

# ECE-305: Spring 2018

## Ideal Diodes+Solar Cells

Pierret, *Semiconductor Device Fundamentals* (SDF)  
Chapter 6

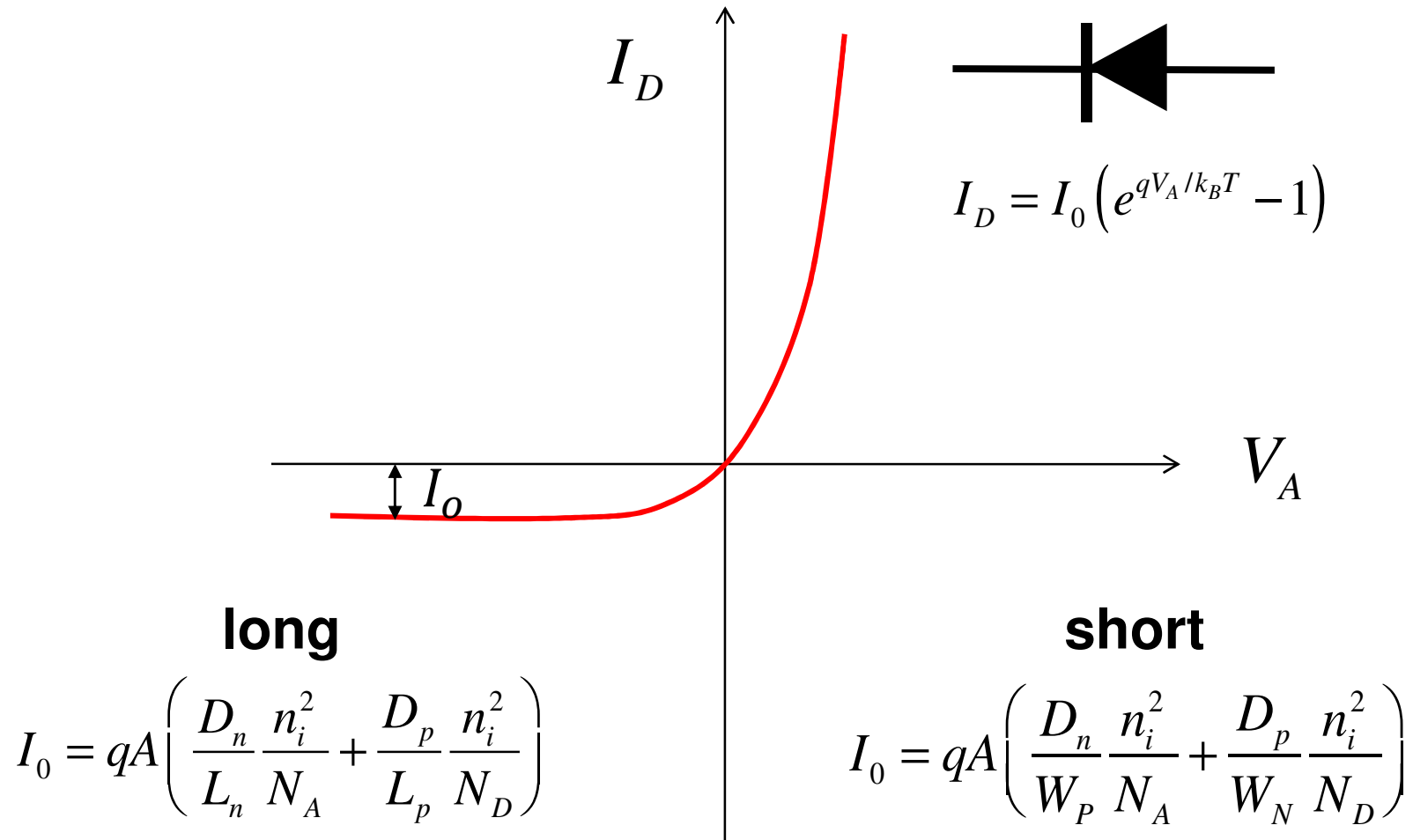
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# outline

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- 1) Ideal Diode Equation
- 2) Ideal Diode Example
- 3) A Primer on Solar Cells
- 4) Diode Non-idealities

# ideal diode equation recap

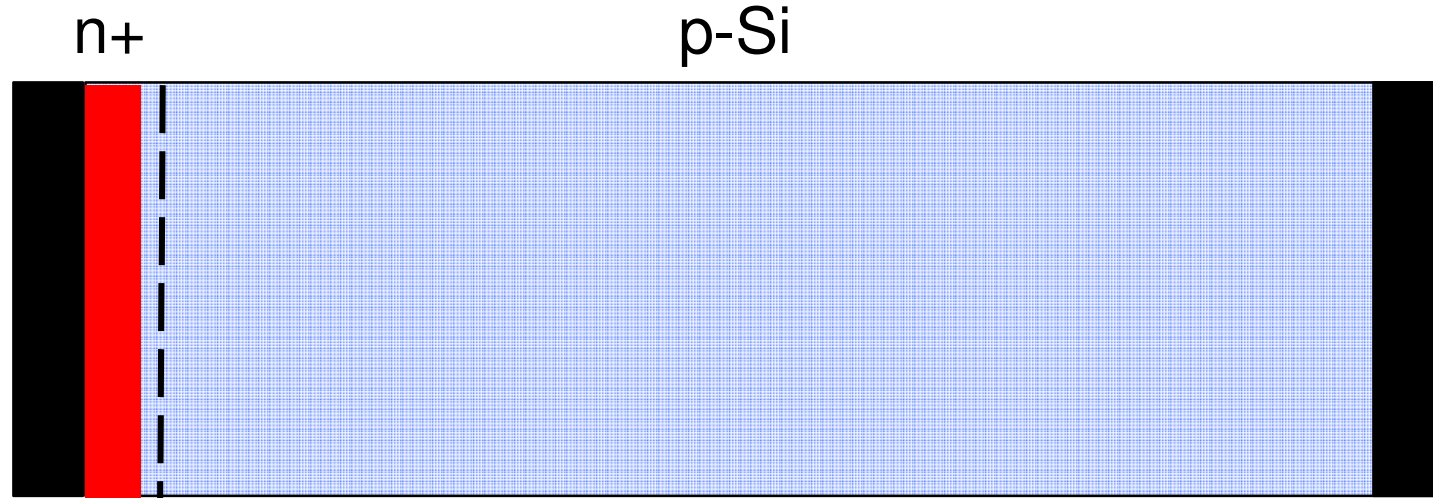


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# example



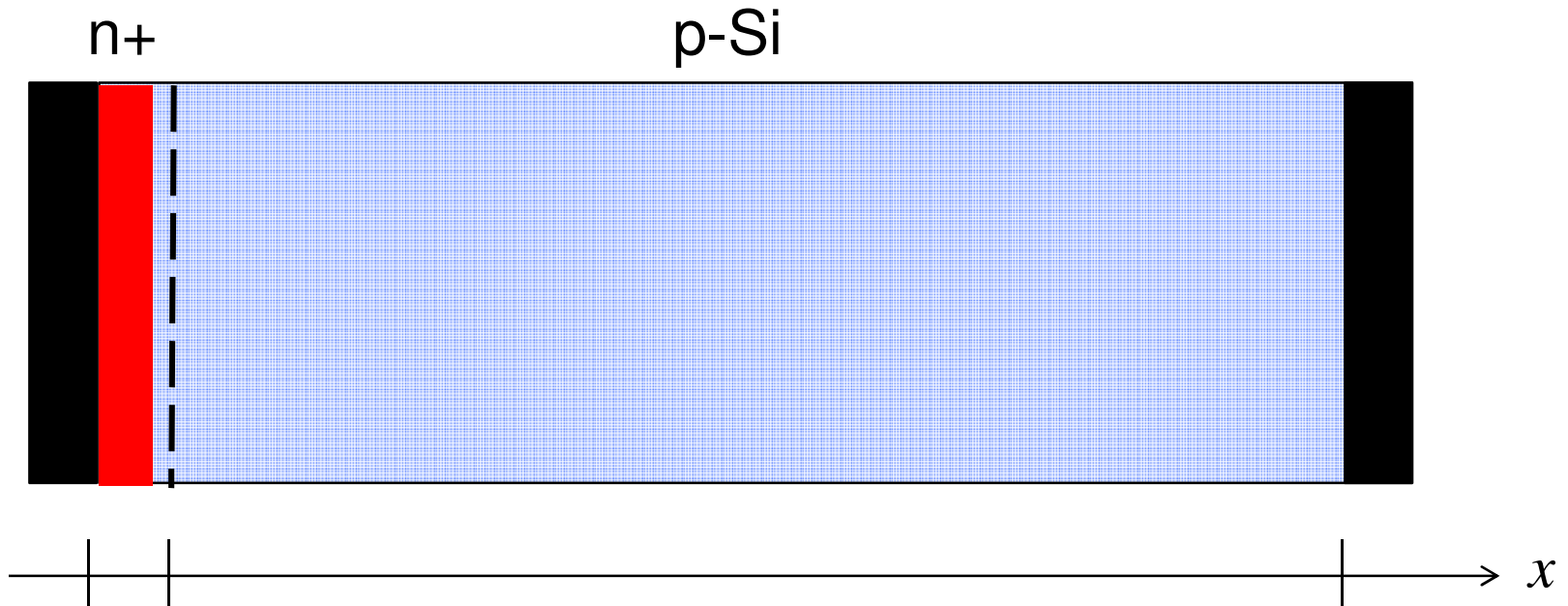
$-W_N$     $0$                        $\tau_n = 10 \mu s$                        $W_P$

$N_D = 10^{20} \text{ cm}^{-3}$        $W_N = 0.1 \mu m$                        $I_D = I_0 \left( e^{qV_A/k_B T} - 1 \right)$

$N_A = 10^{17} \text{ cm}^{-3}$        $\tau_p = 1 \mu s$                                        $I_0 = ?$

$W_P = 10 \mu m$                       **Is this a one-sided diode?**

# example: one-sided diodes



$$I_0 = qA \left( \frac{D_n}{L_n} \frac{n_i^2}{N_A} + \frac{D_p}{L_p} \frac{n_i^2}{N_D} \right) \rightarrow qA \left( \frac{D_n}{L_n} \frac{n_i^2}{N_A} \right)$$

$$I_0 = qA \left( \frac{D_n}{W_P} \frac{n_i^2}{N_A} + \frac{D_p}{W_n} \frac{n_i^2}{N_D} \right) \rightarrow qA \left( \frac{D_n}{W_P} \frac{n_i^2}{N_A} \right)$$

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# solar cells

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SunPower <http://us.sunpower.com>

