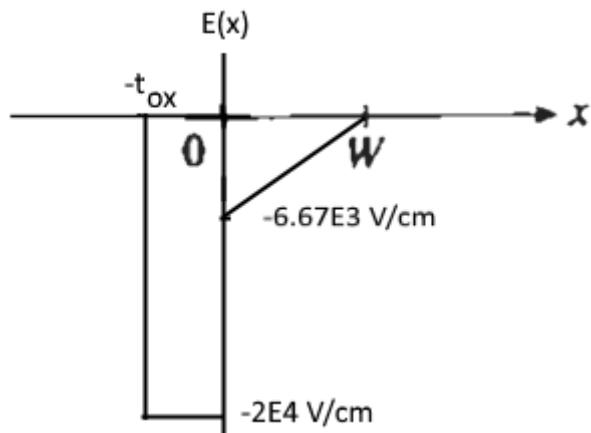


ECE 305 – Spring 2018

Homework 9 Solution

1.

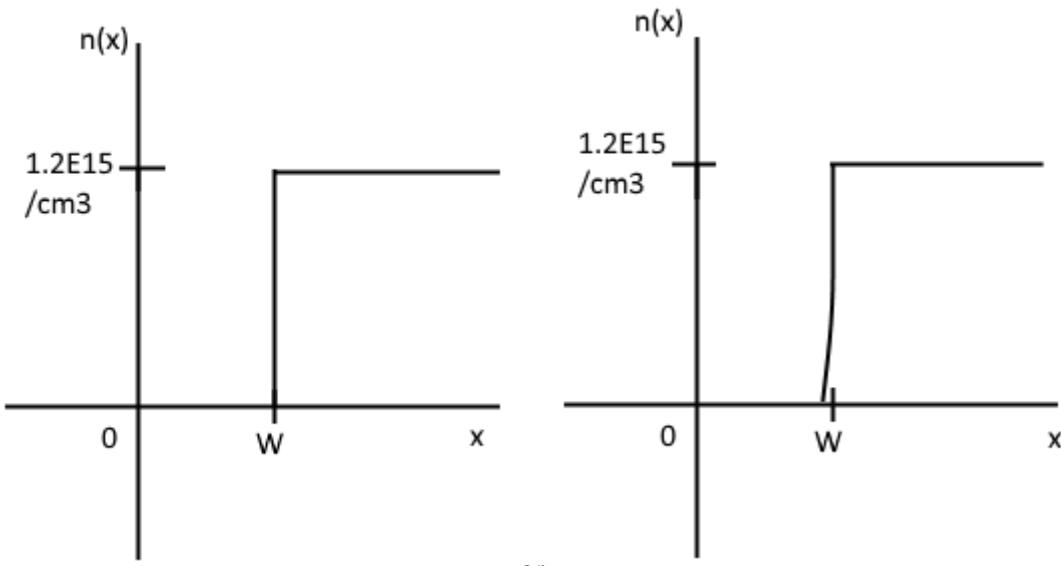


$$E(0+) = K_{ox}/K_{Si} \times E(0-) = 4/12 \times -2 \times 10^4 = -6.67 \times 10^3 \text{ V/cm}$$

b.

$$n_i = 1.1 \times 10^{10} \text{ cm}^{-3}$$

$$\text{n at } x=W: n = n_i e^{(E_F - E_i)/kT} = n_i e^{0.29 \times 40} = 1.2 \times 10^{15} \text{ cm}^{-3}$$

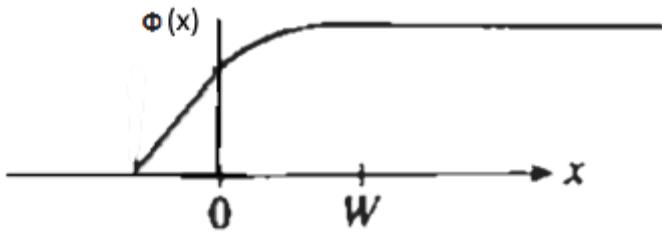


or

c.

$$\text{n at } W \approx N_D \approx 1.2 \times 10^{15} \text{ cm}^{-3}$$

d.



$\Phi_S = \text{change in potential from bulk to surface} = (E_{FS} - E_i)/q = 0.29 \text{ V}$ (As $E_i = E_{FS}$ at $x=0$)

Or,

$$E_S = \sqrt{\frac{2qN_D\phi_S}{K_S\epsilon_0}} \text{ where } E_S = 6.67 \times 10^3 \text{ V}, N_D \approx 1.2 \times 10^{15} \text{ cm}^{-3}$$

$$\Phi_S = 0.12 \text{ V}$$

e.

