

ECE-305: Spring 2018

Non-Ideal Diodes+Solar Cells

Pierret, *Semiconductor Device Fundamentals* (SDF)
Chapter 6

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outline

- 1) Recap of Ideal Diodes
- 2) Diode Non-idealities:
 - Breakdown
 - High forward bias
 - Recombination-generation current
- 3) Small-signal model

ideal diode + solar cell summary

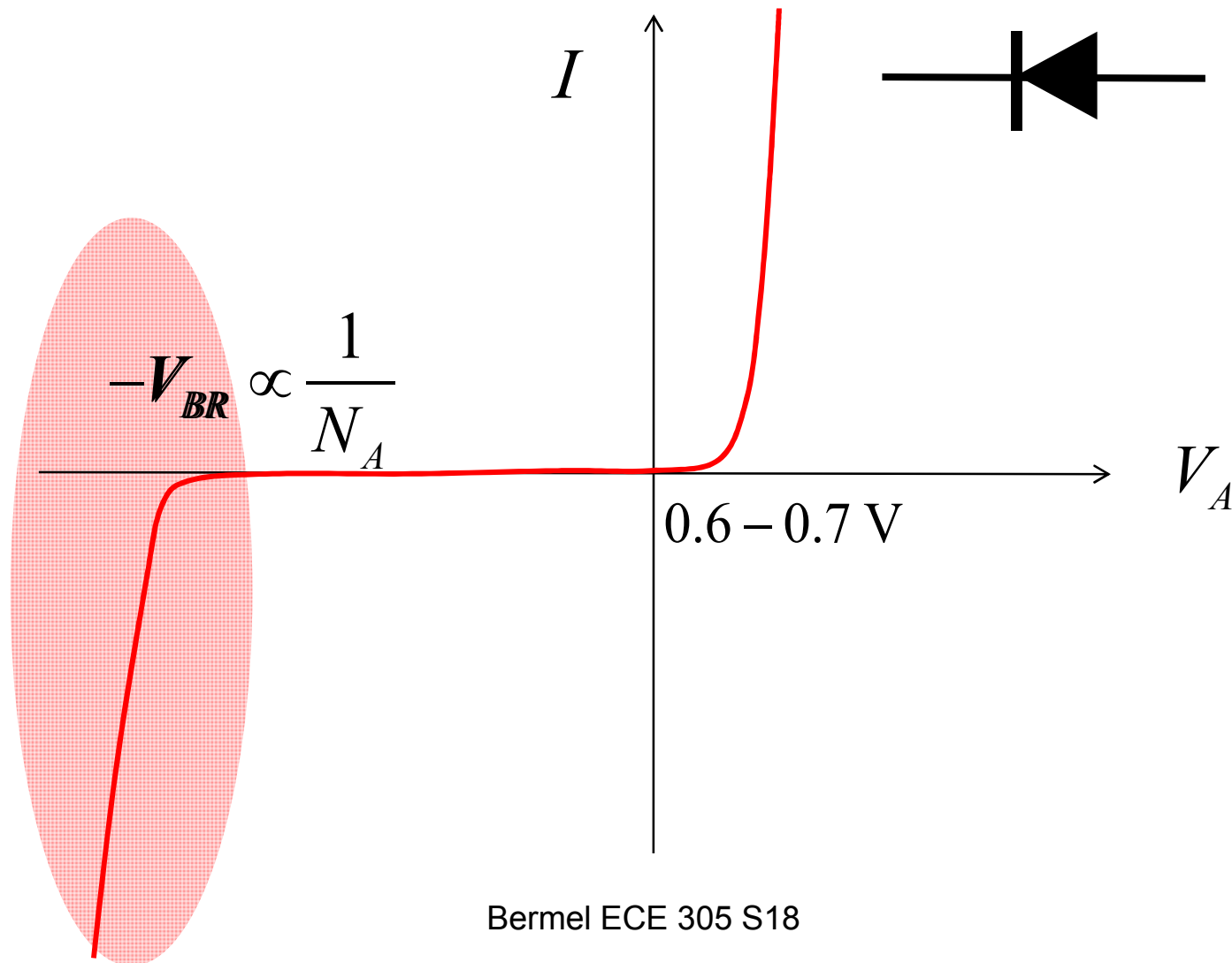
Ideal diode equation: $I_D = I_0 \left(e^{qV_A/nk_B T} - 1 \right)$

- 1) Light is absorbed and produces e-h pairs
- 2) PN junctions separate e-h pairs and collect the carriers.
- 3) Current flow in external circuit produces a FB voltage and the FB diode current reduces the total current.
- 4) Power out $|P_{out}| = I_{mp} V_{mp} = I_{SC} V_{OC} FF$
- 5) Unlike integrated circuit chips, where the value added comes from the design/system, manufacturing costs are critical in PV.

outline

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reverse bias breakdown



critical electric field

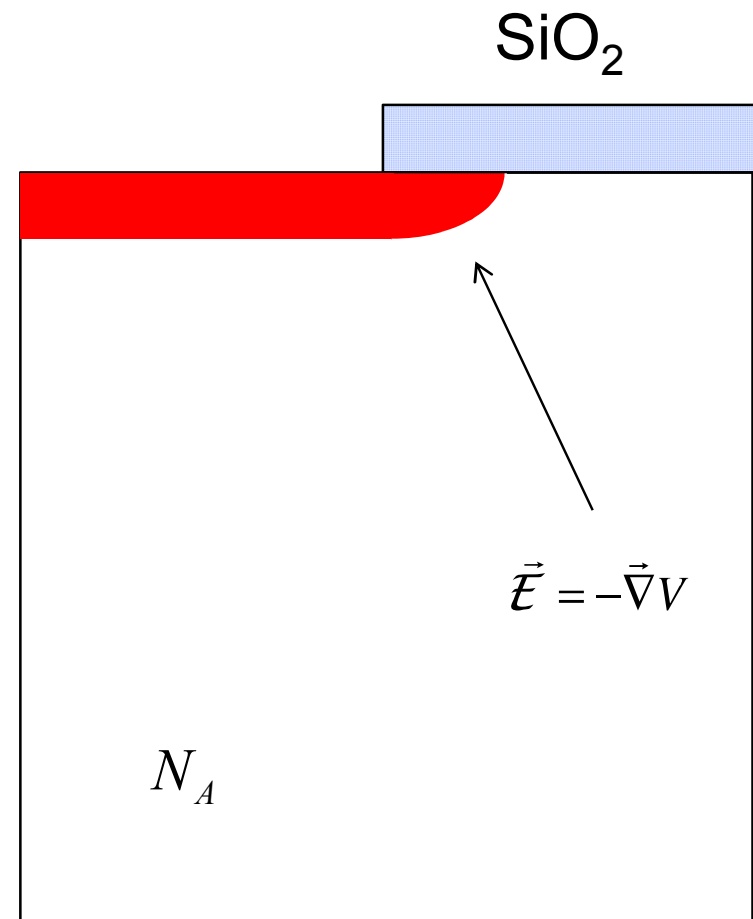
$$\mathcal{E}_{CR} = \sqrt{\frac{2q(V_{bi} + V_{BR})N_A}{K_s \epsilon_0}} \quad V_{BR} \propto \frac{1}{N_A}$$

$$\mathcal{E}_{CR} \approx 3 \times 10^5 \text{ V/cm} \quad (\text{Silicon})$$

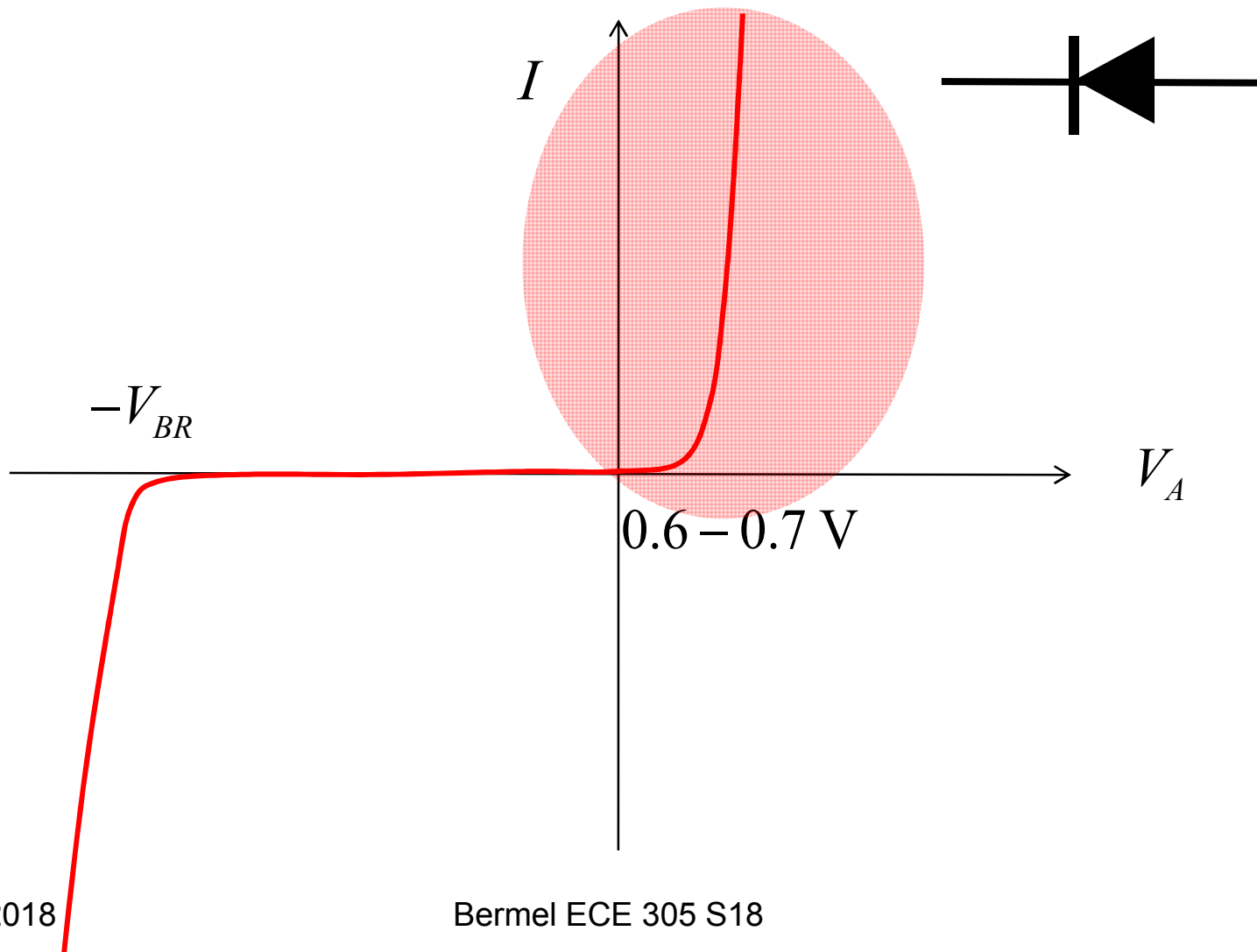
$$\mathcal{E}_{CR} \approx 1 \times 10^5 \text{ V/cm} \quad (\text{Germanium})$$

