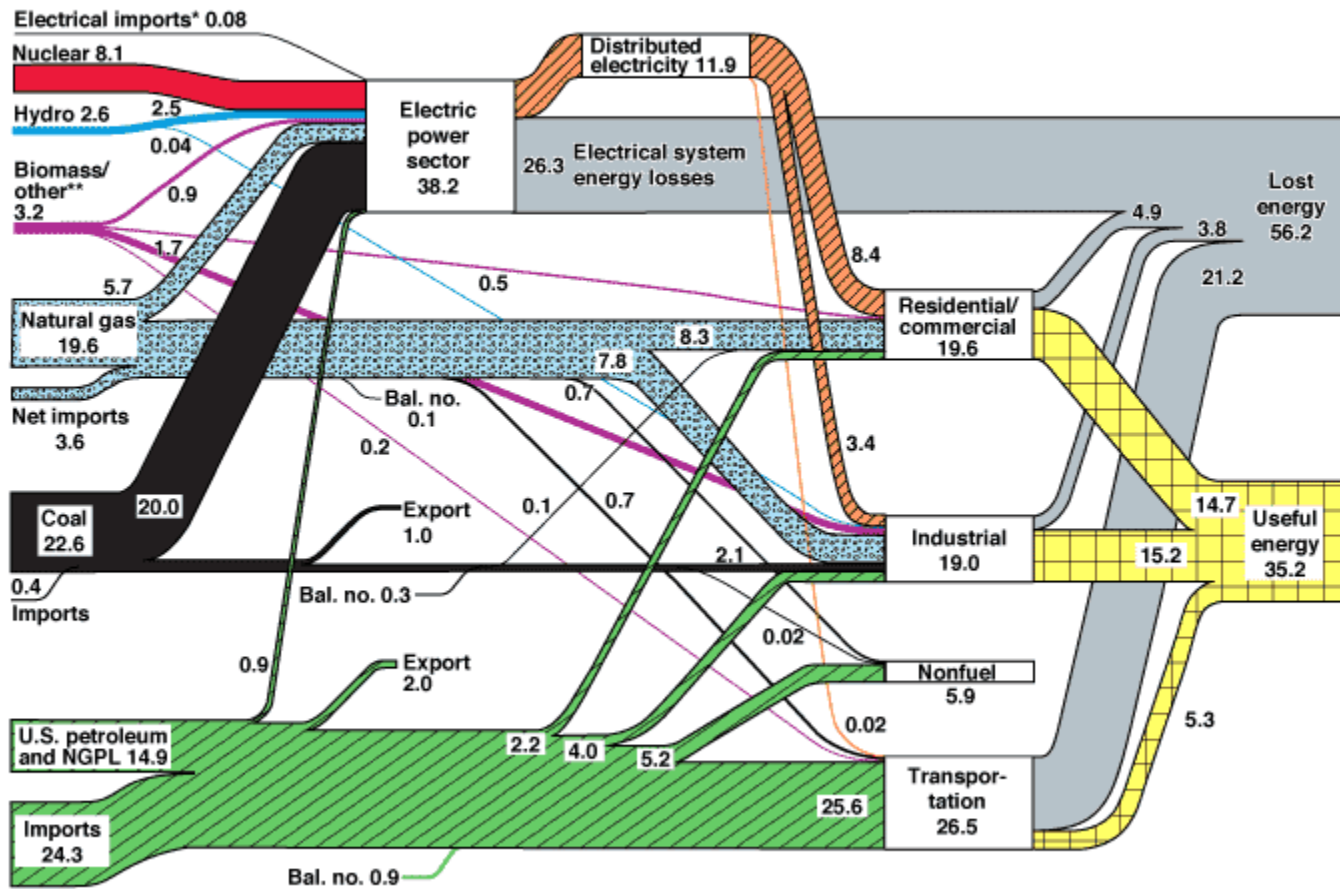




Importance of Heat

U.S. Energy Flow Trends – 2002 Net Primary Resource Consumption ~97 Quads



Source: Production and end-use data from Energy Information Administration, *Annual Energy Review 2002*.