Voltage drop across oxide = $2 \times 10^4 \text{ V/cm} \times 2 \times 10^{-5} \text{ cm} = 0.4 \text{ V}$

f.

$$V'_G = -(0.29 + 0.4) = -0.69 \text{ V}$$

Or

$$V'_G = -(0.12 + 0.4) = -0.52 \text{ V}$$

2.

$$\text{a. } W = \sqrt{\frac{2K_{Si}\epsilon_0}{qN_A}} \phi_s$$

$$\Rightarrow \phi_s = \frac{qN_A}{2K_{Si}\epsilon_0} W^2$$

$$V_a' = \phi_s + \frac{K_{Si}}{K_{ox}} t_{ox} \sqrt{\frac{2qN_A}{K_{Si}\epsilon_0} \phi_s}$$

$$\Rightarrow 0 = \frac{qN_A}{2K_{Si}\epsilon_0} W^2 + \frac{K_{Si}}{K_{ox}} t_{ox} \frac{qN_A}{K_{Si}\epsilon_0} W - V_a'$$

This is a quadratic equation:

$$aW^2 + bW + c = 0$$

$$W = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-\frac{qN_A t_{ox}}{K_{ox} \epsilon_0} \pm \sqrt{\frac{\tilde{q}^2 N_A^2 t_{ox}^2}{K_{ox}^2 \epsilon_0^2} - q \frac{qN_A}{2k_{si} \epsilon_0} V_h}}{2 \cdot \frac{qN_A}{2k_{si} \epsilon_0}}$$

$$= \frac{-\frac{qN_A t_{ox}}{K_{ox} \epsilon_0} \pm \sqrt{\frac{\tilde{q}^2 N_A^2 t_{ox}^2}{K_{ox}^2 \epsilon_0^2} + \frac{2qN_A}{K_{si} \epsilon_0} V_h'}}{\frac{qN_A}{K_{si} \epsilon_0}}$$

$$= -\frac{k_{si}}{K_{ox}} t_{ox} \pm \sqrt{\frac{k_{si}}{K_{ox}^2} t_{ox}^2 + \frac{2K_{si} \epsilon_0}{qN_A} V_a'}$$

$$W \geq 0$$

$$\therefore W = -\frac{k_{si}}{K_{ox}} t_{ox} + \sqrt{\frac{k_{si}}{K_{ox}} t_{ox}^2 + \frac{2K_{si} \epsilon_0}{qN_A} V_h'}$$

$$= \frac{k_{si}}{K_{ox}} t_{ox} \left(-1 + \sqrt{1 + \frac{V_a'}{\left(\frac{qN_A k_{si} t_{ox}^2}{2K_{ox}^2 \epsilon_0} \right)}} \right)$$

$$= \frac{k_{si}}{K_{ox}} t_{ox} \left(-1 + \sqrt{1 + \frac{V_a'}{V_s}} \right)$$

$$\text{where } V_s = \frac{qN_A K_{si} t_{ox}^2}{2K_{ox}^2 \epsilon_0}$$

b.

$$\begin{aligned}
 V'_T &= 2\phi_f + \Delta\phi_{ox} \\
 \text{where } 2\phi_f &= \frac{2kT}{q} \ln\left(\frac{N_A}{n_i}\right) \\
 &= 0.6 \text{ V} \\
 \Delta\phi_{ox} &= \mathcal{E}_{ox} t_{ox} \\
 \mathcal{E}_{ox} &= \frac{K_{Si}}{K_{ox}} \mathcal{E}_{Si}
 \end{aligned}$$

$$\mathcal{E}_{si} = \sqrt{\frac{2qN_A 2\phi_f}{K_s \epsilon_o}}$$

Therefore,

$$V'_T = 2\phi_f + \frac{K_{Si}}{K_{ox}} \sqrt{\frac{2qN_A 2\phi_f}{K_s \epsilon_o}} t_{ox} = 0.6 + 1.8 = 2.4 \text{ V}$$

From equation derived in a., depletion width at $V'_G = 0$ is 0

$$\text{Depletion width at } V'_G = V'_T \text{ is: } \sqrt{\frac{2K_s \epsilon_o 2\phi_f}{qN_A}} = 2 \times 10^{-5} \text{ cm}$$

For capacitance:

$$C = \frac{C_0}{\sqrt{1 + V'_G/V'_\delta}}$$

Capacitance at $V'_G = 0$ is C_0 .

Capacitance at $V'_G = V'_T$ is $0.47 C_0$, as $V'_\delta = 0.678$.