

# ECE-305: Spring 2018

## Metal-Semiconductor Junctions

Pierret, *Semiconductor Device Fundamentals* (SDF)  
Chapter 14 (pp. 477-487)

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# outline

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- 1) Equilibrium band-diagrams and  $V_{bi}$
- 2) Band diagram under bias

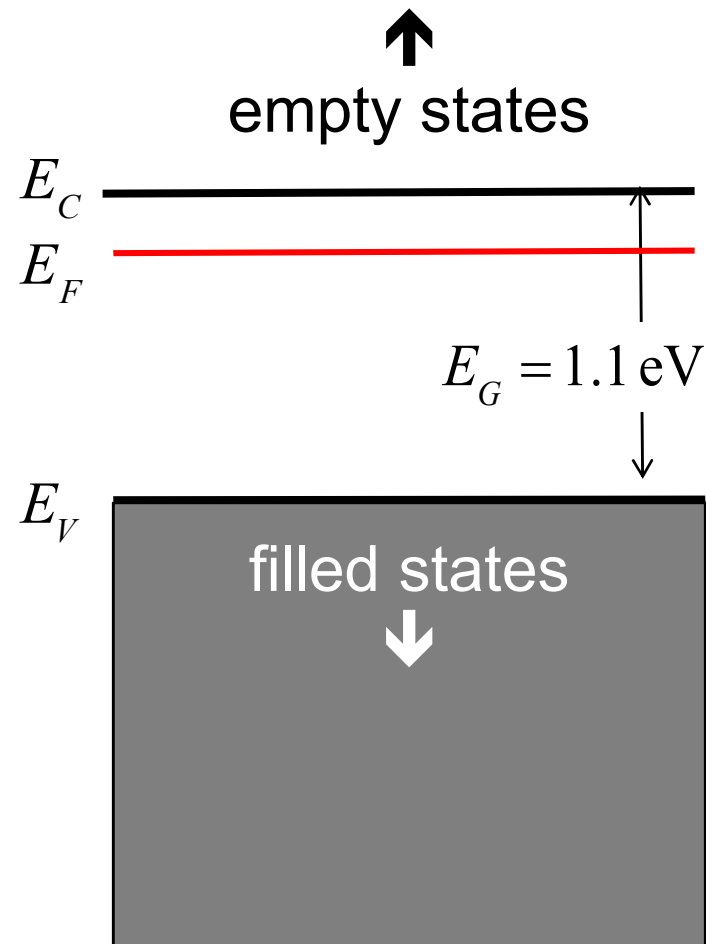
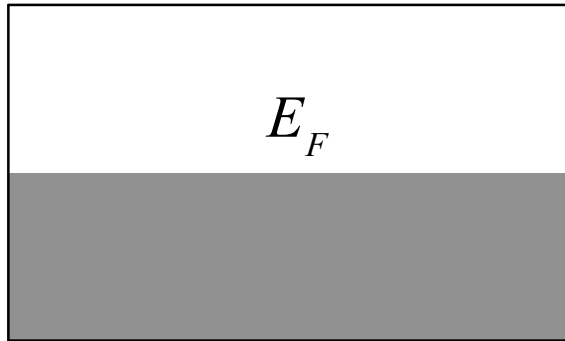
# Topic Map

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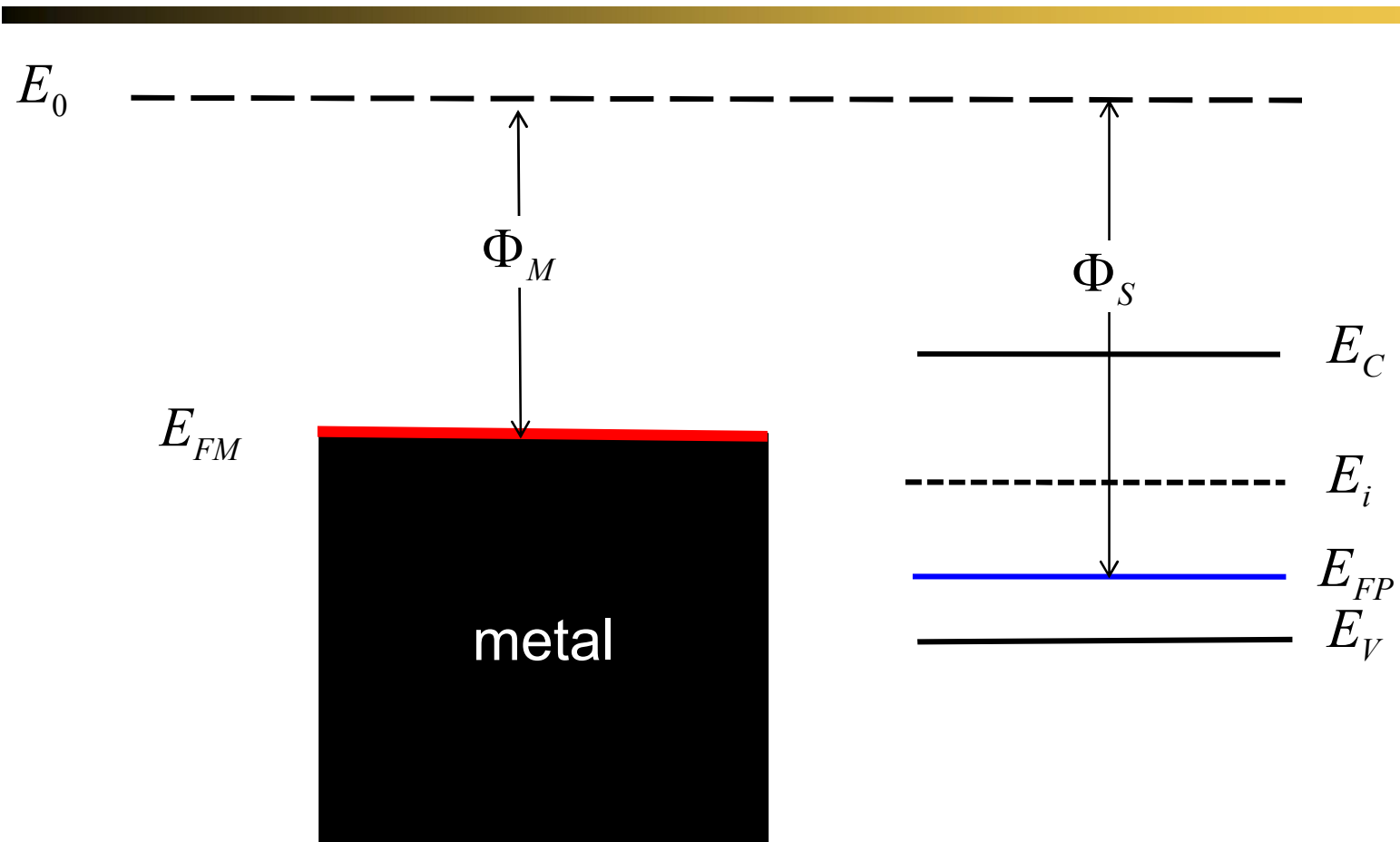
	<b>Equilibrium</b>	<b>DC</b>	Small signal	Large Signal	Circuits
Diode					
<b>Schottky</b>					
BJT/HBT					
MOSFET					