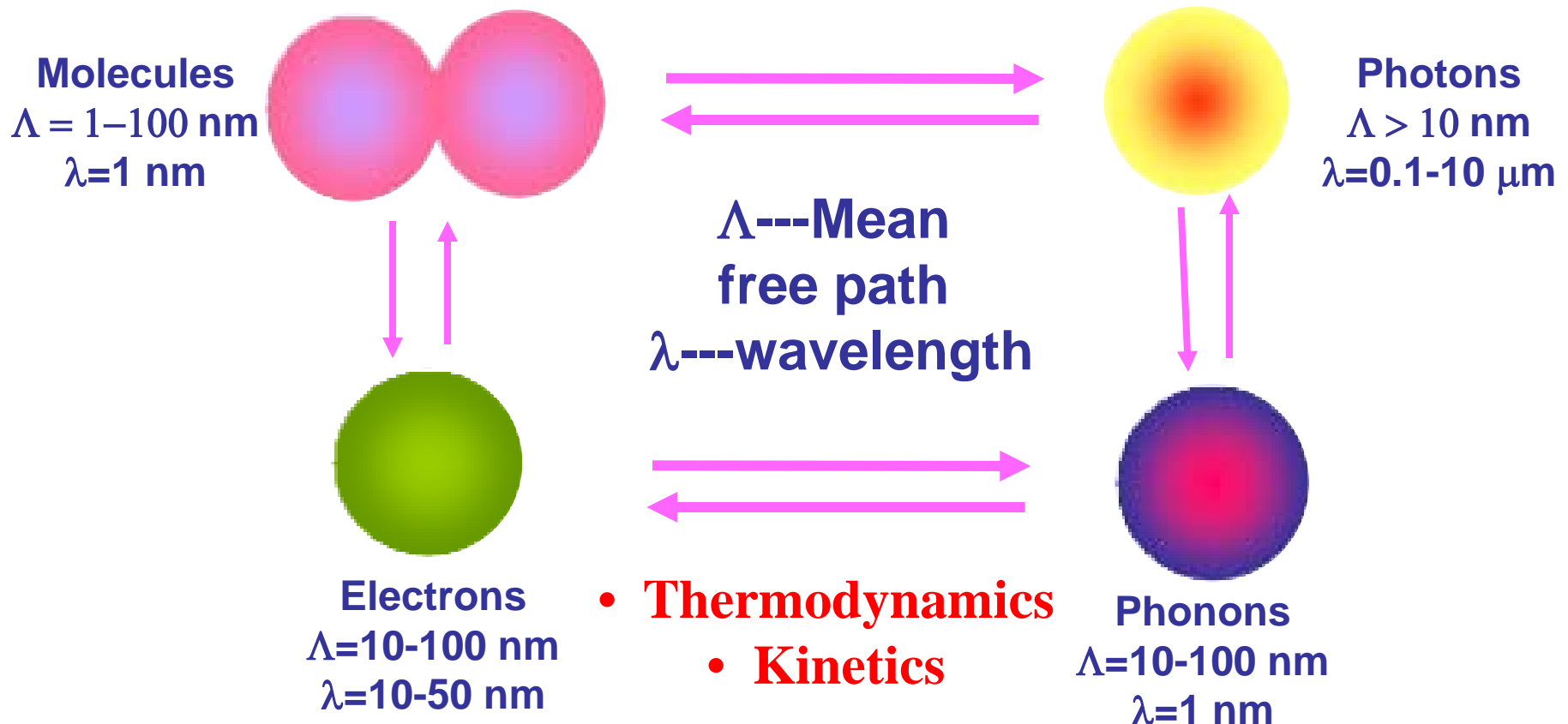
*Net fossil-fuel electrical imports.

**Biomass/other includes wood, waste, alcohol, geothermal, solar, and wind.

June 2004
Lawrence Livermore
National Laboratory
<http://eed.llnl.gov/flow>

Nano for Energy

- Increased surface area
- Interface and size effects

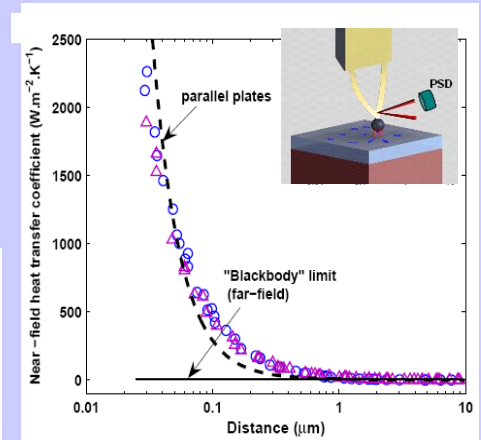
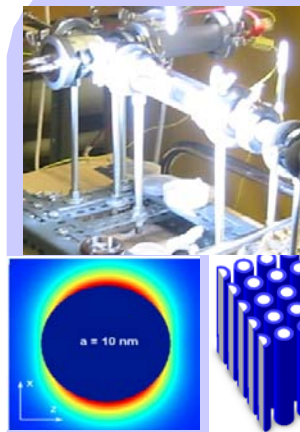


