

# Theory and Practice of Solar Cells: A Cell to System Perspective

## How a Module gets its Stripes: c-Si

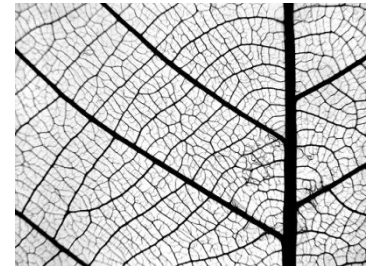
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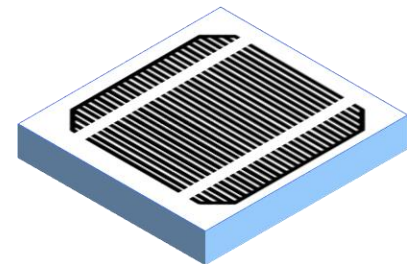
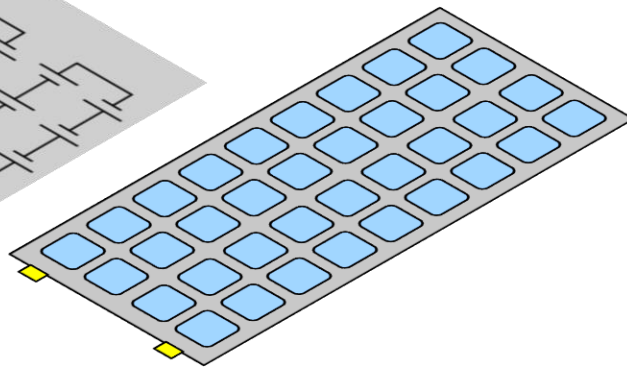
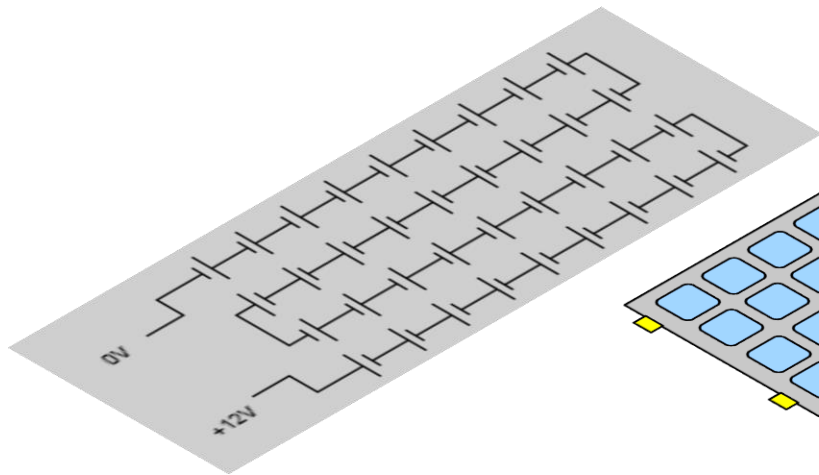
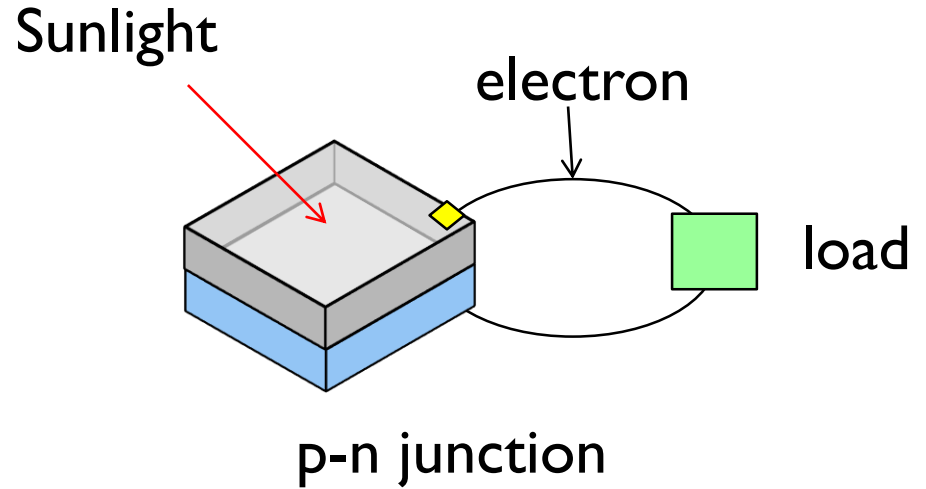
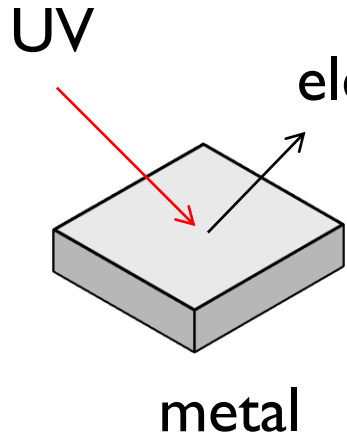
West Lafayette, IN USA



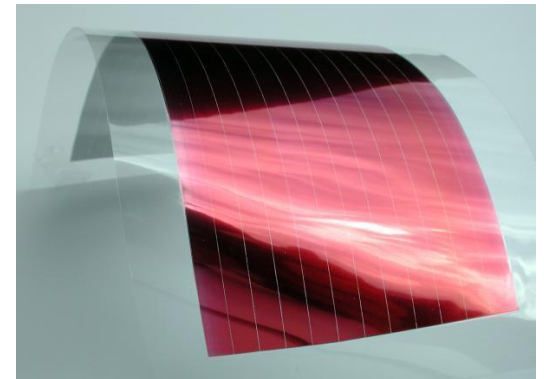
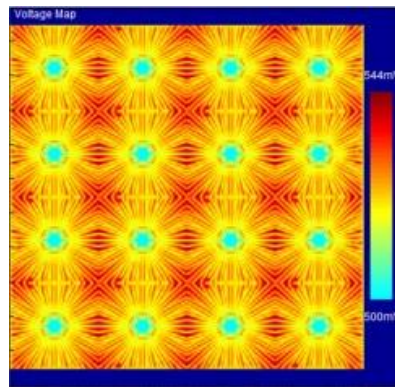
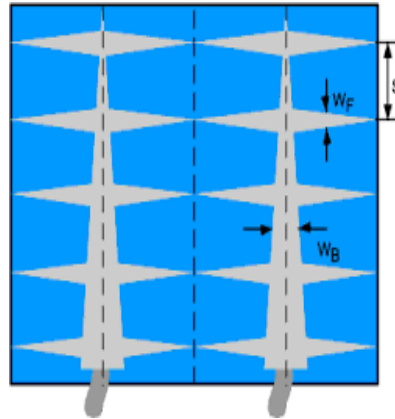
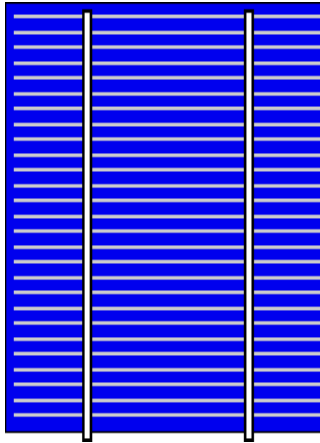
# Outline

- 1) Three types of c-Si gridding
- 2) Physics of standard c-Si cell gridding
- 3) Physics of bifacial cell design
- 4) Inter-digitated back-contact design
- 5) Conclusion

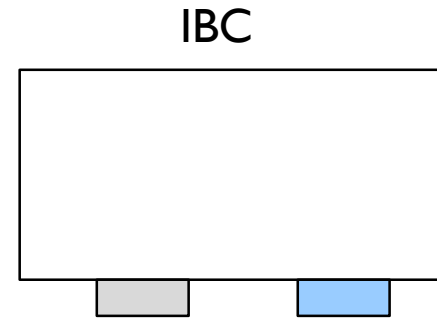
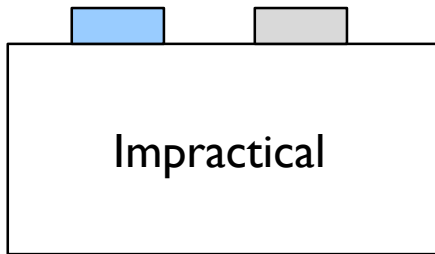
# Photoelectric effect and solar cells