2/22/2018

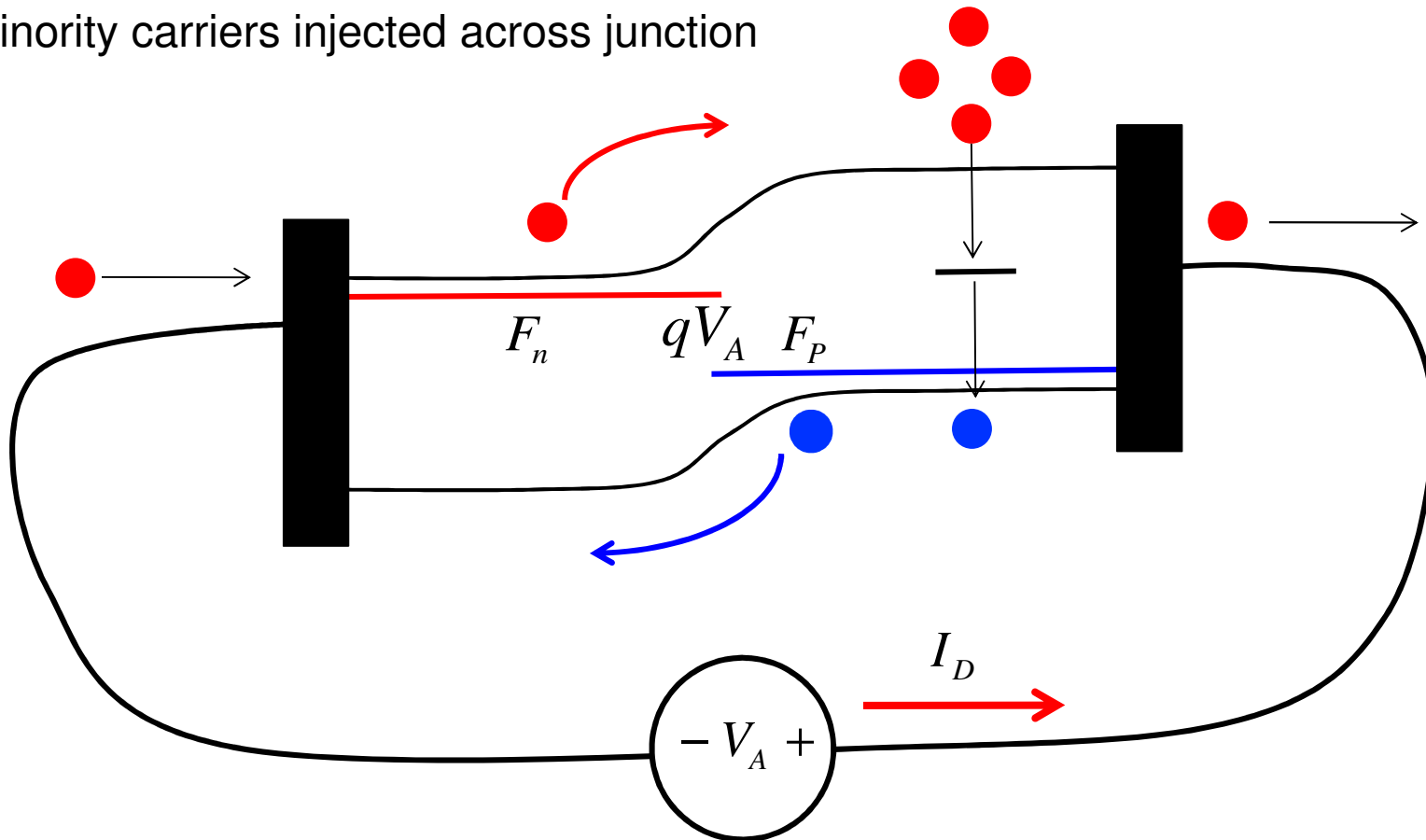
Bermel ECE 305 S18

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# recombination and dark current

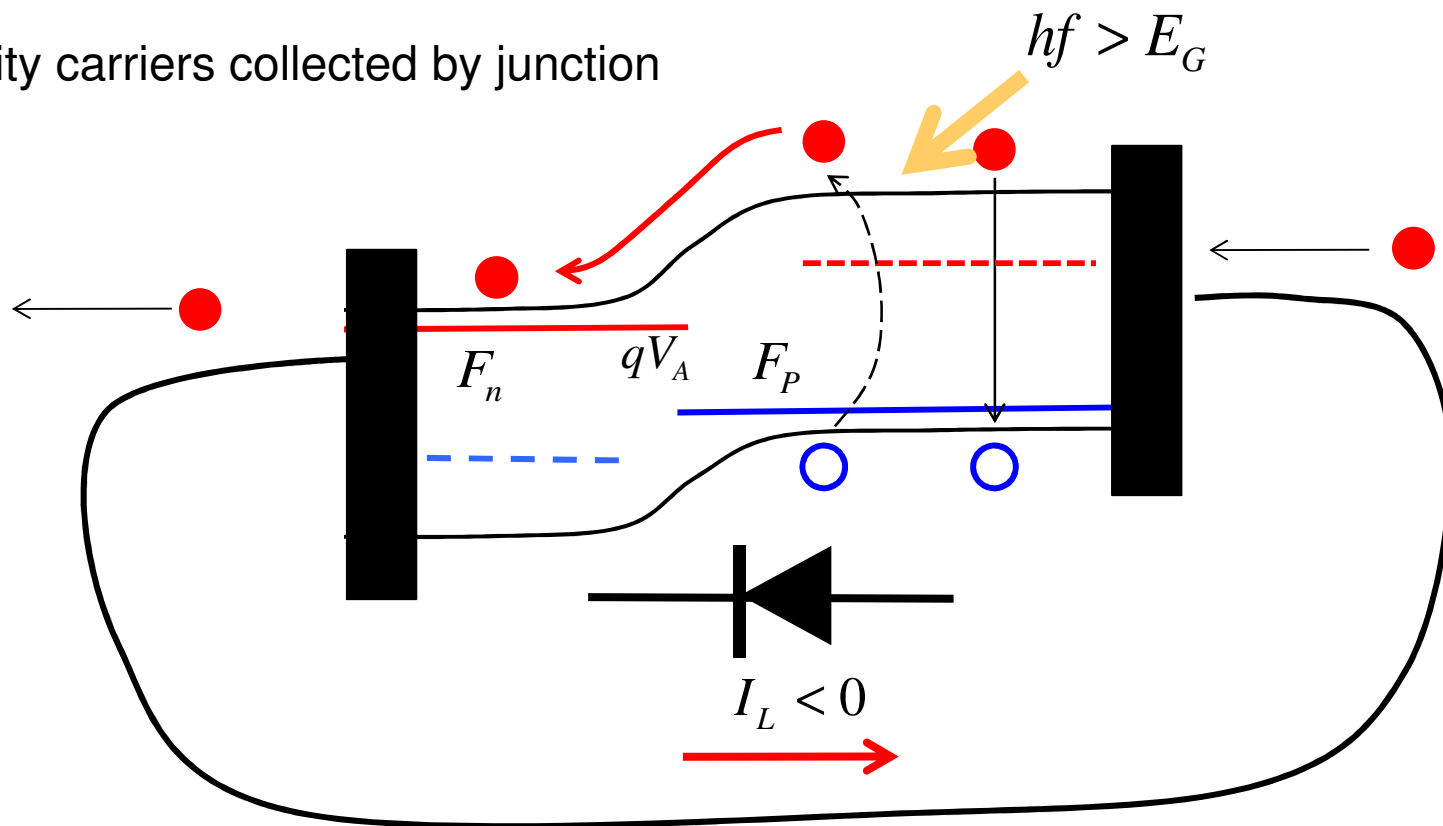
minority carriers injected across junction



Every time a minority electron **recombines** on the p-side, one electron flows in the external current.

# generation and current

minority carriers collected by junction

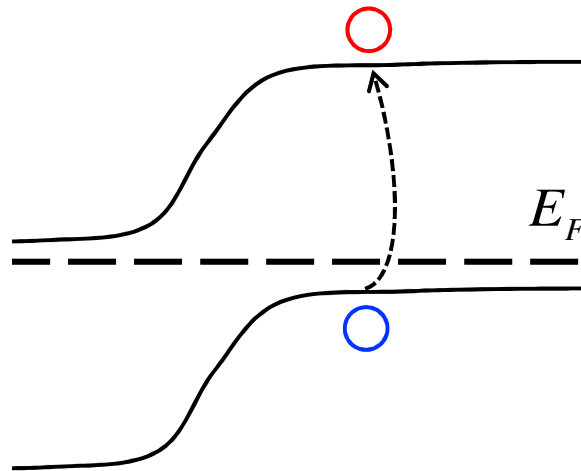


**Every time a minority electron is generated and collected by the PN junction, one electron flows in the external current.**

# solar cell operation

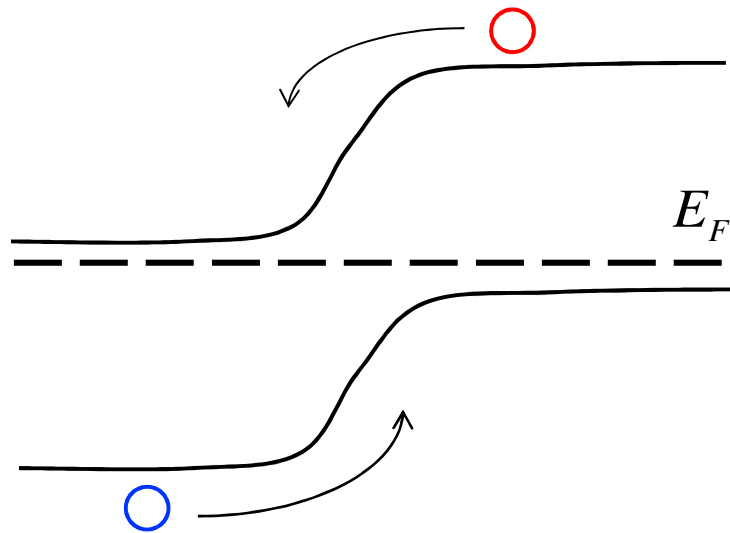
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## 1) Light generates e-h pairs