$$\mathcal{E}_{CR} \approx 5 \times 10^6 \text{ V/cm} \quad (\text{GaN})$$

$$\mathcal{E}_{CR} \approx 3 \times 10^6 \text{ V/cm} \quad (\text{air})$$



forward bias

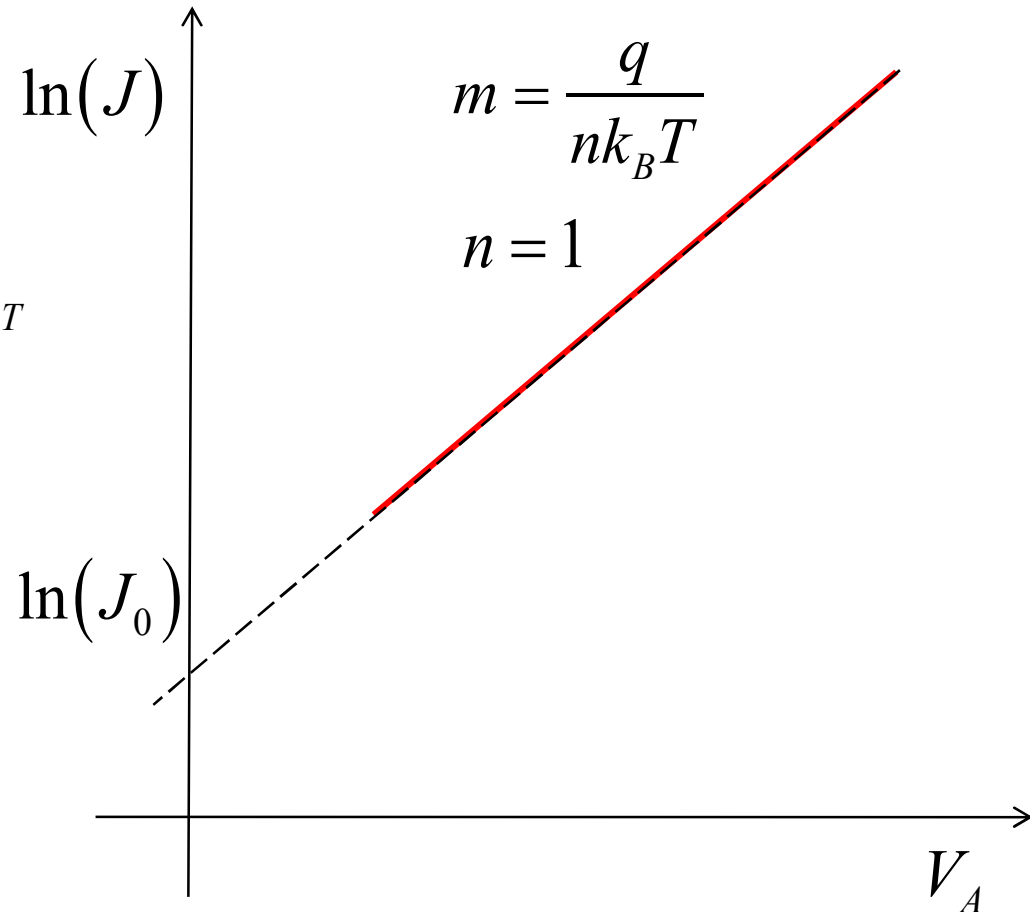


ideal diode current in forward bias

$$J = J_0 \left(e^{qV_A/k_B T} - 1 \right) \approx J_0 e^{qV_A/k_B T}$$

$$\ln(J) = \ln(J_0) + qV_A / k_B T$$

$$\ln(J) = \ln(J_0) + mV_A$$



real diodes in forward bias

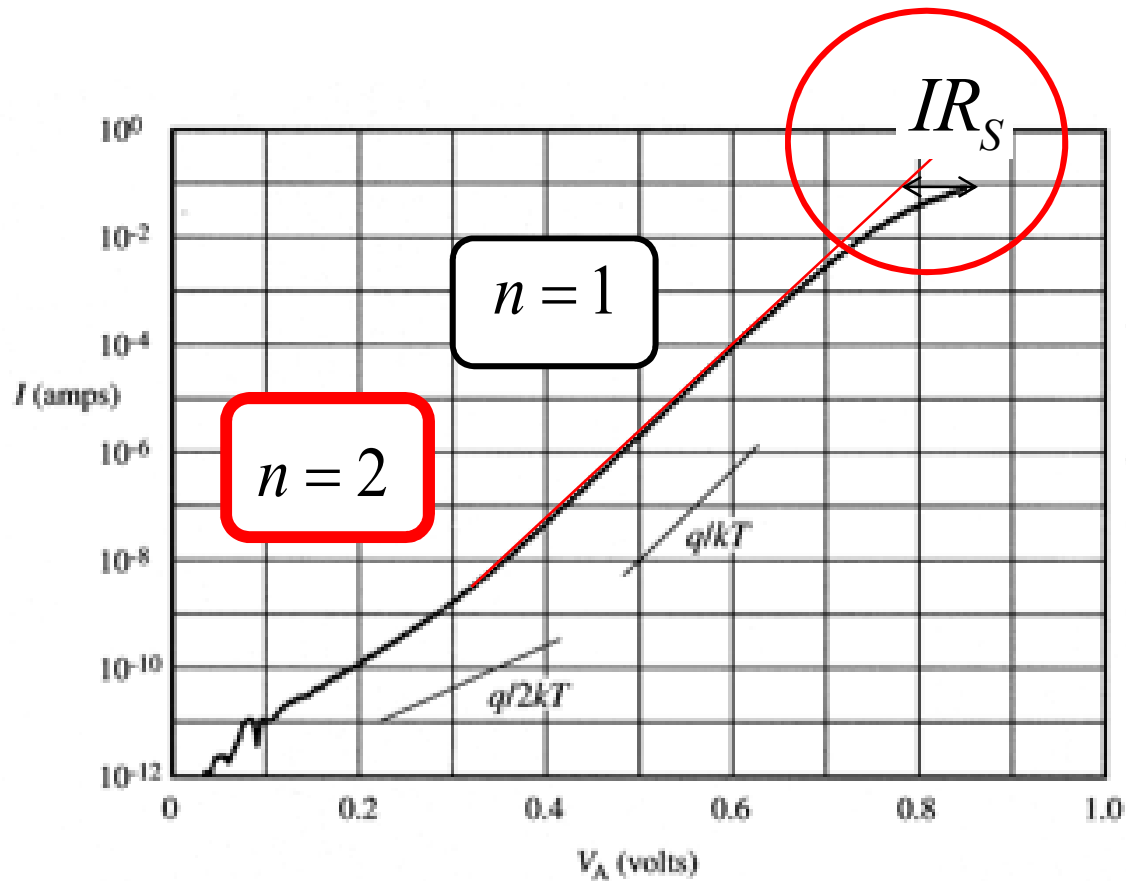
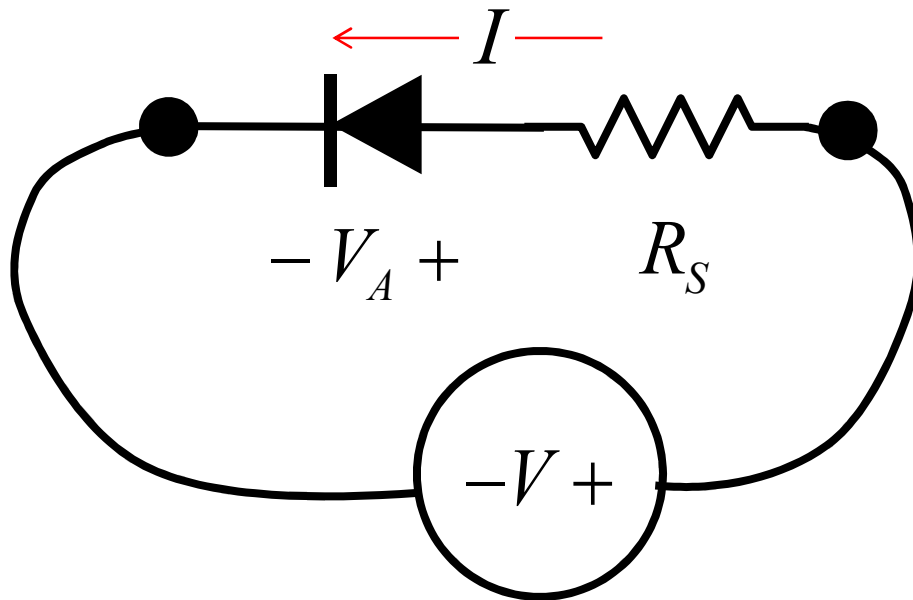


Fig. 6.10(a), Semiconductor Device Fundamentals, R.F. Pierret

high forward bias

1) series resistance



$$I = I_0 \left(e^{q(V - IR_S)/k_B T} - 1 \right)$$

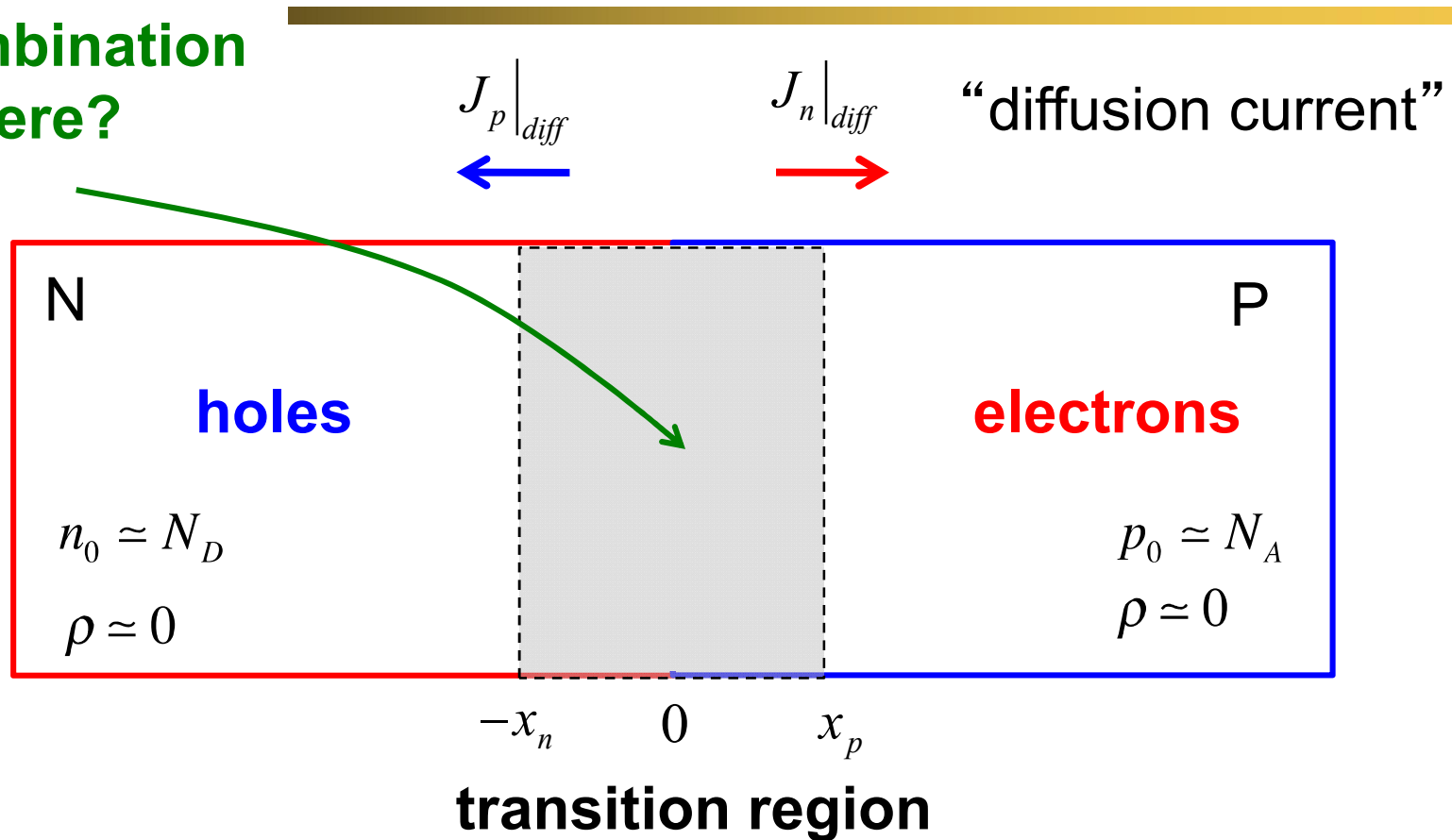
$$V_A = V - IR_S$$

2) “high level injection”