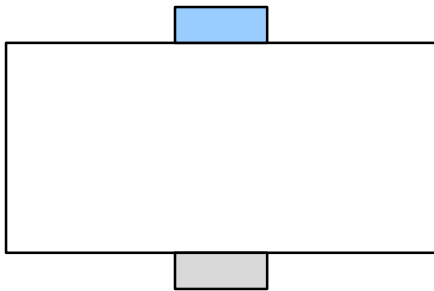
# The Puzzle of Striping



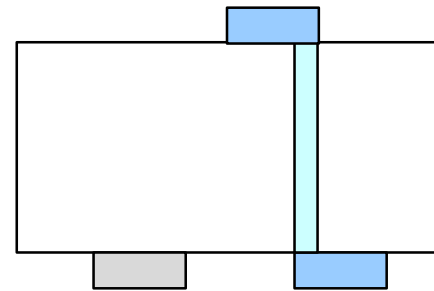
# Grid arrangement of c-Si



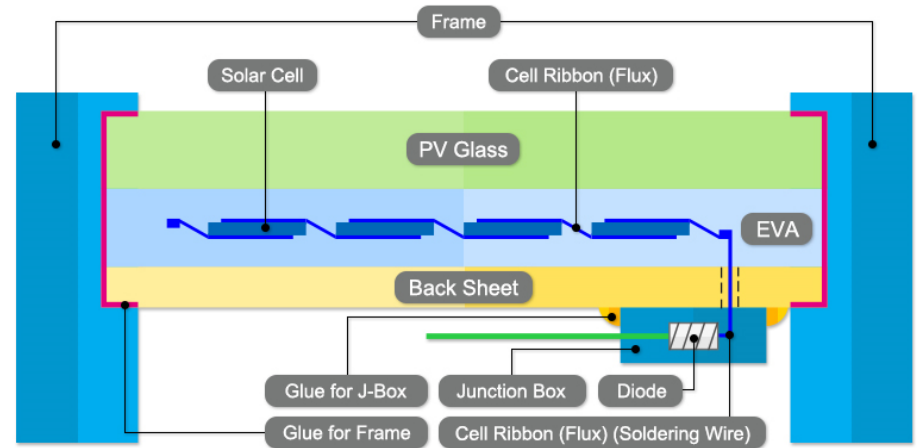
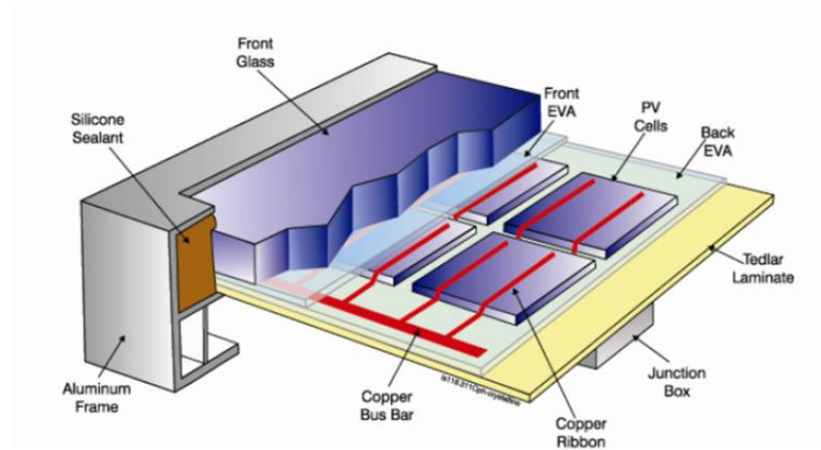
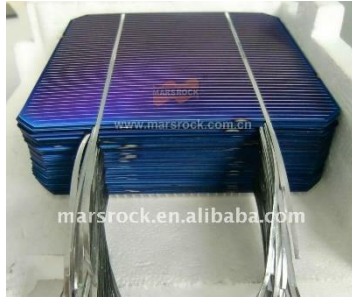
PE-BSF, PERC,  
PERL, HIT



Emitter Wrap through  
Metal Wrap through



# A module consists of many cells



# Outline

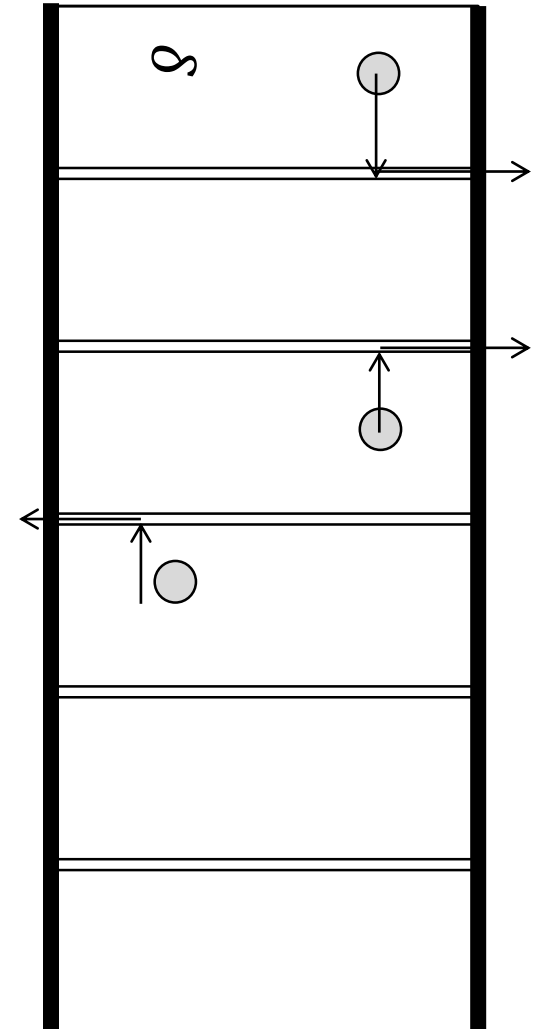
- 1) Three types of c-Si gridding
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- 3) Physics of bifacial cell design
- 4) Normal grid vs. percolation grid
- 5) Conclusion

# What about c-Si?

$$\frac{N_{opt,1}}{N_{opt,2}} = \left( \frac{J_{0,1}/\eta_1}{J_{0,2}/\eta_2} \right)^{\frac{2}{3}} = \left( \frac{W_2}{W_1} \right)$$

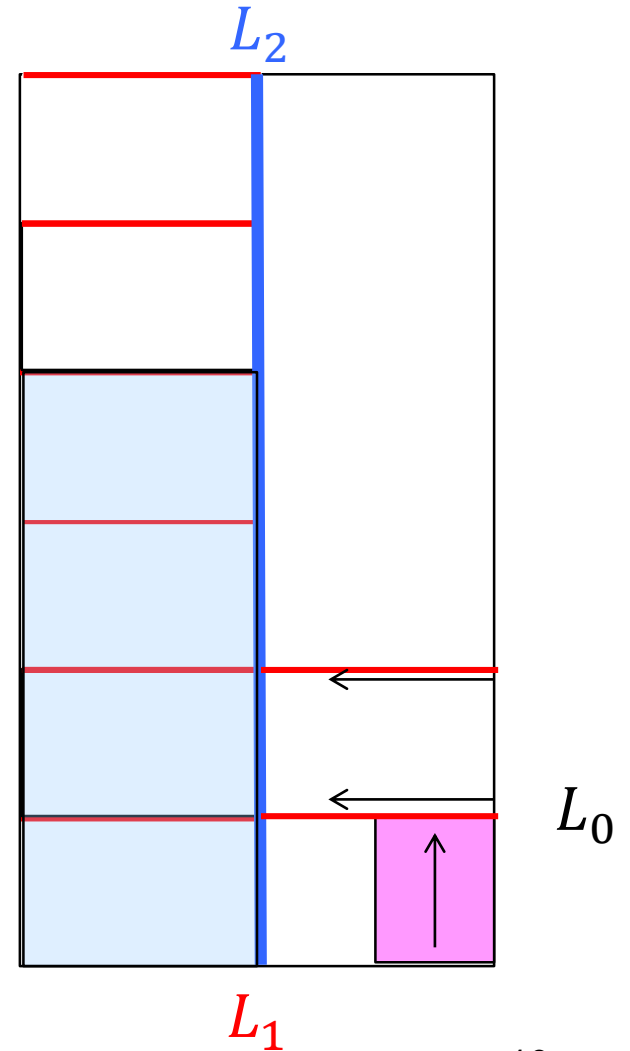
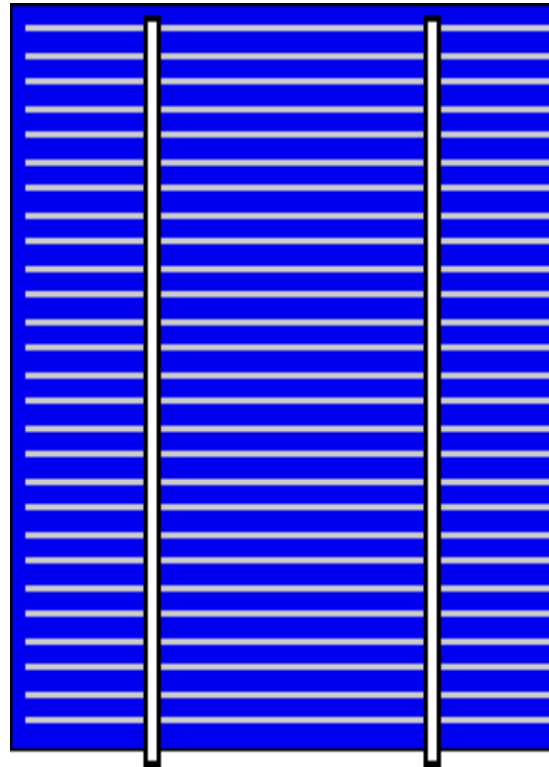
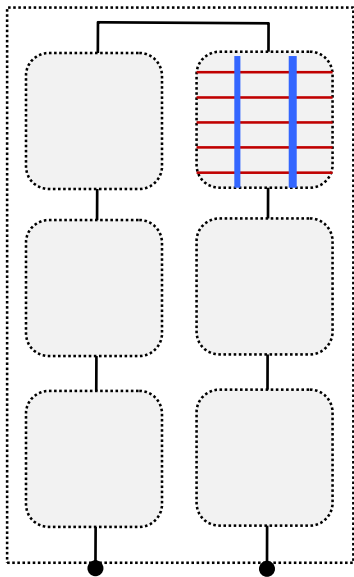
$$W^{c-Si} = W^{\alpha-Si} \left( \frac{J_0^{\alpha-Si}/\eta_1}{J_0^{c-Si}/\eta_2} \right)$$
$$\sim \left( \frac{16}{40} \right)^{\frac{2}{3}} \sim 0.52 \text{ cm}$$

Scribing through 200  $\mu\text{m}$  Si is difficult.

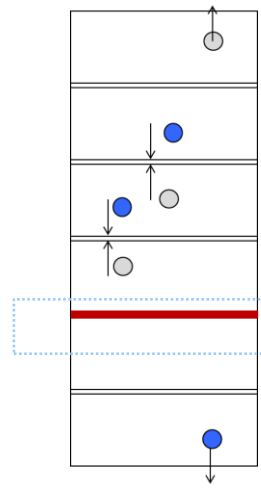




# Power dissipation in hierarchical grids



# Thin film solar cells: the case for rectangular cells



$$P_1 = \int_0^{L_1} dx \frac{\rho_1}{a_1 h_1} I^2(x)$$

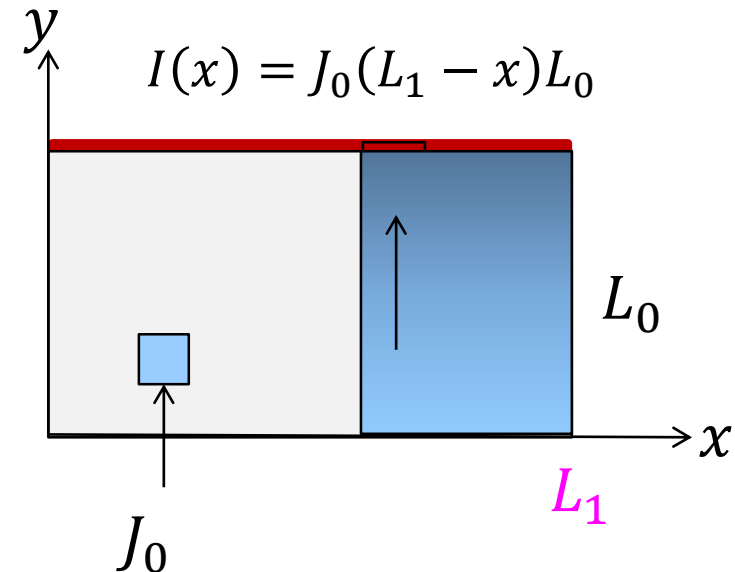
← cross-section

$$P_1 = \int_0^{L_1} dx \frac{\rho_1}{a_1 h_1} J_0^2 (L_1 - x)^2 L_0^2$$

← Shape factor

$$P_1 = \frac{1}{3} \frac{\rho_1 L_1}{a_1 h_1} J_0^2 L_1^2 L_0^2 = \frac{1}{3} R_{s,1} J_0^2 A_1^2$$

$$P_i = \frac{1}{3} \frac{\rho_i L_i}{a_i h_i} J_0^2 L_i^2 L_{i-1}^2 = \frac{1}{3} R_{s,i} J_0^2 A_i^2$$