# metal energy bands    semiconductor energy bands

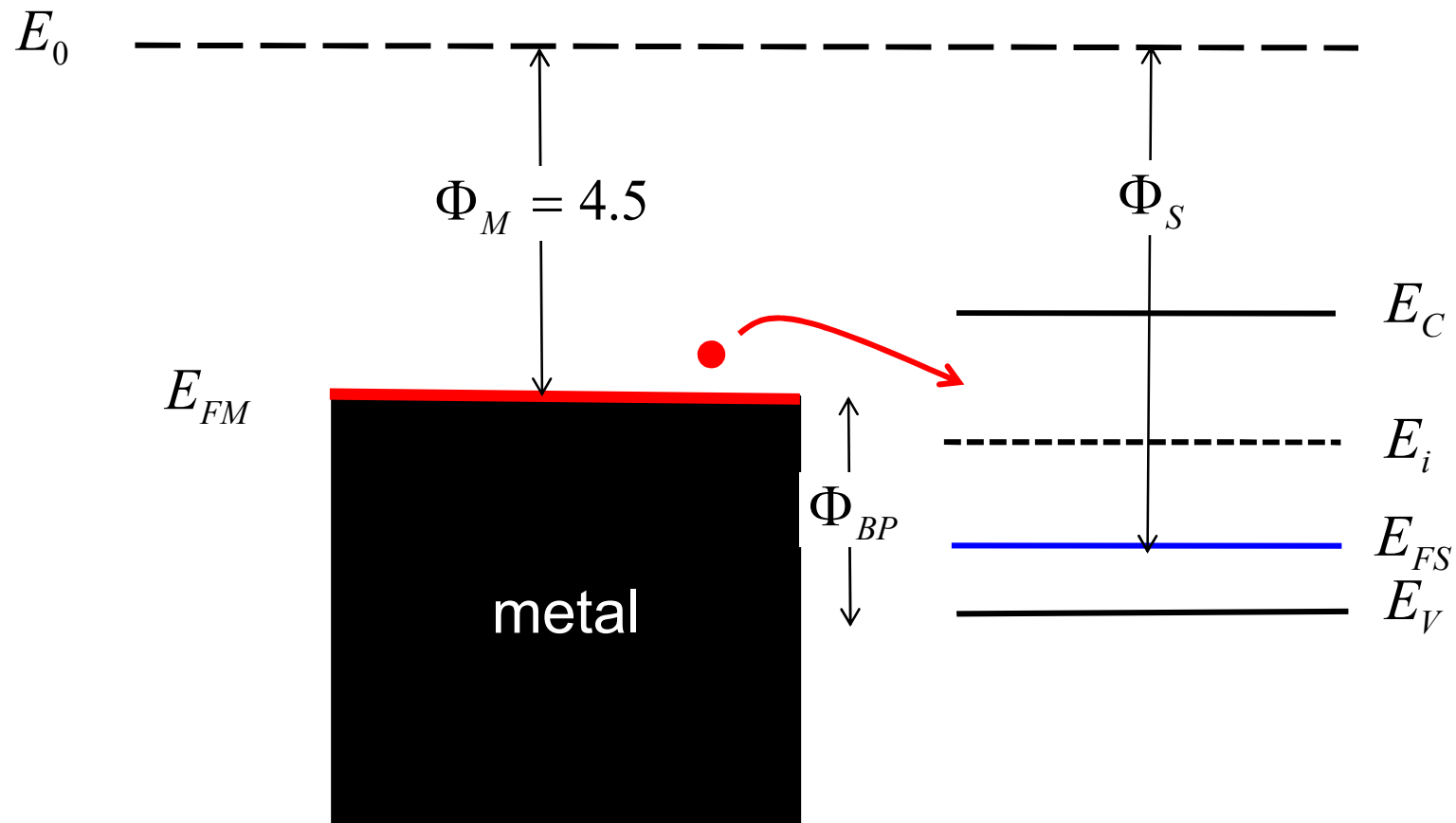
top most band is half-filled



# metal: p-type junction

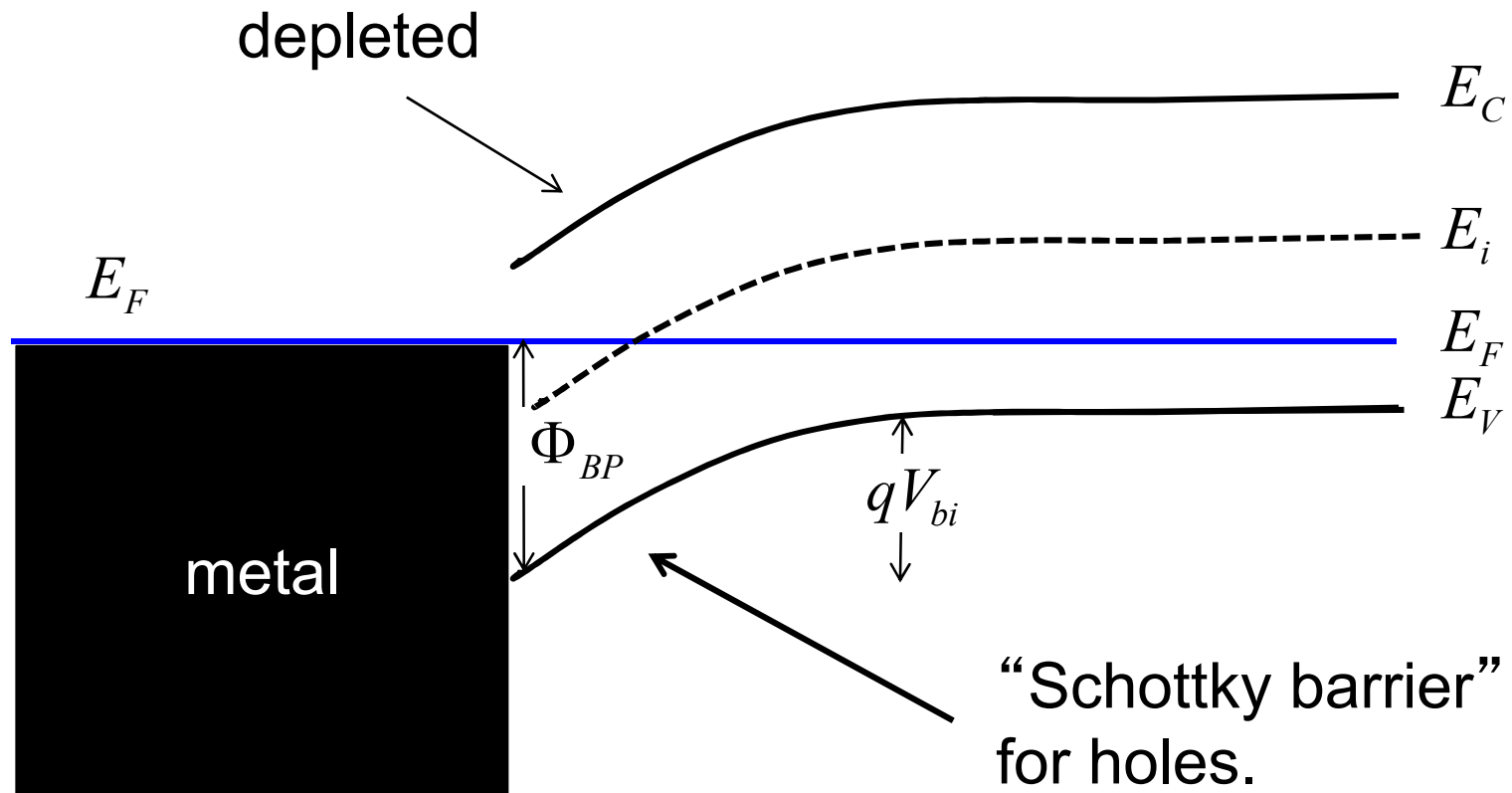


# now the band diagram



# band diagram

from the band diagram....potential, e-field,  $p(x)$ ,  $\rho(x)$



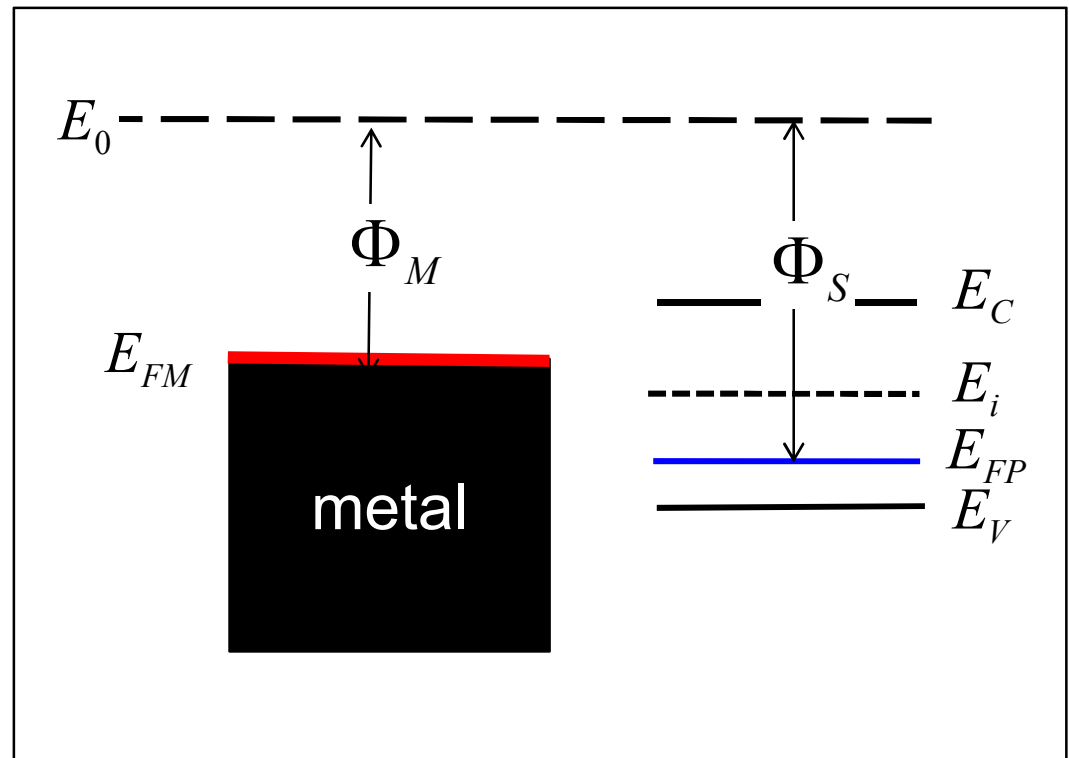
# metal: p-type junction

What is the built-in voltage of a MS junction?

$$qV_{bi} = E_{FM} - E_{FS}$$

$$qV_{bi} = (E_0 - \Phi_M) - (E_0 - \Phi_S)$$

$$qV_{bi} = (\Phi_S - \Phi_M)$$



$\Phi_M$  is a known material parameter



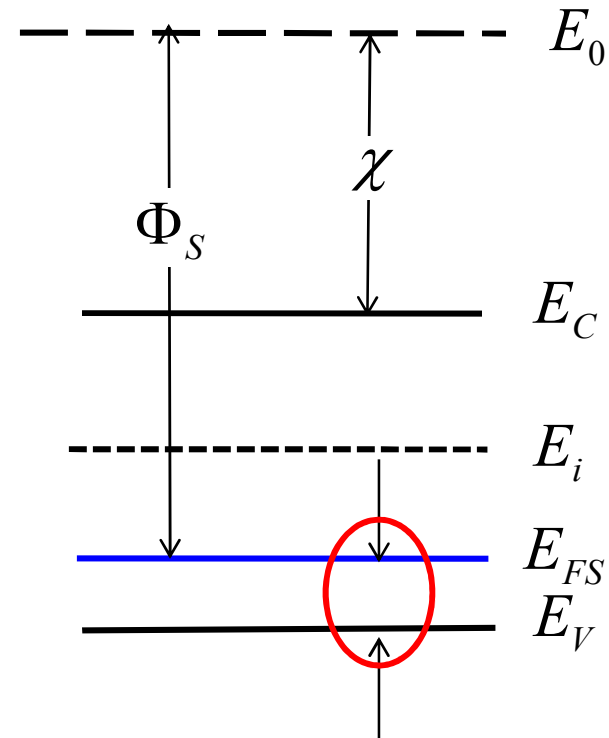
# Semiconductor workfunction

Electron affinity,  $\chi$ , and bandgap are known material parameters.