$$\Delta n_P = \frac{n_i^2}{N_A} \left(e^{qV_A/k_B T} - 1 \right) \ll N_A$$

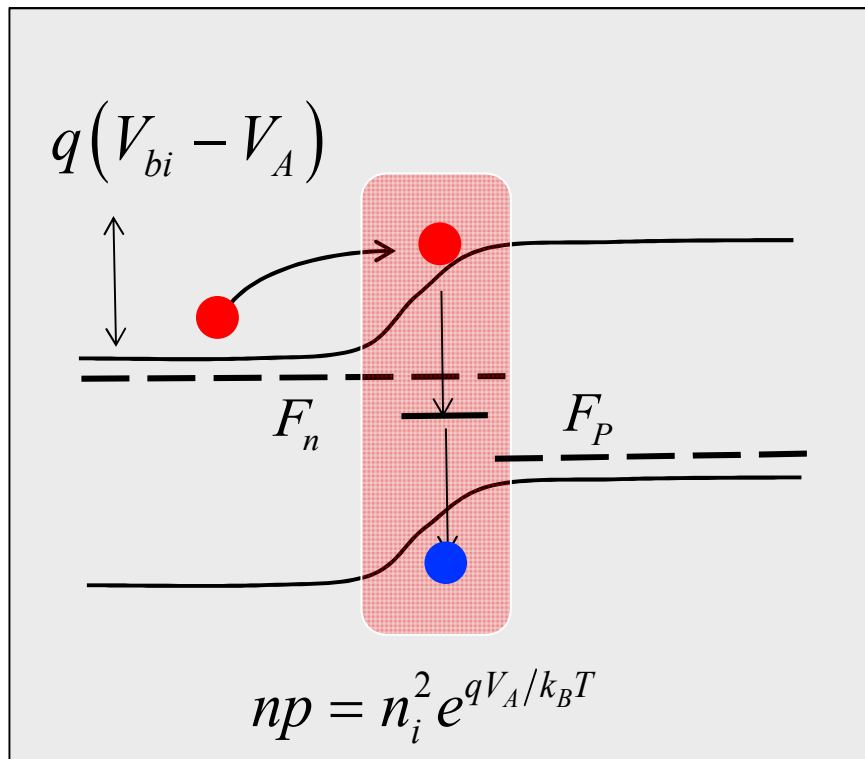
moderate forward bias diode current

What about recombination here?



Minority carrier recombination in quasi-neutral regions leads to diode current.

recombination in SCR: forward bias



$$J(V_A) = qR_{TOT}(V_A)$$

Maximum recombination occurs when $n(x) \approx p(x)$

$$n(x)p(x) = n_i^2 e^{qV_A/k_B T}$$

$$\hat{n} \approx \hat{p} \propto n_i e^{qV_A/2k_B T}$$

$$qR(V_A) = \frac{qn_i e^{qV_A/2k_B T}}{\tau_{eff}}$$

Recombination in space-charge regions gives rise to $n = 2$ currents that go as n_i not n_i^2 .

recombination-generation in SCR: reverse bias

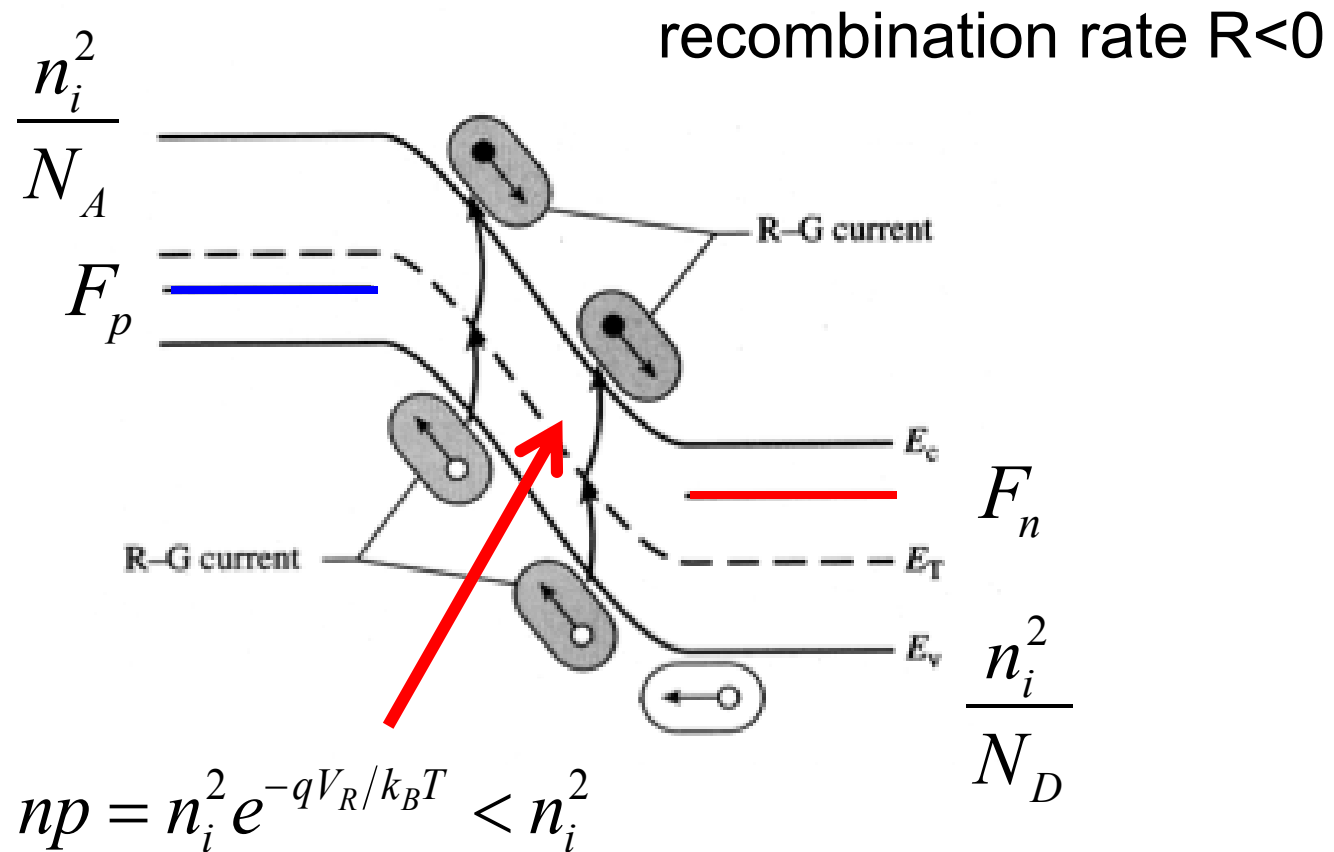
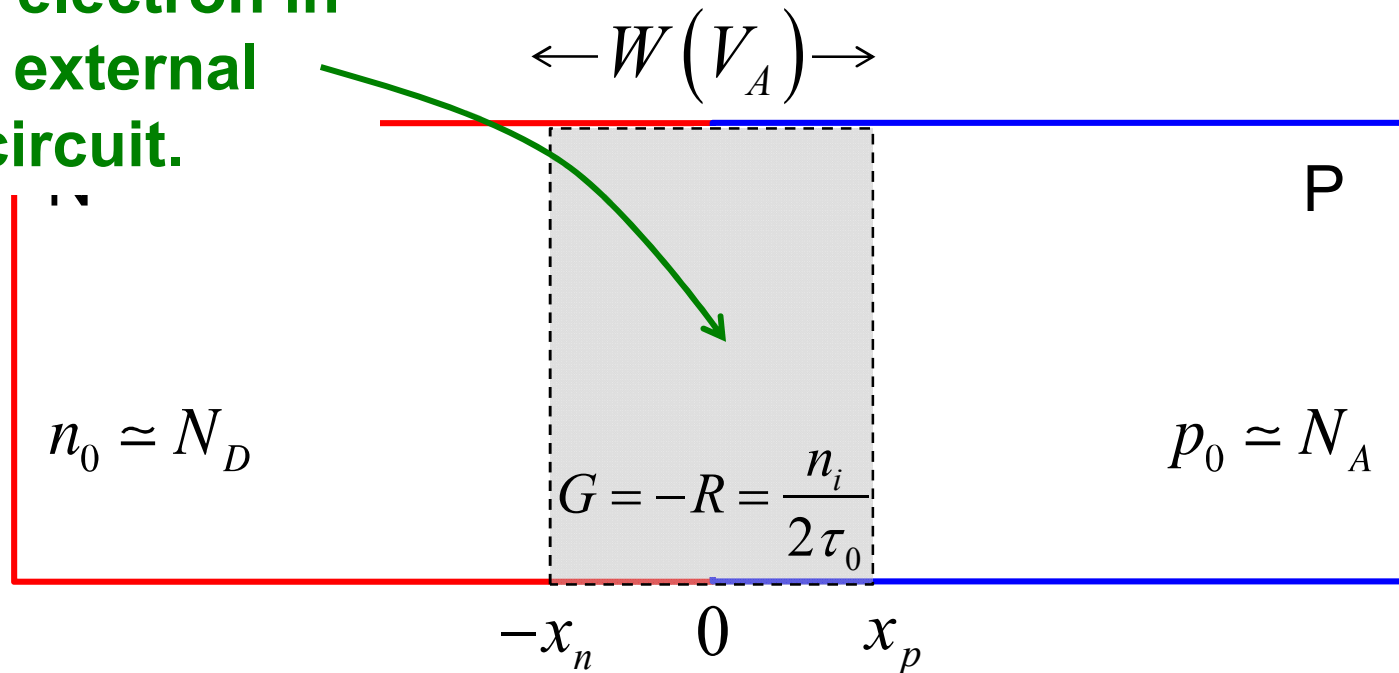