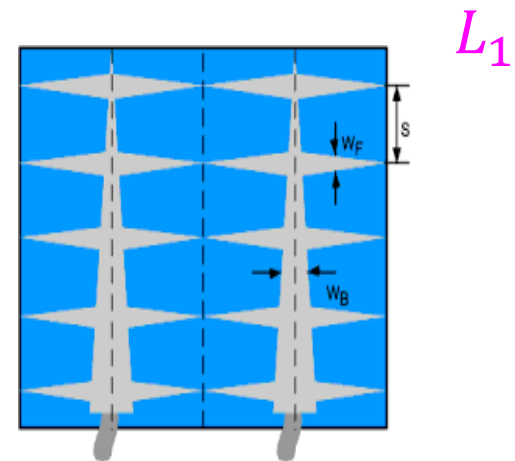
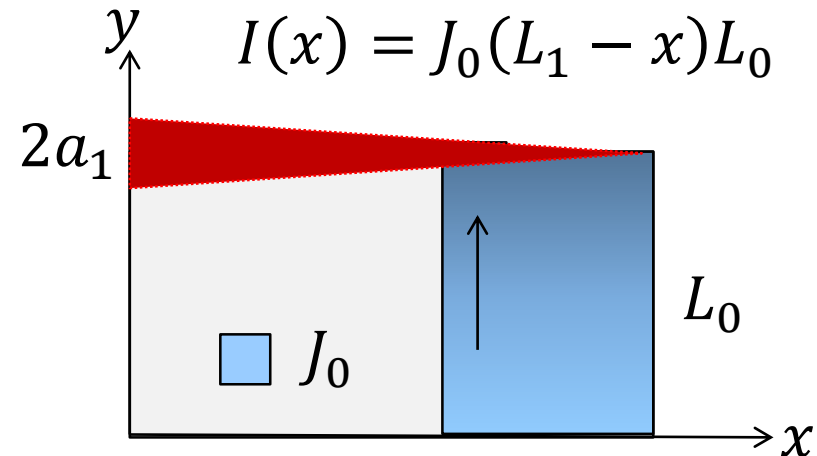
# Homework: Other wire shapes may reduce power dissipation further

$$P_1 = \int_0^{L_1} dx \frac{\rho_1}{\frac{2a_1(L_1 - x)}{L_1} h_1} I^2(x)$$

$$P_1 = \frac{1}{4} \frac{\rho_1 L_1}{a_1 h_1} J_0^2 L_1^2 L_0^2 = \frac{1}{4} R_{s,1} J_0^2 A_1^2$$

$$P_i = \frac{1}{4} \frac{\rho_i L_i}{a_i h_i} J_0^2 L_1^2 L_0^2$$

$$R_s = \int_0^{L_1} dx \frac{\rho_1}{\frac{2a_1(L_1 - x)}{L_1} h_1} \rightarrow \infty$$



# Hierarchical Design Rules

$$P_i = \frac{1}{3} \frac{\rho_i L_i}{a_i h_i} J_0^2 L_i^2 L_{i-1}^2 = \frac{1}{3} R_{s,i} J_0^2 A_i^2$$

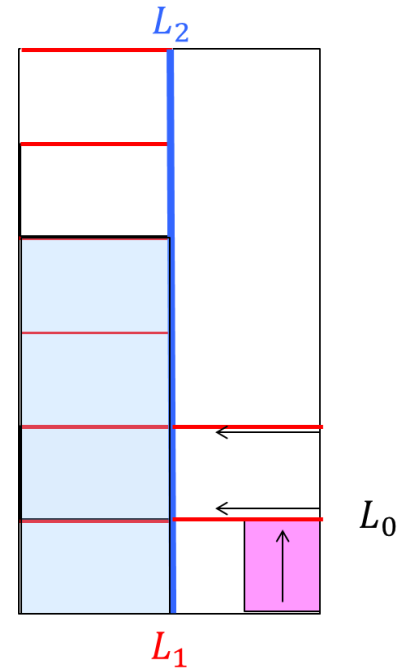
Constant dissipation

$$P_{i+1} = N_i P_i = \frac{L_{i+1}}{L_i} P_i$$

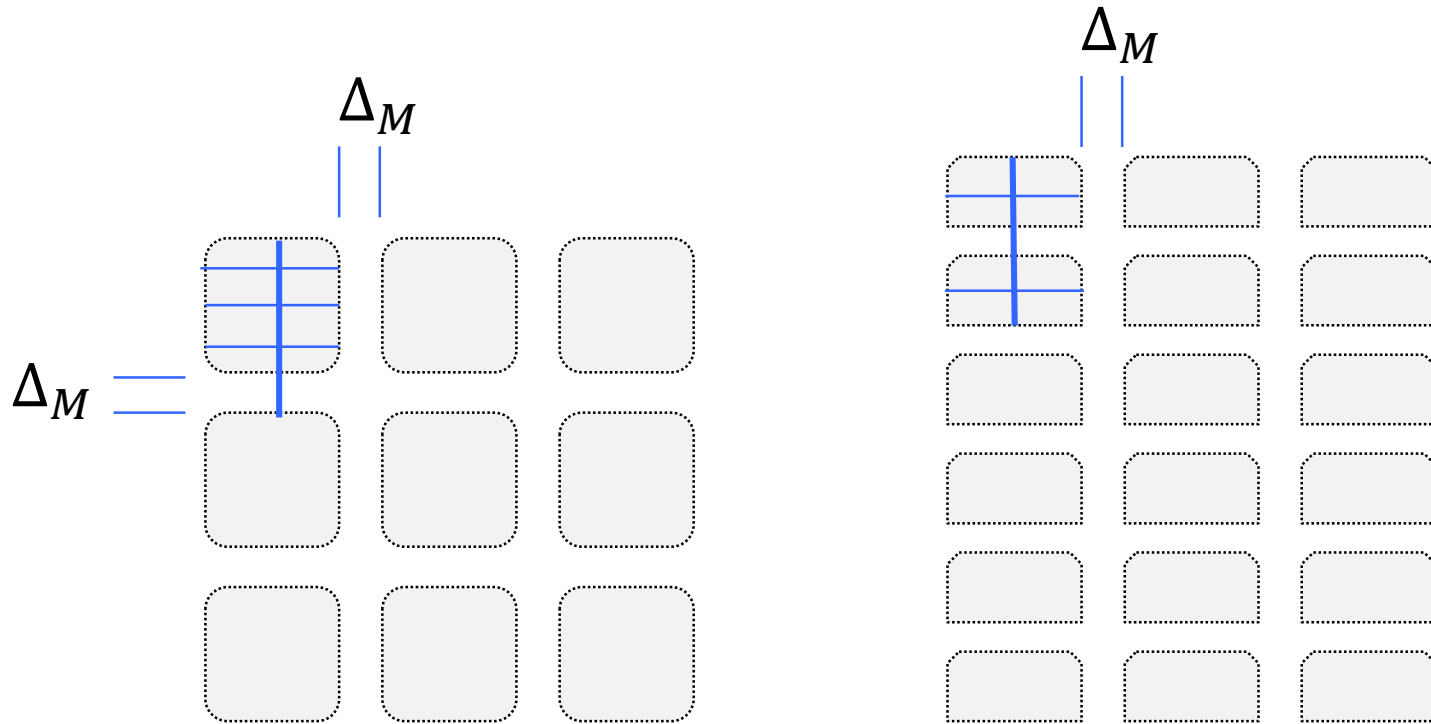
$$\frac{L_{i+1}}{L_i} \times \frac{1}{3} \frac{\rho_i L_i}{a_i h_i} J_0^2 L_i^2 L_{i-1}^2 = \frac{1}{3} \frac{\rho_{i+1} L_{i+1}}{a_{i+1} h_{i+1}} J_0^2 L_{i+1}^2 L_i^2$$