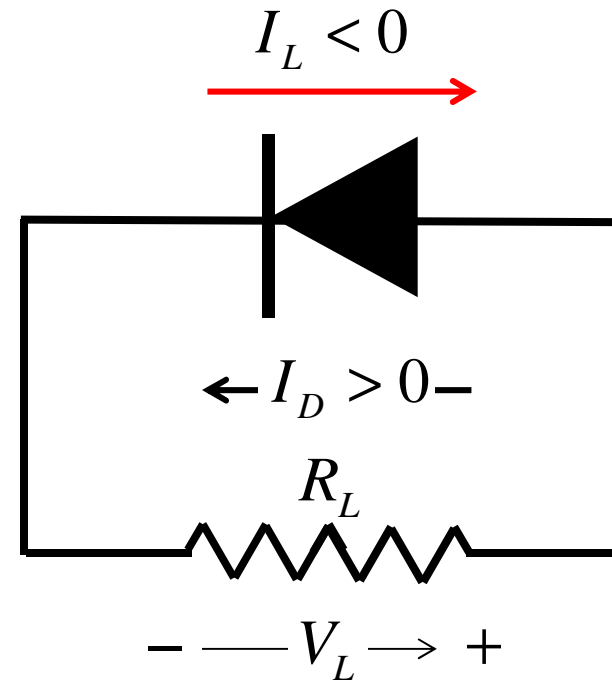


# solar cell operation

2) PN junction collects e-h pairs



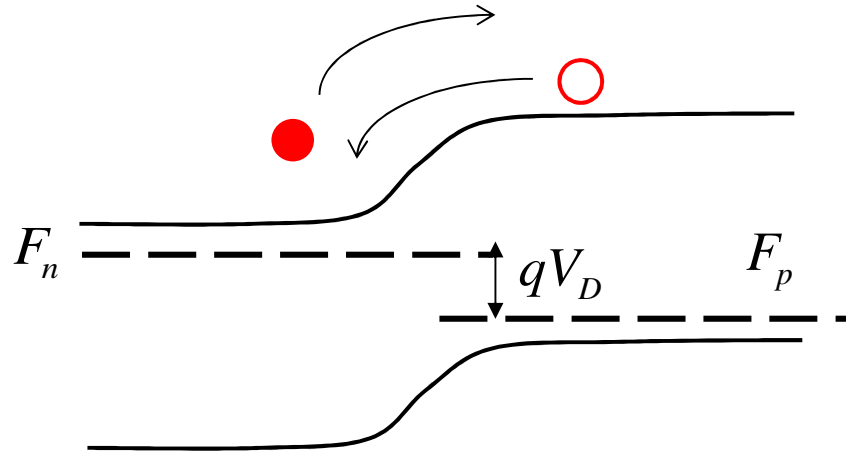
3) Current flows through load



forward bias develops across PN junction

# solar cell operation

## 4) Forward bias reduces current



## 5) IV characteristic is a superposition

$$I_{TOT} = I_0 \left( e^{qV_D/k_B T} - 1 \right) - I_{SC}$$

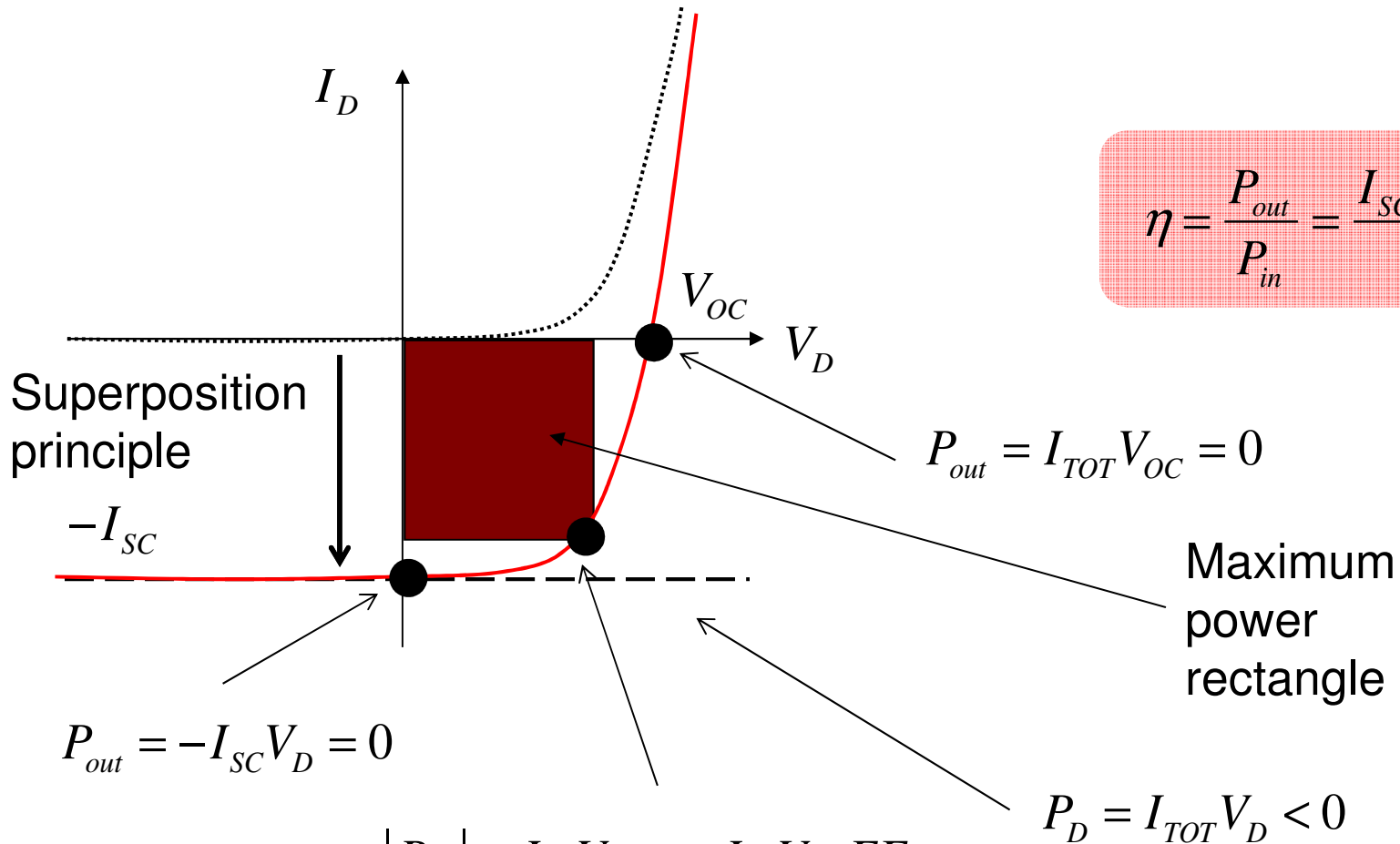
diode (dark)  
current

light-generated  
current

# IV characteristic

$$I_D = I_0 \left( e^{qV_D/k_B T} - 1 \right)$$

$$I_{TOT} = I_0 \left( e^{qV_D/k_B T} - 1 \right) - I_{SC}$$



$$\eta = \frac{P_{out}}{P_{in}} = \frac{I_{SC} V_{OC} FF}{P_{in}}$$

# solar cell efficiency

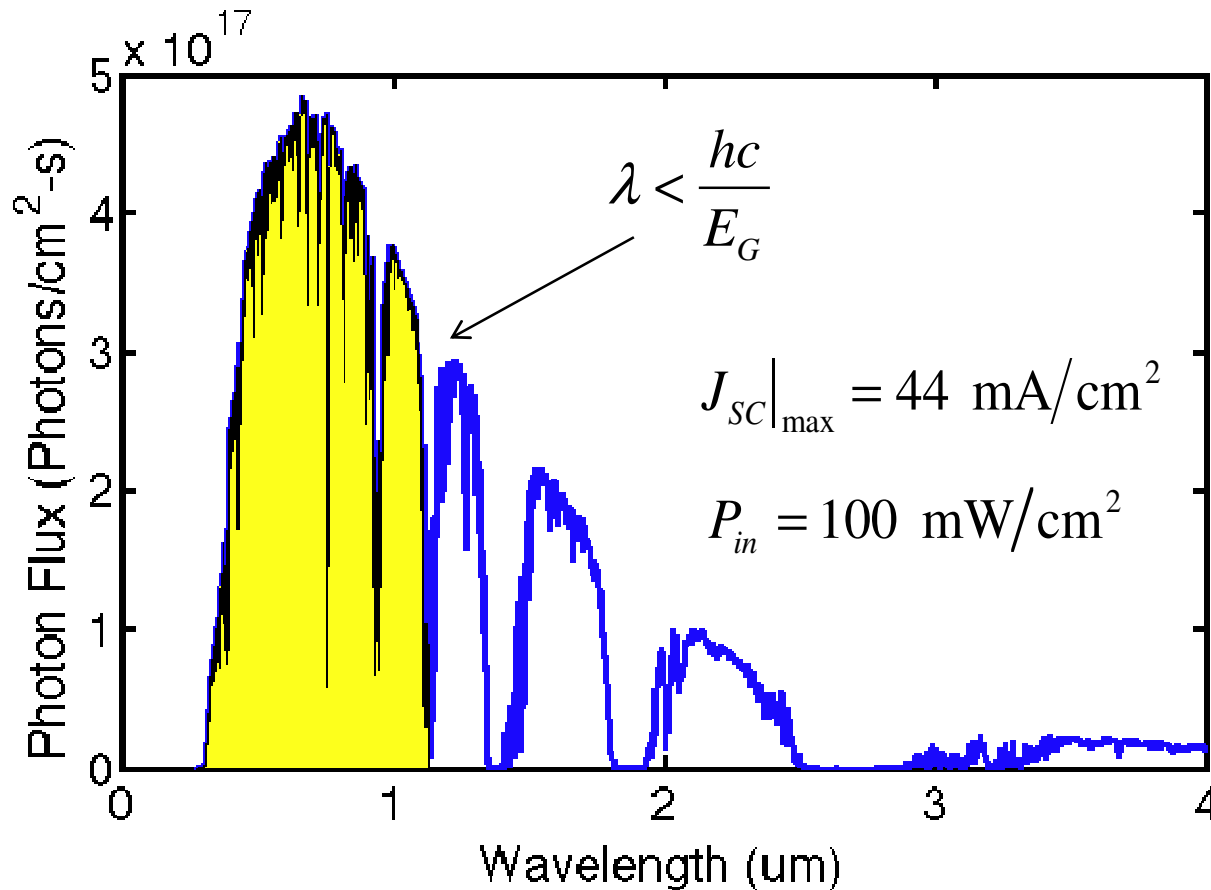
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$$\eta = \frac{P_{out}}{P_{in}} = \frac{I_{SC} V_{OC} FF}{P_{in}}$$

- 1) Short circuit current
- 2) Open-circuit voltage
- 3) Fill factor

# maximum short circuit current

Example: Silicon  $E_g = 1.1\text{ eV}$ . Only photons with a wavelength  $< 1.12\ \mu\text{m}$  will be absorbed.



solar  
spectrum  
(AM1.5G)



## open-circuit voltage and efficiency

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$$I_{TOT} = I_0 \left( e^{qV/k_B T} - 1 \right) - I_{SC} \quad V_{OC} = \frac{k_B T}{q} \ln \left( \frac{I_{SC}}{I_0} \right) \quad \eta = \frac{P_{out}}{P_{in}} = \frac{I_{SC} V_{OC} FF}{P_{in}}$$

Example for silicon photovoltaics:

$$I_0 = 1 \times 10^{-12} \text{ A}$$

$$\eta = \frac{P_{out}}{P_{in}} = \frac{40 \times 0.63 \times 0.8}{100} = 0.20$$

$$I_{SC} = 0.90 \times 44 \times 10^{-3} = 40 \text{ mA}$$

$$V_{OC} = 0.026 \ln \left( \frac{40 \times 10^{-3}}{1 \times 10^{-12}} \right) = 0.63$$

## Increasing the efficiency

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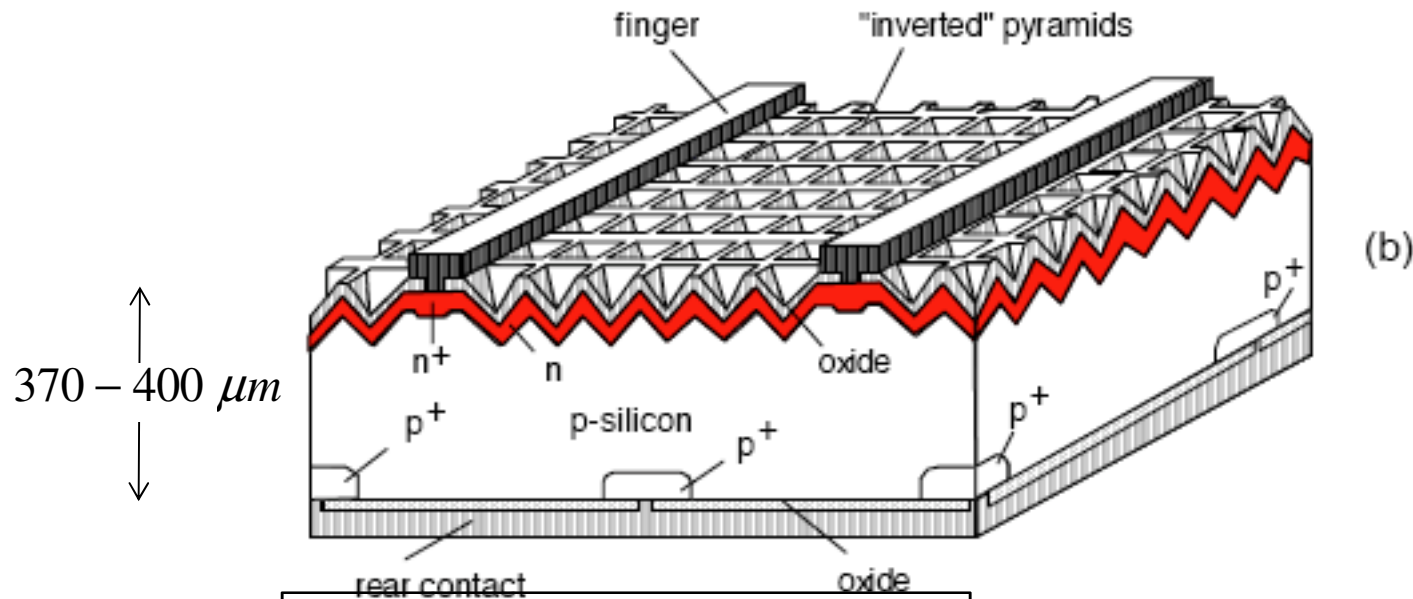
$$\eta = \frac{P_{out}}{P_{in}} = \frac{I_{SC} V_{OC} FF}{P_{in}}$$

