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ECE 255: L3.2

Doped Semiconductors (Sedra and Smith, 7th Ed., Sec. 3.2)

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Lundstrom: 2019

Doping makes semiconductors useful

metal



gold (Au)

semiconductor



silicon (Si)

insulator



glass (SiO₂)

Doped semiconductors

- 1) The np product
- 2) Doping
- 3) Carrier concentration vs. doping density
- 4) Carrier concentration vs. temperature

The equilibrium np product

For intrinsic semiconductors: $n = p = n_i$ $n_i = 10^{10} \text{ cm}^{-3}$
Silicon T = 300 K

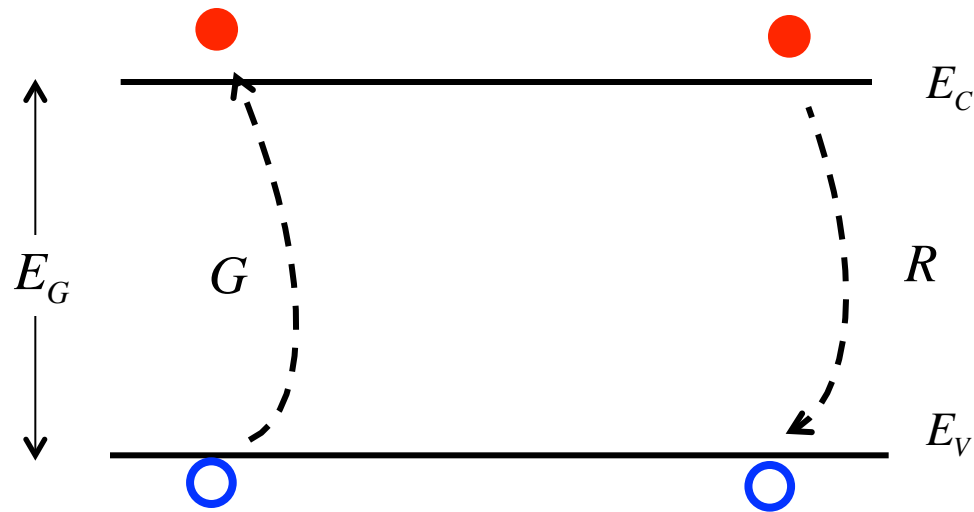
$$np = n_i^2$$

$$n_i^2 \propto e^{-\frac{E_G}{k_B T}}$$

n_i is typically **small at room temperature**

n_i can become **very large at high temperatures** and **very small at low temperatures**