Nanoengineering Group

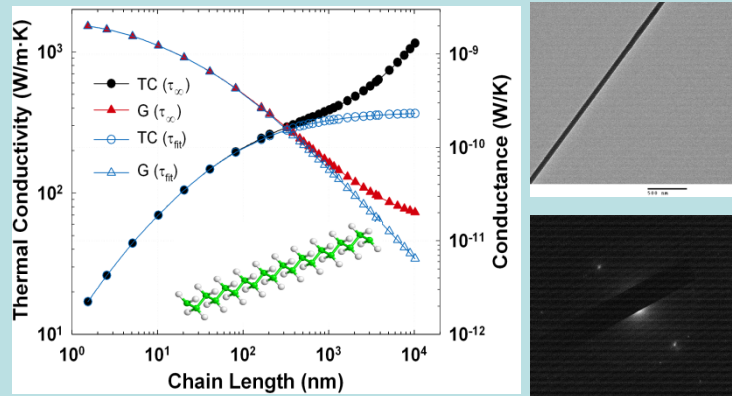
Nano: Heat: Energy



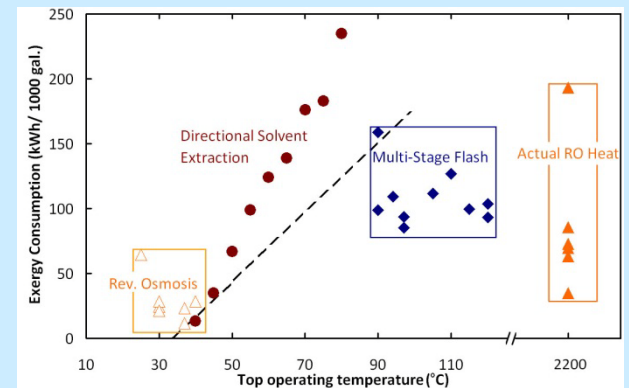
Nanostructured Thermoelectric Materials, Thermoelectric Power Generators and Refrigerators



Photon Control, Thermal and Solar Photovoltaics, Solar Thermal



High Thermal Conductivity Polymers



High Thermal Conductivity Liquids, Desalination

Thermoelectric Energy Conversion: Transport, Materials, and Systems

Gang Chen

**Department of Mechanical Engineering
Massachusetts Institute of Technology
Cambridge, MA 02139**

Email: gchen2@mit.edu

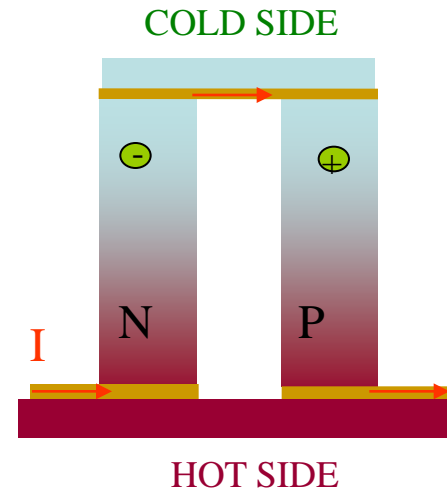
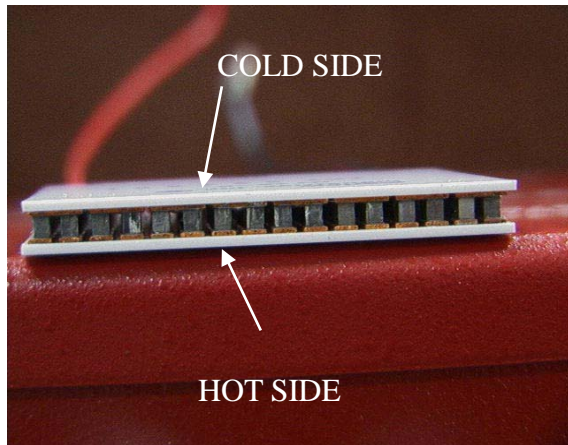
<http://web.mit.edu/nanoengineering>

**Hawkins Memmorial Lecture, 2012
School of Mechanical Engineering
Purdue University**

Outline

- Thermoelectrics and materials
- Phonon and electron engineering
- Solar thermoelectric energy conversion