1) Increase the short circuit current from 40 towards 44

2) Increase  $V_{OC}$  (decrease  $I_0$ )  $V_{OC} = \frac{k_B T}{q} \ln\left(\frac{I_{SC}}{I_0}\right)$

$$I_0 = qA \left( \frac{D_n n_i^2}{W_P N_A} \right)$$

# efficiency



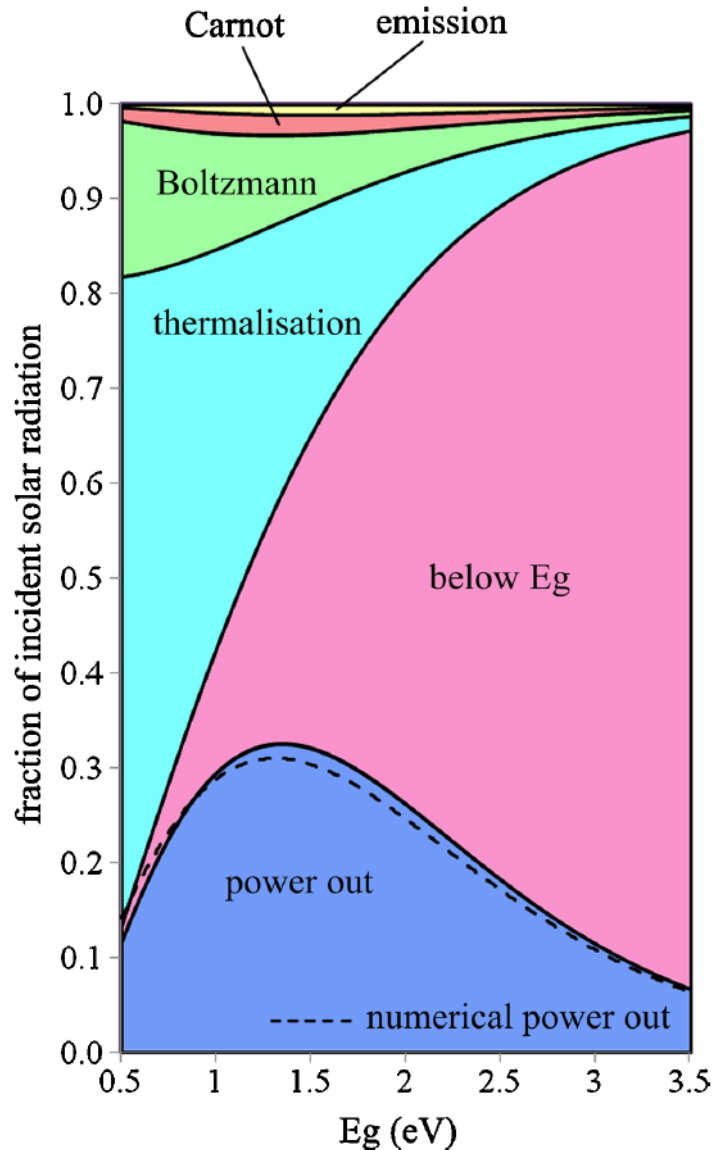
$$J_{SC} = 41.5 \text{ mA/cm}^2 \quad (94\%)$$

$$V_{OC} = 0.703 \quad FF = 0.81$$

$$I_0 = 0.075 \times 10^{-12} \text{ A}$$

Martin Green Group UNSW – Zhao *et al.*, 1998 (25% at 1 sun)

# $J_{SC} - V_{OC}$ trade-off



- 1) Smaller bandgaps give higher short circuit current
- 2) Larger bandgaps give higher open-circuit voltage
- 3) For the given solar spectrum, an optimum bandgap exists.

“Shockley-Queisser Limit”

# ideal diode + solar cell summary

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Ideal diode equation:  $I_D = I_0 \left( e^{qV_A / nk_B T} - 1 \right)$

- 1) Light is absorbed and produces e-h pairs
- 2) PN junctions separate e-h pairs and collect the carriers.
- 3) Current flow in external circuit produces a FB voltage and the FB diode current reduces the total current.
- 4) Power out  $|P_{out}| = I_{mp} V_{mp} = I_{SC} V_{OC} FF$
- 5) Unlike integrated circuit chips, where the value added comes from the design/system, manufacturing costs are critical in PV.

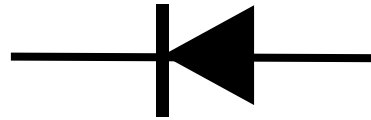
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- ✓ 1) Ideal Diode Equation
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- 4) Diode Non-idealities:
  - Breakdown
  - High forward bias
  - Recombination-generation current

# How large of a voltage can we apply?

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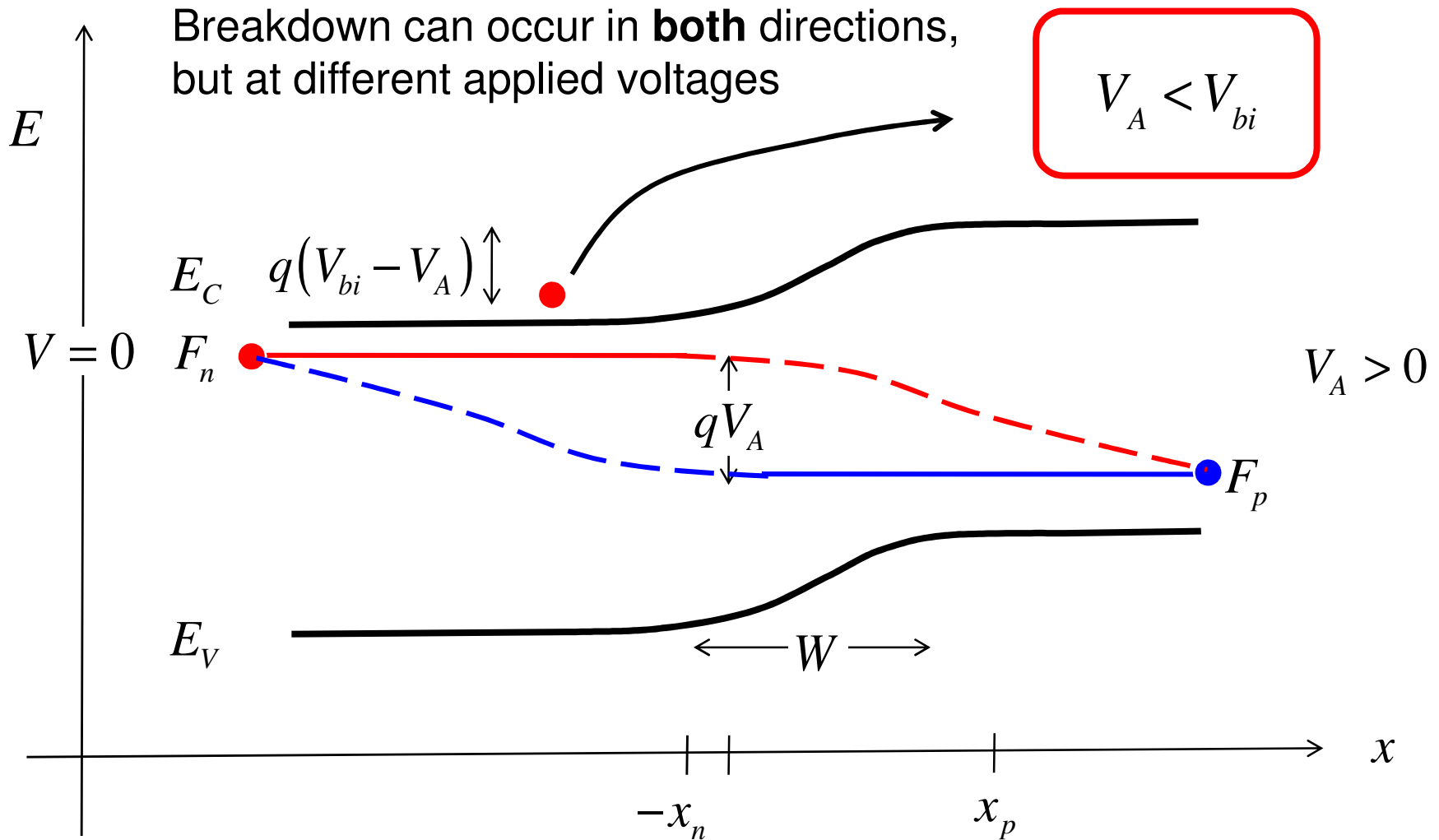


$$I_D = I_0 \left( e^{qV_A/k_B T} - 1 \right)$$

Reverse bias: breakdown

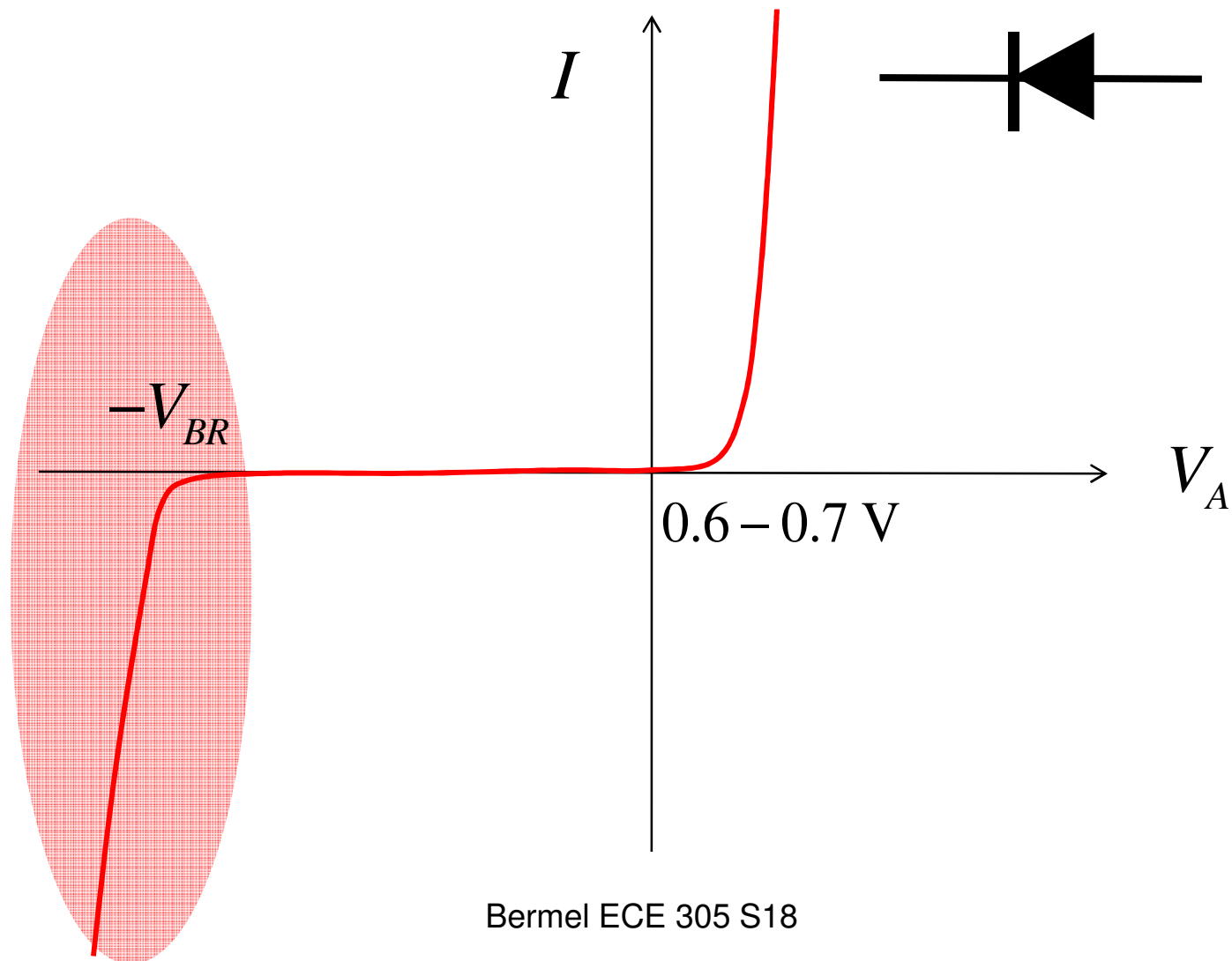
Forward bias: ?