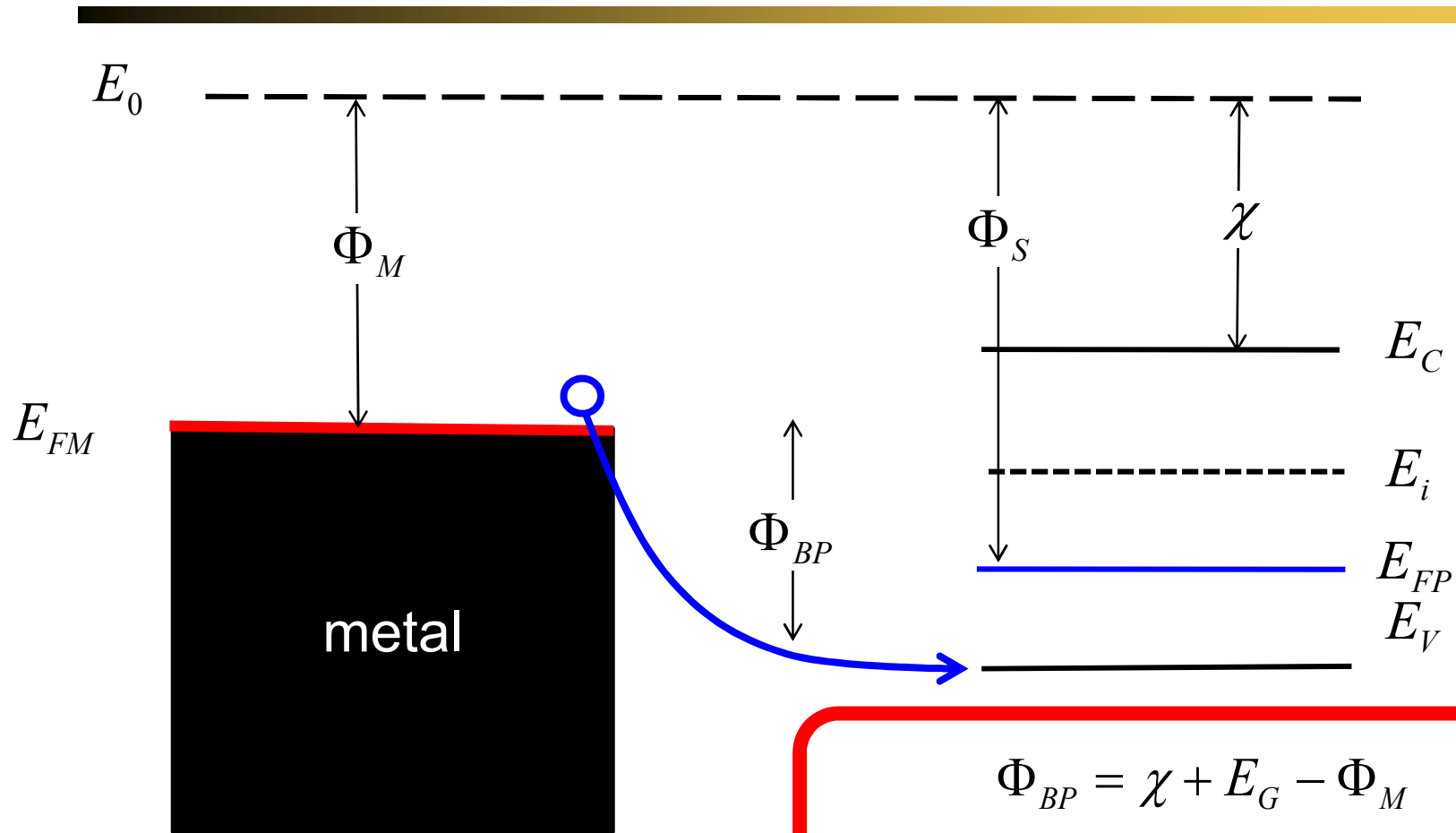
$$\Phi_S = \chi + E_G - (E_{FS} - E_V)|_{bulk}$$

$$p_0 = N_A = N_V e^{(E_V - E_{FS})/k_B T}$$

$$(E_{FS} - E_V) = k_B T \ln \left( \frac{N_A}{N_V} \right)$$



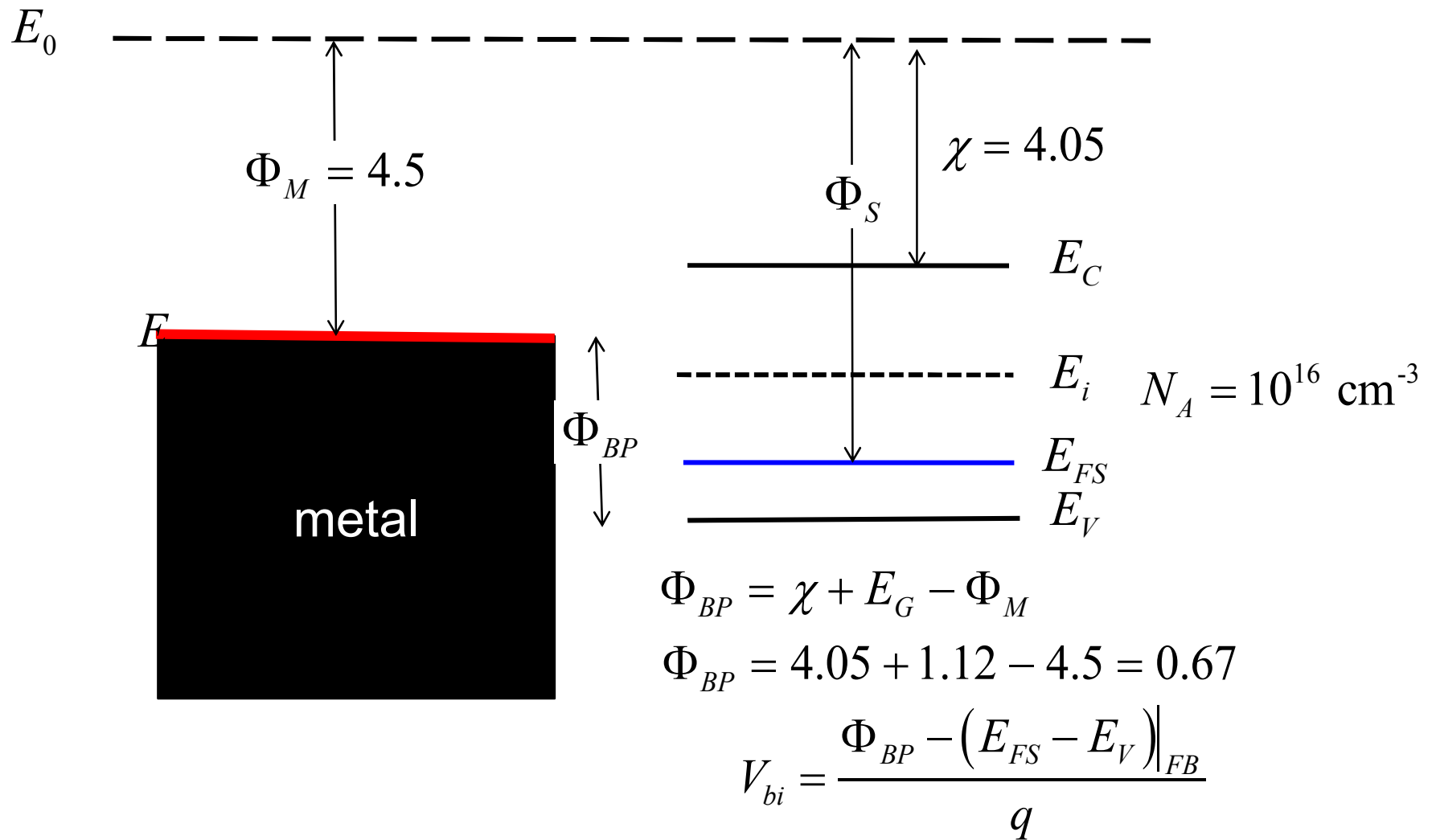
# “Schottky barrier height”