$$\frac{a_{i+1}}{a_i} = \left( \frac{L_{i+1}}{L_{i-1}} \right)^2$$

$$\sum_i^n a_i L_i = \text{const shading.}$$



# Physics of Half-Cells

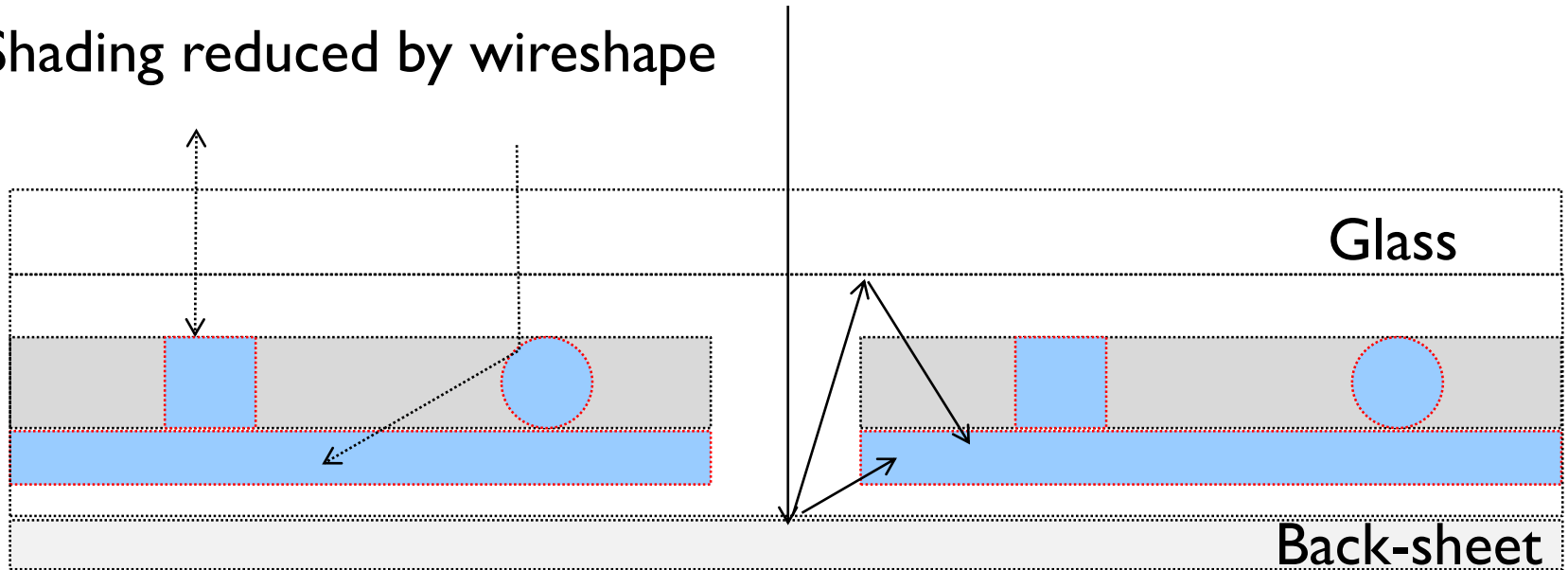


Mimicking thin-film PV

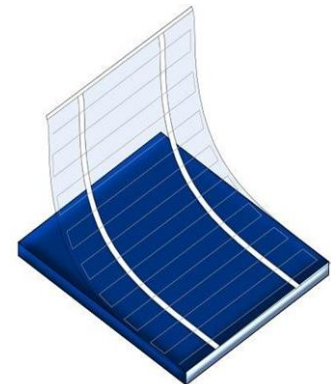
Excess resistance loss cut in half, but increased dead area.

# Not as bad as it seems?

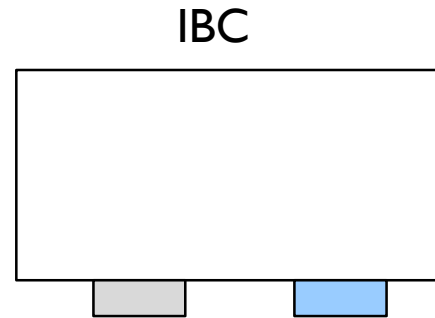
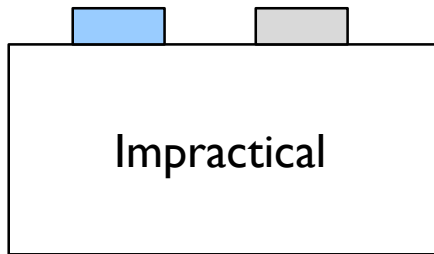
Shading reduced by wireshape



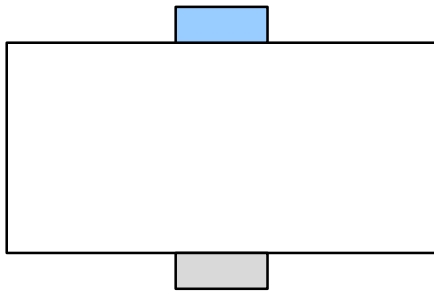
Internal reflection



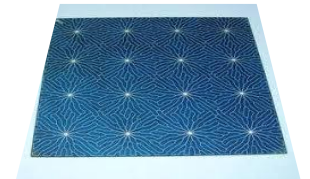
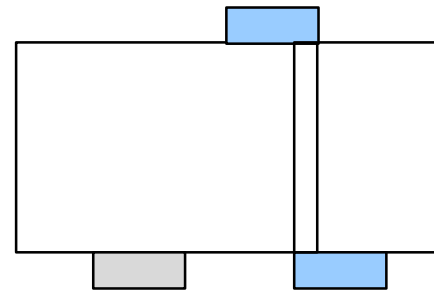
# Grid arrangement of c-Si



PE-BSF, PERC,  
PERL, HIT



Emitter Wrap through  
Metal Wrap through

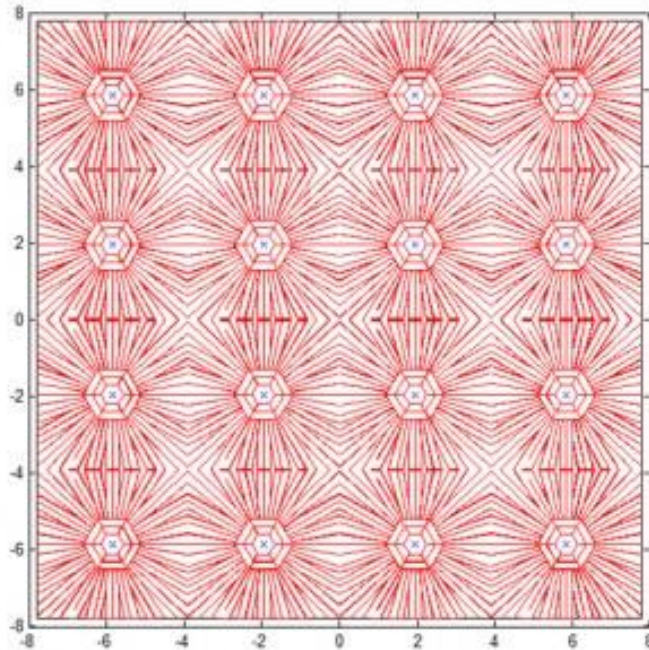


# Simulation Tools: Griddler

a)



Click on the part of the pattern you wish to create metal line breaks.



b)



### Grid Parameters

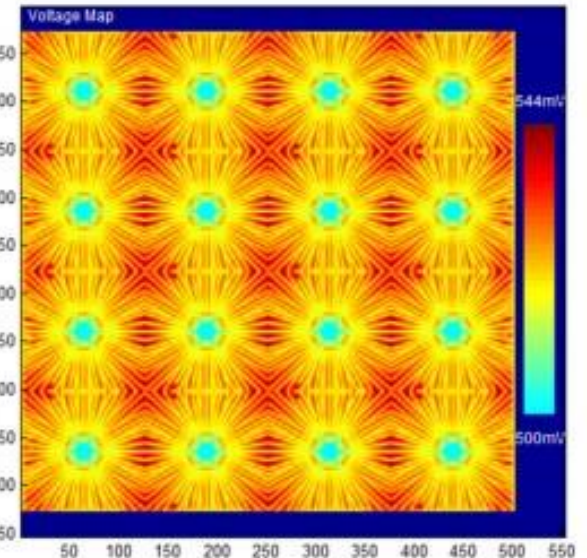
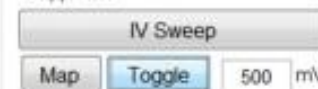
finger sheet res (mohm/sq)   
busbar sheet res (mohm/sq)   
finger contact res (mohm-cm2)   
emitter sheet res (ohm/sq)   
Trans length=Dum  
finger optical factor   
busbar optical factor

### Measurement Method

Extract current at eac.   
ribbon width (mm)   
ribbon line res (mohm/cm)

### IV Parameters

Voc  mV  
Jsc at non-shaded regions  mA/cm2  
Vmpp= mV

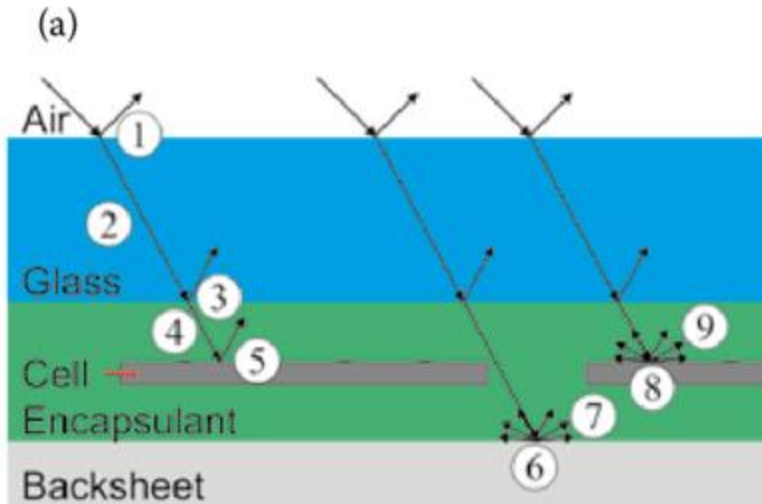


Simulation is not an issue; the question is what to simulate?

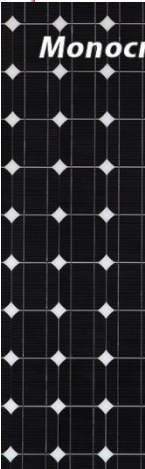
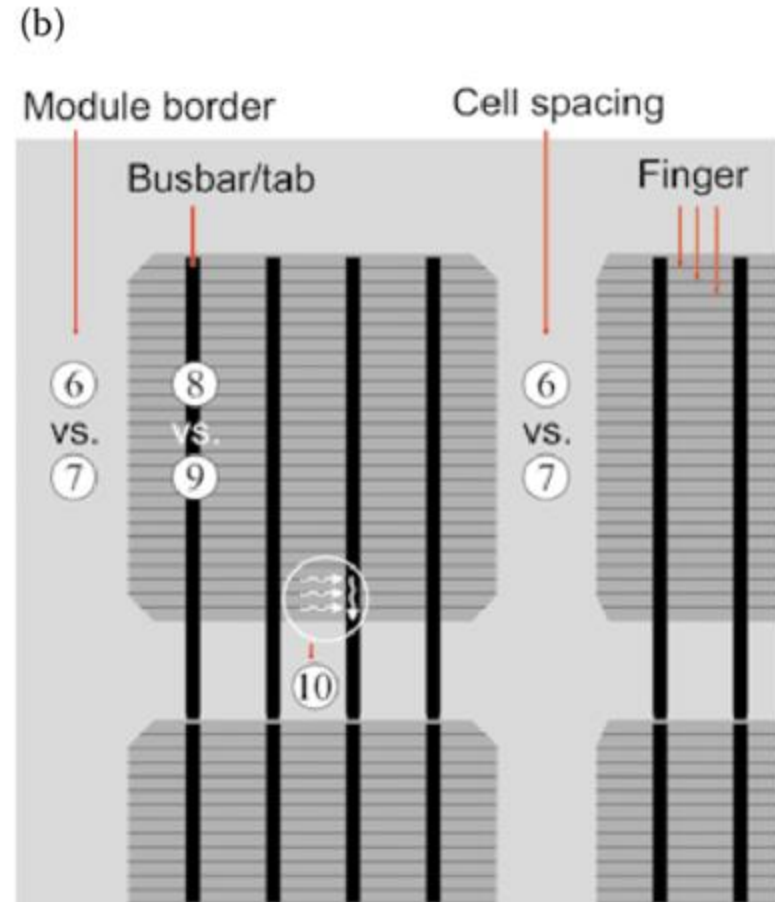
M. A. Alam, PV Lecture Notes