Generation and Recombination



$$G_p = G_n = G > 0$$

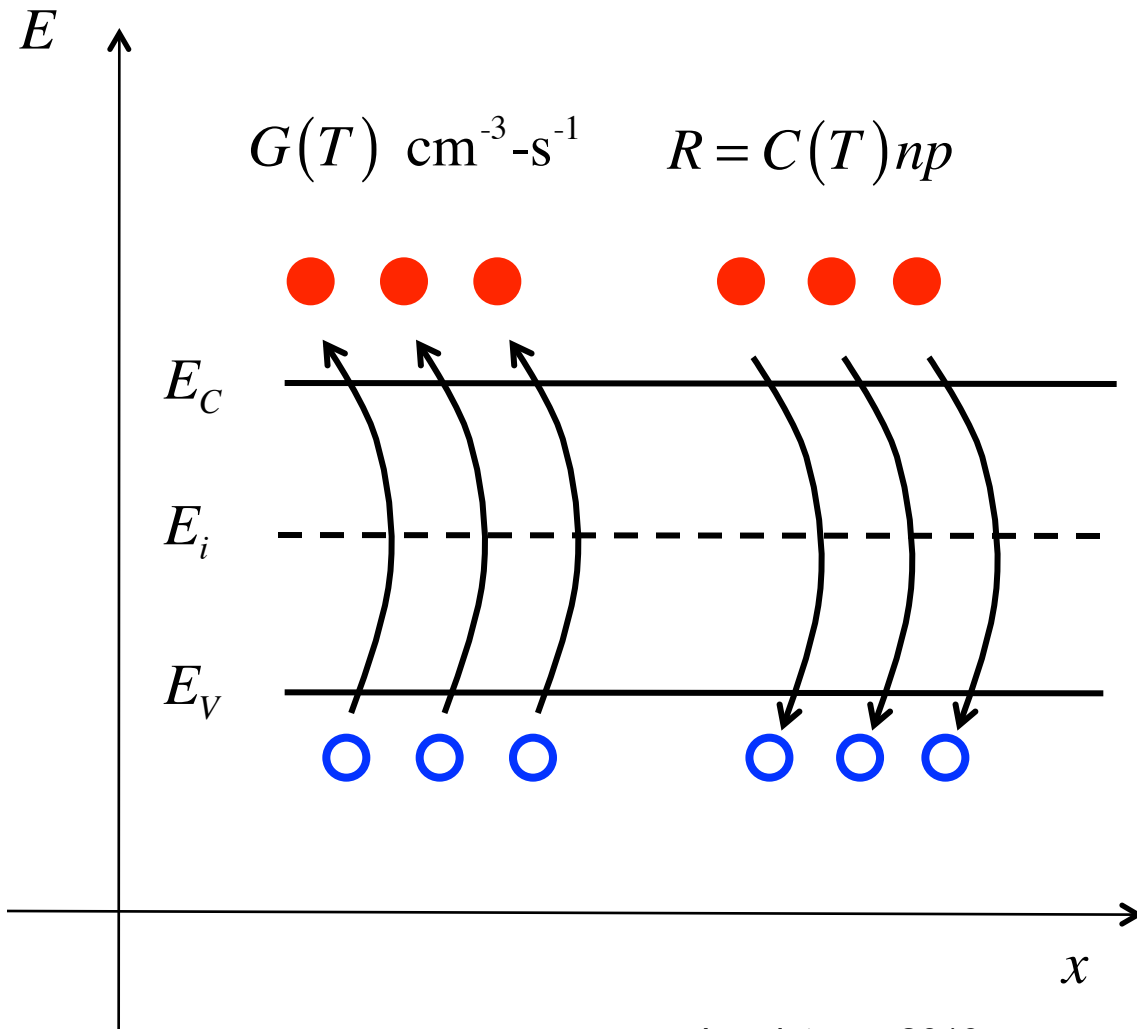
requires energy to
break covalent bonds

$$R_p = R_n = R > 0$$

releases energy

In equilibrium: $G = R$

Why is $np = n_i^2$?



In equilibrium:

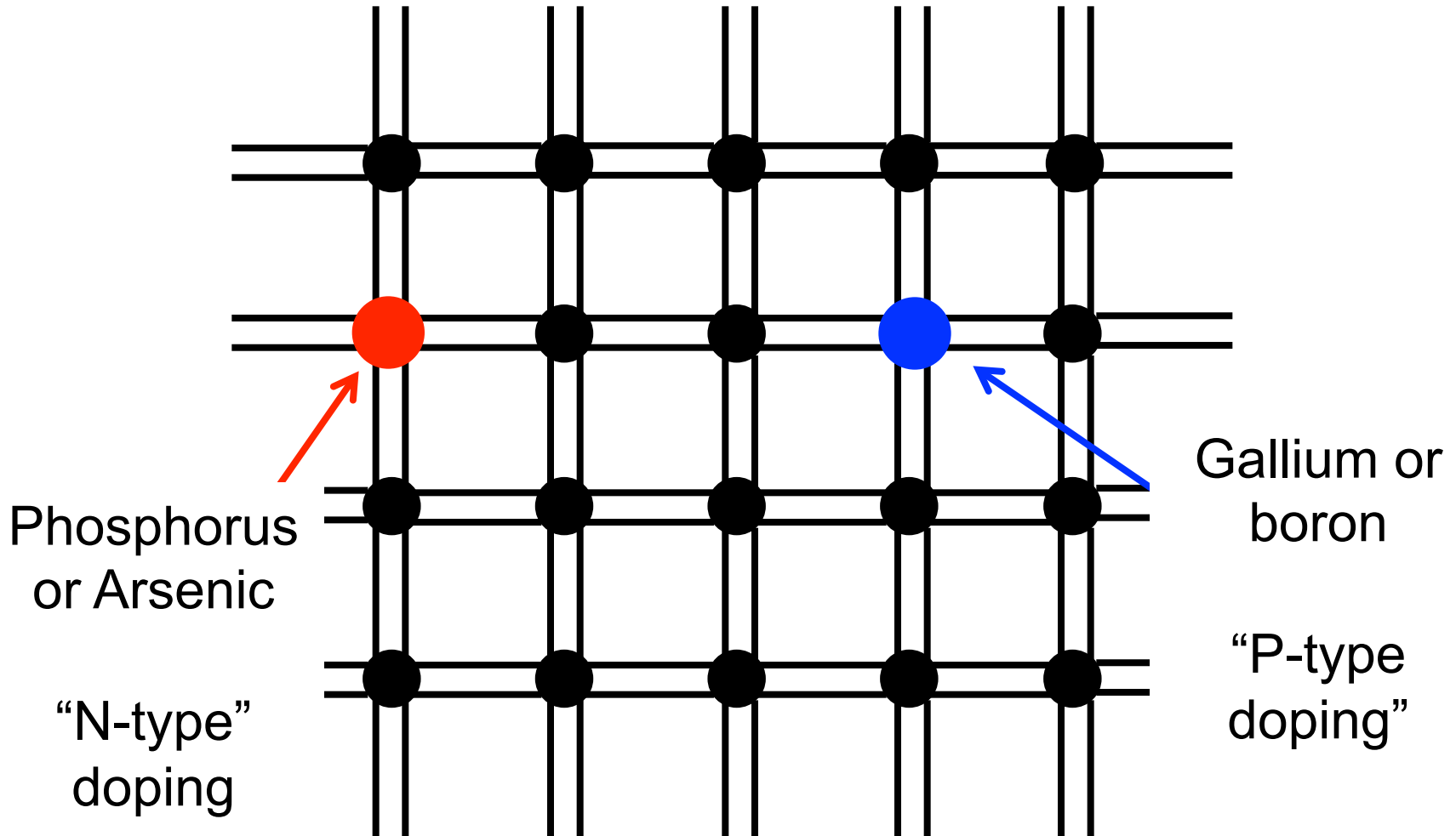
$$G = R$$

$$np = \frac{G(T)}{C(T)} = n_i^2(T)$$

$$np = n_i^2(T)$$

(equilibrium)