$$\Phi_{BP} = \chi + E_G - \Phi_M$$

a known material parameter

# Vbi example for silicon



## Vbi example for silicon

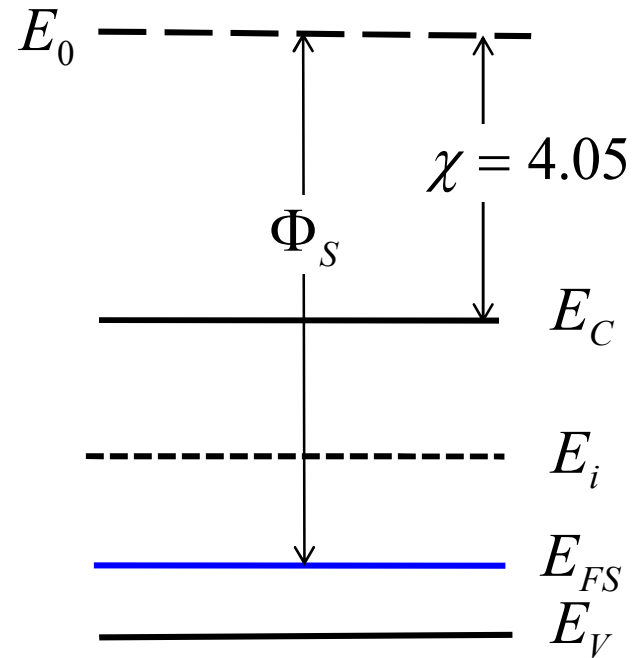
$$N_A = 10^{16} \text{ cm}^{-3}$$

$$p_0 = N_V e^{(E_V - E_{FS})/k_B T} \text{ cm}^{-3}$$

$$E_{FS} - E_V = k_B T \ln \left( \frac{N_V}{N_A} \right)$$

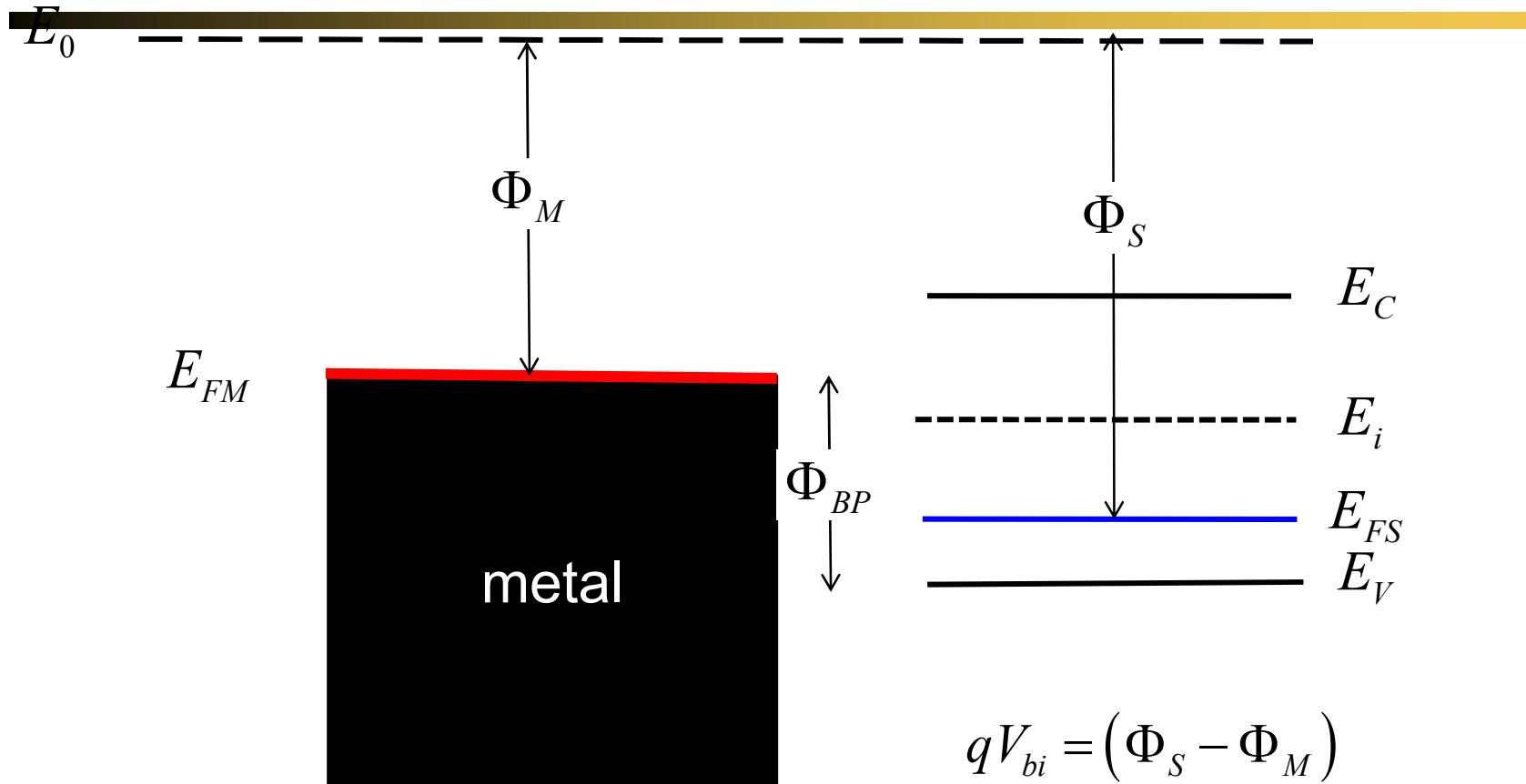
$$N_V = 2 \left[ \frac{(m_p^* k_B T)}{2\pi\hbar^2} \right]^{3/2}$$

$$N_V = 1.83 \times 10^{19} \text{ cm}^{-3}$$



$$\frac{E_{FS} - E_V}{q} = 0.026 \ln \left( \frac{1.83 \times 10^{19}}{10^{16}} \right) = 0.2$$

# V<sub>bi</sub>

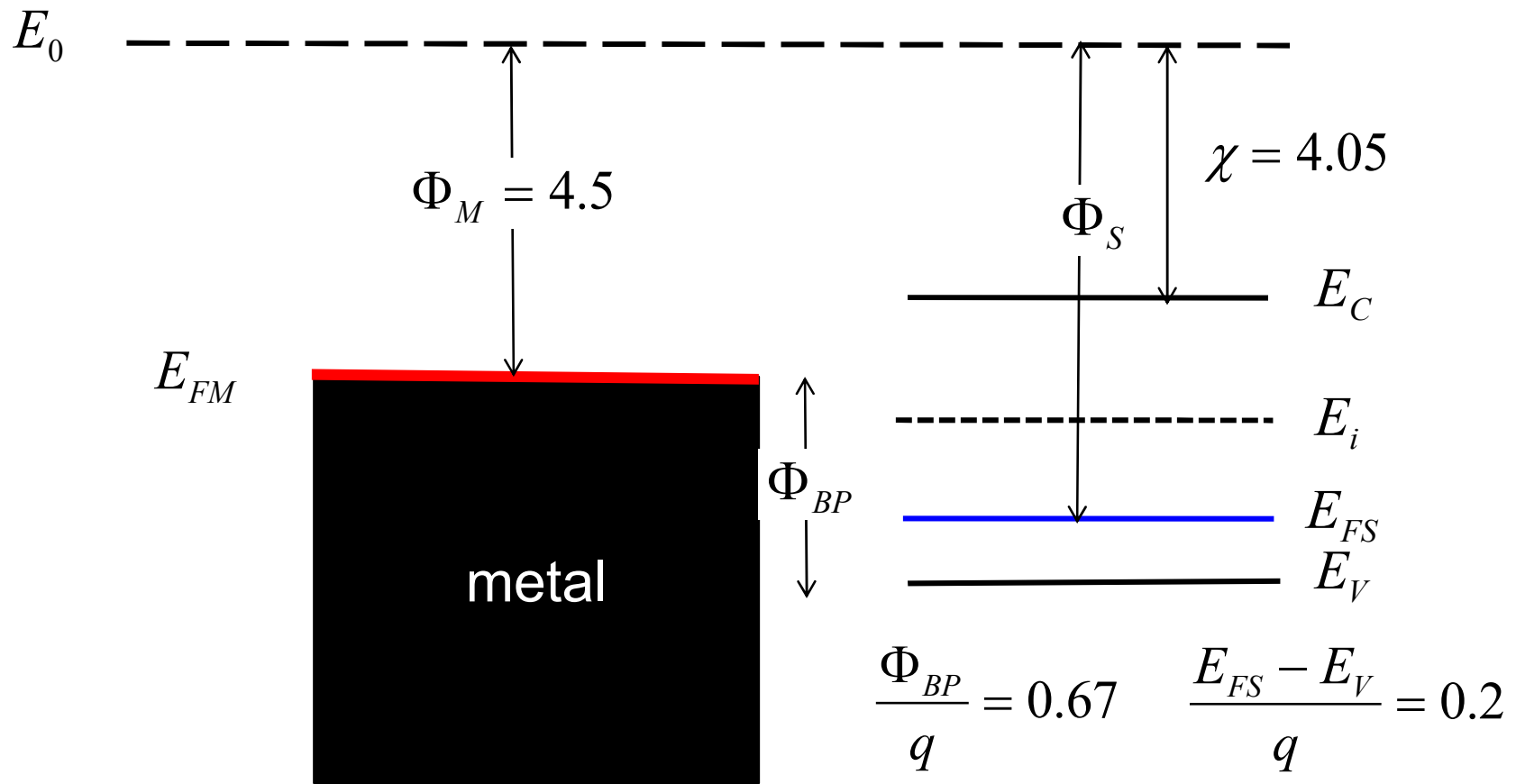


$$\Phi_S = \chi + E_G - (E_{FS} - E_V)|_{bulk}$$

$$\Phi_M = \chi + E_G - \Phi_{BP}$$

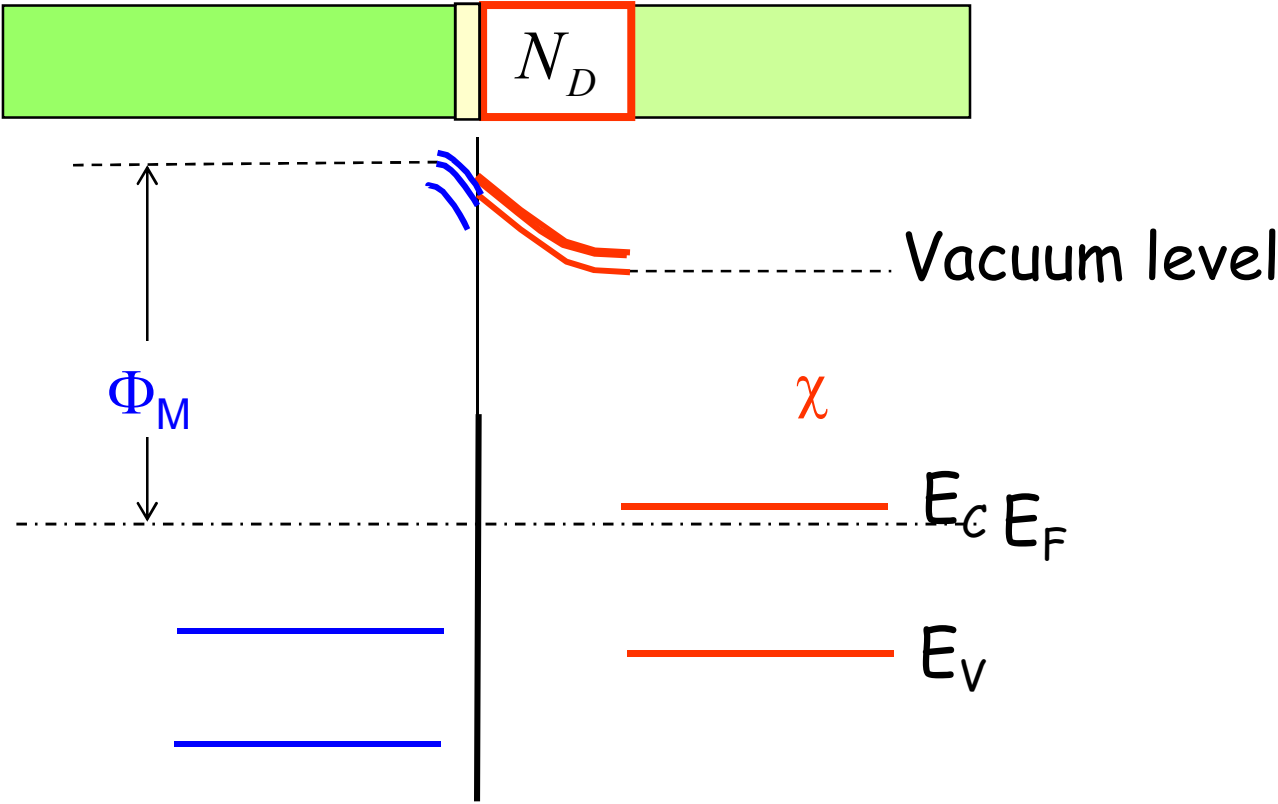
$$qV_{bi} = \Phi_{BP} - (E_{FS} - E_V)|_{bulk}$$