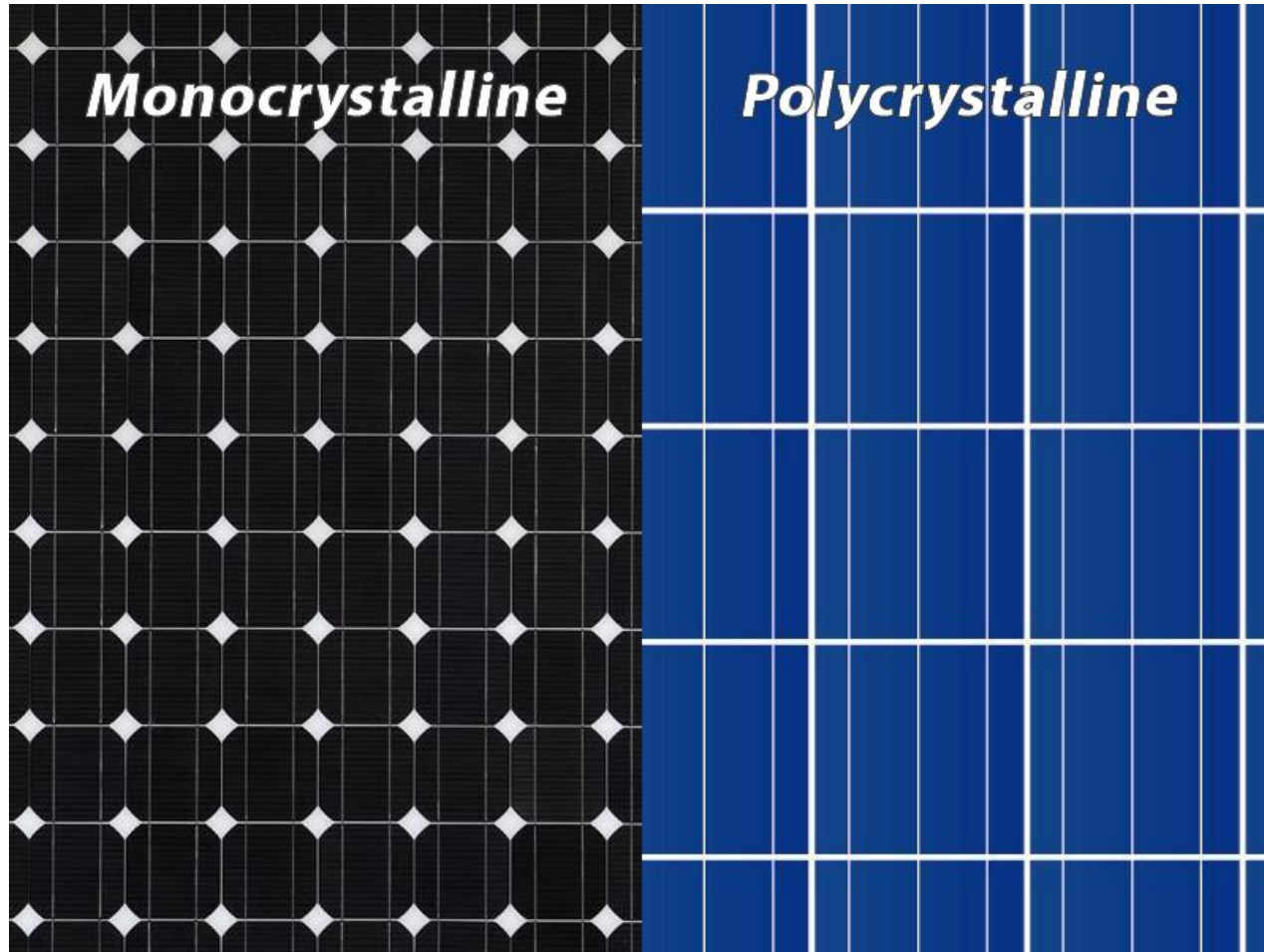
# Module optical design



- 1 Reflection loss air/glass
- 2 Absorption loss glass
- 3 Reflection loss glass/encap.
- 4 Absorption loss encap.
- 5 Coupling gain encap./cell
- 6 Loss on module border and cell spacing
- 7 Redirection gain from inactive areas
- 8 Shading loss of ribbon
- 9 Light redirection gain from ribbon
- 10 Ohmic losses in the interconnection



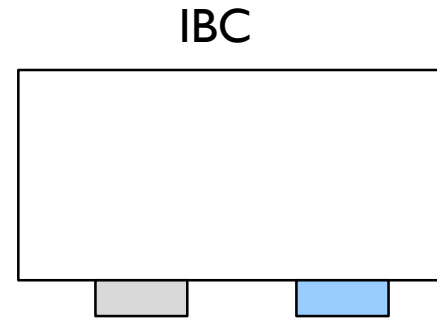
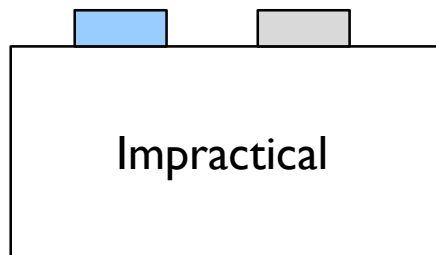
# Optical design: Dead area loss



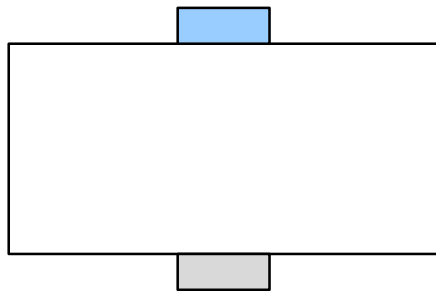
# Outline

- 1) Three types of c-Si gridding
- 2) Physics of standard c-Si cell gridding
- 3) Physics of bifacial cell design
- 4) Normal grid vs. percolation grid
- 5) Conclusion

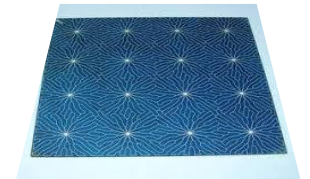
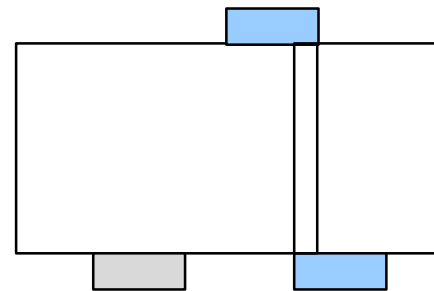
# Grid arrangement of c-Si



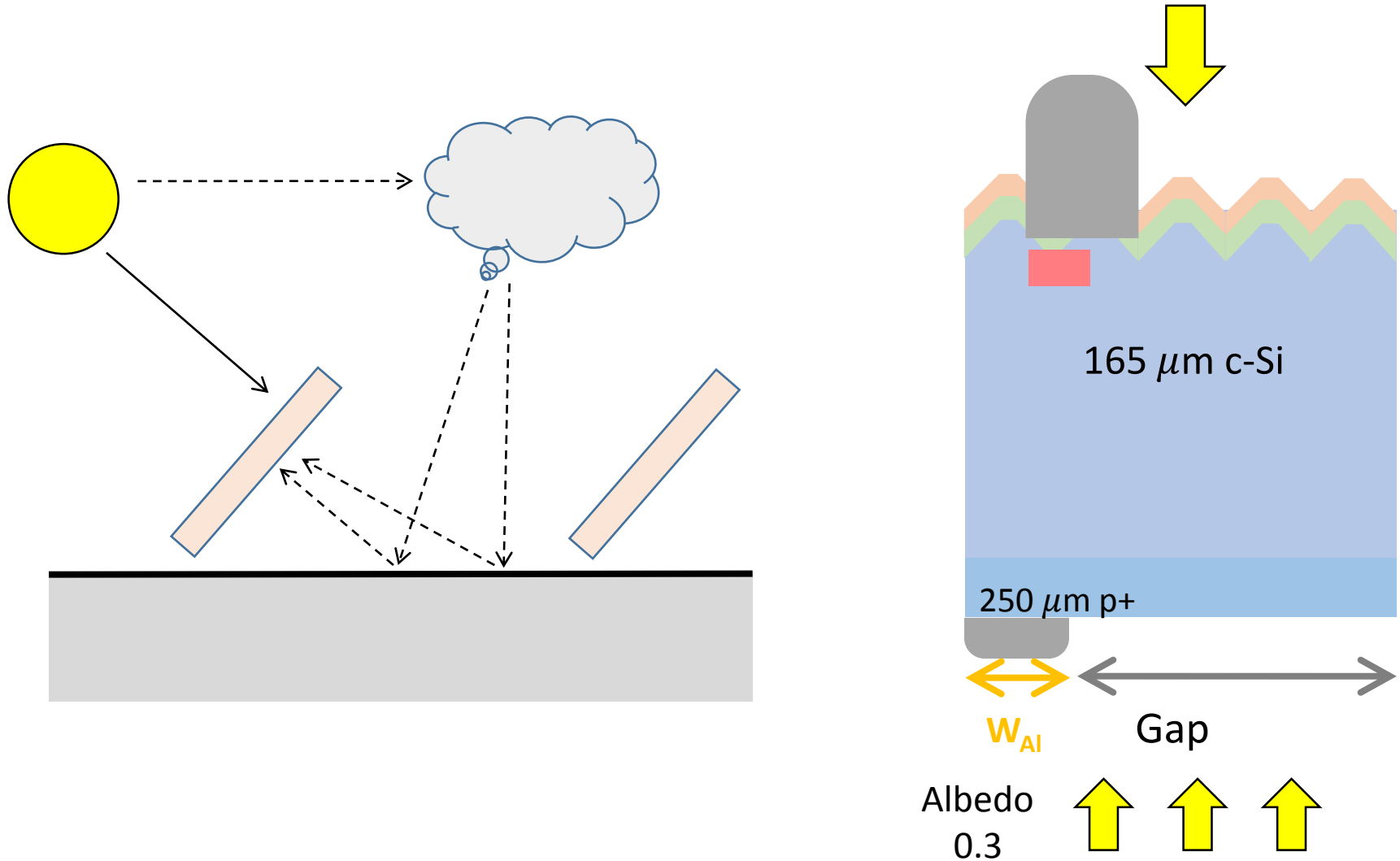
PE-BSF, PERC,  
PERL, HIT



Emitter Wrap through  
Metal Wrap through



# Theory of bifacial grid



## Recall: monofacial solar cells

$$\begin{aligned} P_j &= P_o \times N = (J_0^2 \rho) \times \frac{(n+1)^3}{3(3n+1)} \times \left(\frac{A^3}{L^2}\right) \times N \\ &= (J_0^2 \rho) \times \frac{(n+1)^3}{3(3n+1)} \times \left(\frac{A_T}{N}\right)^3 (N/L^2) = c_1/N^2 \end{aligned}$$

