

# Lecture 8: Connection to Traditional Model

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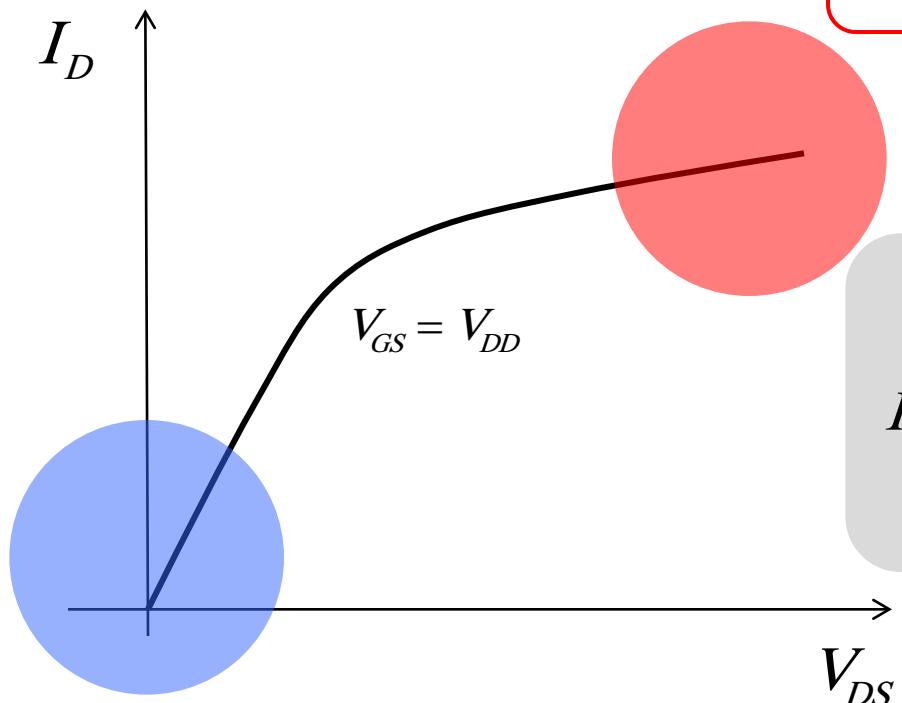
# ballistic MOSFET (MB)

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$$I_D = WQ_n(V_{GS}, V_{DS})\langle v(0) \rangle$$

$$\langle v(0) \rangle = \left( \frac{1 - e^{-qV_{DS}/k_B T_L}}{1 + e^{-qV_{DS}/k_B T_L}} \right) v_T = F_{SAT}(V_{DS}) v_T$$

# ballistic MOSFET (MB)



$$I_D = WQ_n(V_{GS}, V_{DS})v_T$$

$$I_D = WQ_n(V_{GS}, V_{DS})F_{SAT}(V_D)v_T$$

$$I_D = WQ_n(V_{GS}, V_{DS}) \frac{v_T}{2k_B T_L/q} V_{DS}$$

# VS model for the MOSFET

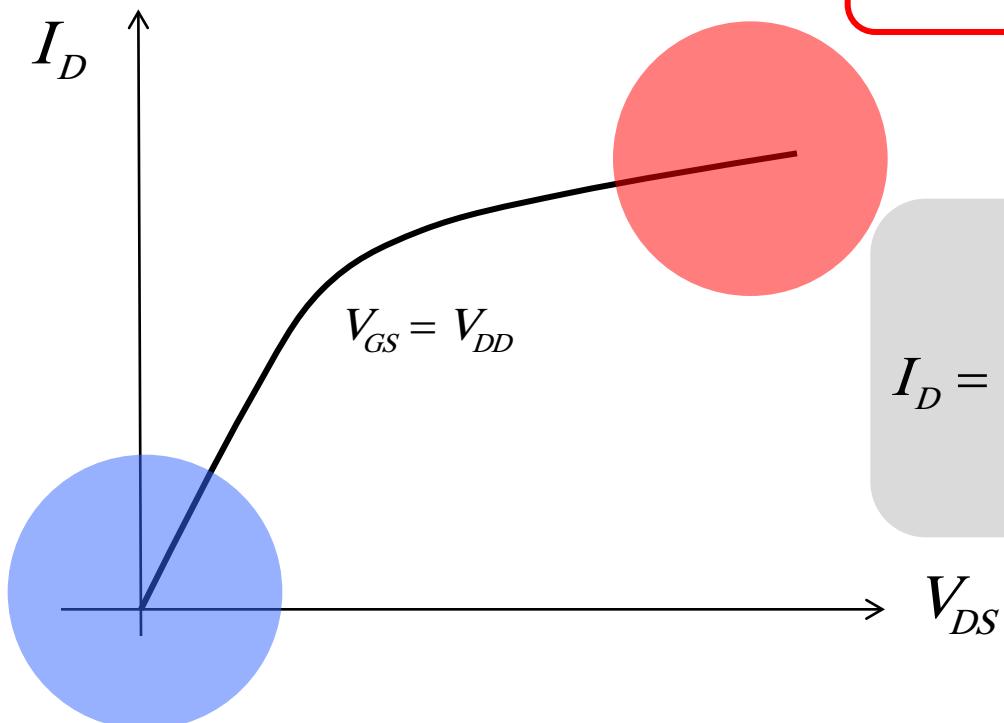
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$$I_D = WQ_n(V_{GS}, V_{DS})\langle v(0) \rangle$$