# e-band diagram under bias





# reverse bias breakdown



# real diodes in RB

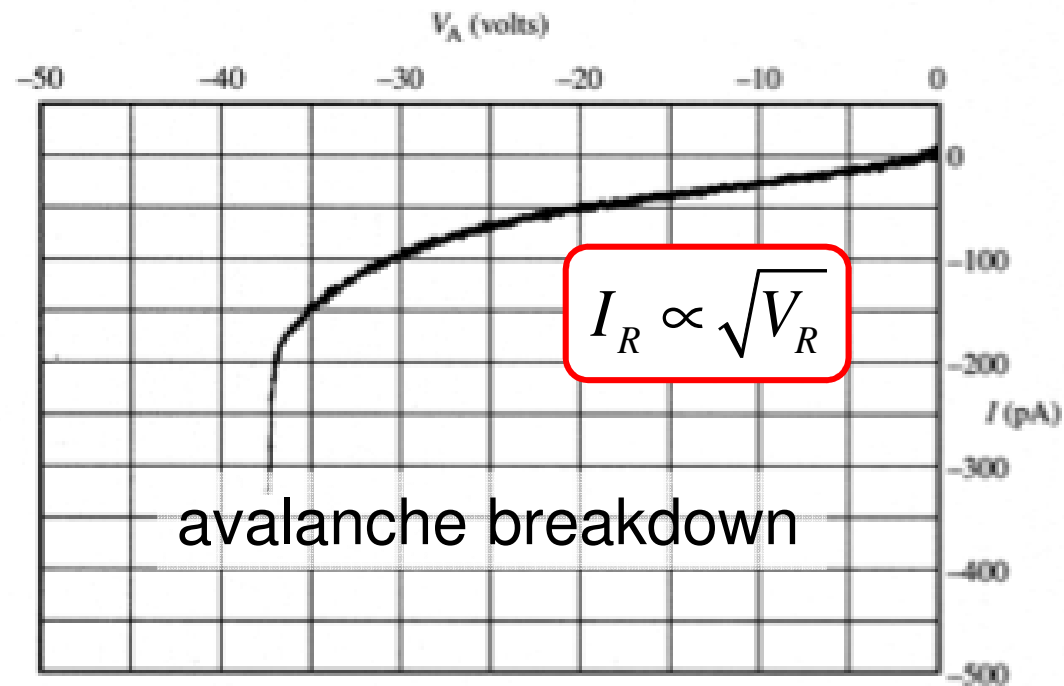


Fig. 6.10(b), Semiconductor Device Fundamentals, R.F. Pierret

# avalanche breakdown

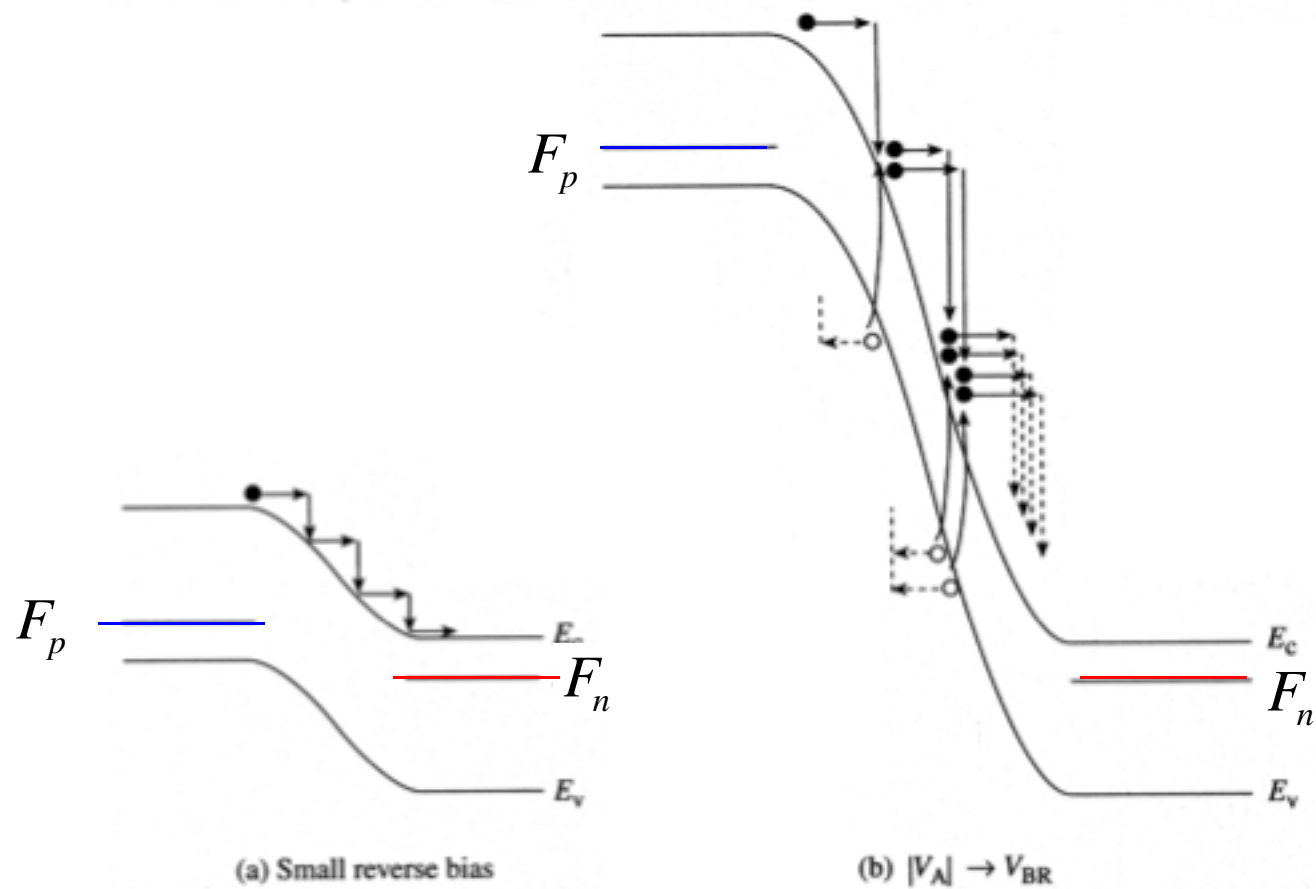
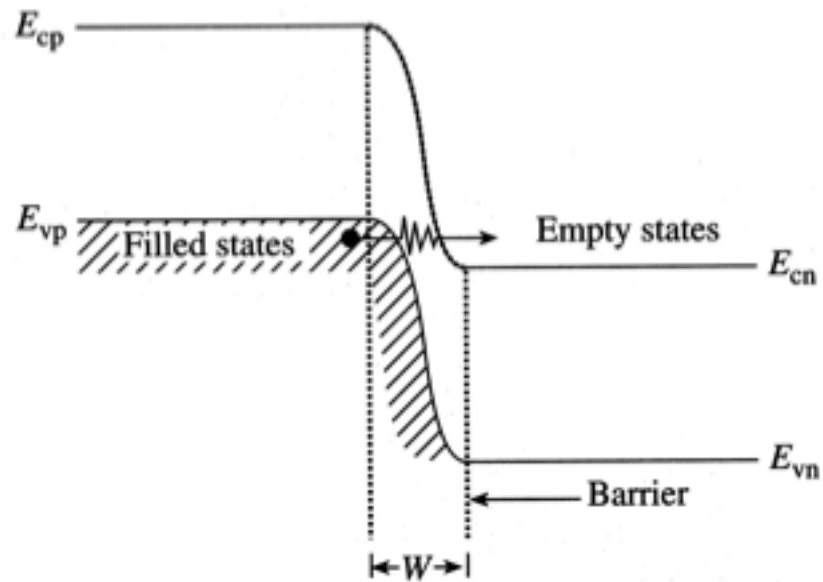


Fig. 6.12, Semiconductor Device Fundamentals, R.F. Pierret

# tunneling



$$W = \left[ \frac{2K_S \epsilon_0}{q} \left( \frac{N_A + N_D}{N_D N_A} \right) V_{bi} \right]^{1/2} \approx \left[ \frac{2K_S \epsilon_0}{q N_A} V_{bi} \right]^{1/2}$$