$$P_{scribe} = (N-1)\delta \times LP_{ideal}/A_T \sim c_2 N$$

$$P_{ideal} = \left(\frac{I}{N}\right) \times (V \times N) = c_0$$

## Recall: Optimum number of monofacial cells

$$P_j = c_1/N^2 \quad P_{ideal} = C_0 \quad P_{scribe} \sim C_2N$$

$$\begin{aligned} P_{out} &= P_{ideal} - P_j - P_{scribe} \\ &= C_0 - C_1/N^2 - C_2N \end{aligned}$$

$$N_{opt} = (2C_1/C_2)^{\frac{1}{3}}$$

# Homework: Theory of bifacial grid

Joule      Shadow

$$P_{out} = P_0(1 + R) - P_{j,R} - P_{s,R} - P_{j,F} - P_{s,F}$$

$$= C_0 - C_{1,R}/N_R^2 - C_{2,R}N_R - C_{1,F}/N_F^2 - C_{2,F}N_F$$

$$C_{1,F} = (J_0^2 \rho_F / 3) (A_T^3 / L^2)$$

$$C_{2,F} = P_0 \delta$$

$$C_{1,R} = (J_0^2 \rho_R / 3) (A_T^3 / L^2)$$

$$C_{2,R} = RP_0 \delta$$

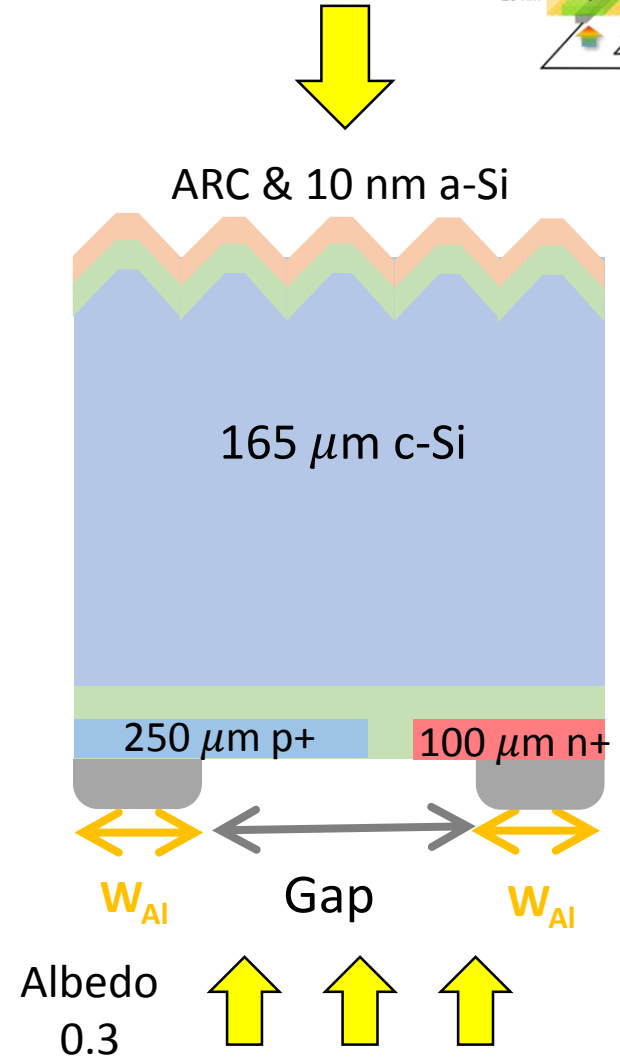
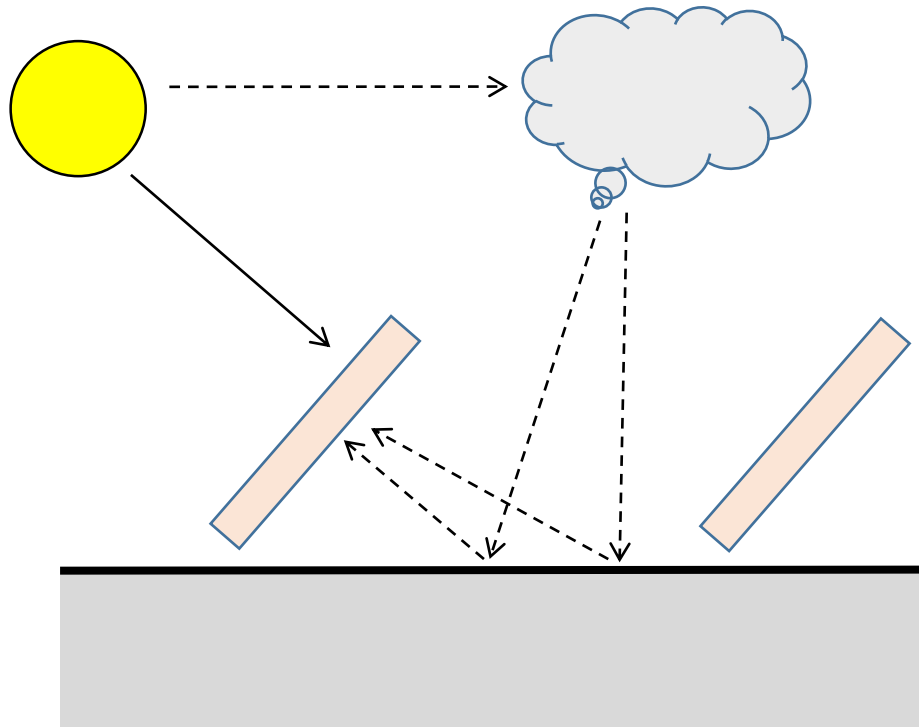
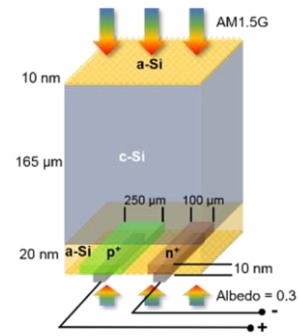
$$\frac{dP_{out}}{dN_F} = 0 \quad N_F = \left( \frac{2C_{1,F}}{P_0} \right)^{\frac{1}{3}}$$

$$\frac{dP_{out}}{dN_B} = 0 \quad N_R = \left( \frac{2C_{1,R}}{RP_0} \right)^{\frac{1}{3}}$$

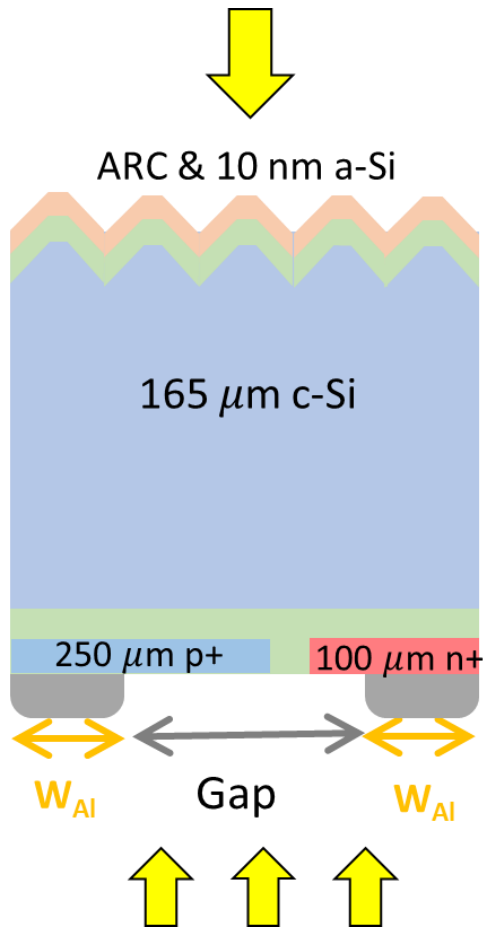
$$\frac{N_F}{N_R} = \left( R \frac{\rho_T}{\rho_B} \right)^{\frac{1}{3}}$$