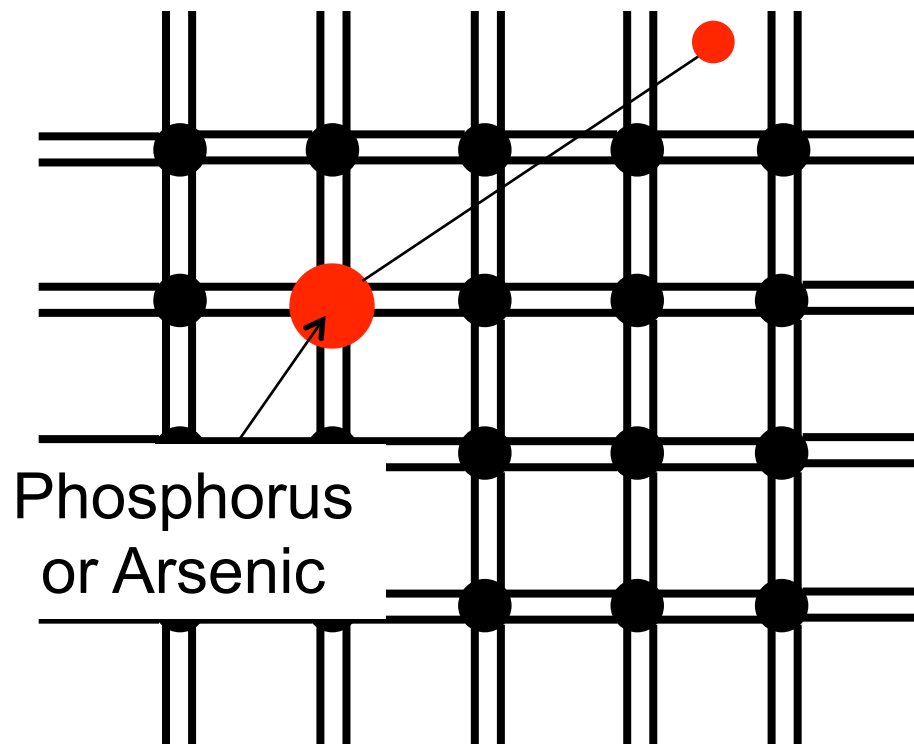
Doping a semiconductor



Dopants in Si

Group #	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
Period 1	1 H																	2 He
Period 2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne
Period 3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
Period 4	19 K									28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
Period 5	37 Rb									46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
Period 6	55 Cs									78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
Period 7	87 Fr	88 Ra	**	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og
* Lanthanoids				57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu
** Actinoids				89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr

Donors: N-type doping



$$E_B = -\frac{m_0 q^4}{2(4\pi\kappa_r \epsilon_0 \hbar)^2} \text{ eV}$$

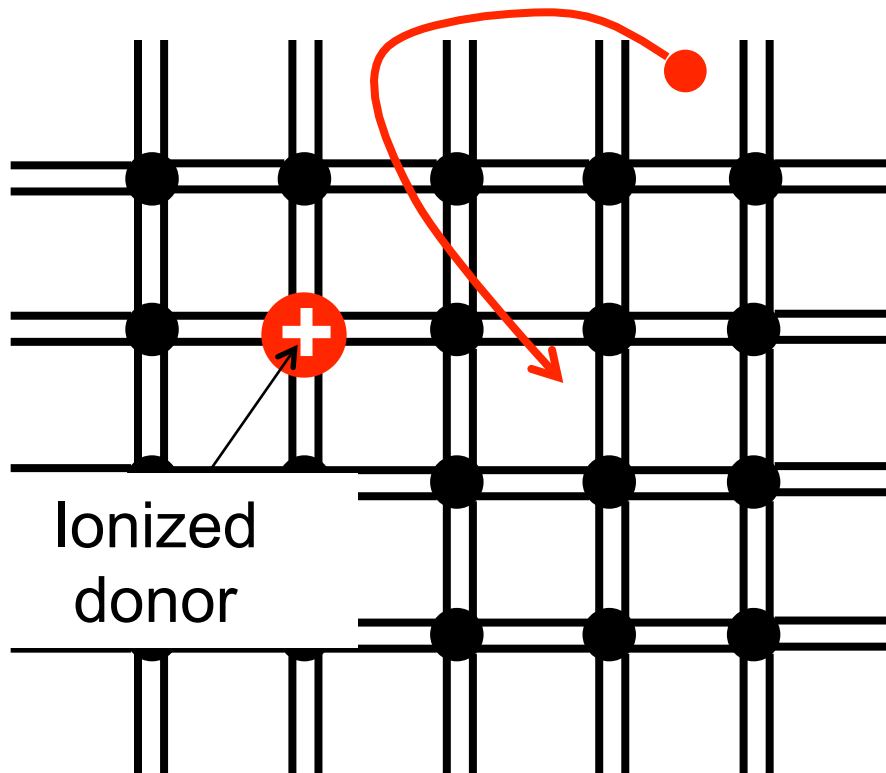
$$E_B \approx -0.05 \text{ eV}$$

Weakly bound

Easily broken at room temperature

Produces an electron in the conduction band.