Fig. 6.15, Semiconductor Device Fundamentals, R.F. Pierret

RB diode current

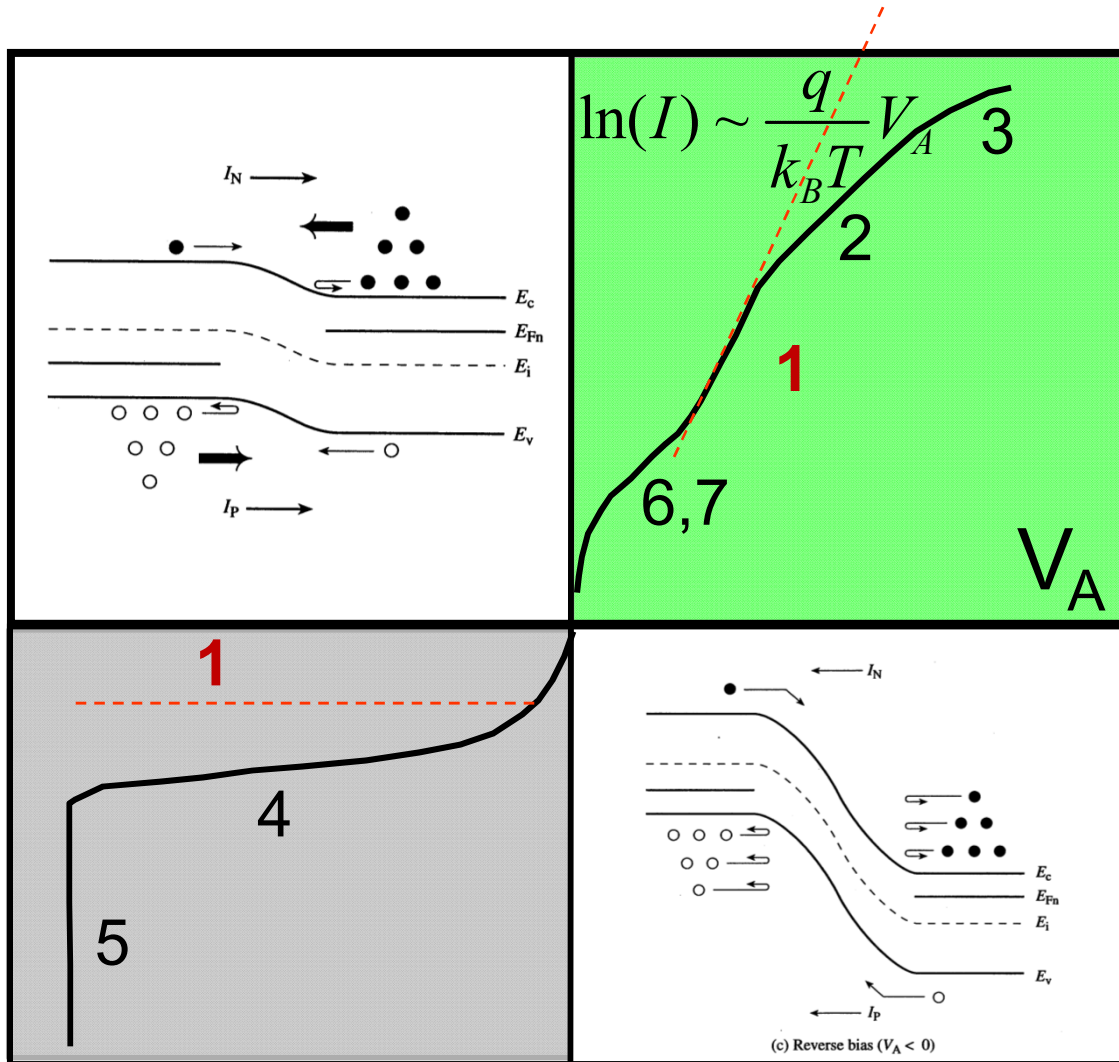
e-h pairs
generated here
give 1 electron in
the external
circuit.

recombination rate $R < 0$



$$I = -q \frac{n_i}{2\tau_0} W A \quad W \propto \sqrt{V_{bi} + V_R}$$

Various Regions of I-V Characteristics



1. **Diffusion limited**
2. *Ambipolar transport*
3. *High injection*
4. *R-G in depletion*
5. *Breakdown*
6. *Trap-assisted R-G*
7. *Esaki Tunneling*

non-ideal diode summary

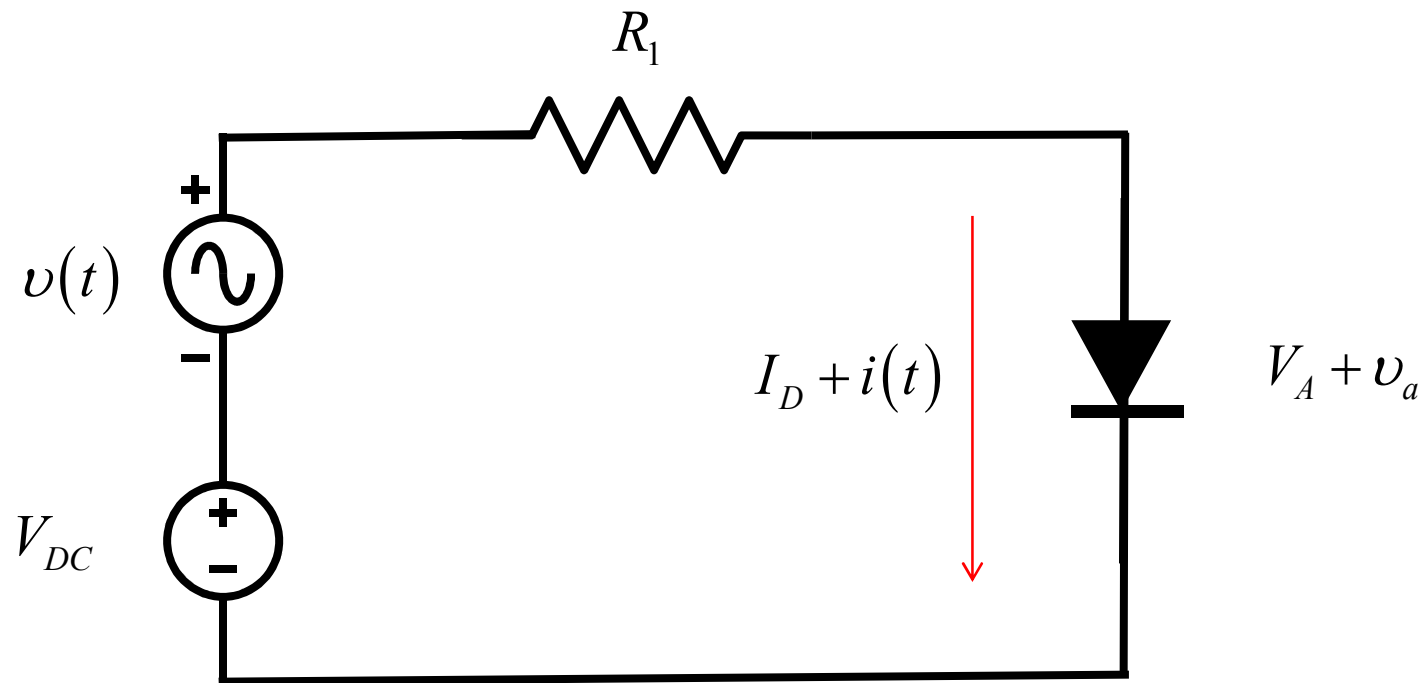
Non-ideal diode equation:
$$I_D = I_0 \left(e^{q(V - I_D R_S) / nk_B T} - 1 \right)$$

- 1) FB: recombination in quasi-neutral regions give $n = 1$ current (diffusion current).
- 2) FB: recombination $R > 0$ in SCR gives $n = 2$ current
- 3) RB: constant when dominated by diffusion current
- 4) RB: increases as W from generation ($R < 0$) in SCR
- 5) RB: avalanche or Zener tunneling

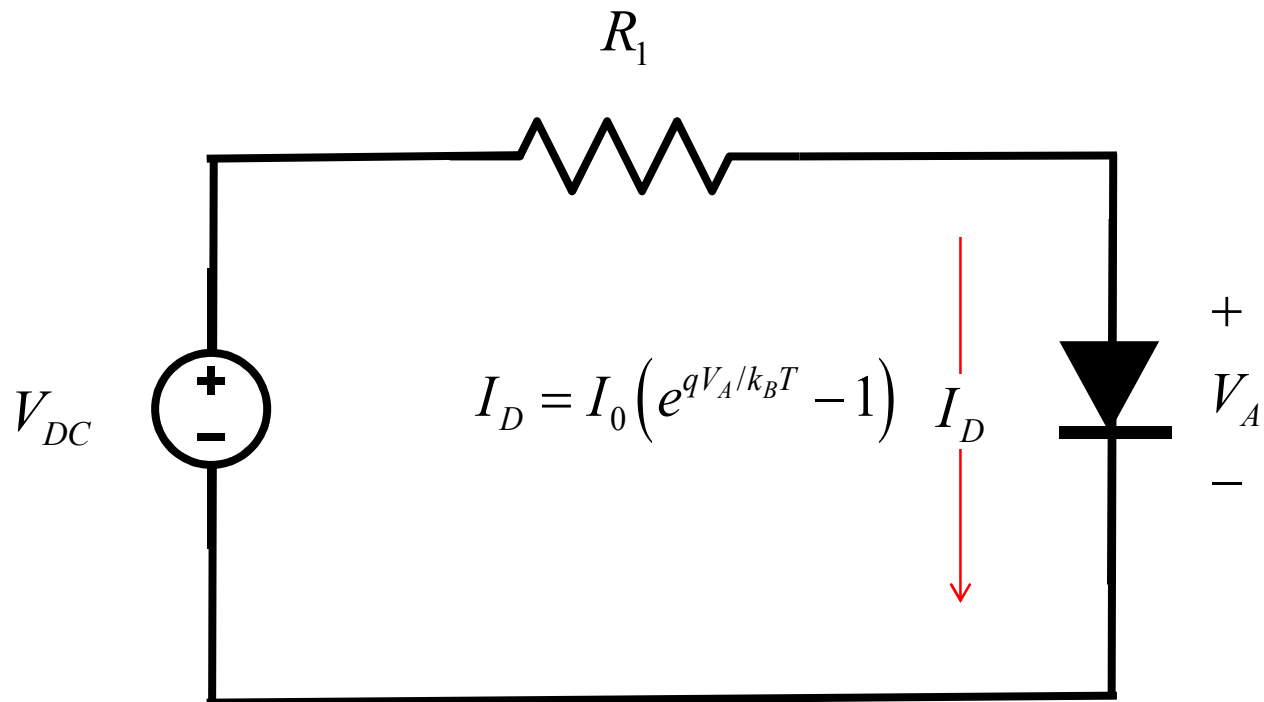
outline

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- ✓ 2) Diode Non-idealities:
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small signal ac