$$\langle v(0) \rangle = \left\{ \frac{V_D / V_{DSAT}}{\left[ 1 + (V_D / V_{DSAT})^\beta \right]^{1/\beta}} \right\} v_{SAT} = F_{SAT}(V_{DS}) v_{SAT}$$

$$V_{DSAT} = \frac{v_{SAT} L}{\mu_{eff}}$$

# VS model for the MOSFET

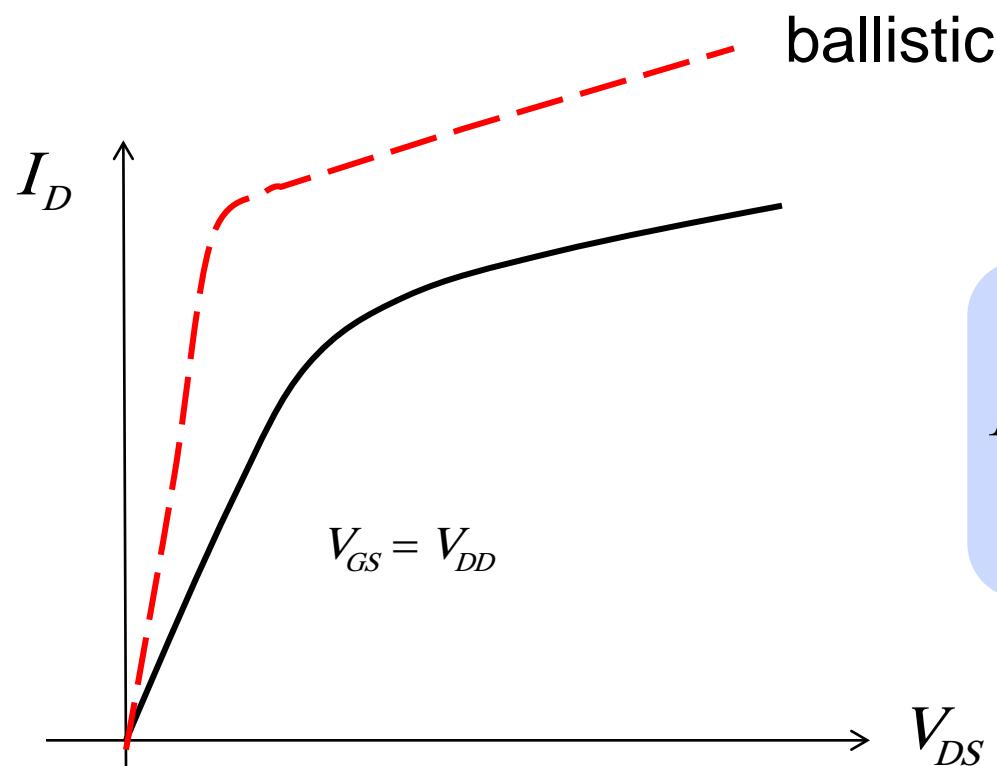


$$I_D = WC_{inv}v_{SAT}(V_{GS} - V_T)$$

$$I_D = WQ_n(V_{GS}, V_{DS})F_{SAT}(V_D)v_{SAT}$$

$$I_D = \frac{W}{L} \mu_{eff} C_{inv} (V_{GS} - V_T) V_{DS}$$

# VS model vs. ballistic



$$I_D = WQ_n(V_{GS}, V_{DS})F_{SAT}(V_D)v_{SAT}$$

# connecting the two: linear region

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## ballistic theory