Thermoelectric Energy Conversion



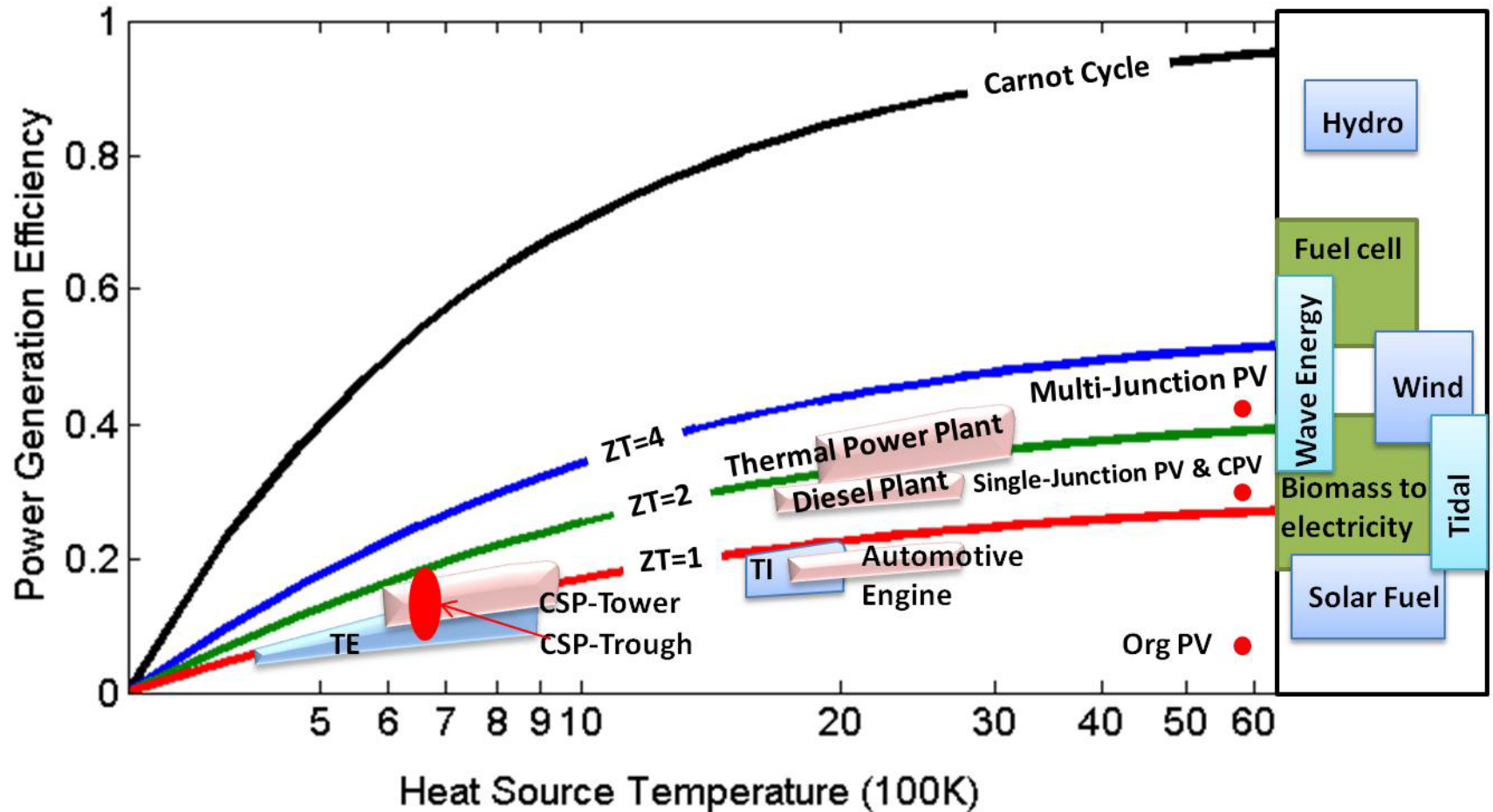
Nondimensional Figure of Merit

Joule Heating Seebeck Coeff.
Electron Cooling

$$ZT = \frac{\sigma S^2 T}{k}$$

Reverse Heat Leakage
Through Heat Conduction

Device Efficiency



Zebarjadi et al., Energy & Env. Sci., 5, 5147, 2012.