Ionized donor



Concentration of dopants:

$$N_D \text{ cm}^{-3}$$

Concentration of ionized donors:

$$N_D^+ \text{ cm}^{-3}$$

Concentration of electrons in the conduction band:

$$n \approx N_D^+ \text{ cm}^{-3}$$

Carrier concentrations

$n \approx N_D^+ \approx N_D \text{ cm}^{-3}$ Phosphorous or arsenic doped Si at 300 K

Example:

$$N_D = 10^{16} \text{ cm}^{-3}$$

$$p \approx 10^{10} \text{ cm}^{-3}$$

$$n = 10^{16} \text{ cm}^{-3} \gg n_i = 10^{10} \text{ cm}^{-3}$$

$$np = n_i^2 = 10^{20} \text{ cm}^{-3}$$

extrinsic semiconductor

$$p = \frac{n_i^2}{n} = \frac{10^{20}}{10^{16}} = 10^4 \text{ cm}^{-3}$$

Be careful about units!

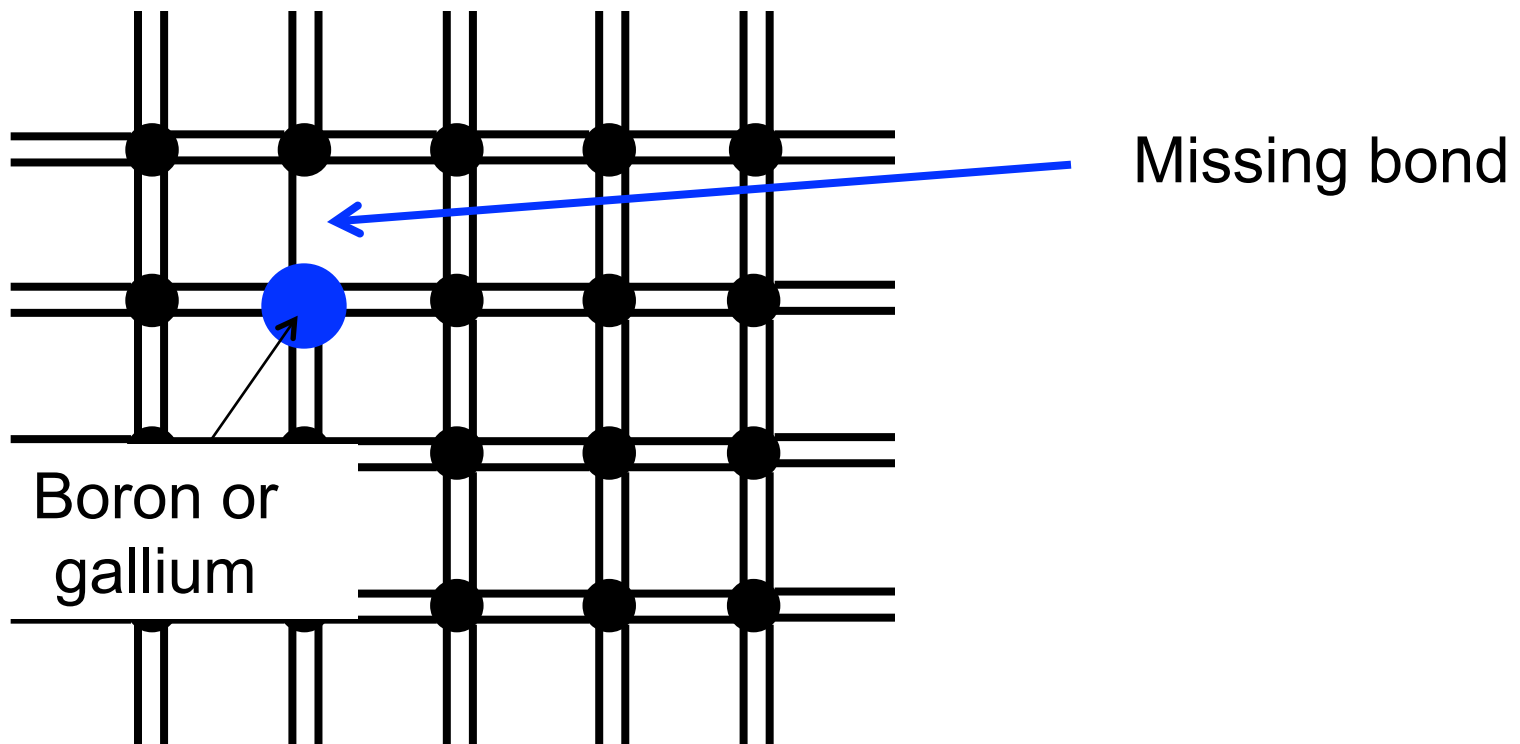
$$n \approx N_D^+ \text{ cm}^{-3}$$

We will be working in SI (MKS) units. The carrier concentration should be given per cubic **meter**, but semiconductor people like to mix their units.