# Vbi example



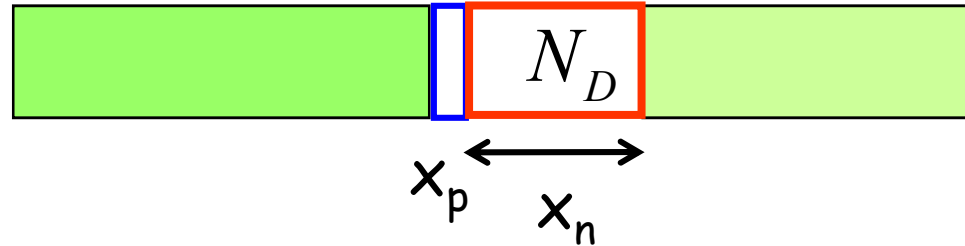
$$V_{bi} = \Phi_{BP} - (E_{FS} - E_V) \Big|_{FB} = 0.67 - 0.20 = 0.47$$

# Band-diagram



Recall:  $N_A x_p = N_D x_n$

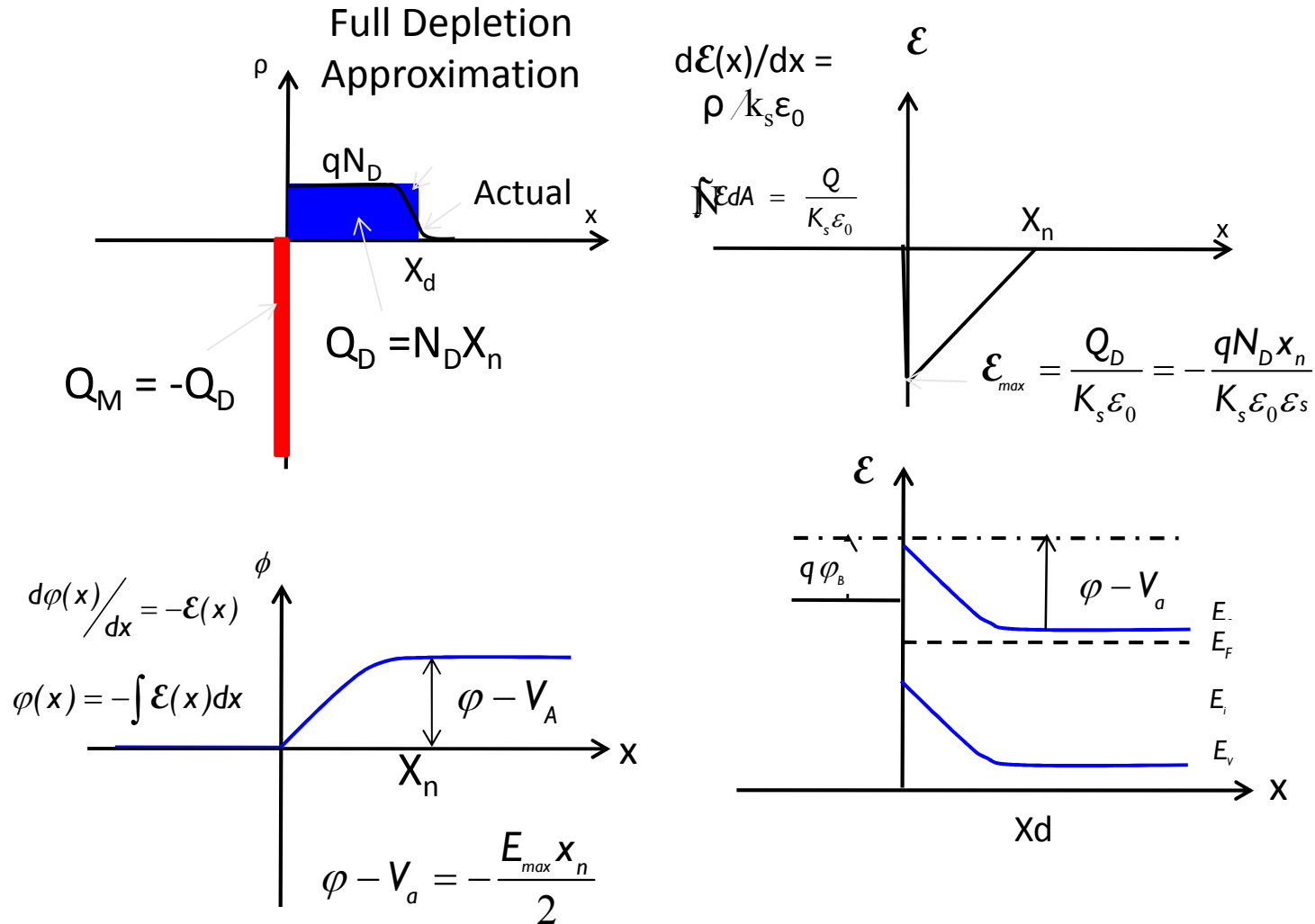
# Depletion Regions



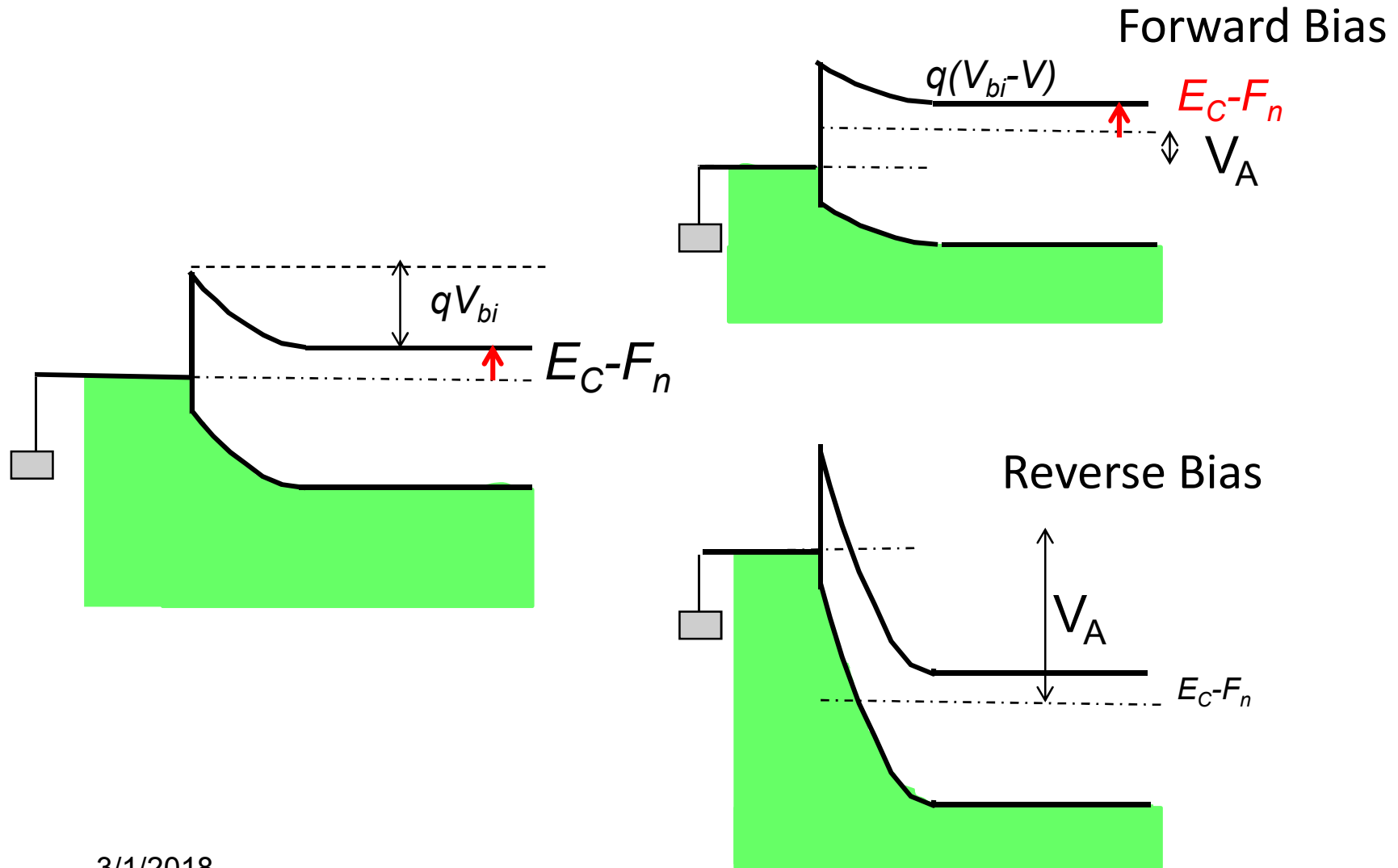
$$\left. \begin{aligned} N_D x_n &= N_M x_p \\ qV_{bi} &= \frac{qN_D x_n^2}{2k_s \epsilon_0} + \frac{qN_M x_p^2}{2k_s \epsilon_0} \end{aligned} \right\} \begin{aligned} x_n &= \sqrt{\frac{2k_s \epsilon_0}{q} \frac{N_M}{N_D (N_M + N_D)} V_{bi}} \rightarrow \sqrt{\frac{2k_s \epsilon_0}{q} \frac{1}{N_D} V_{bi}} \\ x_p &= \sqrt{\frac{2k_s \epsilon_0}{q} \frac{N_D}{N_M (N_M + N_D)} V_{bi}} \rightarrow 0 \end{aligned}$$