Contra Properties

Electrical Conductivity

Seebeck Coefficient

$$ZT = \frac{\sigma S^2 T}{k_e + k_p}$$

Electronic Thermal Conductivity

Phononic Thermal Conductivity

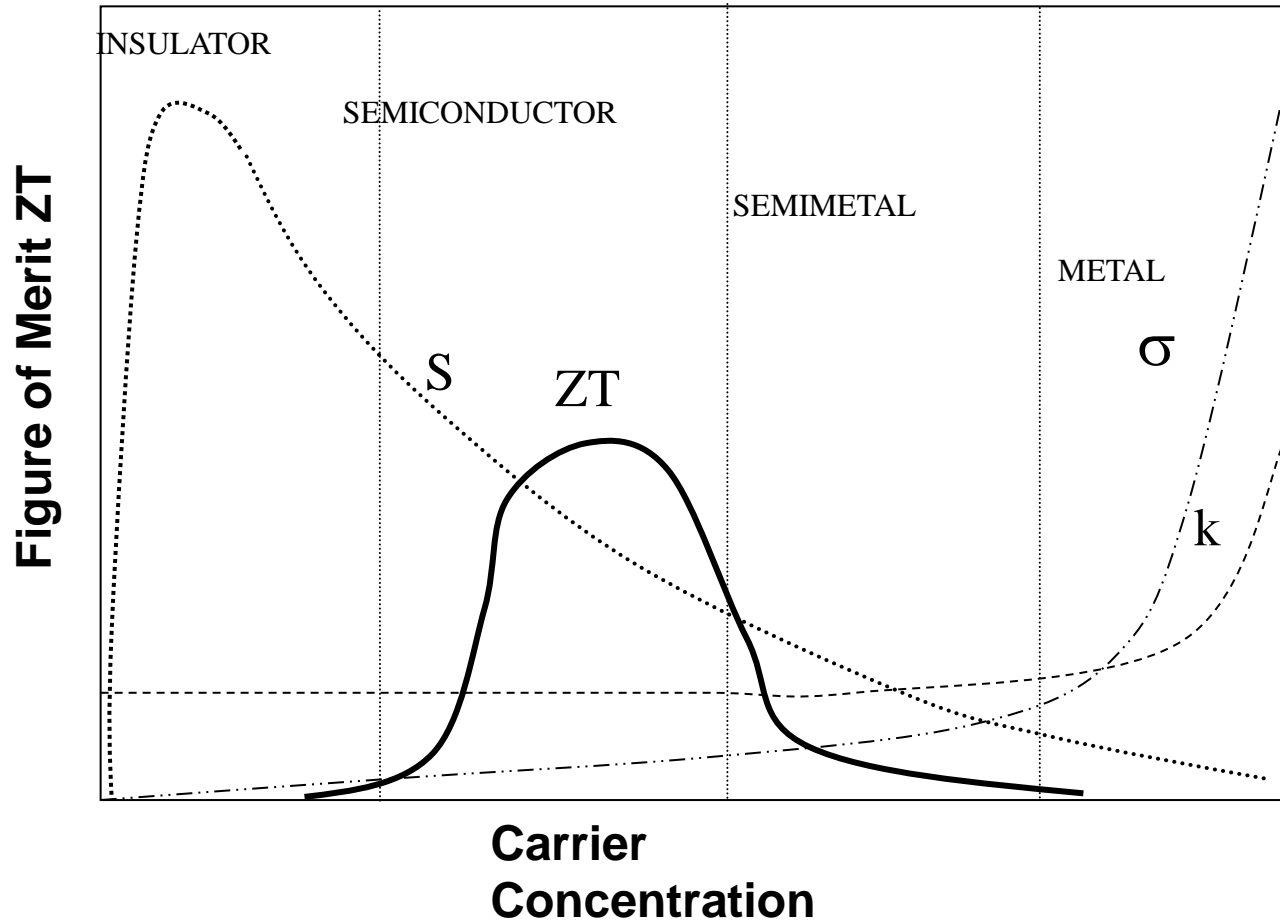
Wiedemann-Franz Law

$$\frac{k_e}{\sigma T} = L(n)$$

Lorenz Number:

In Metal: $L = 2.44 \times 10^{-8} \text{ W}\Omega^{-1}\text{K}^{-2}$
In semiconductor: depends on n