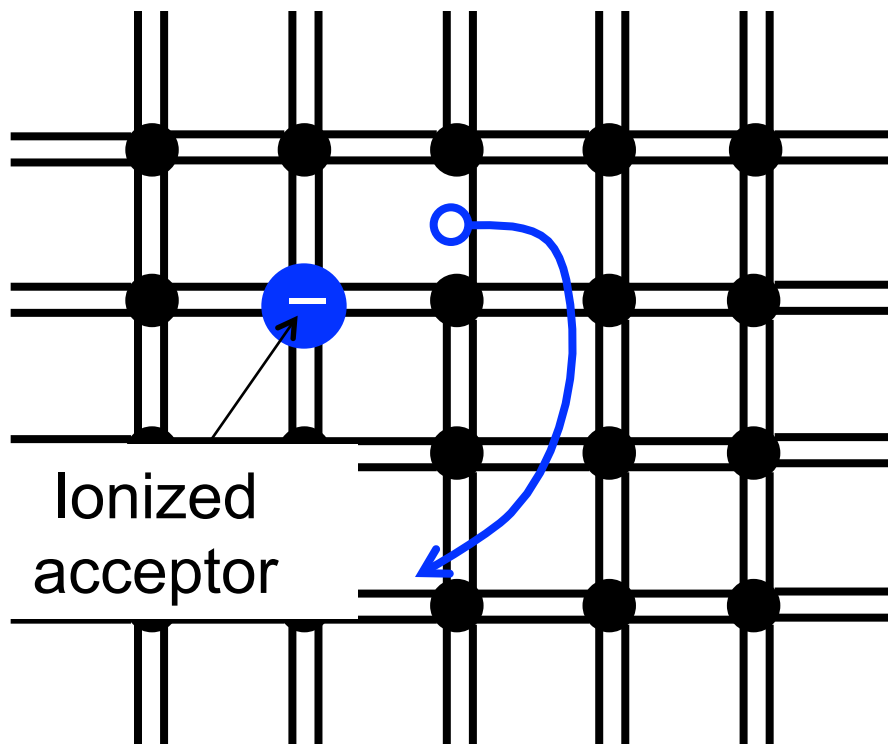
It is safest to do the calculations in SI units, and then convert to cubic cm.

$$n = 10^{26} \text{ m}^{-3} \rightarrow n = 10^{26} \frac{1}{\text{m}^3} \times \left(\frac{10^{-2} \text{ m}}{\text{cm}} \right)^3 \rightarrow n = 10^{20} \text{ cm}^{-3}$$

Acceptors: P-type doping



Ionized acceptor



Concentration of dopants:

$$N_A \text{ cm}^{-3}$$

Concentration of ionized acceptors:

$$N_A^- \text{ cm}^{-3}$$

Concentration of “holes” in the valence band:

$$p \approx N_A^- \text{ cm}^{-3}$$

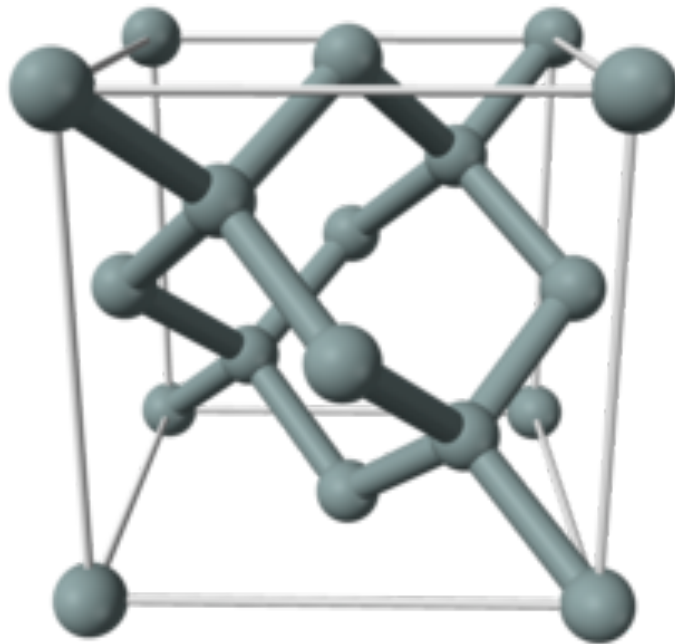
Question

1) What type of dopant is Si in GaAs?

- a) n-type
- b) p-type
- c) either n-type or p-type
- d) neither n-type nor p-type
- e) don't know