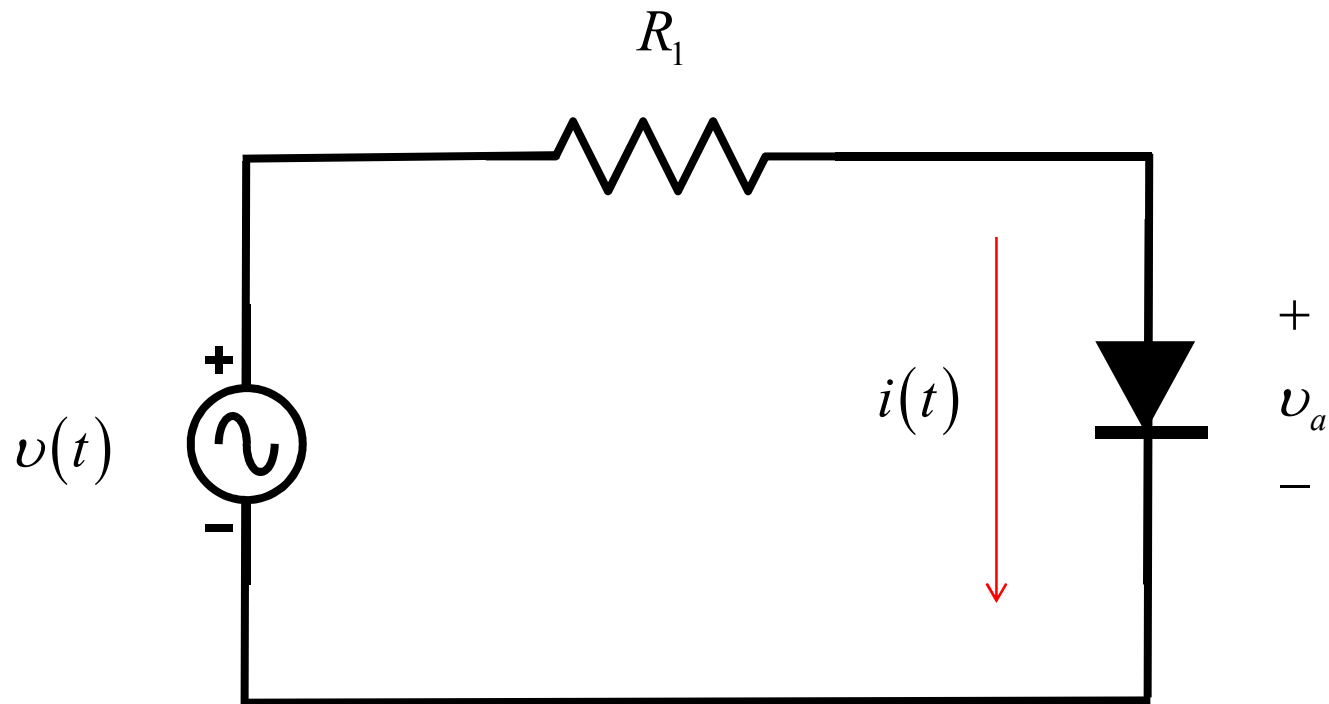


DC solution



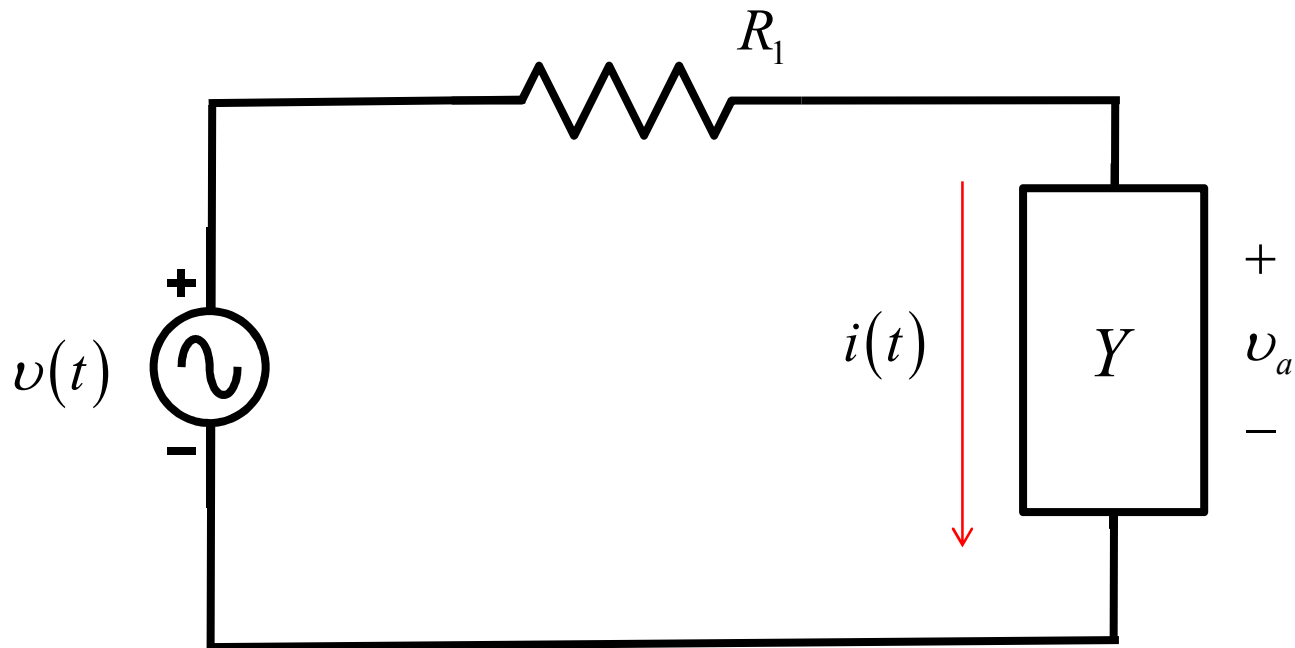
Superposition: 1) DC

small signal ac



Superposition: 2) ac

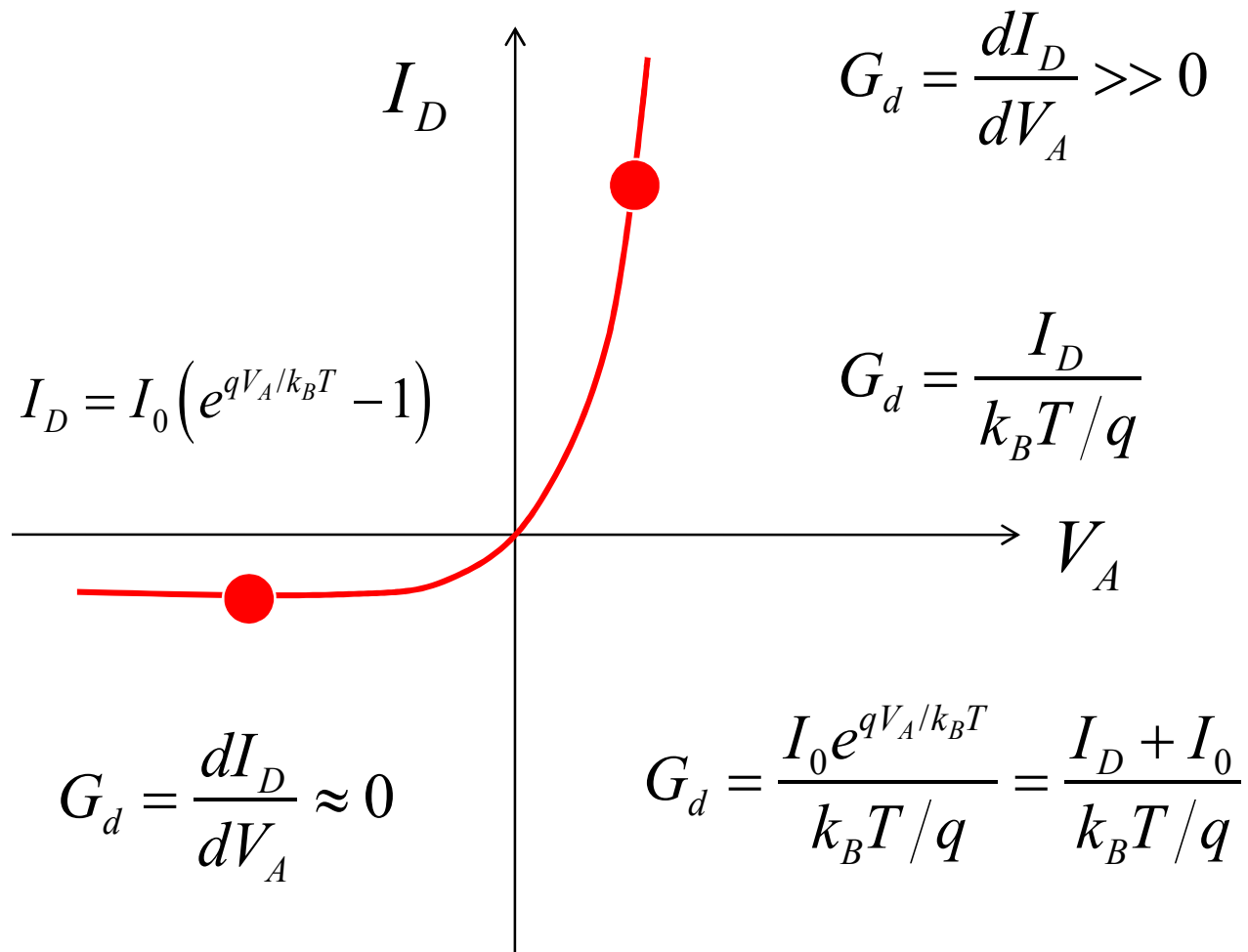
equivalent circuit



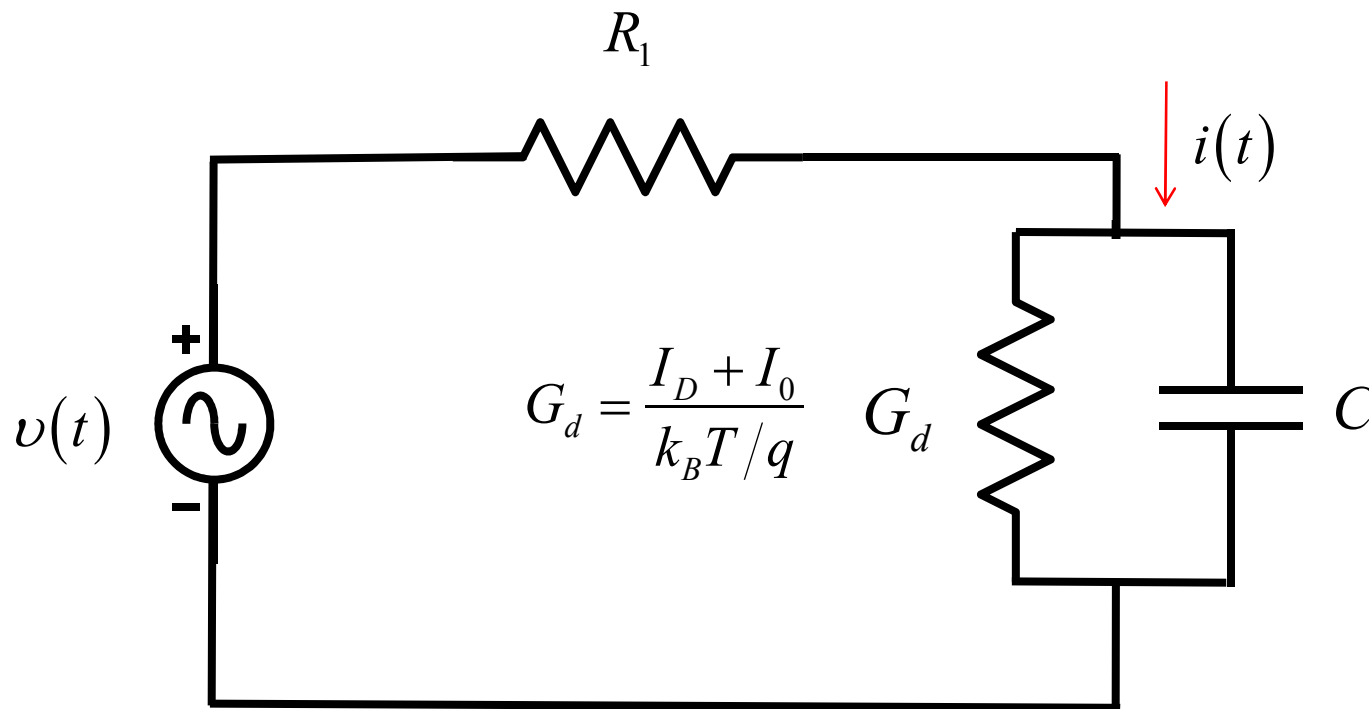
$$Y = G_d + j\omega C$$

For low frequencies, $G_d = \frac{i}{v_a} = \frac{dI_D}{dV_A}$

Ideal diode equation (DC)



