo}/R_{in}/R_{out}$  Representation and chain rule
- Have to calculate stage input/output resistances in order to evaluate intermediate voltage gains
  - Open-circuit  $A_v$ , then resistance dividers, or...
  - Directly calculate stage  $i$  gain in presence of  $R_{in,i+1}$