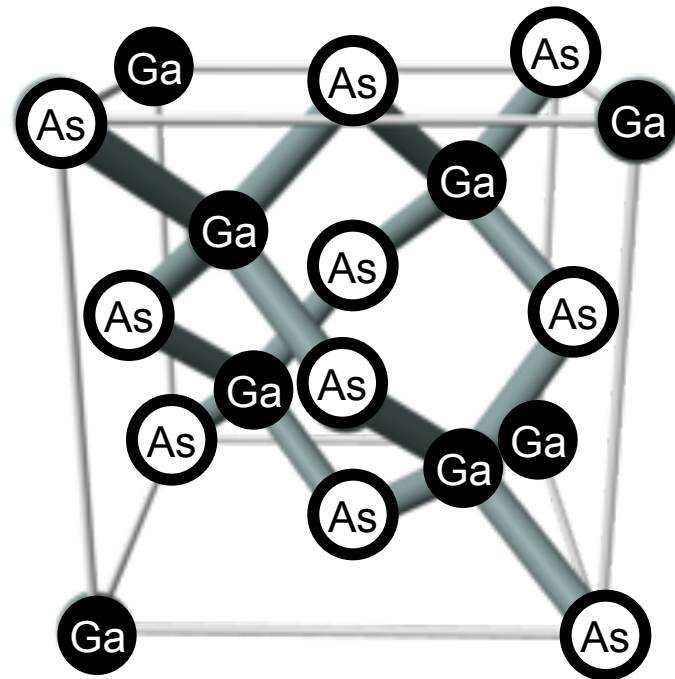
Si vs. GaAs crystals

Si



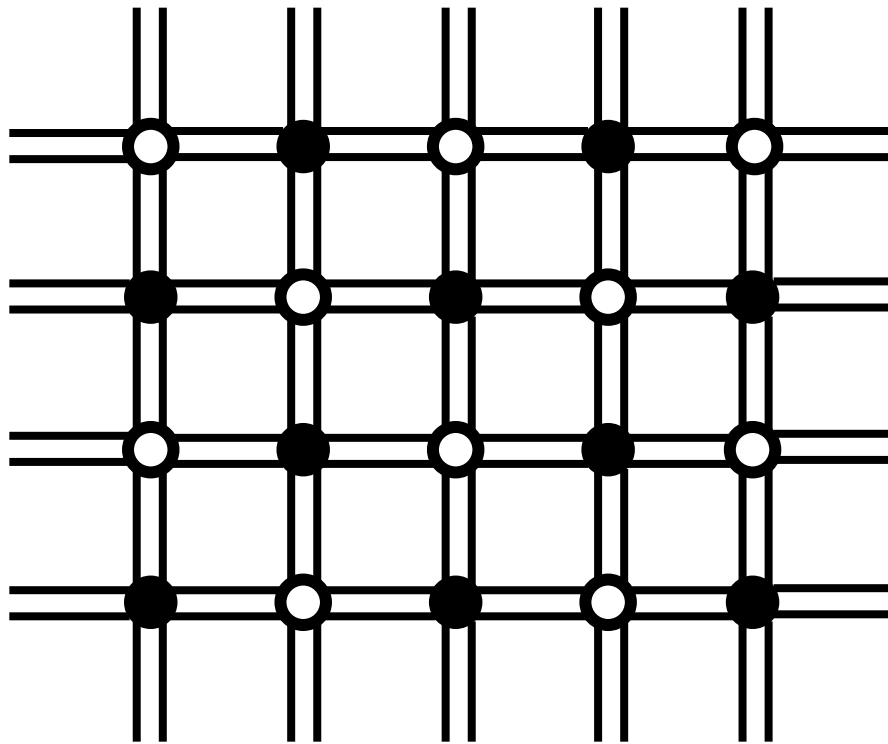
diamond lattice

GaAs



zinc blende lattice

GaAs bonding cartoon



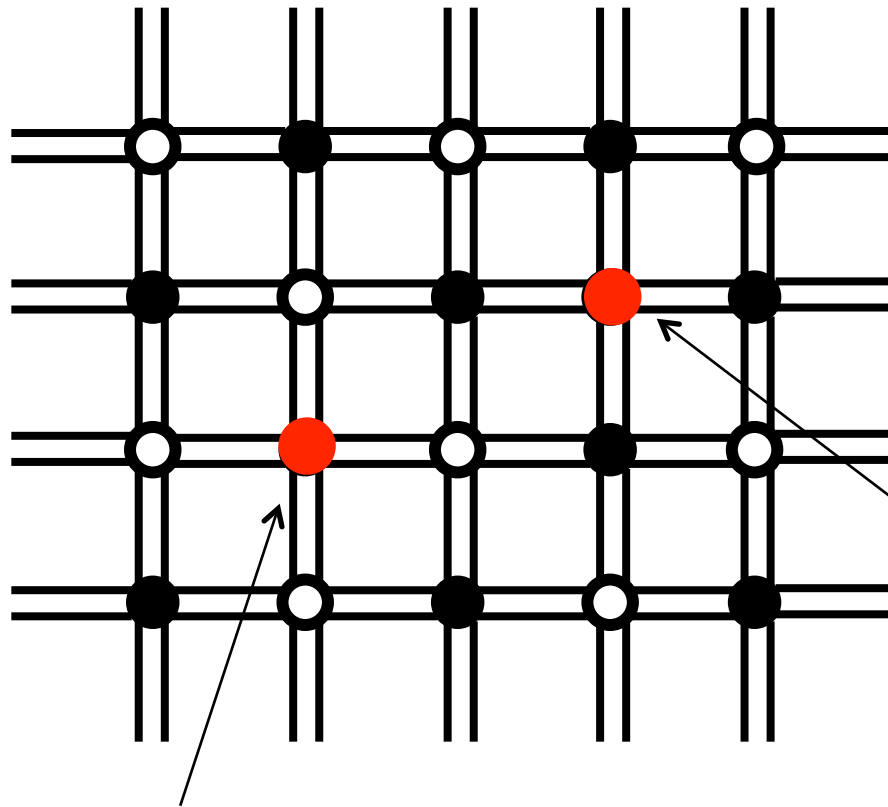
● Ga

○ As

Every Ga atom has
4 NN As atoms.

Every As atom has
4 NN Ga atoms.

Si in GaAs: Two possibilities



- Ga (III)
- As (V)
- Si (IV)

Si on a Ga site is a donor.