$$I_D = WC_{inv} \frac{v_T}{2k_B T_L/q} (V_{GS} - V_T) V_{DS}$$

$$I_D = \frac{W}{L} C_{inv} \frac{v_T L}{2k_B T_L/q} (V_{GS} - V_T) V_{DS}$$

$$\mu_B \equiv \frac{v_T L}{2k_B T_L/q} \quad \text{"ballistic mobility"}$$

$$I_D = \frac{W}{L} C_{inv} \mu_B (V_{GS} - V_T) V_{DS}$$

## traditional theory

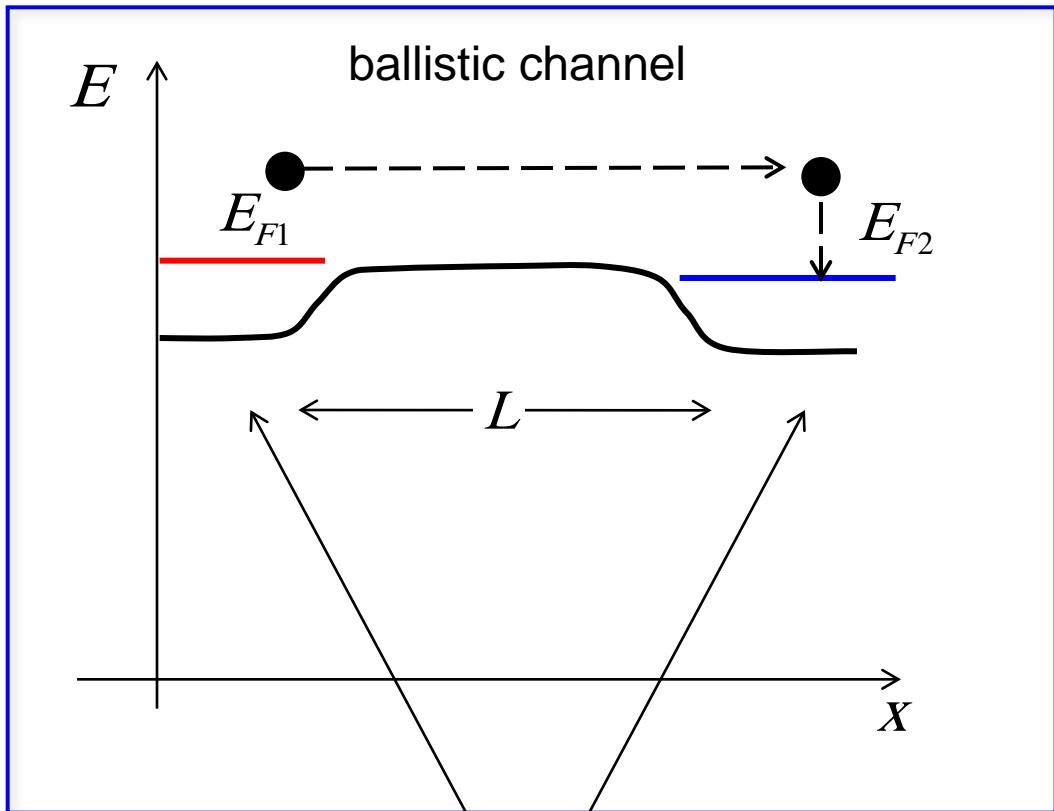
$$I_D = \frac{W}{L} C_{inv} \mu_{eff} (V_{GS} - V_T) V_{DS}$$

$$D_n = \frac{v_T \lambda_0}{2}$$

$$\mu_{eff} = \frac{D_n}{(k_B T_L/q)} \quad \mu_{eff} = \frac{v_T \lambda_0}{2k_B T_L/q}$$