Fig. 6.14, Semiconductor Device Fundamentals, R.F. Pierret

# breakdown vs. doping

$$V_{BR} \propto \frac{1}{N_A}$$

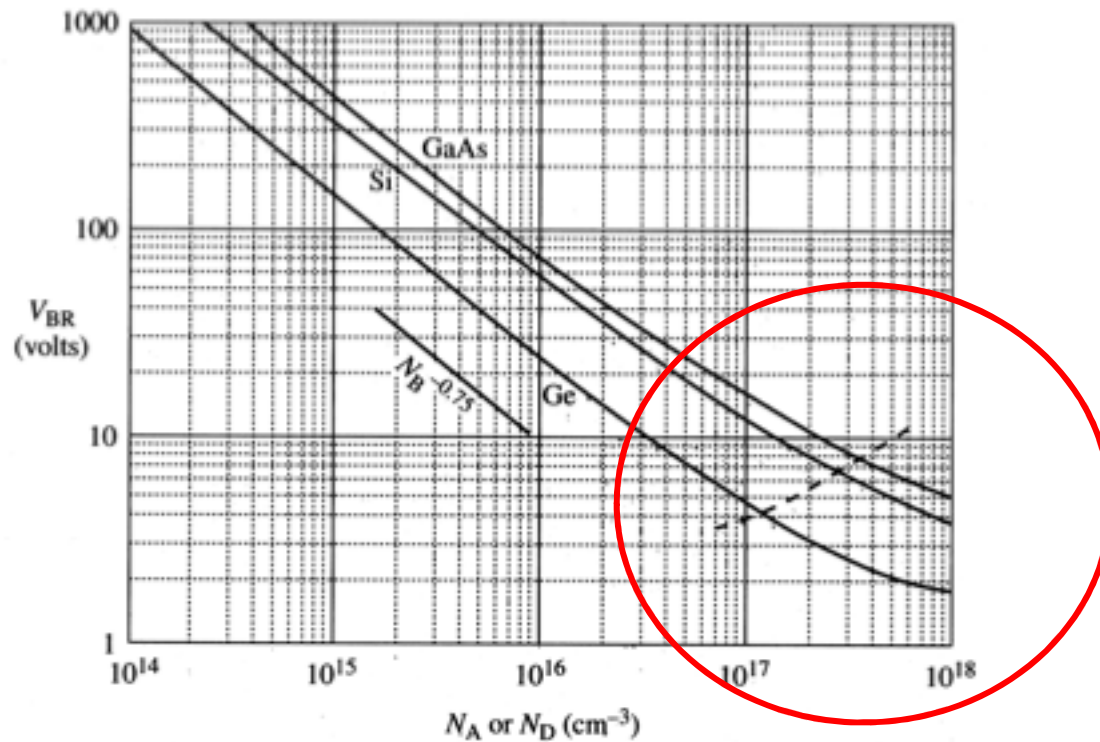


Fig. 6.11, Semiconductor Device Fundamentals, R.F. Pierret

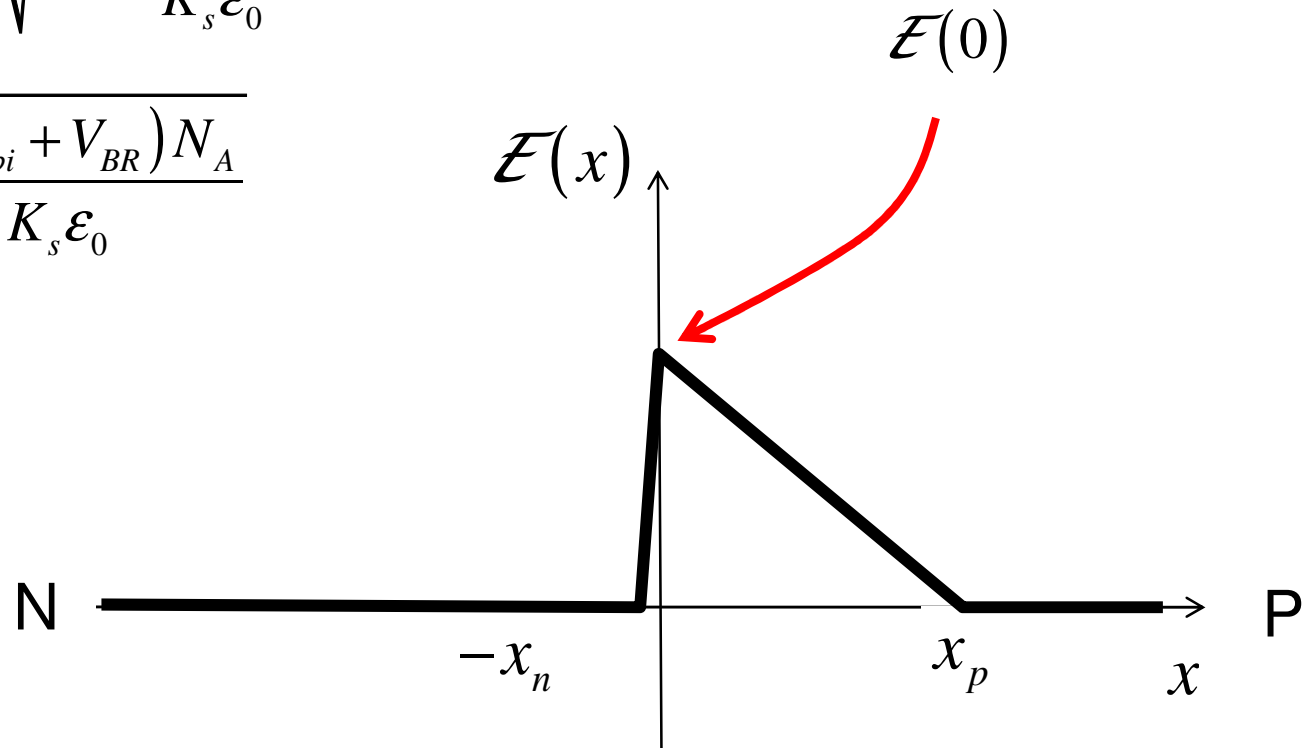
# breakdown voltage and critical electric field

$$N_D \gg N_A \Rightarrow \mathcal{E}(0) = \sqrt{\frac{2q(V_{bi} + V_R)N_A}{K_s \epsilon_0}}$$

$$\mathcal{E}(0) = \mathcal{E}_{CR} = \sqrt{\frac{2q(V_{bi} + V_{BR})N_A}{K_s \epsilon_0}}$$

$$V_{BR} = \frac{K_s \epsilon_0}{2qN_A} \mathcal{E}_{CR}^2 - V_{bi}$$

$$V_{BR} \propto \frac{1}{N_A}$$



# critical electric field

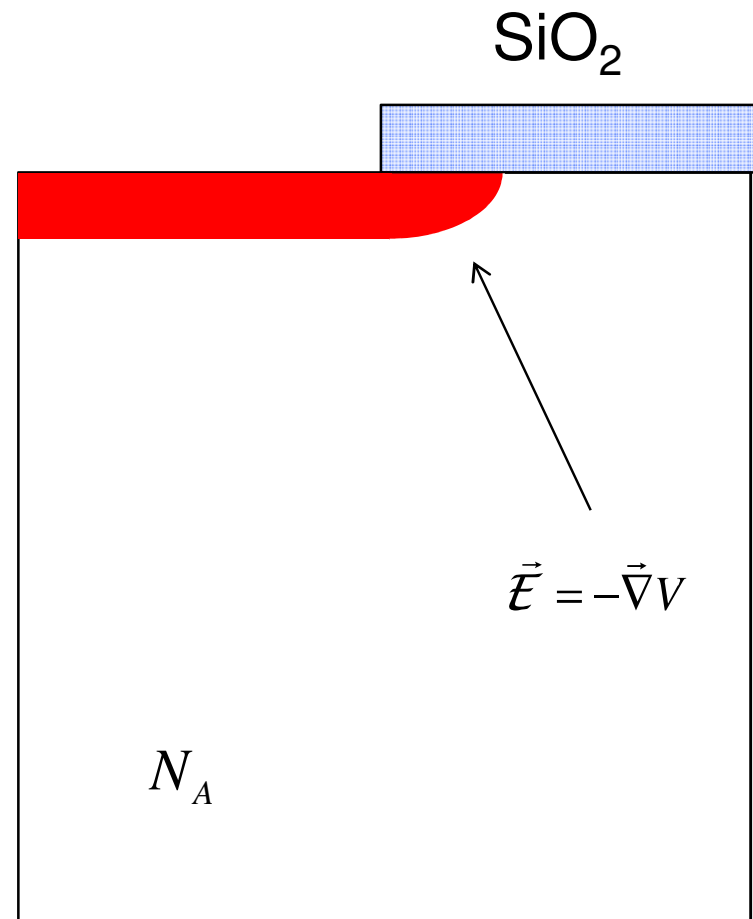
$$\mathcal{E}_{CR} = \sqrt{\frac{2q(V_{bi} + V_{BR})N_A}{K_s \epsilon_0}} \quad V_{BR} \propto \frac{1}{N_A}$$

$$\mathcal{E}_{CR} \approx 3 \times 10^5 \text{ V/cm} \quad (\text{Silicon})$$

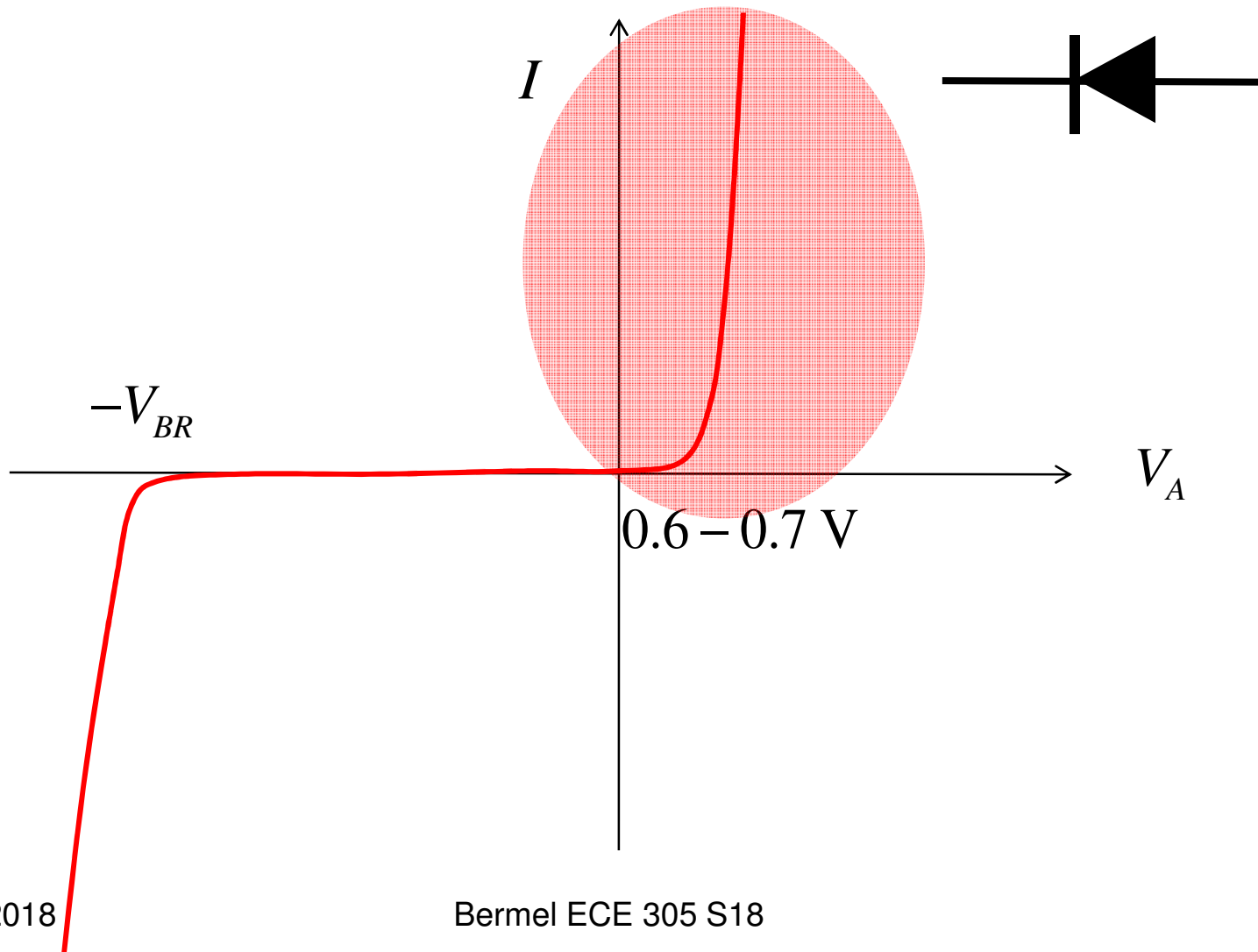
$$\mathcal{E}_{CR} \approx 1 \times 10^5 \text{ V/cm} \quad (\text{Germanium})$$