# Theory of IBC bifacial grid



# Shadow vs. resistance optimization



$$w \equiv W_g / W_p$$

$$P_{out}(w, \alpha) = P_{ideal}(\alpha) - P_r(w, \alpha) - P_s(w, \alpha)$$

$$P_{ideal}(\alpha) = P_{ideal}(1 + \alpha)$$

$$P_s(w, \alpha) = P_{ideal}(1 - w)\alpha$$

$$P_r(w, \alpha) = kJ_0^2(1 + \alpha w)^2 \left( \frac{\rho}{(1 - w)t_{Al}} \right)$$

$$W_{Al} = W_p - W_g \equiv W_p(1 - w)$$

# Optimum gap and maximum power

$$P_{out}(w, \alpha) = P_{ideal}(\alpha) - P_r(w, \alpha) - P_s(w, \alpha)$$

$$dP_{out}/dw = 0$$

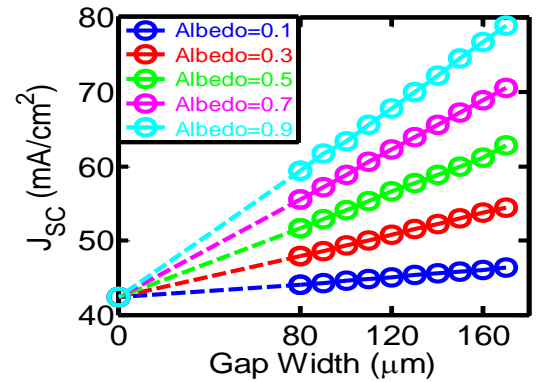
Optimum gap:

$$w_{opt} = 1 - \frac{1 + \alpha}{\sqrt{\alpha(\alpha + c)}}$$

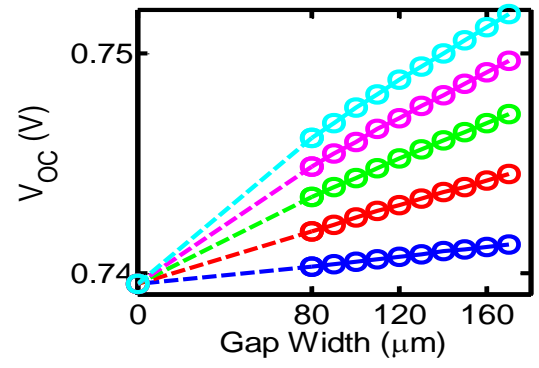
Maximum power:

$$P_{out} = (1 + \alpha) \left( 1 - 2\sqrt{\frac{\alpha}{c}} \right)$$

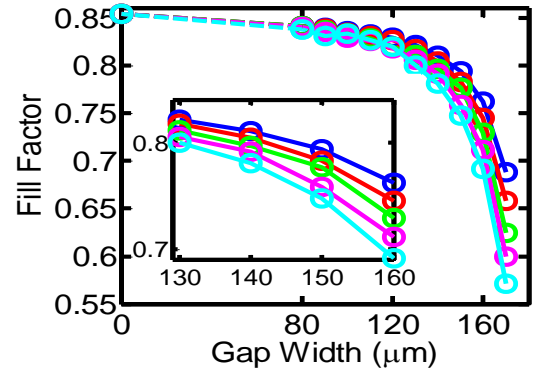
$$c^{-1} \equiv J_0^2 \left( \frac{L_{Al}^2 \rho}{2t_{Al}} + \rho_c \right) / P_0$$



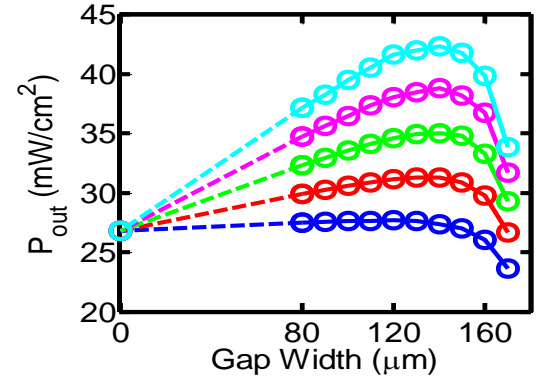
(a)



(b)



(c)



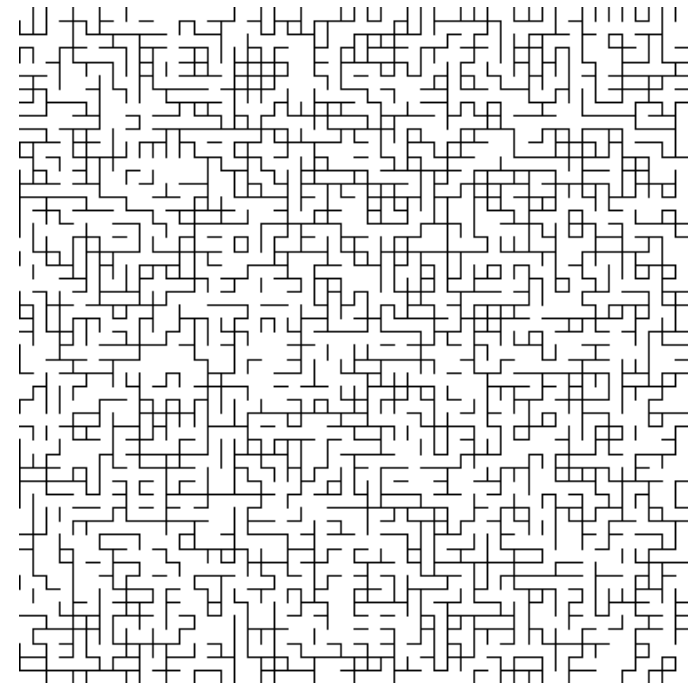
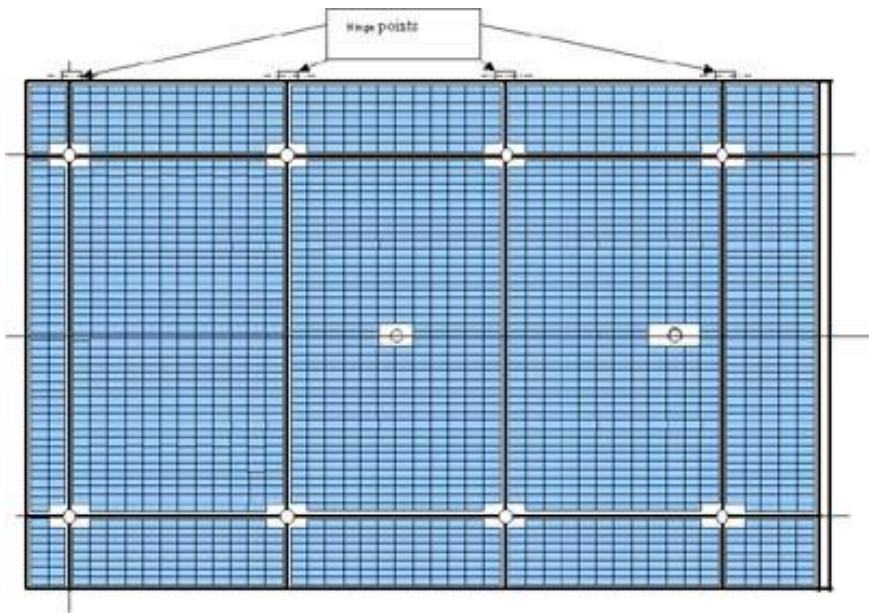
(d)

# Outline

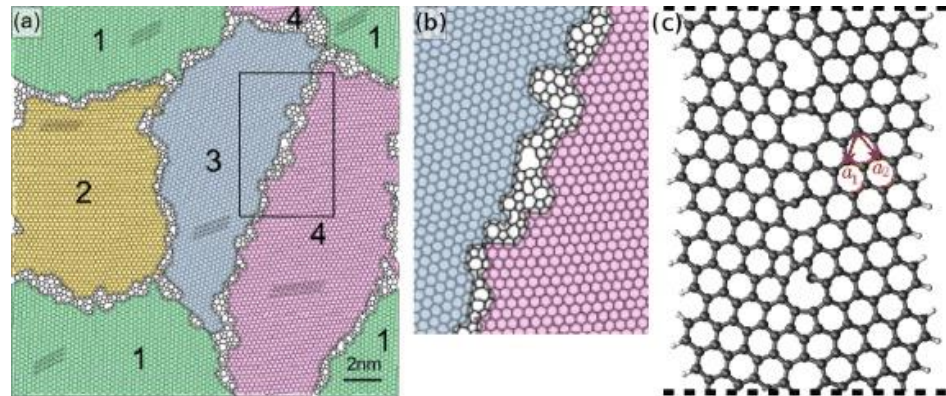
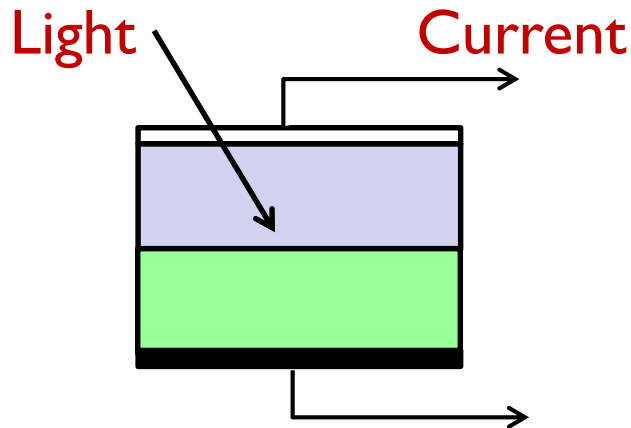
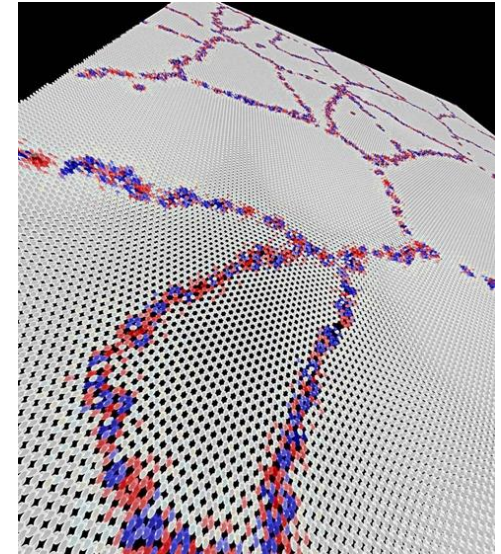
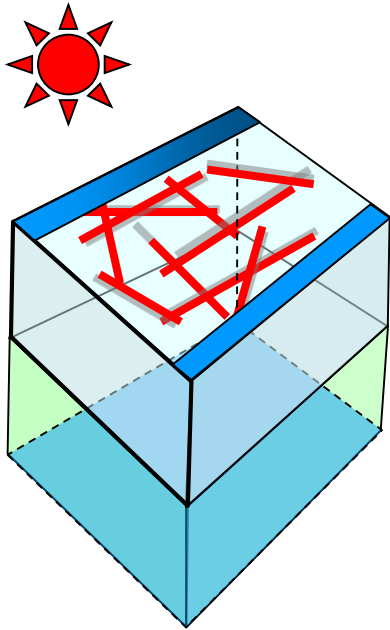
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# Ordered vs. Percolating systems