# Complete Analytical Solution

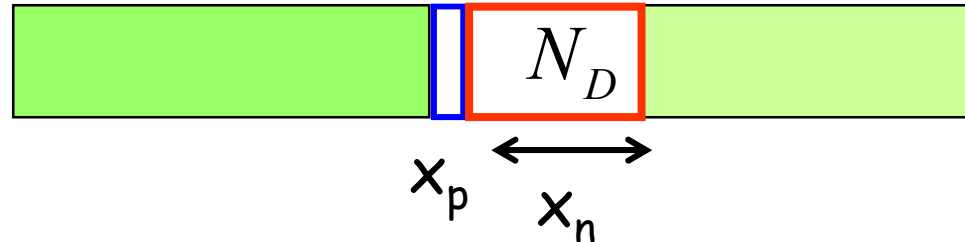


# Band-diagram with Bias



3/1/2018

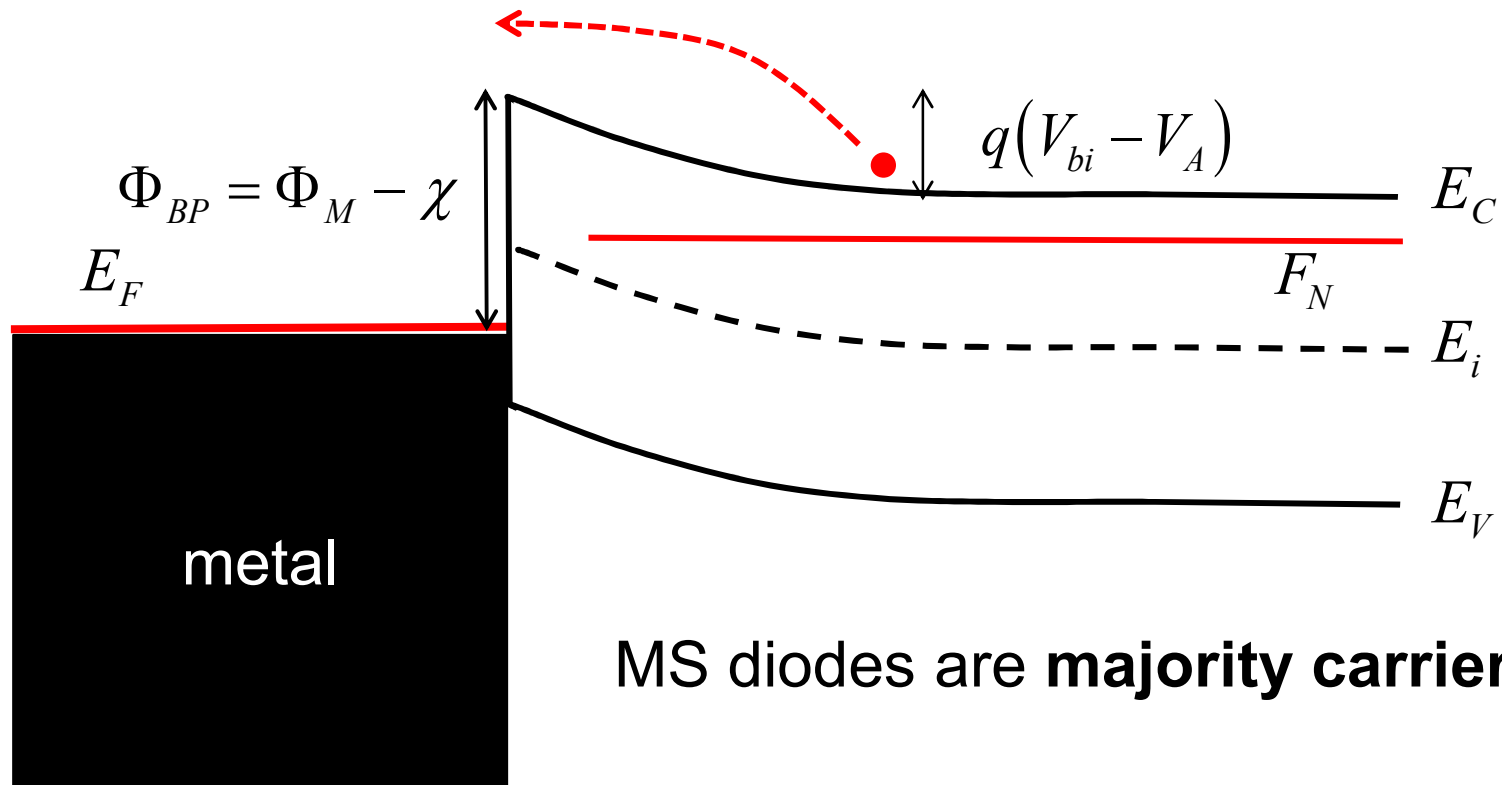
# Depletion Regions with Bias



$$x_n = \sqrt{\frac{2k_s \epsilon_0}{q} \frac{N_M}{N_D (N_M + N_D)} V_{bi}} \rightarrow \sqrt{\frac{2k_s \epsilon_0}{q} \frac{1}{N_D} (V_{bi} - V_A)}$$

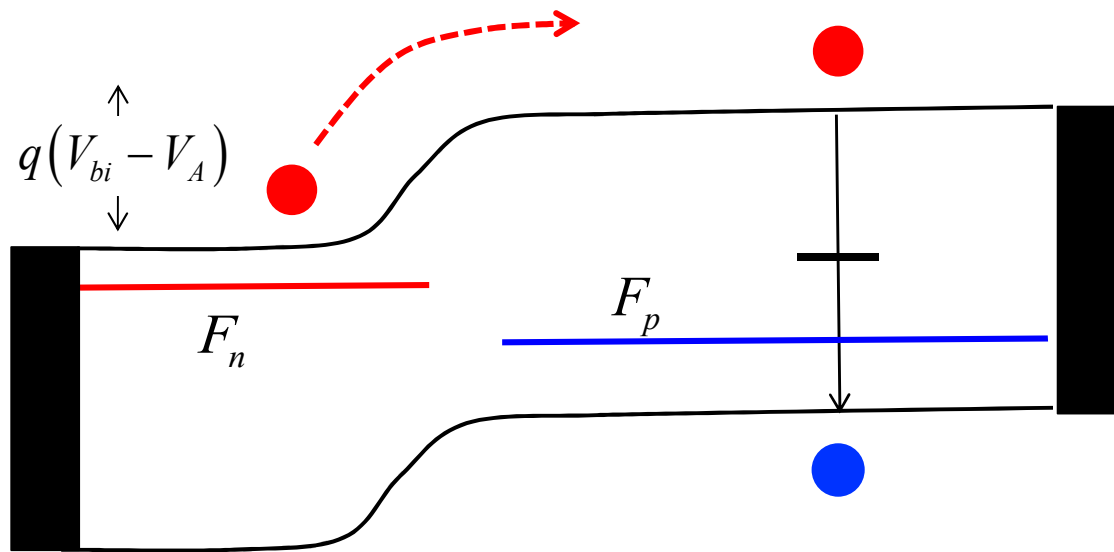
$$x_p = \sqrt{\frac{2k_s \epsilon_0}{q} \frac{N_D}{N_M (N_M + N_D)} V_{bi}} \rightarrow 0$$

# band diagram



MS diodes are **majority carrier** devices


# MS diodes vs. PN junctions



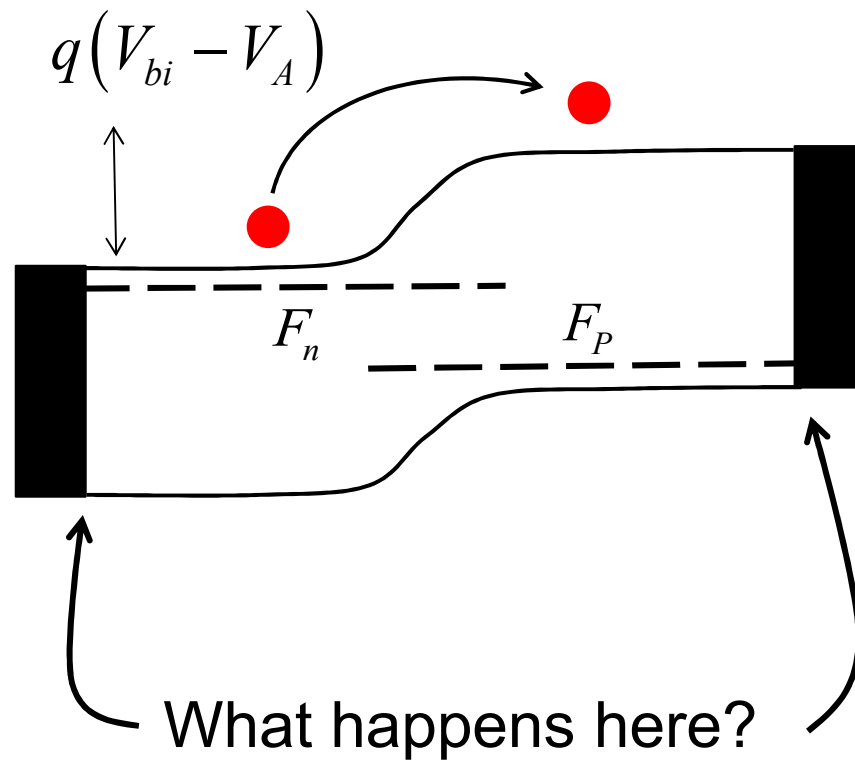
In contrast, NP junctions are **minority carrier** devices