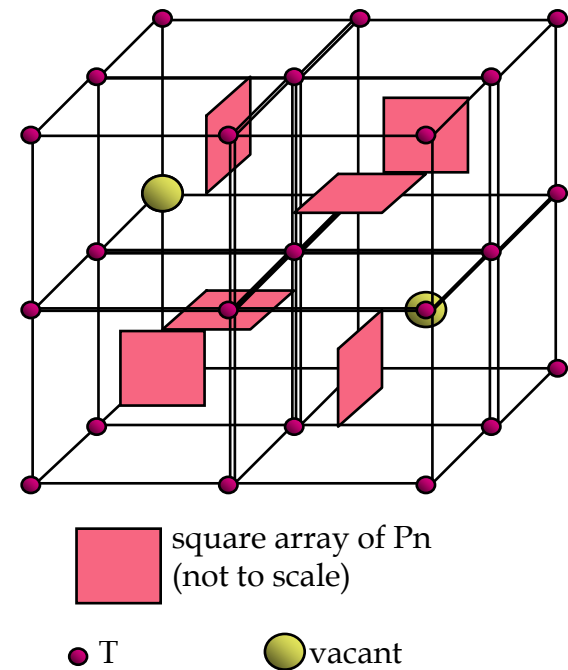
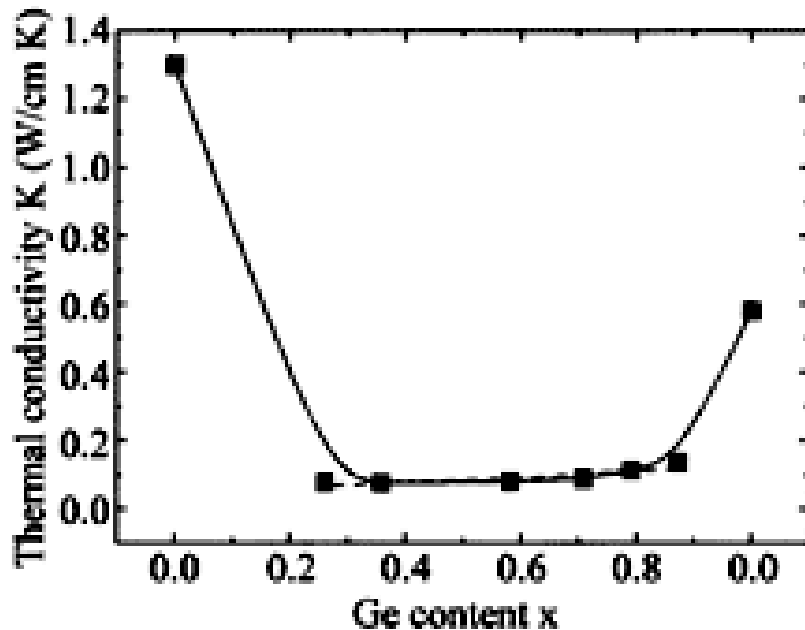
ZT Dilemma