## Robustness against Cracks

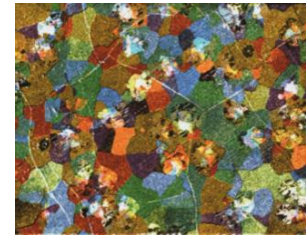


# Conductivity vs. Transparency

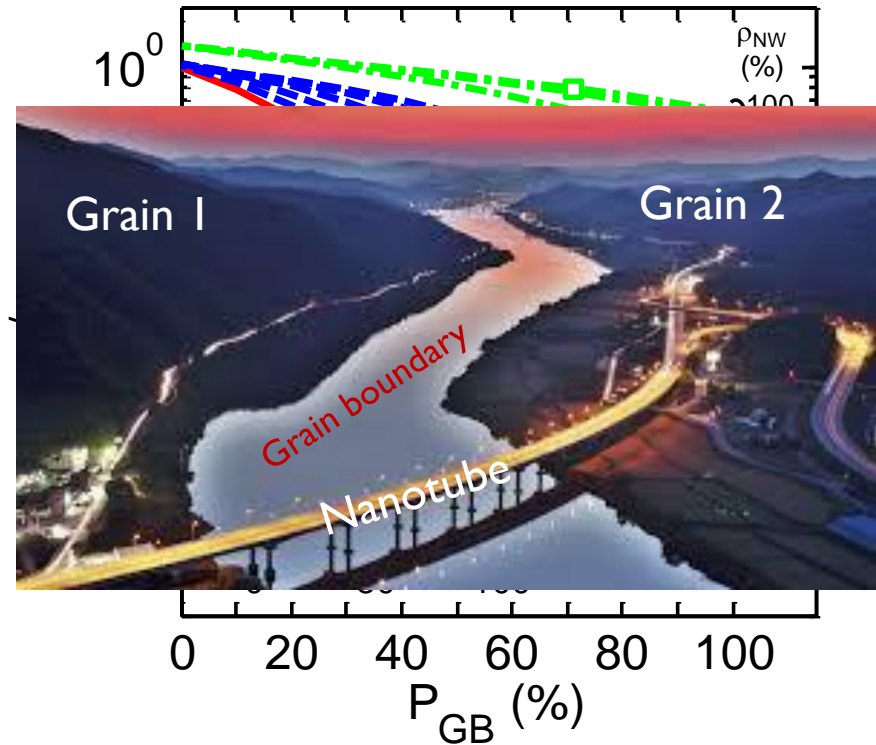
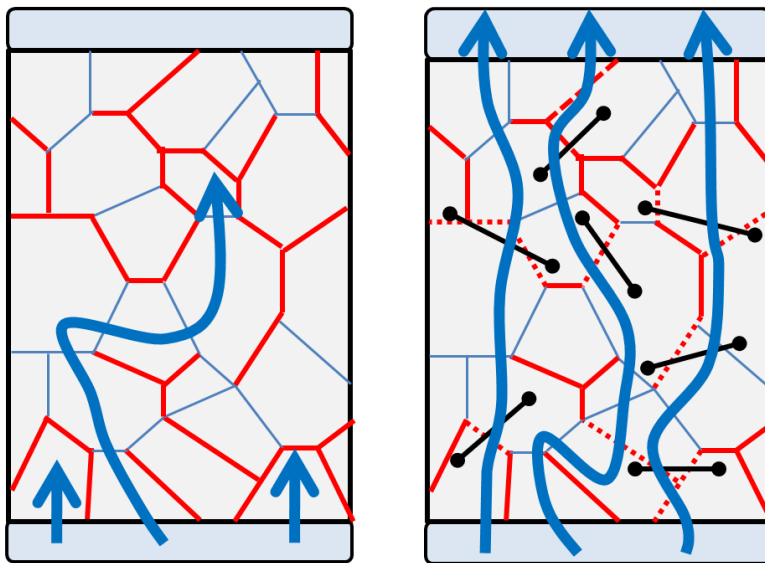




# 'Positive' Percolation Doping



C. Jeong Nano Letters, 2011.

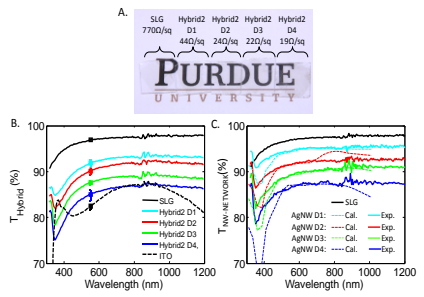
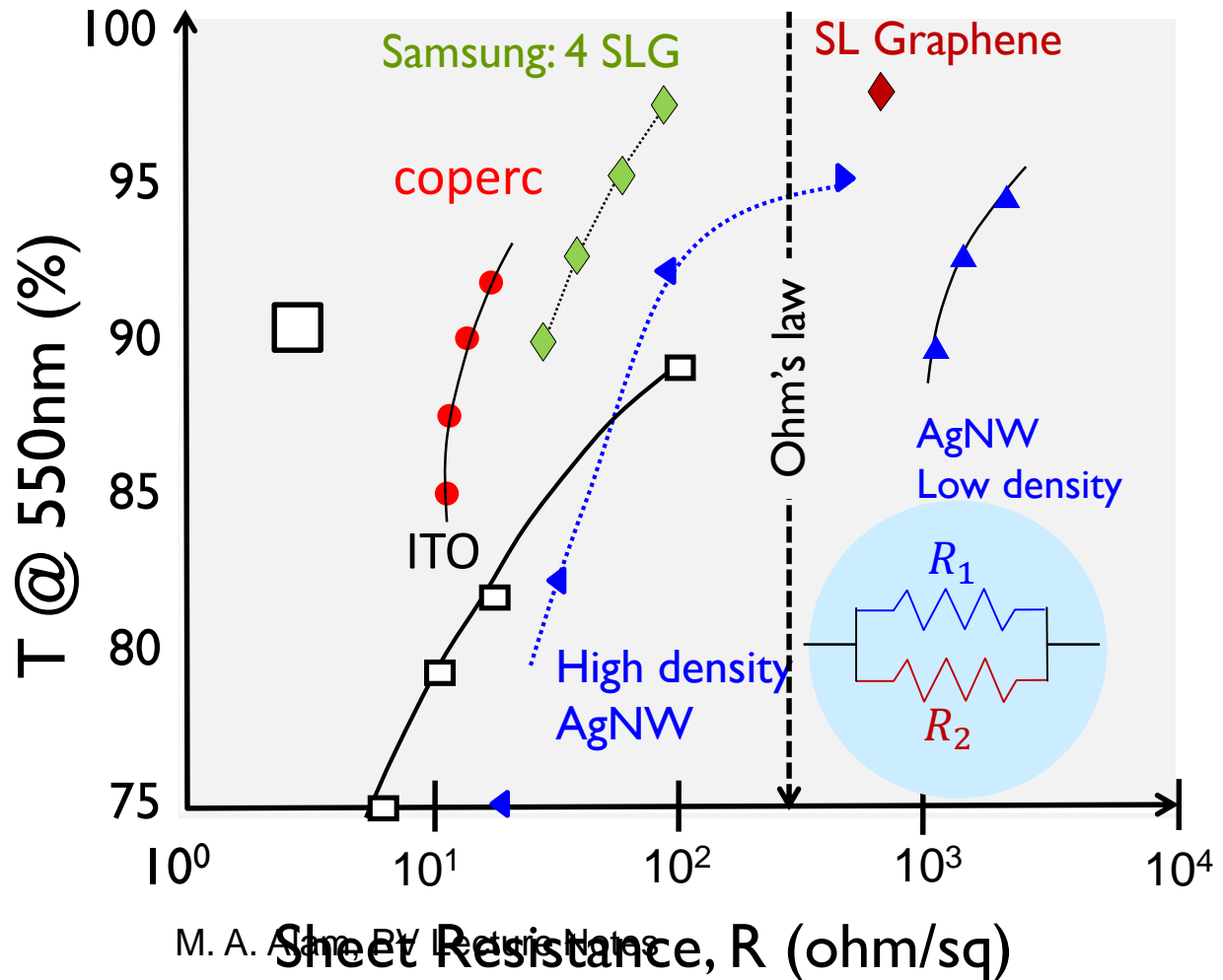
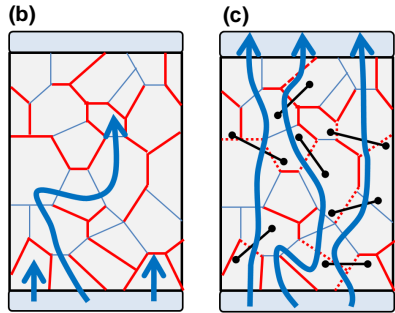


$$G = \frac{\sigma \times W}{L}$$

Percolating doping manipulates transport channels

# World record performance!

~10 ohms/sq at 90% transmission



M. A. Alam, et al., Nature Photonics



# Conclusions

- ➔ Series resistance plays a deeply important role in the design of solar modules.
- ➔ c-Si PV has additional series resistance compared to thin-film solar cell. Hierarchical gridding keeps the “excess resistance” in c-Si cell to a minimum. Modern simulation tools are helpful.
- ➔ .C-Si industry is adopting half-cell approach to mimic thin-film PV.
- ➔ Bifacial technologies require special grid design.

# Self-assessment

1. How does half-cell reduce series resistance loss. How does the strategy compare to that of thin-film solar cells.
2. For the same series resistance, c-Si solar cells will always have higher series resistance loss compared to thin-film solar cells. Explain.
3. What is the essential difference between nutrient flow in a leaf and that of current collection in a solar cell?
4. Mention a few key characteristics of the bifacial solar grids.
5. Emitter-wrap through, metal-wrap-through, smart-grid, and IBC cells all reduce the following loss mechanism of a crystalline solar cell.

# References

Back-surface field: <https://www.youtube.com/watch?v=i4jqmTR-rv4>

HIT cells: <https://www.youtube.com/watch?v=FfU9jxGnYzs>  
<https://www.youtube.com/watch?v=HaCAwTlc9QM>  
<https://www.youtube.com/watch?v=SLvMjSHoVfk>

PERC (PERL, HIT; PERT, PERF) Emitter-Wrap through  
<https://www.youtube.com/watch?v=fVhjVWwwOCI>

Optimal tilt (very shallow tilt)  
<https://www.youtube.com/watch?v=mb0l17XxQBY>

Tilt calculator <https://www.youtube.com/watch?v=MNSu9Rnlm9c>