small signal ac (capacitance)



diode capacitance in RB

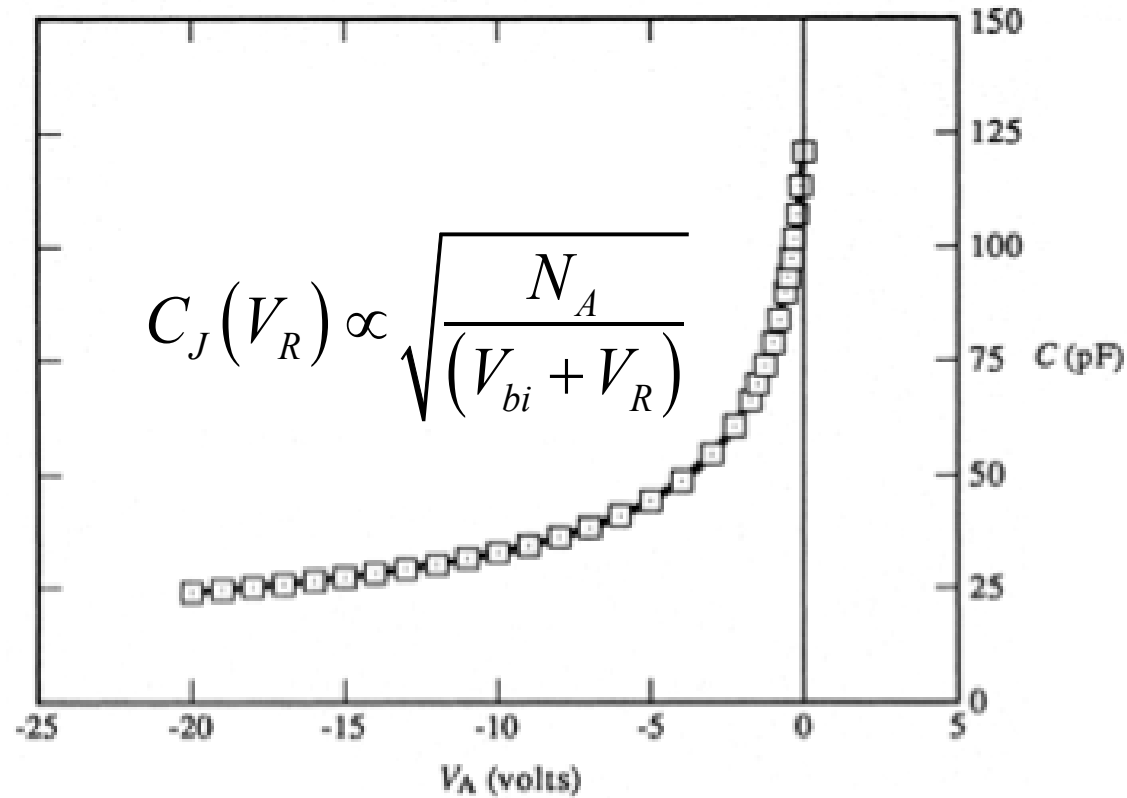
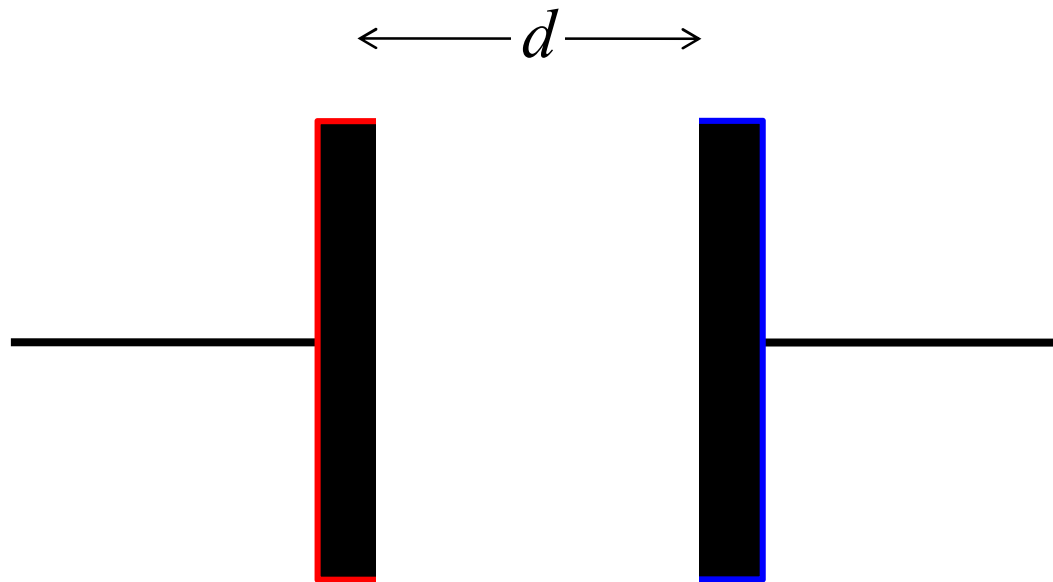


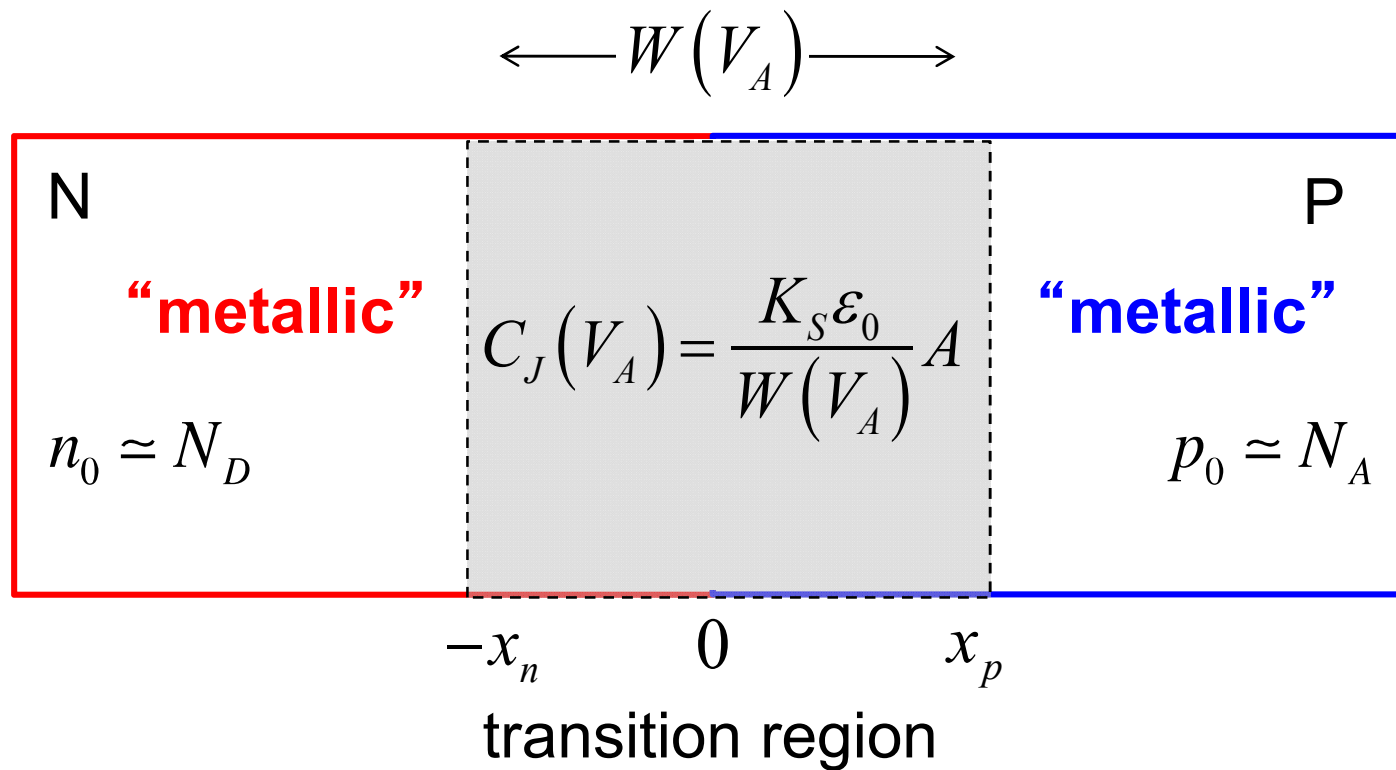
Fig. 7.3, Semiconductor Device Fundamentals, R.F. Pierret

capacitance



$$C = \frac{K_r \epsilon_0}{d} A$$

reverse bias capacitance



reverse bias capacitance

$$C_J(V_A) = \frac{K_S \epsilon_0}{W(V_A)} A$$

$$W(V_A) = \left[\frac{2K_S \epsilon_0}{qN_A} (V_{bi} - V_A) \right]^{1/2} = \left[\frac{2K_S \epsilon_0}{qN_A} (V_{bi} + V_R) \right]^{1/2}$$

$$C_J(V_R) = \boxed{\phantom{C_J(V_R) = \frac{K_S \epsilon_0 A}{\left[\frac{2K_S \epsilon_0}{qN_A} (V_{bi} + V_R) \right]^{1/2}}} } \propto \sqrt{\frac{N_A}{(V_{bi} + V_R)}}$$