# Topic Map

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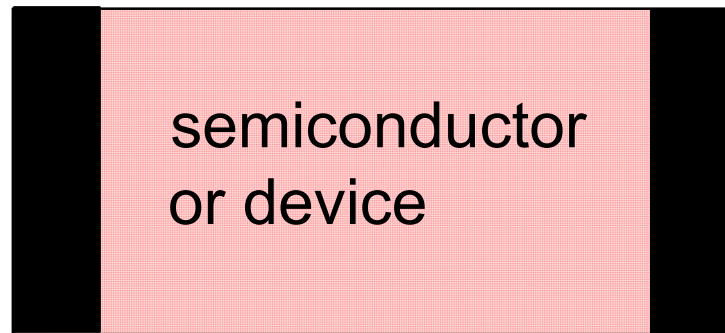
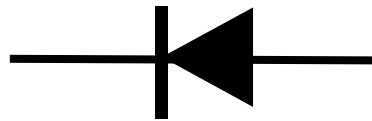
	Equilibrium	<b>DC</b>	Small signal	Large Signal	Circuits
Diode					
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MOSFET					

# NP junctions

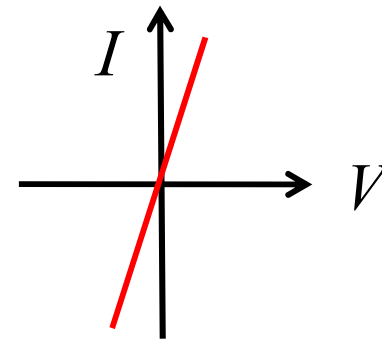
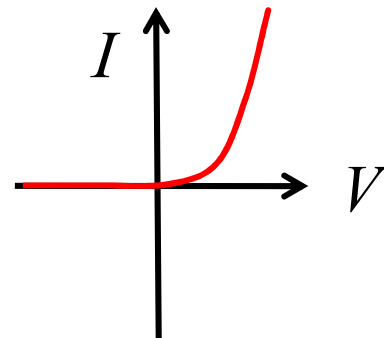


# two types of MS diodes

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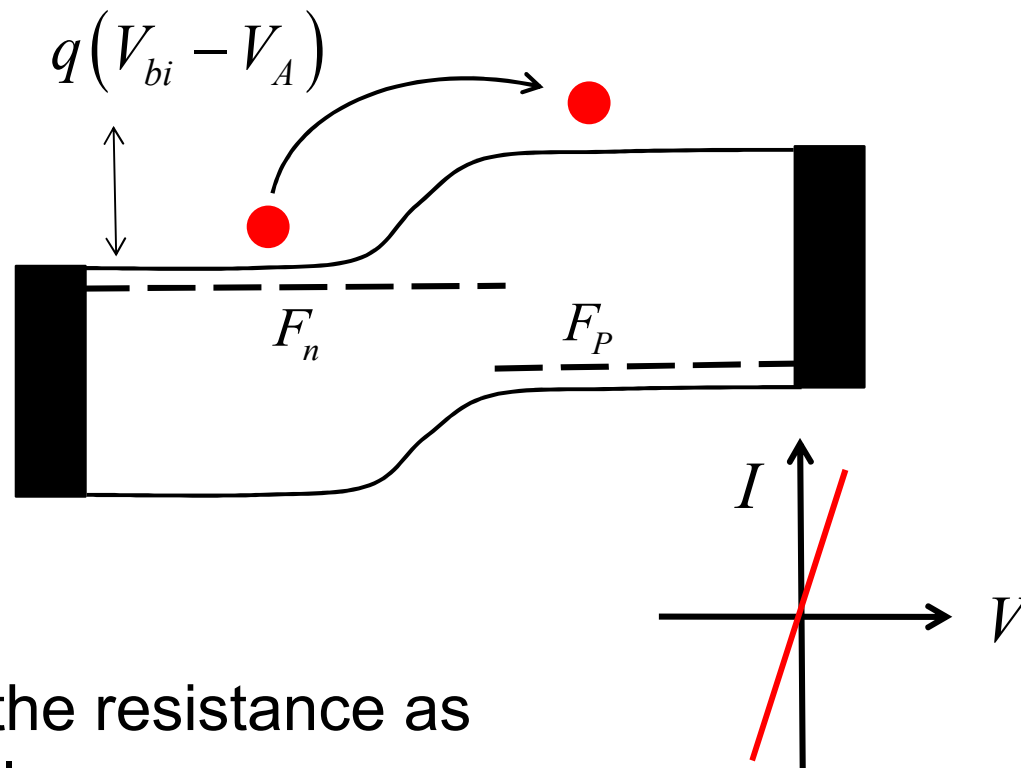
rectifying