Wanted: Phonon Glass / Electron Crystal

Phonon Engineering

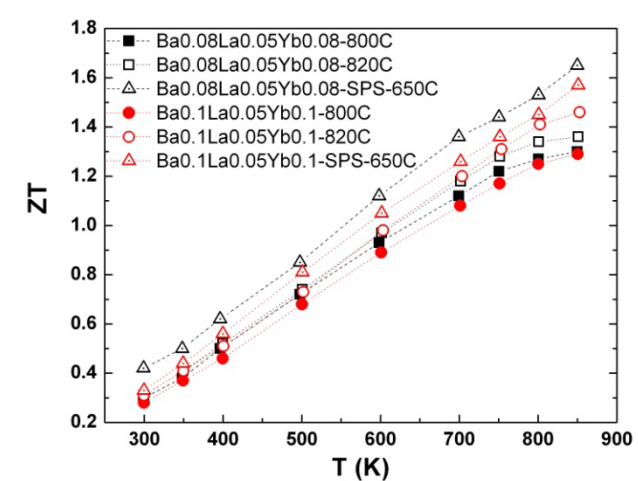
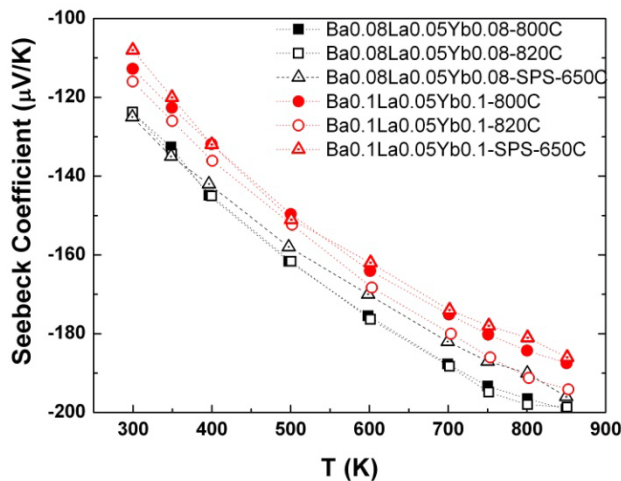
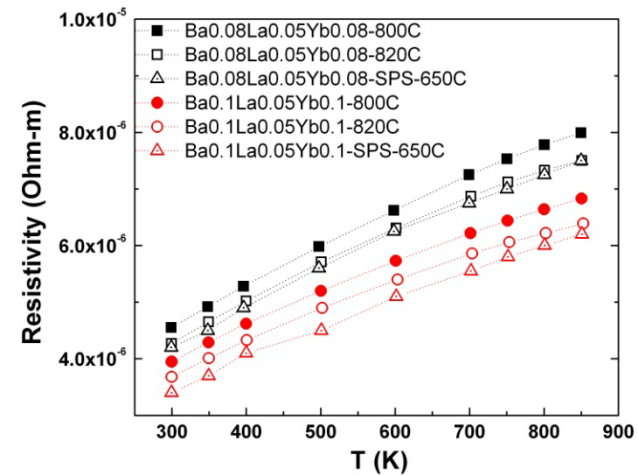
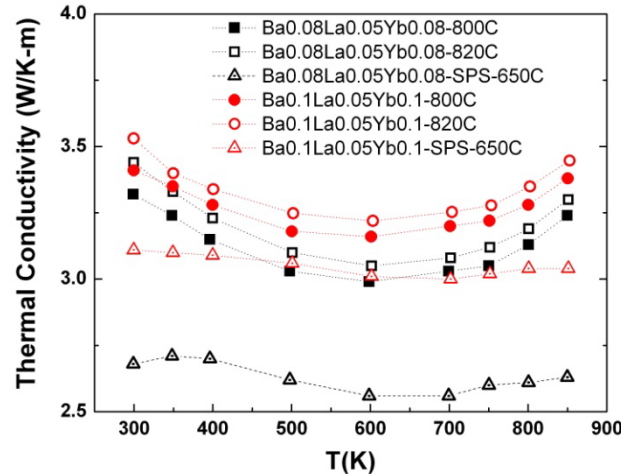
Methods of Reducing k_p In Bulk Materials:



- Alloy, 1950s (Ioffe)

- Rattlers, 1990 (Slack)

Triple Filled n-type Skutterudites

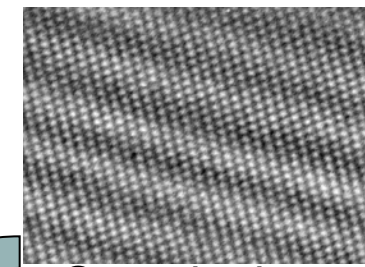
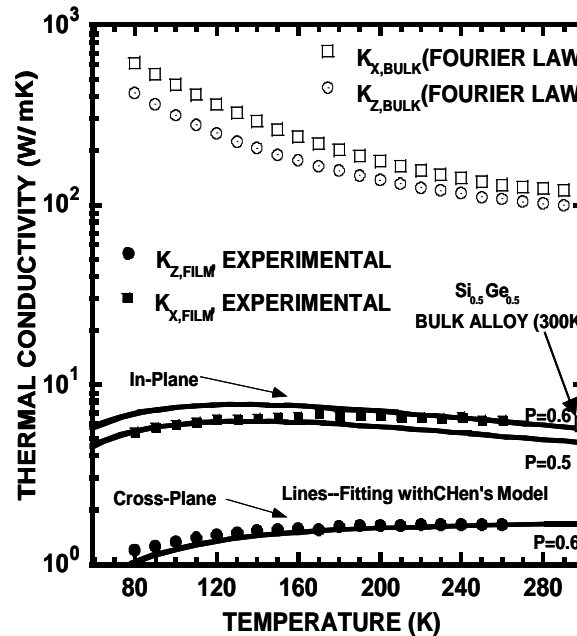
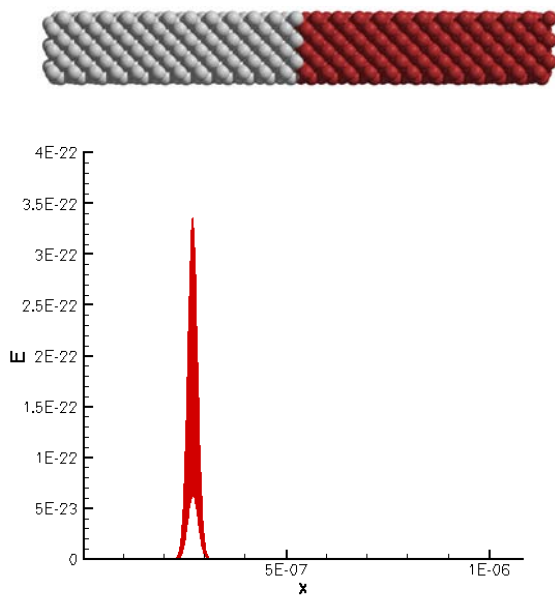
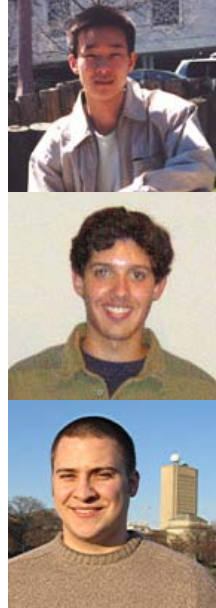
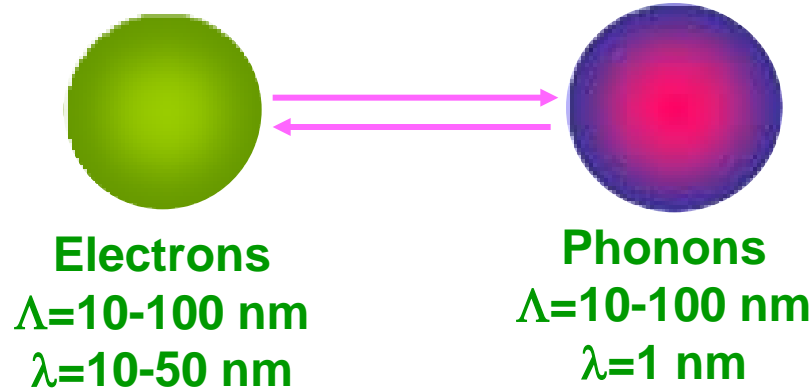