$$\mu_n \rightarrow \mu_B$$

# ballistic mobility

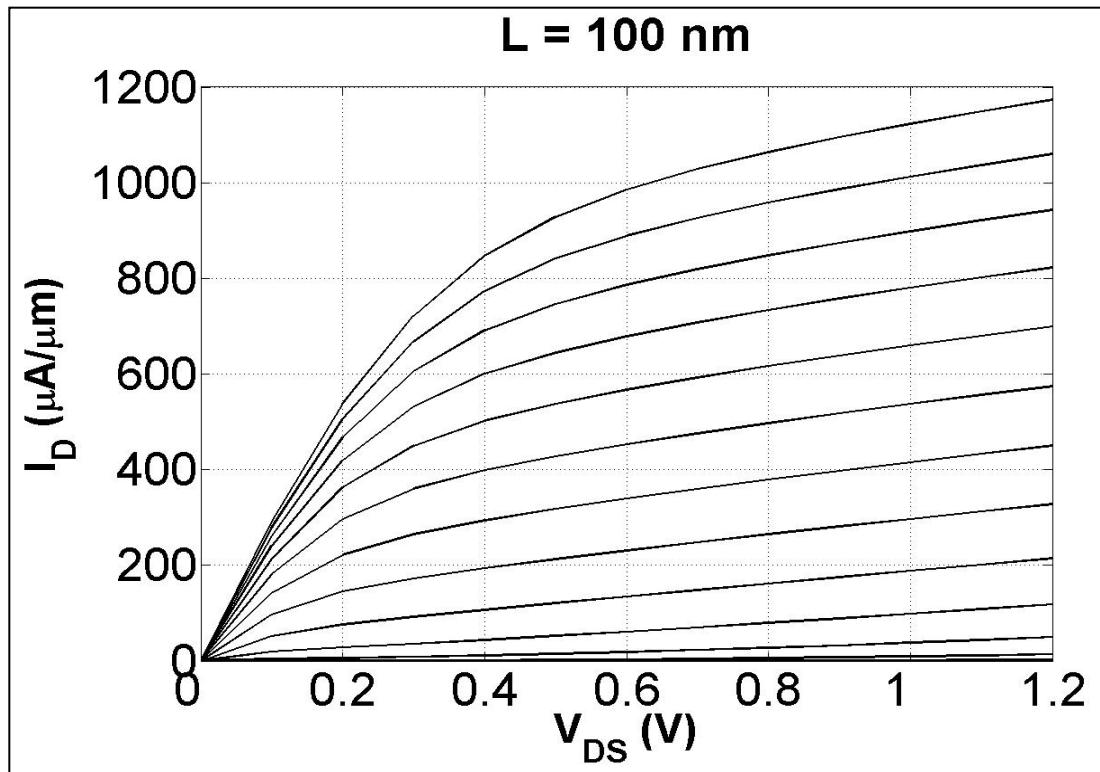


strong scattering in the S/D contacts

$$\mu_n = \frac{v_T \lambda_0}{2 k_B T_L / q}$$

$$\mu_B = \frac{v_T L}{2 k_B T_L / q}$$

# ballistic mobility



(Thanks to Shuji Ikeda of ATDF for supplying these devices in Dec. 2007)

$$\mu_{eff} \approx 250 \text{ cm}^2/\text{V-s}$$

$$\mu_B \approx 3200 \text{ cm}^2/\text{V-s}$$

$$\mu_B \gg \mu_{eff}$$

$$\mu_B = \frac{v_T L}{2 k_B T_L / q}$$

# connecting the two: saturation region

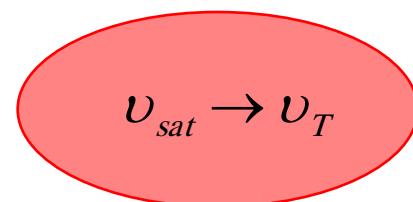
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ballistic theory