ohmic



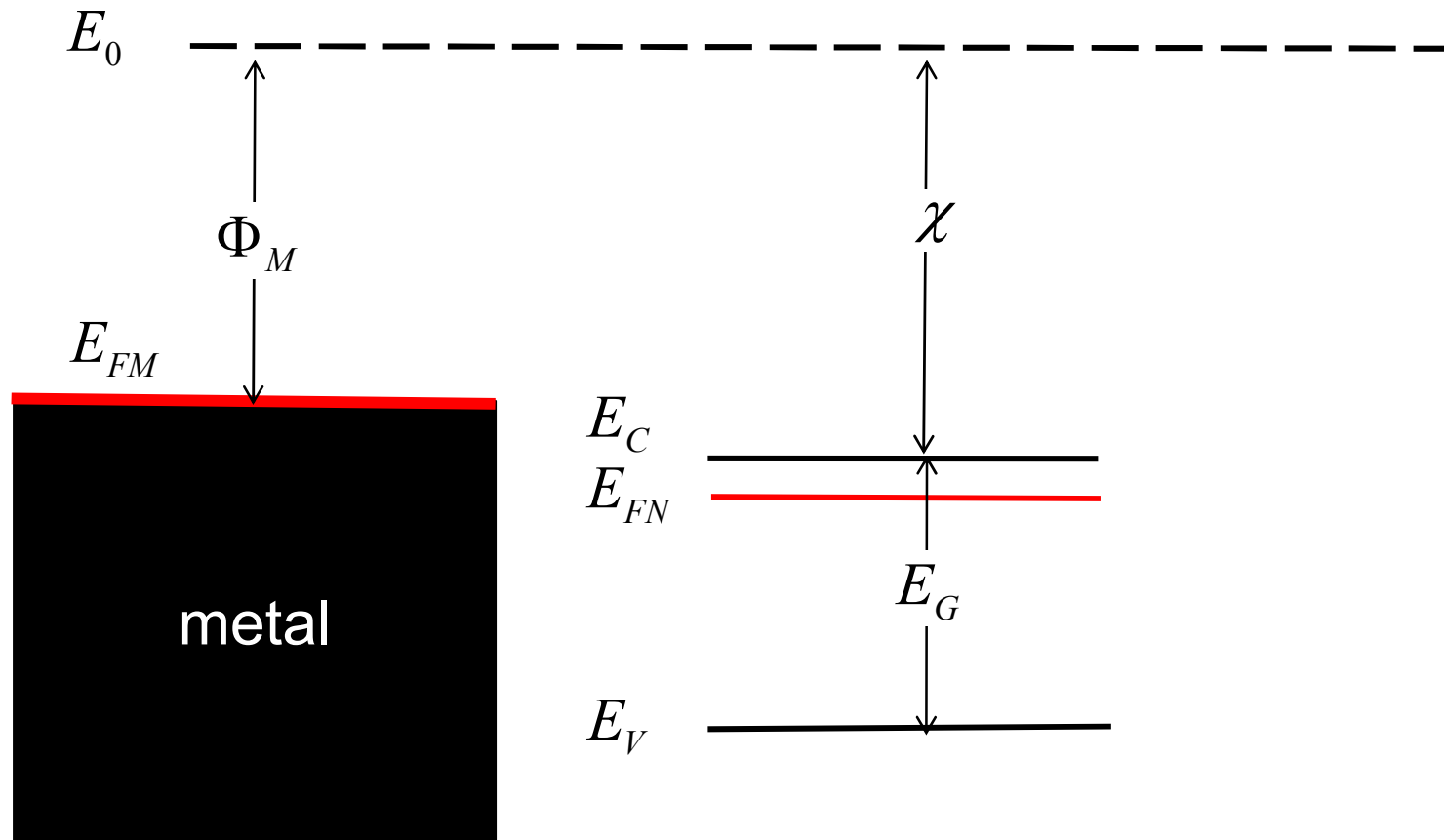
# MS ohmic contacts



**Goal:** make the resistance as low as possible.

one way to make an ohmic contact

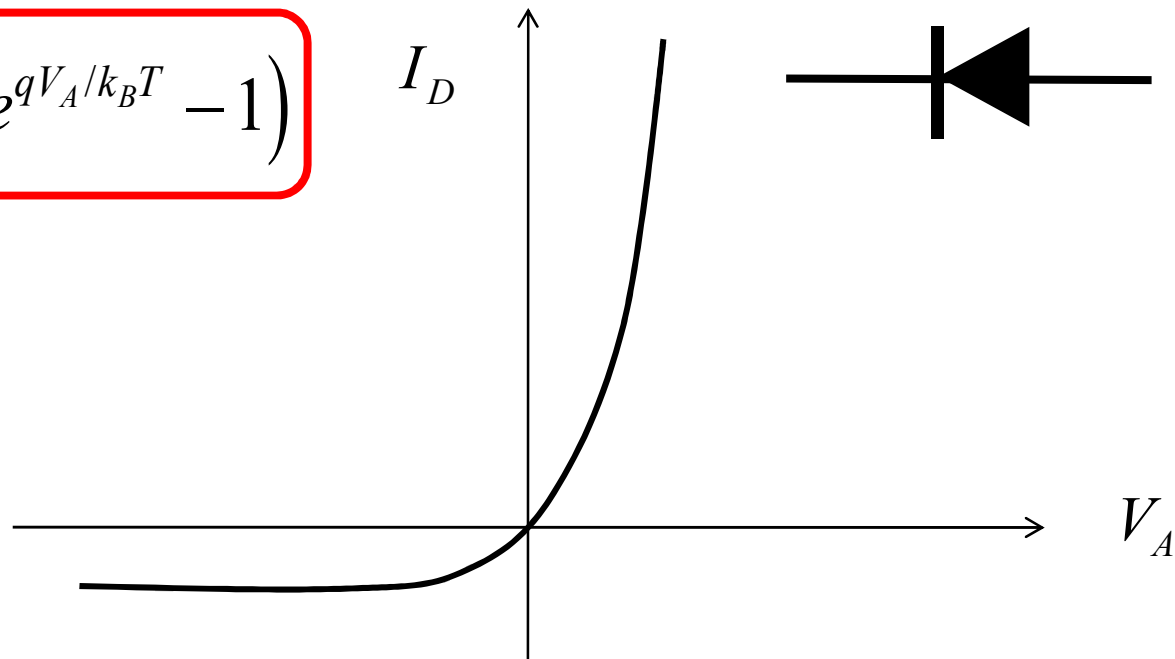
**Use a low workfunction metal (for n-type semiconductors)**



# expected IV characteristics: rectifying diodes

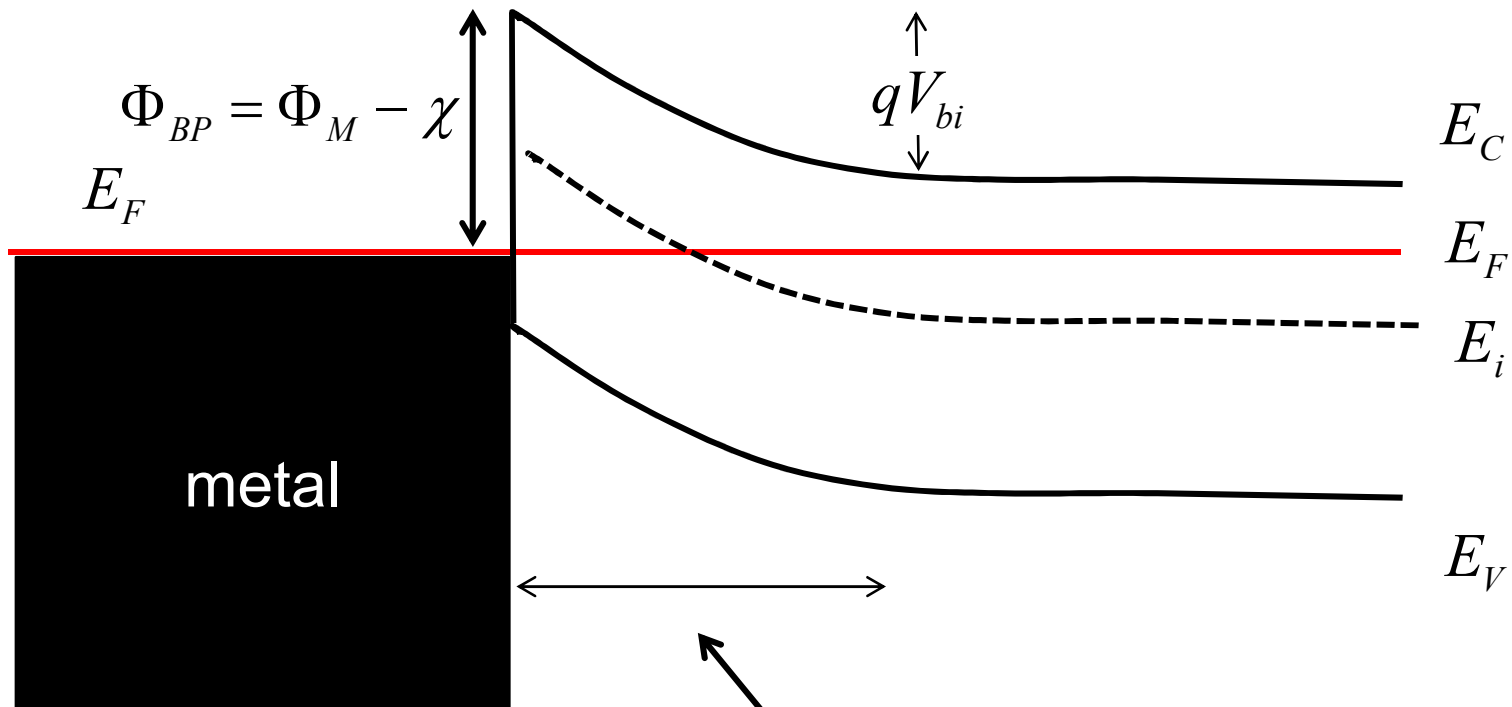
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$$I_D = I_0 \left( e^{qV_A/k_B T} - 1 \right)$$



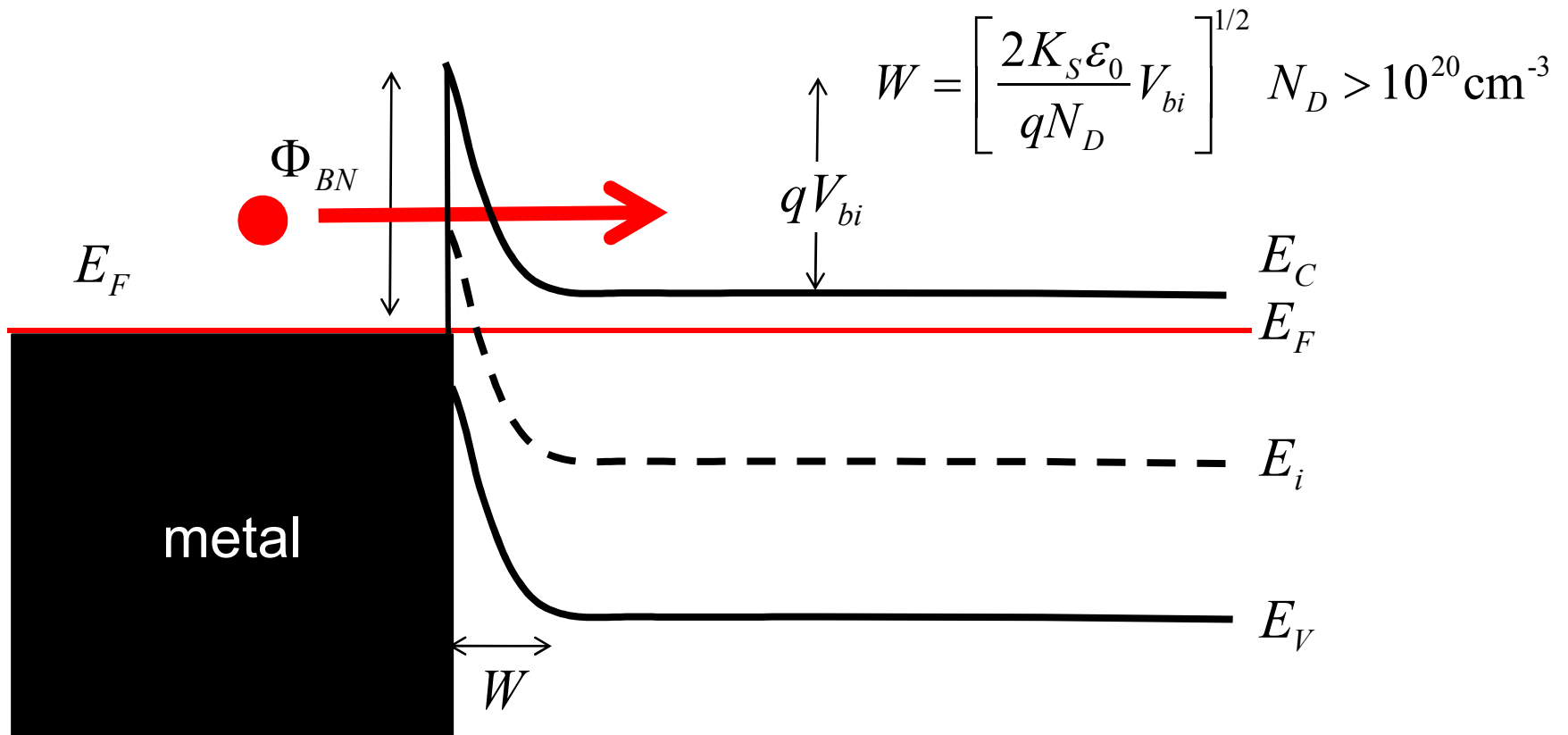
In Schottky diodes,  $I_0 = ?$

# Another way to make an ohmic contact



$$W = \left[ \frac{2K_S \epsilon_0}{qN_D} V_{bi} \right]^{1/2}$$

# alternative way to make an ohmic contact



Dope the semiconductor **very heavily** to promote quantum mechanical tunneling.

# conclusions

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- Studied equilibrium properties of metal-semiconductor junctions
- Bias affects semiconductor bands but leaves metal bands unchanged
- Two types of metal-semiconductor junctions: Ohmic and Schottky
- Next time, will study I-V characteristics of devices based on Schottky metal-semiconductor junctions