$1/C^2$ vs. V_R

$$C_J(V_R) = \frac{K_S \epsilon_0 A}{\left[\frac{2K_S \epsilon_0}{qN_A} (V_{bi} + V_R) \right]^{1/2}}$$

$$\frac{1}{C_J^2(V_R)} = \frac{2}{qN_A K_S \epsilon_0 A^2} (V_{bi} + V_R)$$

$1/C^2$ vs. V_R

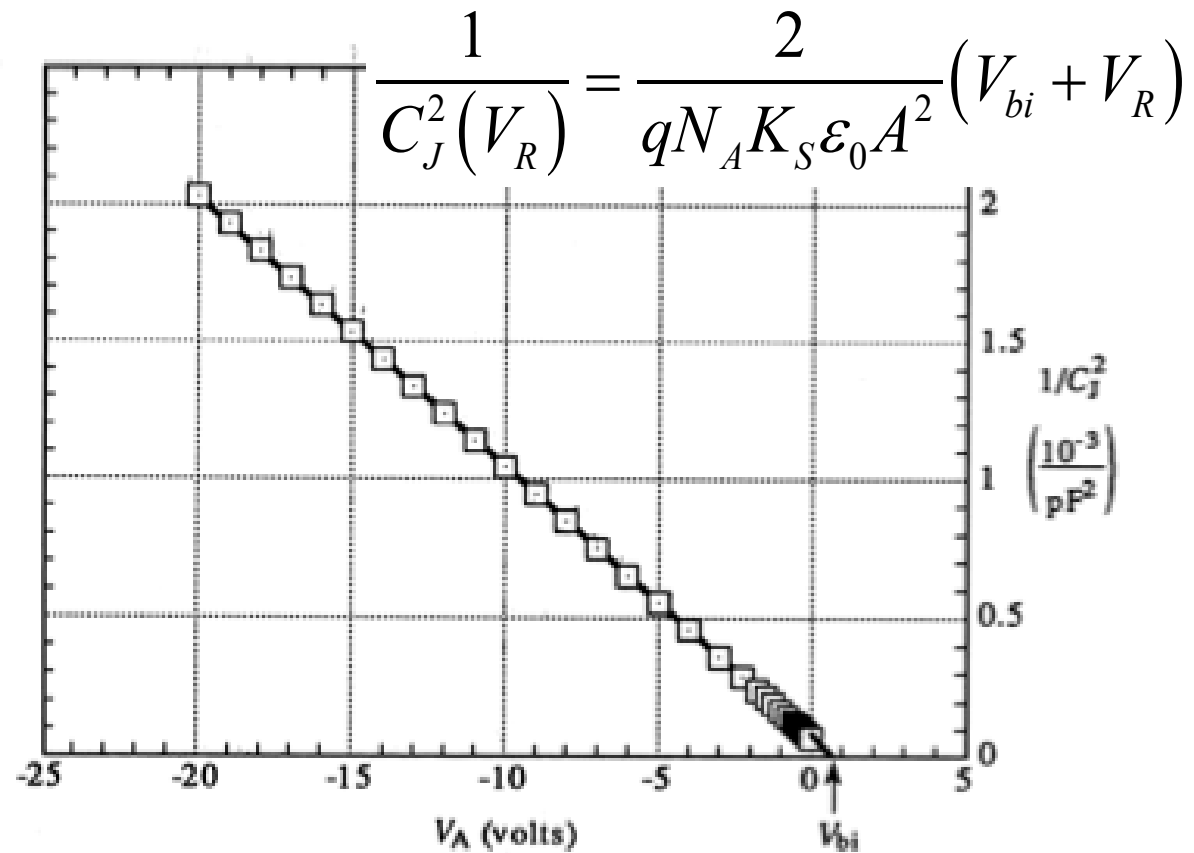
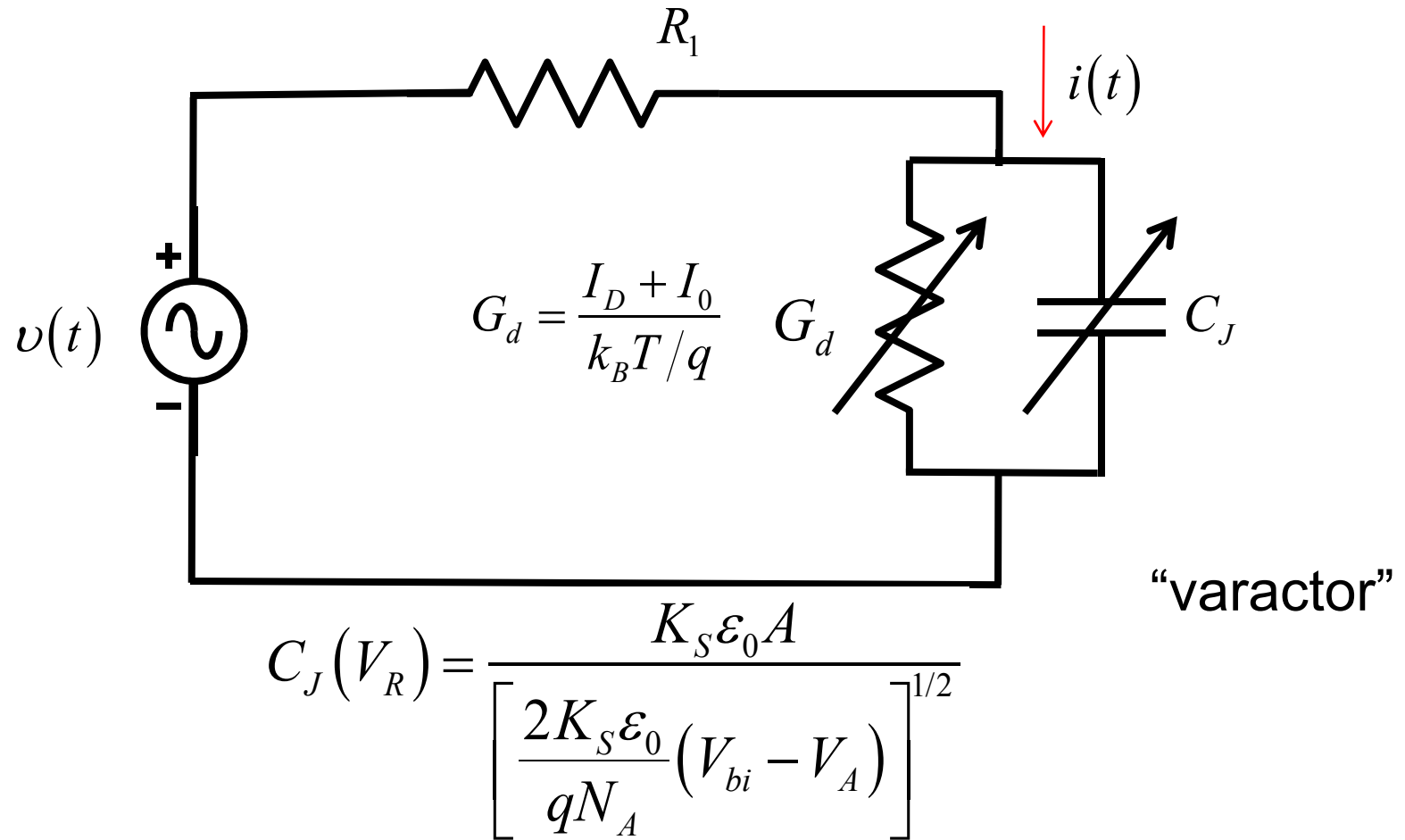
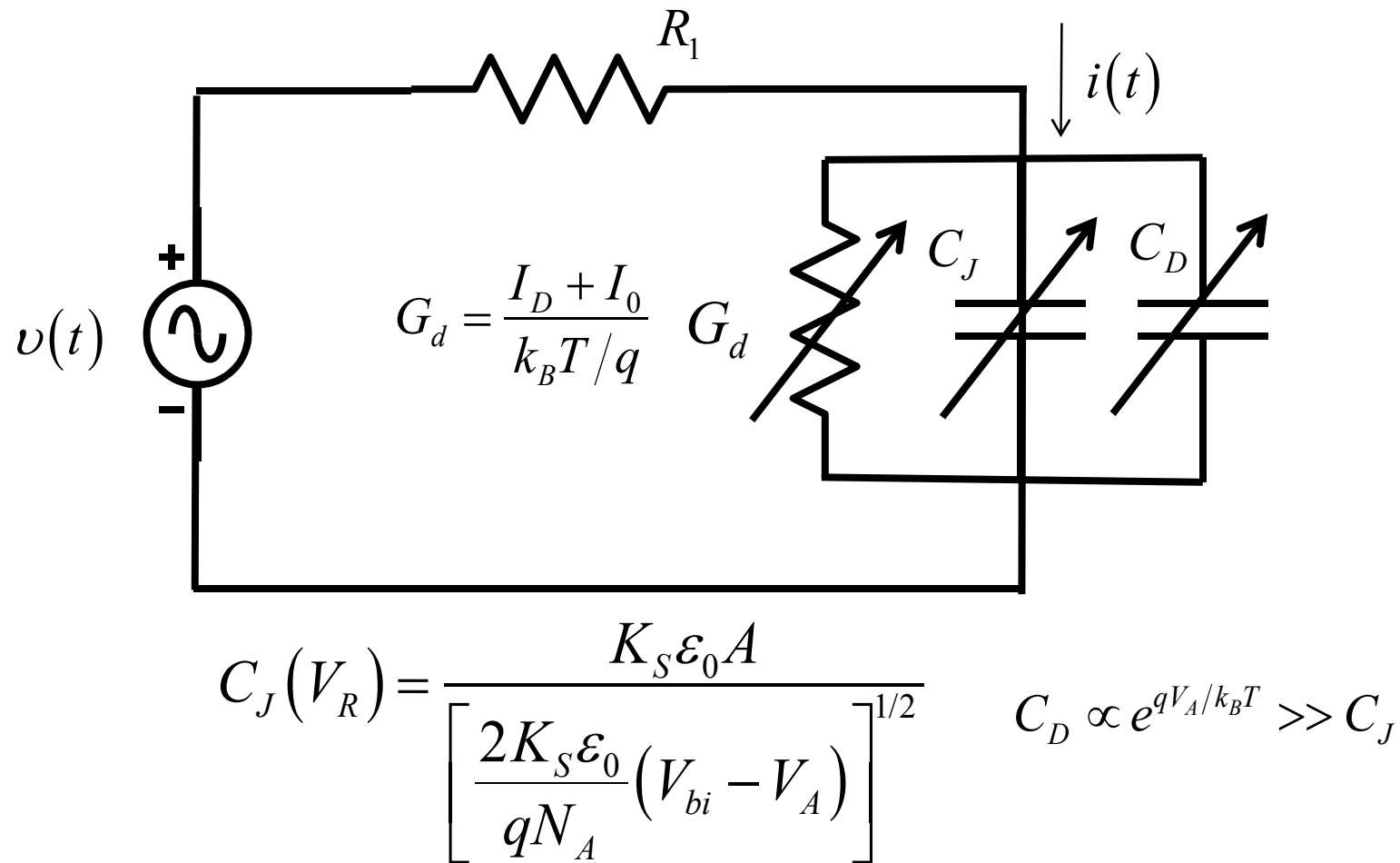


