

Quiz ANSWERS Week 6
ECE 656: Electronic Conduction In Semiconductors
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- 1) What are the special properties of a contact in the Landauer model?
- a) Strong inelastic scattering keeps them near equilibrium.
 - b) Any electron incident upon the contact is completely absorbed (no reflections).
 - c) Each contact is described by its own Fermi level.
 - d) Contacts have a very large number of channels (modes) compared to the device.
 - e) **All of the above.**
- 2) Which of the follow is true about the Landauer expression for current:
 $I = (2q/h) \int \mathcal{T}(E) M(E) (f_1 - f_2) dE$?
- a) It applies to electrons in the conduction band.
 - b) It applies to electrons in the valence band.
 - c) It applies to holes in the valence band.
 - d) It applies to **both** electrons in the conduction band and holes in the valence band.
 - e) **It applies to both electrons in the conduction band and electrons in the valence band.**
- 3) What are the units of the quantity, $h \langle v_x^+(E) \rangle D(E) / 4$? The units of $D(E)$ are J^{-1} .
- a) Energy
 - b) One over energy
 - c) Ohms
 - d) One over Ohms or Siemens.
 - e) **The quantity is unitless.**
- 4) What is meant by the term “near-equilibrium” transport?
- a) The contacts stay very close to equilibrium.
 - b) The Fermi level in the contact is close to its equilibrium value.
 - c) The Fermi levels of the two contacts, f_1 and f_2 , can be replaced by the equilibrium Fermi level.
 - d) **The difference in Fermi levels between the two contacts can be replaced by a first order Taylor series expansion of $f_1 - f_2$.**
 - e) The temperature of the two contacts is the same.

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- 5) Consider a small nano-device under bias with a steady-state current flowing. Which of the following is true?
- a) One contact tries to fill states in the device and the other one tries to empty them.**
- b) Both contacts try to fill states in the device.
- c) Both contacts try to empty states in the device.
- d) All of the above.
- e) None of the above.
- 6) Mathematically, the number of modes (channels) at energy, E , is proportional to what?
- a) The density of states.
- b) The velocity.
- c) The density of states times velocity.**
- d) The density of states divided by velocity.
- e) The deBroglie wavelength.
- 7) How is the transmission, \mathcal{T} , related to the mean-free-path for backscattering, λ , and the length of the resistor, L ?
- a) $\mathcal{T} = e^{-L/\lambda}$.
- b) $\mathcal{T} = e^{+L/\lambda}$.
- c) $\mathcal{T} = \lambda/L$.
- d) $\mathcal{T} = L/\lambda$.
- e) $\mathcal{T} = \lambda/(\lambda + L)$.**
- 8) For parabolic band semiconductors, $M(E)$ is independent of energy (above the bottom of the conduction band) for which of the following cases?
- a) 1D**
- b) 2D
- c) 3D
- d) 1D and 2D
- e) 2D and 3D

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9) Under what conditions does the Landauer expression for current,

$$I = \frac{2q}{h} \int \mathcal{T}(E) M(E) (f_1 - f_2) dE, \text{ apply?}$$

- a) Near-equilibrium.
- b) For near-ballistic transport conditions, $L \ll \lambda$.
- c) For diffusive transport conditions, $L \gg \lambda$
- d) Far from equilibrium.
- e) **All of the above.**

10) When should we NOT use the Landauer expression, $I = \frac{2q}{h} \int \mathcal{T}(E) M(E) (f_1 - f_2) dE$?

- a) When quantum transport is important.
- b) When semi-classical transport dominates.
- c) When the temperatures of the two contacts are different.
- d) When hole conduction dominates.
- e) **When it is necessary to spatially resolve quantities inside the device.**

11) The electron current equation commonly used in semiconductor physics is written as $J_n = \sigma_n d(F_n/q)/dx$. To derive this from the Landauer approach, what assumptions are needed?

- a) Near-equilibrium transport.
- b) Constant temperature.
- c) A conductor that is many mean-free-paths long.
- d) Answers a) and c) above
- e) **Answers a) b), and c) above.**

12) The drift-diffusion equation commonly used in semiconductor physics is written as $J_{nx} = nq\mu_n E_x + qD_n dn/dx$. What assumption is **NOT needed** to derive this equation from the Landauer approach?

- a) Near-equilibrium transport.
- b) Constant temperature.
- c) A conductor that is many mean-free-paths long.
- d) **Maxwell-Boltzmann statistics.**
- e) Steady-state conductions.

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13) Which of the following is correct about the conductivity of a 2D metal?

- a) $\sigma_S = q^2 D_n(E_F) D_{2D}(E_F)$
- b) $\sigma_S = q^2 D_{2D}(E_F) \frac{v^2(E_F) \tau(E_F)}{2}$
- c) $\sigma_S = \frac{2q^2}{h} M_{2D}(E_F) \lambda(E_F)$
- d) $\sigma_S = n_S q \left(\frac{q \tau(E_F)}{m^*} \right)$

e) All of the above are correct.

14) What is the quantity: $\frac{2q}{hn_S} \int \lambda(E) M_{2D}(E) \left(-\frac{\partial f_0}{\partial E} \right) dE$?

- a) The conductivity of a 2D material.
- b) The mobility of a 2D material.**
- c) The diffusion coefficient of a 2D material.
- d) The average mean-free-path of a 2D material.
- e) The resistivity of a 2D material.

15) How can we determine if a long resistor is operating in near-equilibrium conditions?

- a) The voltage across the resistor must be less than $k_B T / q$.
- b) The measured current is proportional to the applied voltage.**
- c) The magnitude of the electric field satisfies $\mathcal{E} \ll (k_B T / q) / \lambda_E$ where λ_E is the energy relaxation length.
- d) a) and b) above.
- e) a), b), and c) above.

16) The expression for the ballistic conductance, $G_{ball} = \frac{2q^2}{h} M(E_F)$ is valid when?

- a) In the degenerate limit.
- b) For 1D and 2D conductors.
- c) For isothermal conditions.
- d) For ballistic conductors
- e) All of the above.**

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- 17) In general, we can write the ballistic conductance as $G_{ball} = \frac{2q^2}{h} \langle M \rangle$. What is $\langle M \rangle$?
- The number of channels.
 - The number of channels at the Fermi energy.
 - The average number of channels in the Fermi window.**
 - The number of channels at the bottom of the conduction band.
 - The total number of channels in the Fermi window.
- 18) The expression for the resistance, $R = R_{ball} (1 + L/\lambda_0)$ is **not valid** under what conduction conditions?
- In the ballistic limit.
 - In the diffusive limit.
 - In between the ballistic and diffusive limits
 - When the mean-free-path depends on energy.**
 - Under non-degenerate conduction conditions.
- 19) For a ballistic resistor, the power dissipated is $P_D = IV = V^2/R$. Where is this power dissipated?
- Uniformly within the resistor
 - Near the two ends of the resistor
 - In the contact with the most positive voltage
 - In the contact with the most negative voltage
 - In the two contacts.**
- 20) For a ballistic resistor, with a voltage, V , applied across it, where does the voltage drop?
- Uniformly within the resistor.
 - Near the two ends of the resistor.**
 - In the contact with the most positive voltage.
 - In the contact with the most negative voltage.
 - In the two contacts.