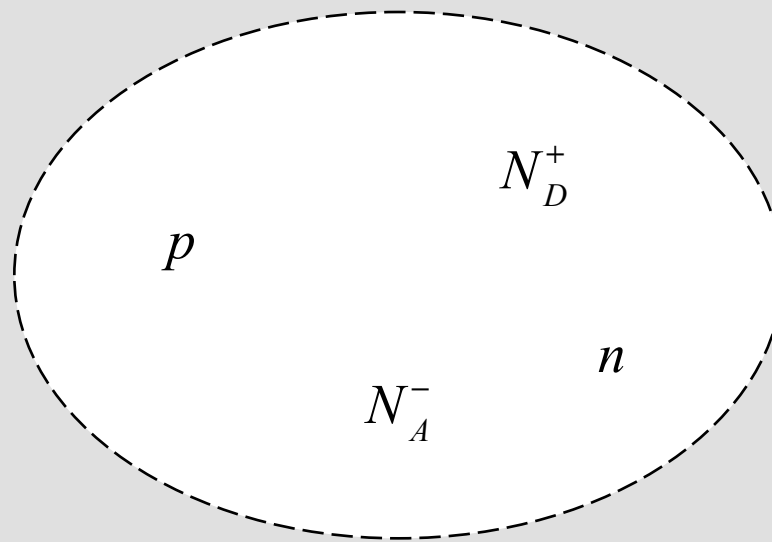
Si on a As site is an acceptor.

Si is an “amphoteric” dopant in GaAs.

Space charge density

What is the net charge in this region?

$$\rho = q[p - n + N_D^+ - N_A^-] \quad \text{C/m}^3$$



bulk, uniform semiconductor

Space charge neutrality

“Nature abhors a vacuum.” Nature also abhors a charge.

Mobile charges (electrons and holes) will be attracted to the immobile ionized dopants), so that the net charge is zero.

$$\rho = q \left[p - n + N_D^+ - N_A^- \right] = 0$$

Almost uniform semiconductors will be nearly neutral, but with strong non-uniformities (e.g. PN junctions), there will be a space charge.

Space charge neutrality + np product

$$\rho = q \left[p - n + N_D^+ - N_A^- \right] = 0$$

$$np = n_i^2$$

Always true in equilibrium – even for doped semiconductors.

These are two equations in two unknowns – p and n .

Solving for the carrier density

1) charge neutrality: $p - n + N_D^+ - N_A^- = 0$

2) eq. np product: $np = n_i^2$

3) result: $\frac{n_i^2}{n} - n + N_D^+ - N_A^- = 0$

$$p - \frac{n_i^2}{p} + N_D^+ - N_A^- = 0$$

N-type extrinsic semiconductors at **moderate** temps

$$n = \frac{N_D^+ - N_A^-}{2} + \left[\left(\frac{N_D^+ - N_A^-}{2} \right)^2 + n_i^2 \right]^{1/2}$$

$$p = \frac{n_i^2}{n}$$

Extrinsic semiconductors:

$$N_D^+ = N_D$$

$$N_A^- = N_A$$

$$N_D - N_A \gg n_i$$

$$n = N_D - N_A$$

Example 1

Consider Si doped with phosphorus at $N_D = 2.00 \times 10^{15} \text{ cm}^{-3}$
The temperature is 300 K. What are n and p ?

Recall that at 300 K in Si, $n_i = 1.00 \times 10^{10} \text{ cm}^{-3}$

Assume that the donors are fully ionized.

$$n = \frac{N_D - N_A}{2} + \left[\left(\frac{N_D - N_A}{2} \right)^2 + n_i^2 \right]^{1/2} = \frac{N_D}{2} + \left[\left(\frac{N_D}{2} \right)^2 + n_i^2 \right]^{1/2}$$

$$N_D \gg n_i$$

$$p = n_i^2 / n$$

$$n = N_D = 2.00 \times 10^{15} \text{ cm}^{-3}$$

$$p = (10^{10})^2 / 2 \times 10^{15} = 5 \times 10^4 \text{ cm}^{-3}$$

Example 2

Consider Si doped with phosphorus at $N_D = 2.00 \times 10^{15} \text{ cm}^{-3}$ and **Boron** at $N_A = 1.00 \times 10^{15} \text{ cm}^{-3}$.

The temperature is 300 K. What are n and p ?

$$n = \frac{N_D - N_A}{2} + \left[\left(\frac{N_D - N_A}{2} \right)^2 + n_i^2 \right]^{1/2}$$

$$N_D - N_A \gg n_i \quad n = N_D - N_A$$

$$p = n_i^2 / n$$

$$n = 1.00 \times 10^{15} \text{ cm}^{-3}$$

$$p = (10^{10})^2 / 1 \times 10^{15} = 1 \times 10^5 \text{ cm}^{-3}$$

N-type semiconductors at **high** temps

$$n = \frac{N_D^+ - N_A^-}{2} + \left[\left(\frac{N_D^+ - N_A^-}{2} \right)^2 + n_i^2 \right]^{1/2}$$

$$p = \frac{n_i^2}{n}$$

Intrinsic semiconductors:

$$N_D^+ = N_D$$

$$N_A^- = N_A$$

$$n_i \gg N_D - N_A$$

$$n = p = n_i$$

N-type semiconductors at **low** temperatures

$$n = \frac{N_D^+ - N_A^-}{2} + \left[\left(\frac{N_D^+ - N_A^-}{2} \right)^2 + n_i^2 \right]^{1/2}$$

$$p = \frac{n_i^2}{n}$$

Freeze out::