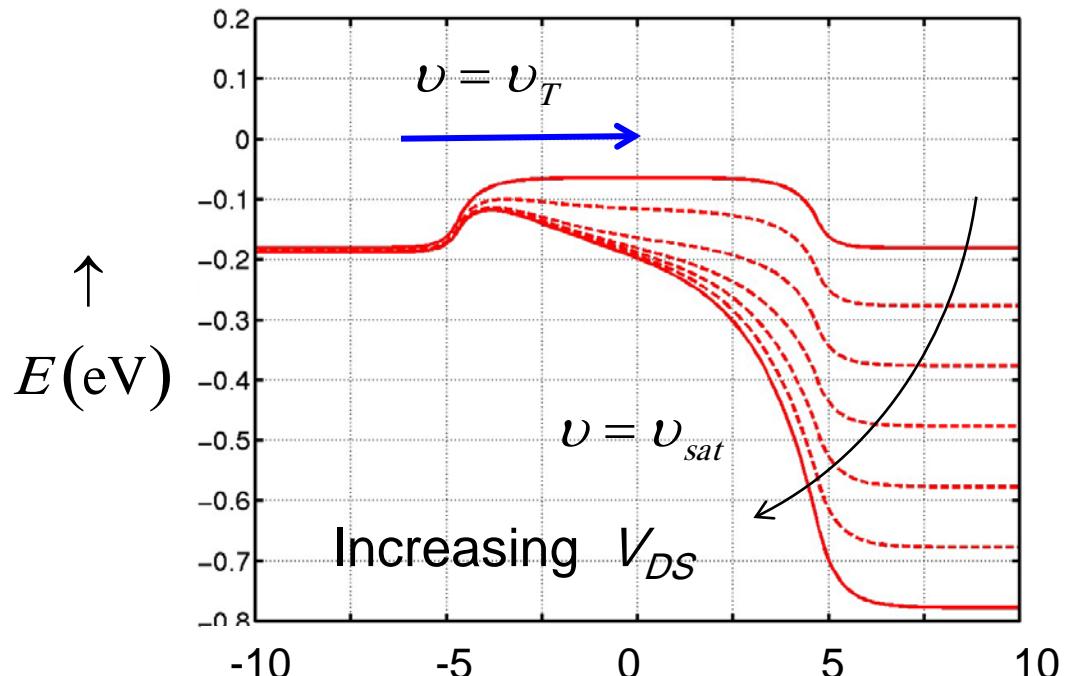
$$I_D = WC_{inv}v_T(V_{GS} - V_T)$$

traditional theory

$$I_{DS} = WC_{inv}v_{sat}(V_{GS} - V_T)$$



# injection vs. saturation velocity

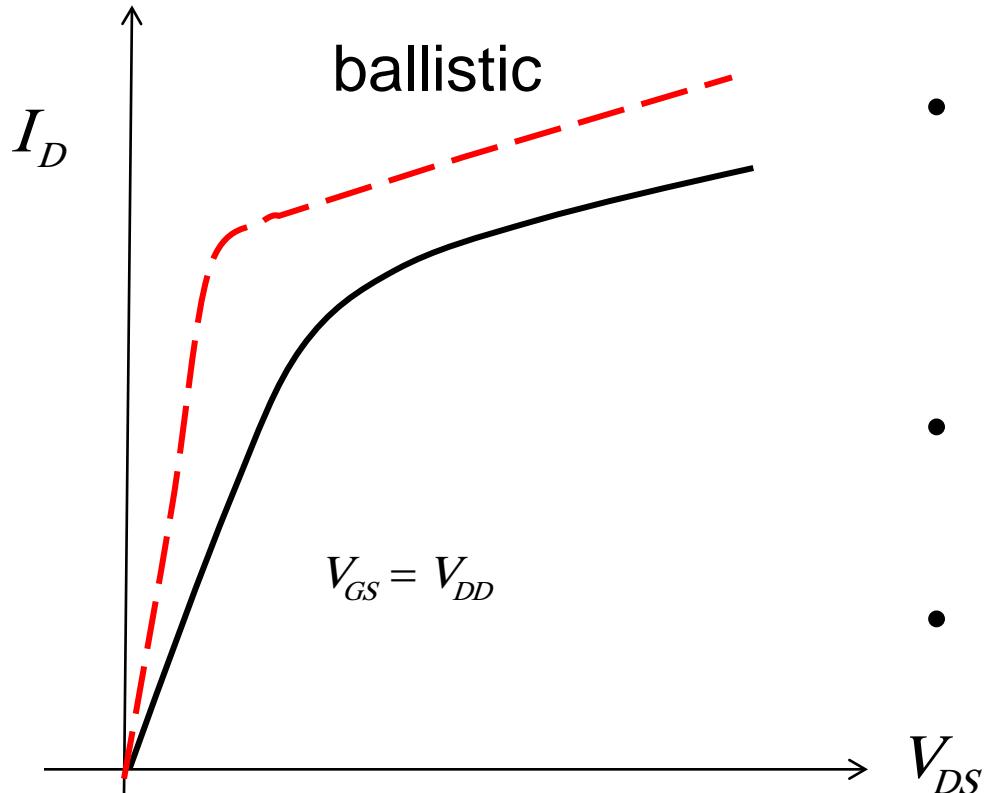


$v_{sat} \rightarrow v_T$

$x(\mu\text{m}) \rightarrow$

## wrap-up

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- Ballistic and DD MOSFET models give similar IV's because the current is controlled by modulating barriers.
- Ballistic currents are higher and...
- transition from linear to saturation is sharper.

## references

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The concept of ballistic mobility was introduced by Shur:

M.S. Shur, “Low ballistic mobility in submicron HEMTs,” *IEEE Electron Dev. Letters*, **9**, 511-513, 2002.