$$\mathcal{E}_{CR} \approx 5 \times 10^6 \text{ V/cm} \quad (\text{GaN})$$

$$\mathcal{E}_{CR} \approx 3 \times 10^6 \text{ V/cm} \quad (\text{air})$$



# forward bias



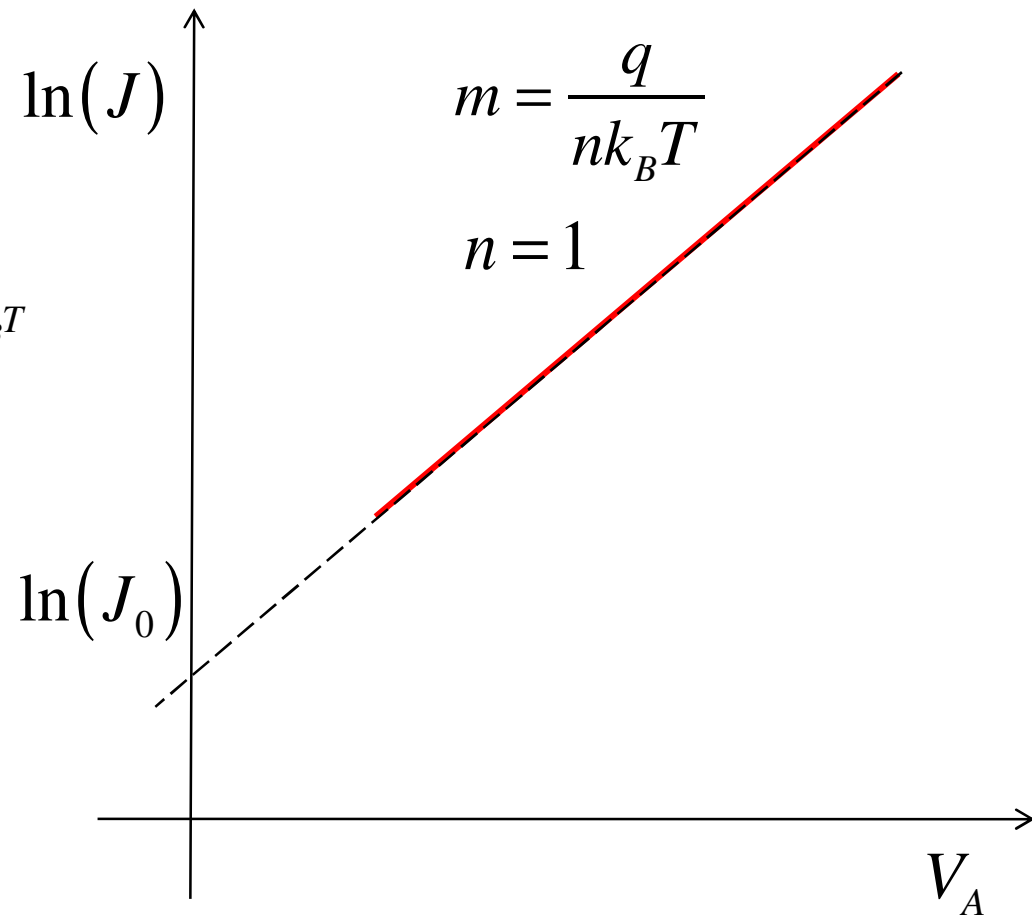


# ideal diode current in forward bias

$$J = J_0 \left( e^{qV_A/k_B T} - 1 \right) \approx J_0 e^{qV_A/k_B T}$$

$$\ln(J) = \ln(J_0) + qV_A / k_B T$$

$$\ln(J) = \ln(J_0) + mV_A$$



# real diodes in forward bias

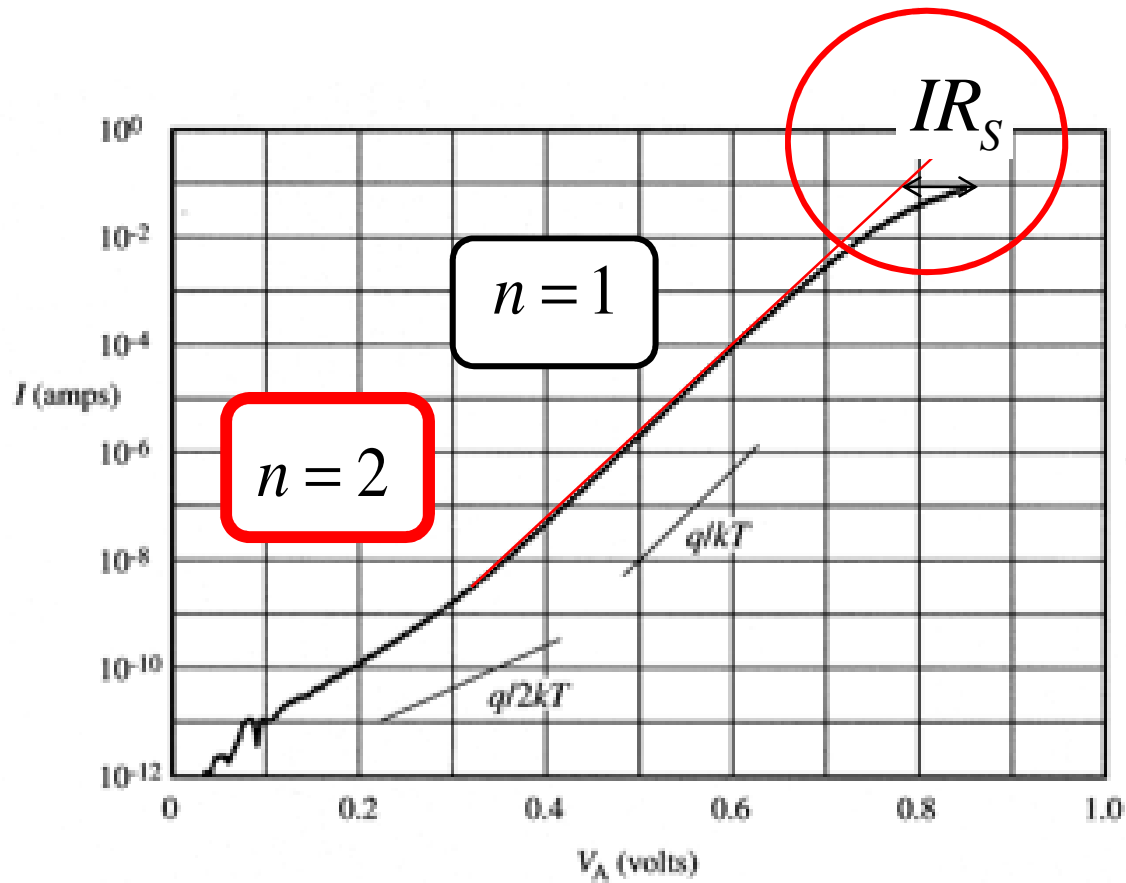
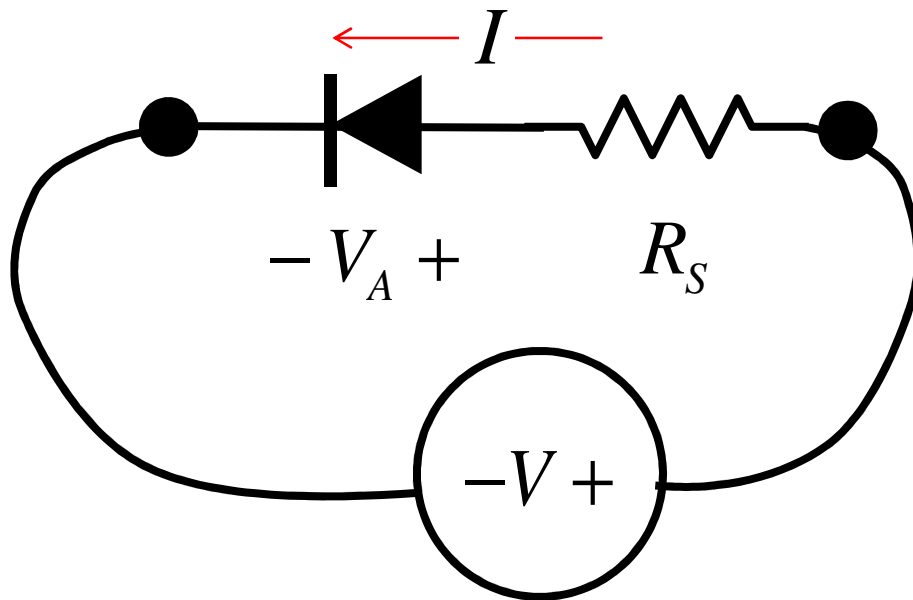


Fig. 6.10(a), Semiconductor Device Fundamentals, R.F. Pierret

# high forward bias

## 1) series resistance



$$I = I_0 \left( e^{q(V-IR_S)/k_B T} - 1 \right)$$

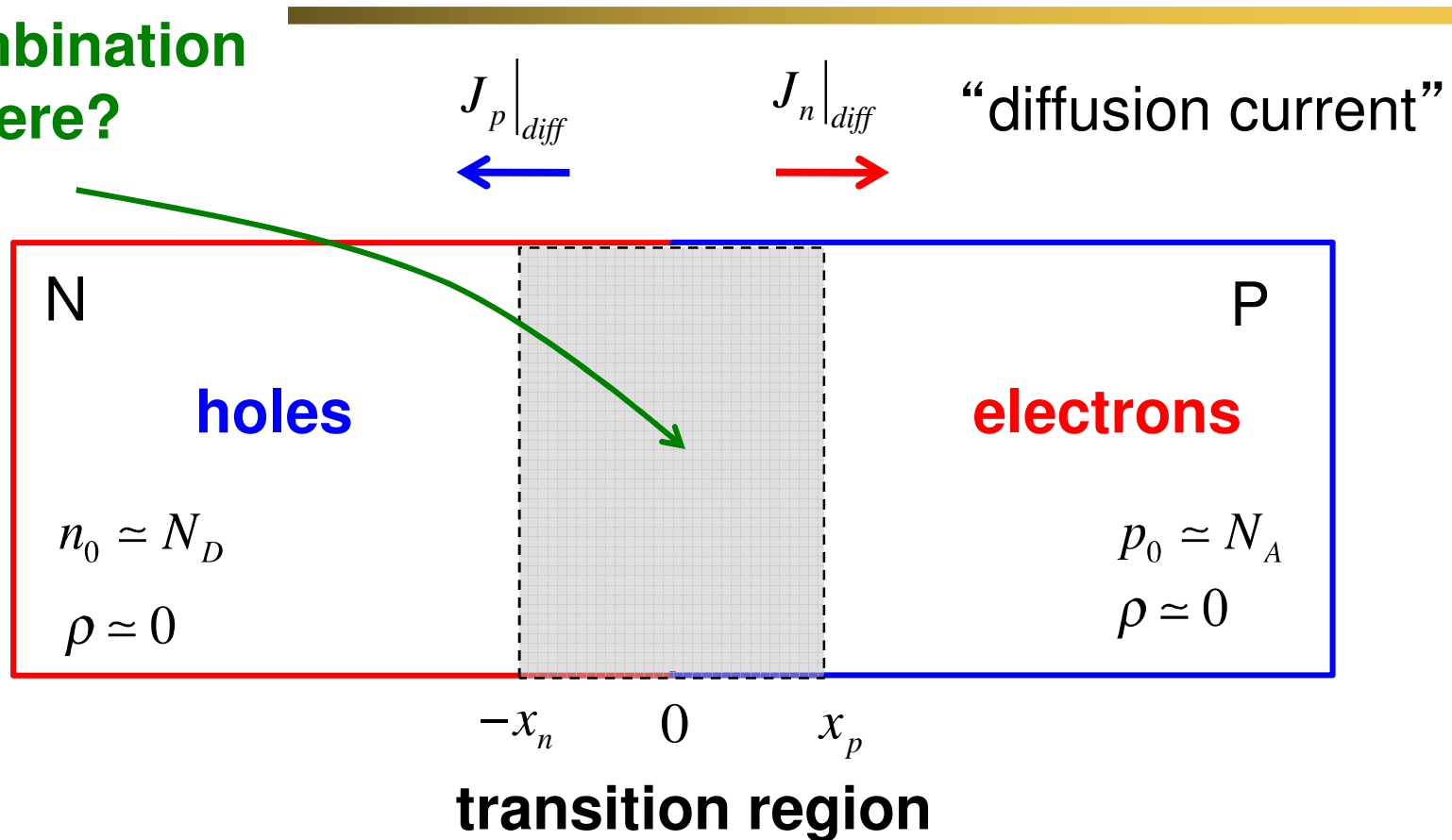
$$V_A = V - IR_S$$

## 2) “high level injection”

$$\Delta n_P = \frac{n_i^2}{N_A} \left( e^{qV_A/k_B T} - 1 \right) \ll N_A$$

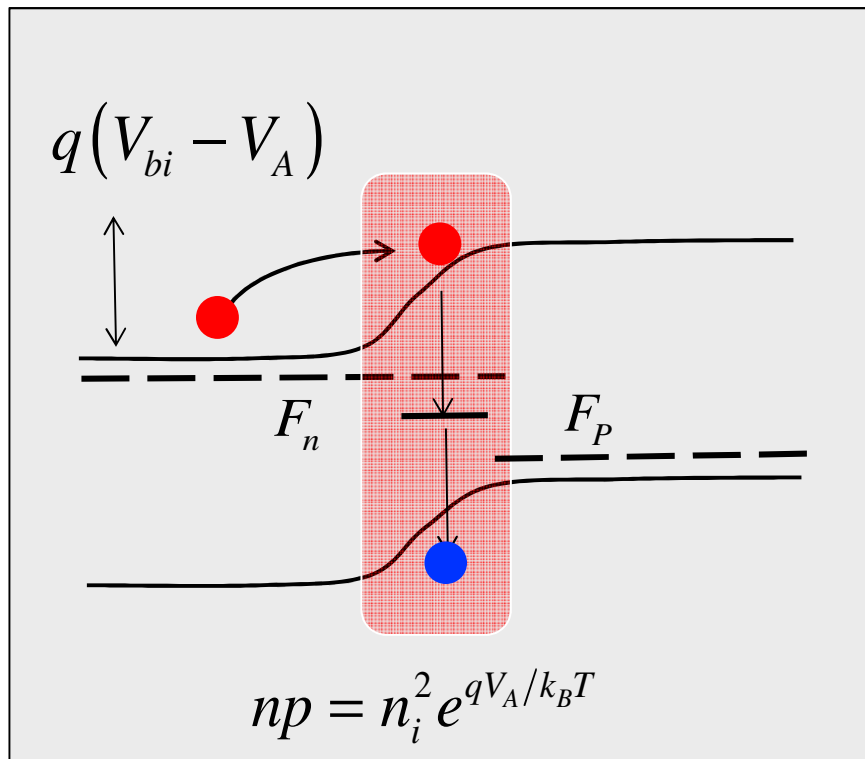
# moderate forward bias diode current

What about recombination here?



Minority carrier recombination in quasi-neutral regions leads to diode current.