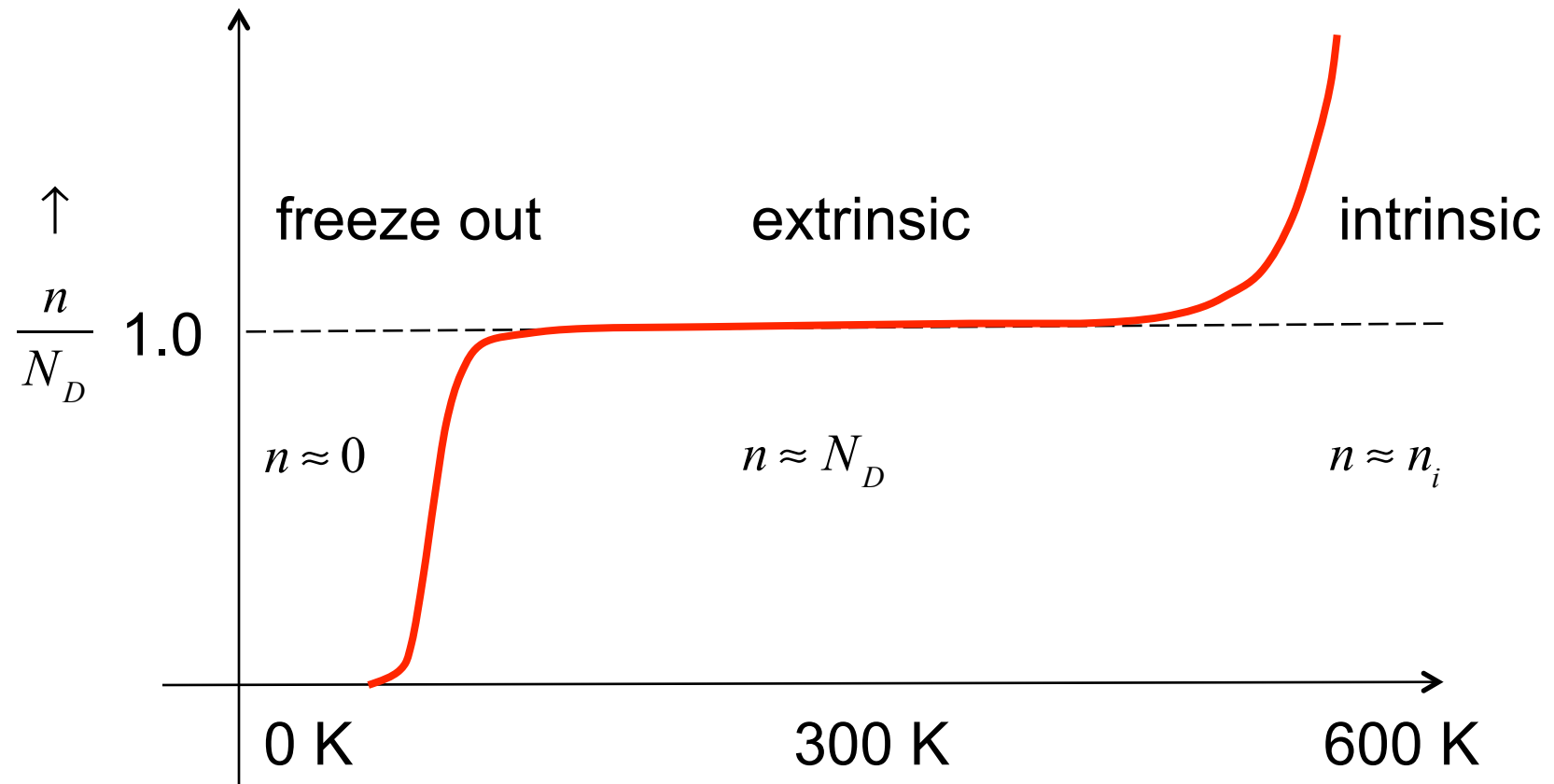
$$N_D^+ = 0$$

$$N_A^- = 0$$

$$n_i \approx 0$$

$$n = p = 0$$

Carrier concentration vs. temperature



P-type semiconductors

1) charge neutrality:

$$p - n + N_D^+ - N_A^- = 0$$

2) np product:

$$np = n_i^2$$

3) quadratic eqn. for p:

$$p - \frac{n_i^2}{p} + N_D^+ - N_A^- = 0$$

$$p = \frac{N_A^- - N_D^+}{2} + \left[\left(\frac{N_A^- - N_D^+}{2} \right)^2 + n_i^2 \right]^{1/2}$$

Exercise: repeat the n-type examples for a p-type semiconductor

Summary

To dope a semiconductor, we replace a few atoms with atoms from a different column of the periodic table.

Ionized dopants produce electrons in the conduction band or holes in the valence band.

The carrier concentration vs. temperature characteristic has freeze out, extrinsic, and intrinsic regions.

A low temperatures, semiconductors become insulators.

A high temperatures, doped semiconductors become intrinsic.

Doped semiconductors

- 1) The np product
- 2) Doping
- 3) Carrier concentration vs. doping density
- 4) Carrier concentration vs. temperature