Fig. E7.2, Semiconductor Device Fundamentals, R.F. Pierret

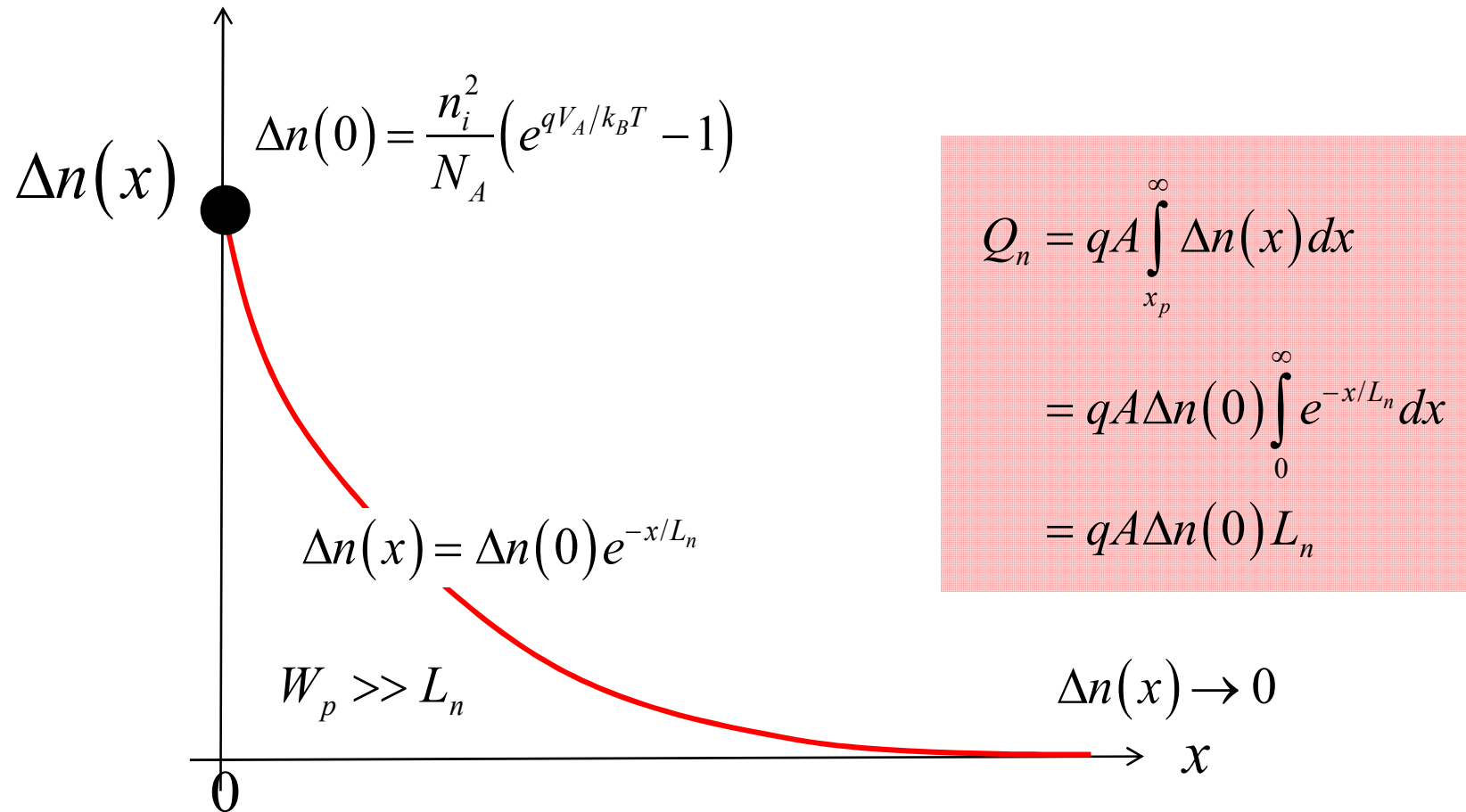
equivalent circuit (reverse bias)



equivalent circuit (forward bias)



stored minority carrier charge



stored minority carrier charge

$$Q_n = qA\Delta n(0)L_n \quad \Delta n(0) = \frac{n_i^2}{N_A} (e^{qV_A/k_B T} - 1)$$

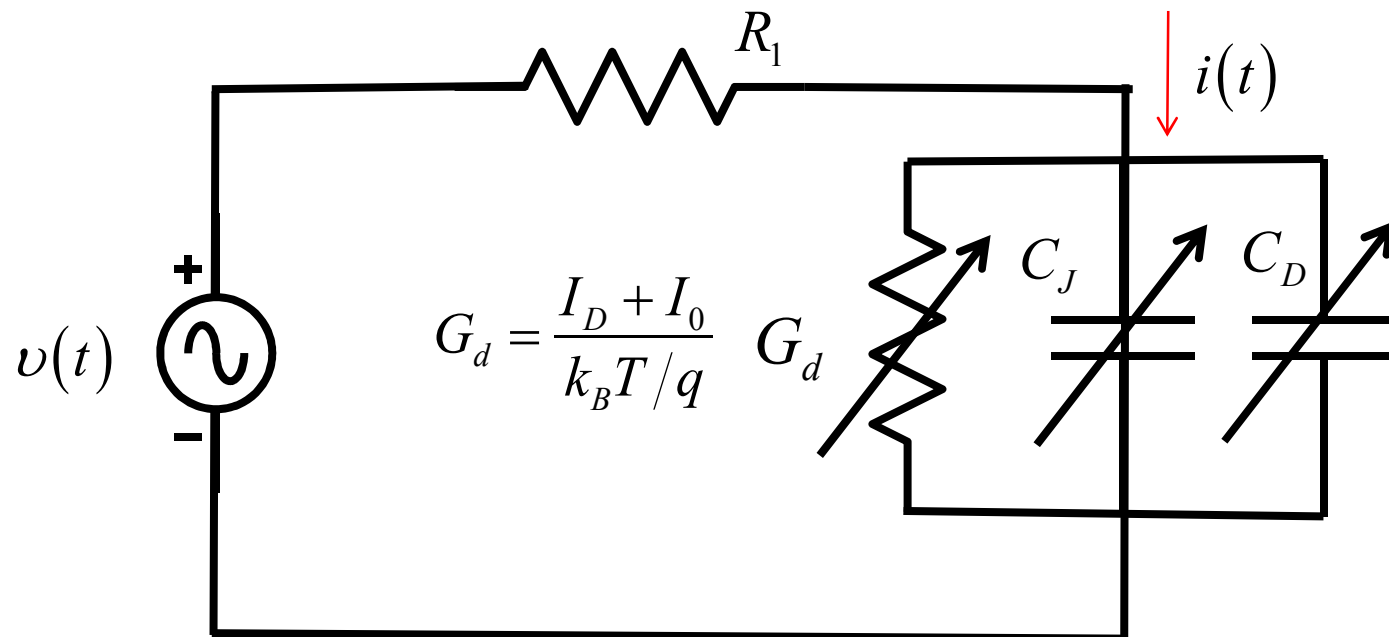
$$C_D = \frac{dQ_n}{dV_A} = A \frac{q}{k_B T / q} \frac{n_i^2}{N_A} L_n e^{qV_A/k_B T}$$

$$G_d = \frac{I_0 e^{qV_A/k_B T}}{k_B T / q} = \frac{qA}{k_B T / q} \frac{D_n}{L_n} \frac{n_i^2}{N_A} e^{qV_A/k_B T}$$

$$C_D = G_d \tau_n$$

Check units:

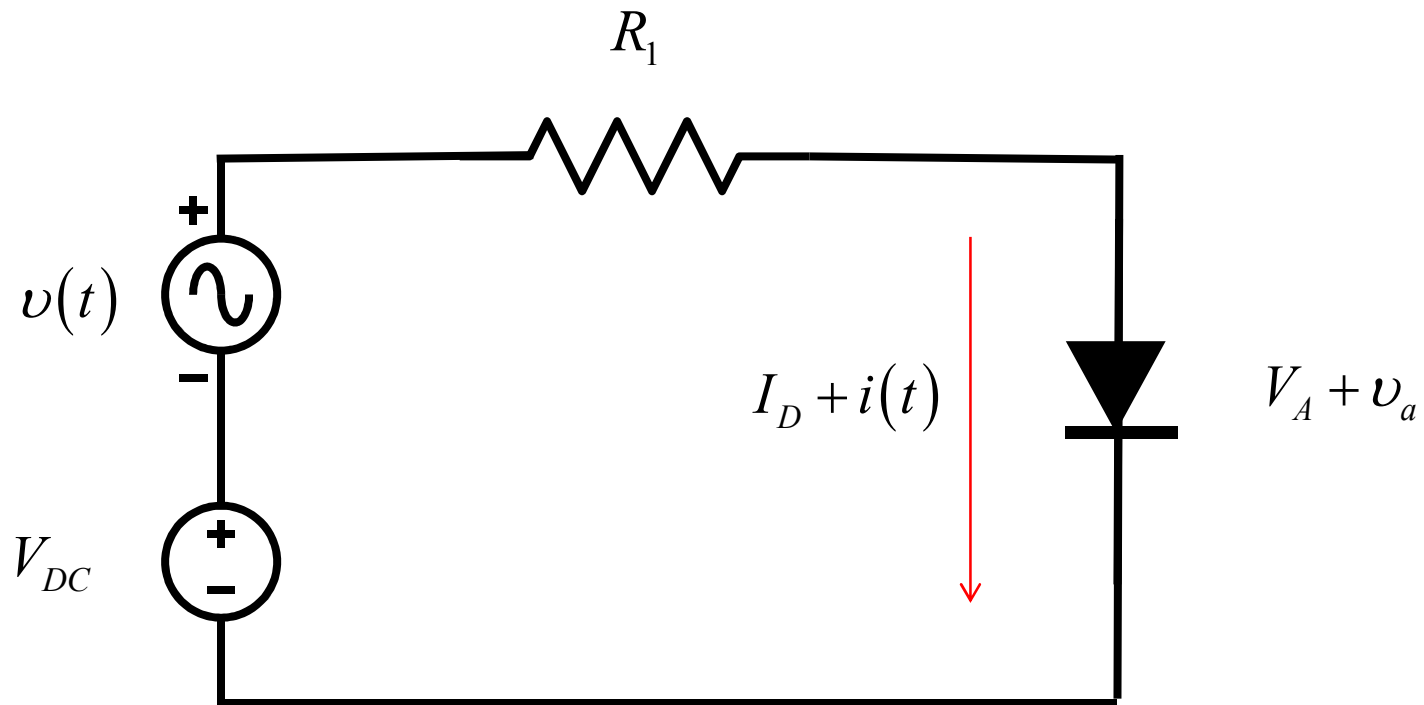
equivalent circuit (general)



$$C_J(V_R) = \frac{K_S \epsilon_0 A}{\left[\frac{2K_S \epsilon_0}{qN_A} (V_{bi} - V_A) \right]^{1/2}}$$

$$C_D = G_d \tau_n$$

small signal ac



- 1) Compute the DC bias current
- 2) Replace the diode with the s.s. a.c. model and do the a.c. analysis.

Summary of Small Signal Model

- In small signal approximation, can treat AC response of pn junction as small perturbation to DC ideal diode equation
- In reverse bias, we find a variable complex impedance (varactor): a junction capacitance and conductance in parallel, i.e., $Y_{eq} = G_c + j\omega C_J$
- In forward bias, we also have a diffusion capacitance, so: $Y_{eq} = G_c + j\omega(C_J + C_D)$