# recombination in SCR: forward bias



$$J(V_A) = qR_{TOT}(V_A)$$

Maximum recombination occurs when  $n(x) \approx p(x)$

$$n(x)p(x) = n_i^2 e^{qV_A/k_B T}$$

$$\hat{n} \approx \hat{p} \propto n_i e^{qV_A/2k_B T}$$

$$qR(V_A) = \frac{qn_i e^{qV_A/2k_B T}}{\tau_{eff}}$$

**Recombination in space-charge regions gives rise to  $n = 2$  currents that go as  $n$ , not  $n_i^2$ .**

# recombination-generation in SCR: reverse bias

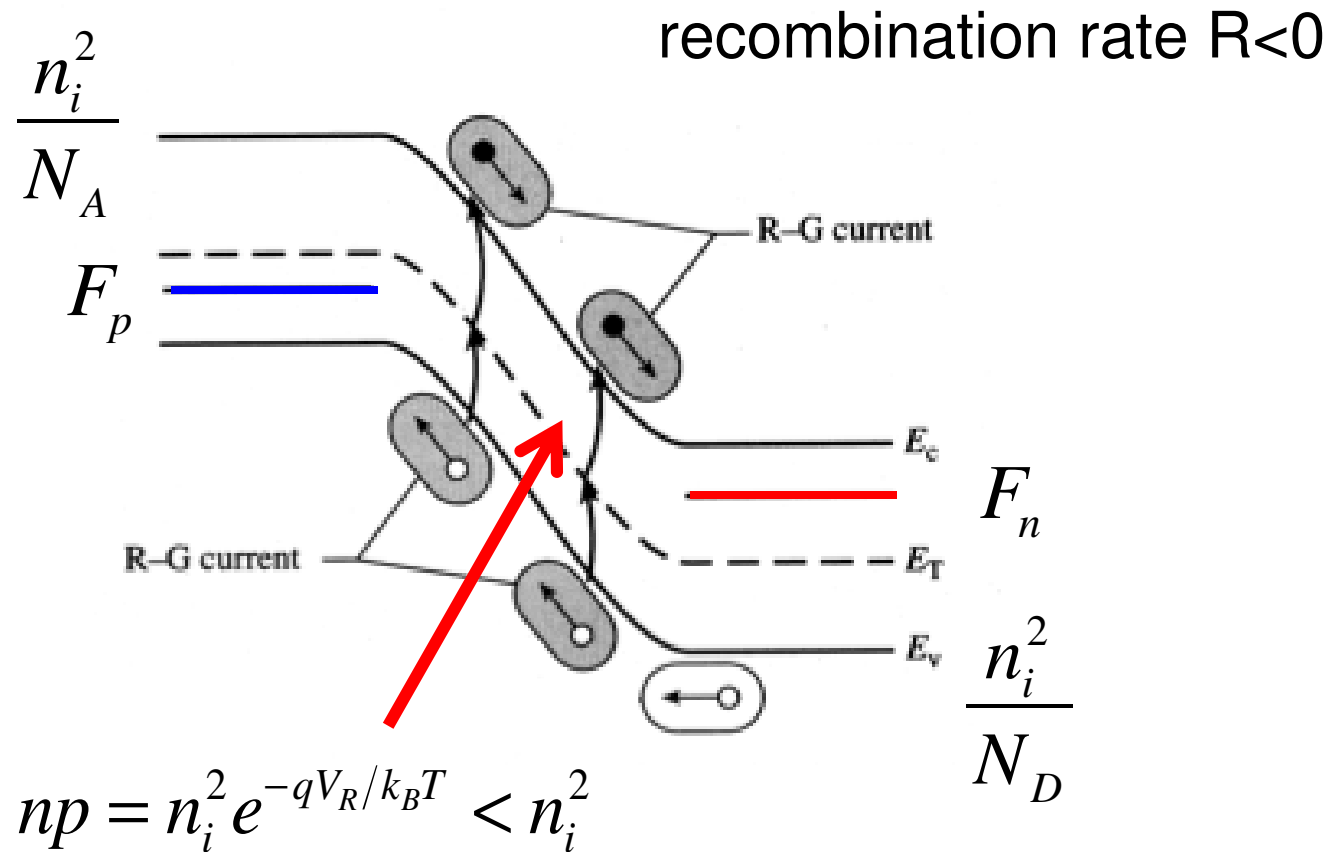
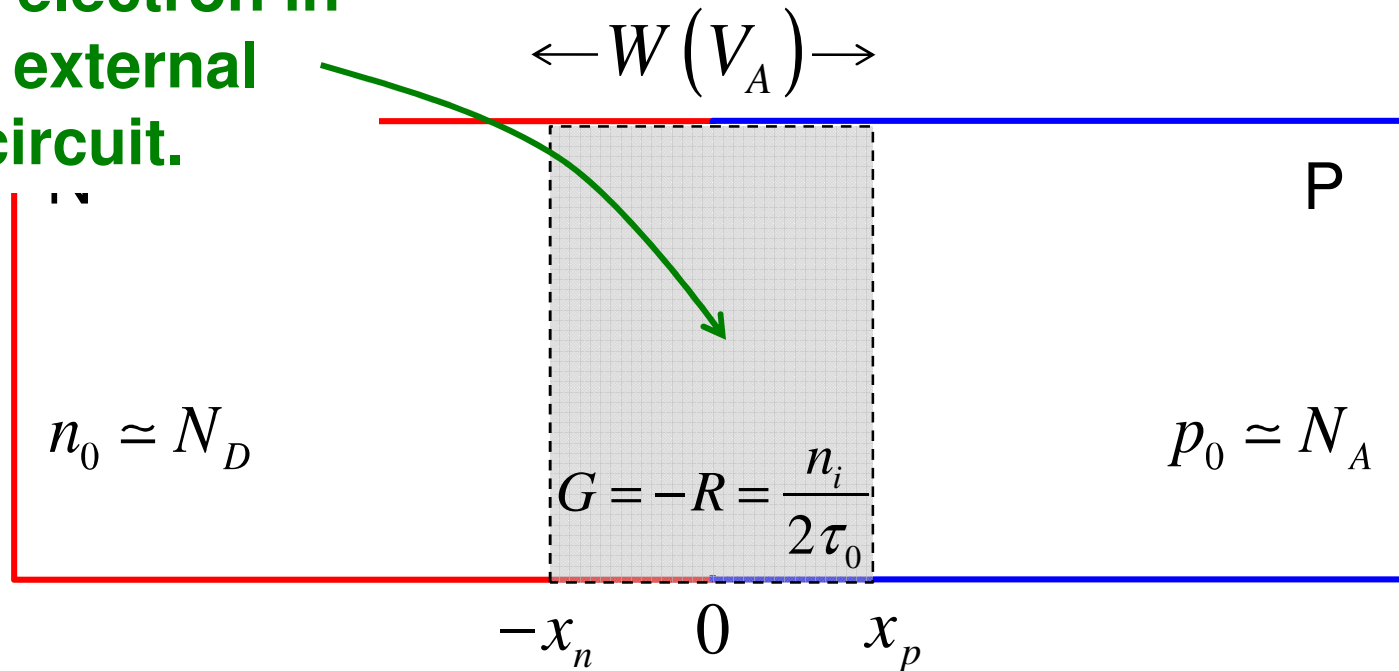


Fig. 6.15, Semiconductor Device Fundamentals, R.F. Pierret

# RB diode current

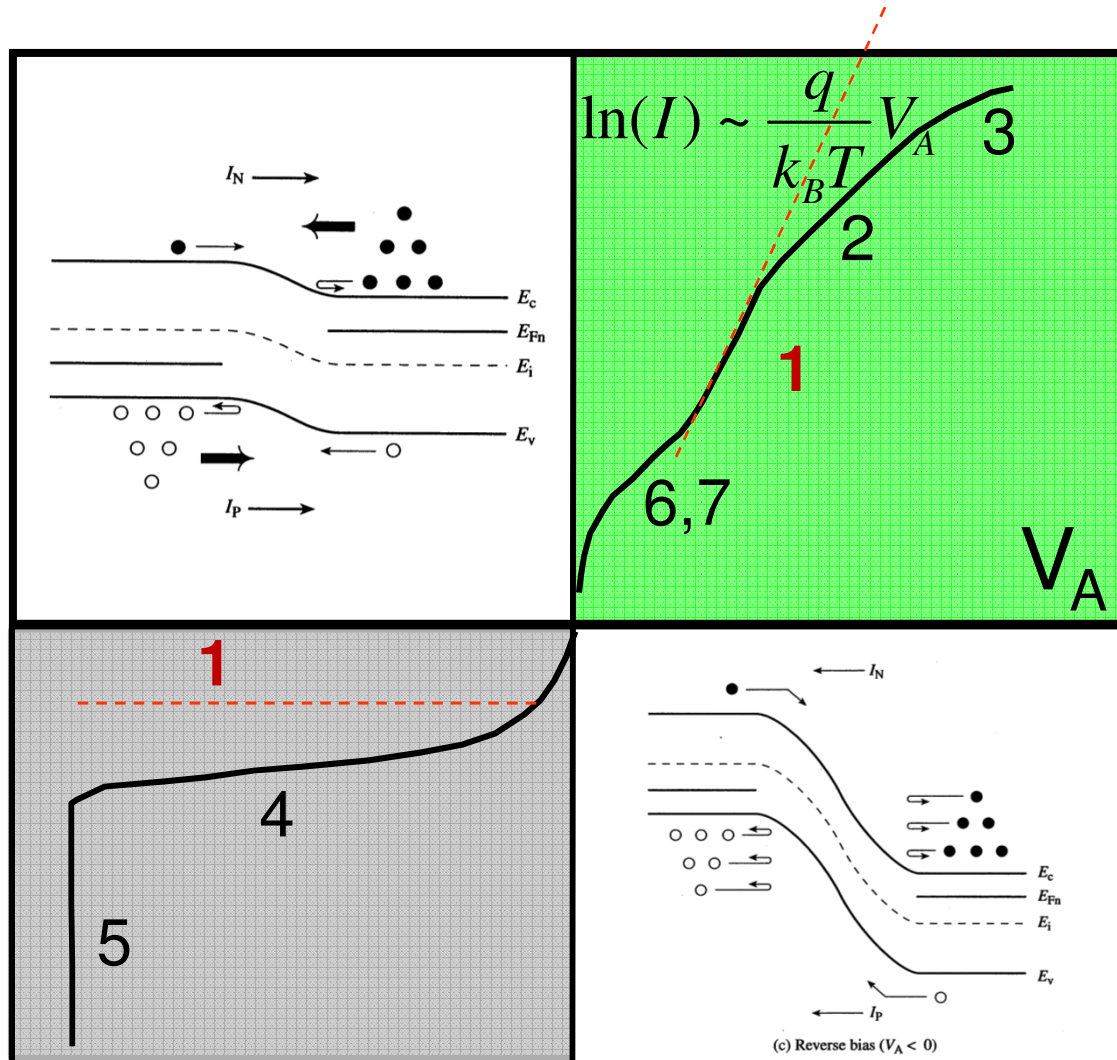
e-h pairs  
generated here  
give 1 electron in  
the external  
circuit.

recombination rate  $R < 0$



$$I = -q \frac{n_i}{2\tau_0} WA \quad W \propto \sqrt{V_{bi} + V_R}$$

# Various Regions of I-V Characteristics



1. **Diffusion limited**
2. *Ambipolar transport*
3. *High injection*
4. *R-G in depletion*
5. *Breakdown*
6. *Trap-assisted R-G*
7. *Esaki Tunneling*



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# non-ideal diode summary

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Non-ideal diode equation:  $I_D = I_0 \left( e^{q(V - I_D R_S) / nk_B T} - 1 \right)$

- 1) FB: recombination in quasi-neutral regions give  $n = 1$  current (diffusion current).
- 2) FB: recombination  $R > 0$  in SCR gives  $n = 2$  current
- 3) RB: constant when dominated by diffusion current
- 4) RB: increases as  $W$  from generation ( $R < 0$ ) in SCR
- 5) RB: avalanche or Zener tunneling