Triangles: the literature data.

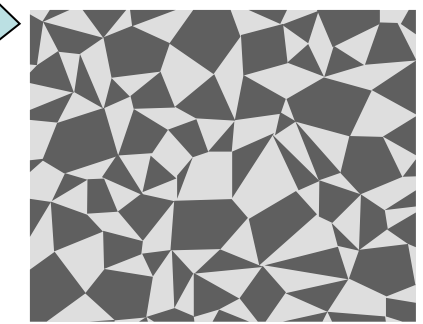
From Z.F. Ren

Benefits of Nanostructures

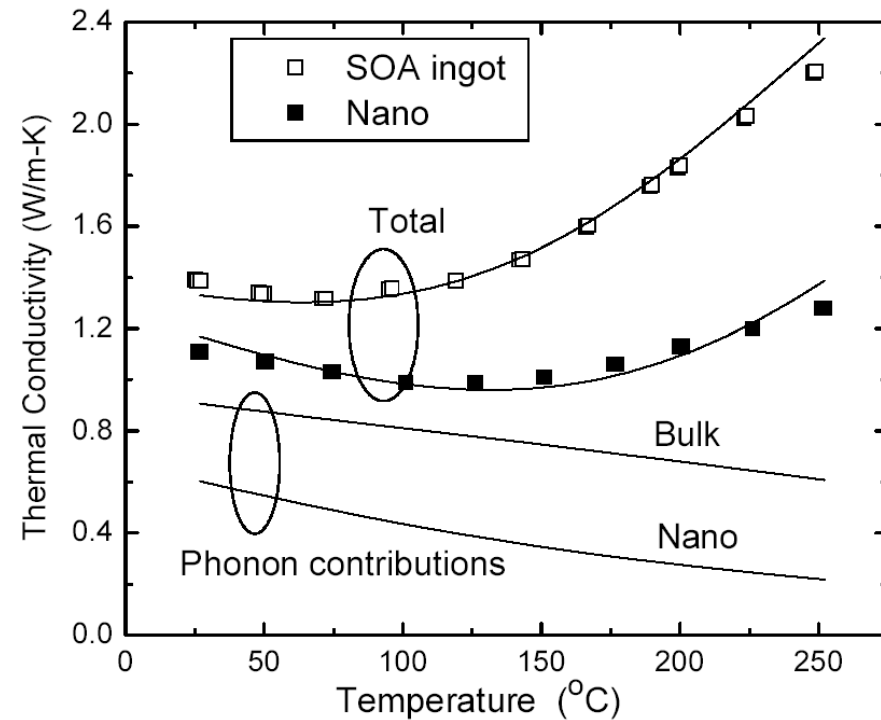
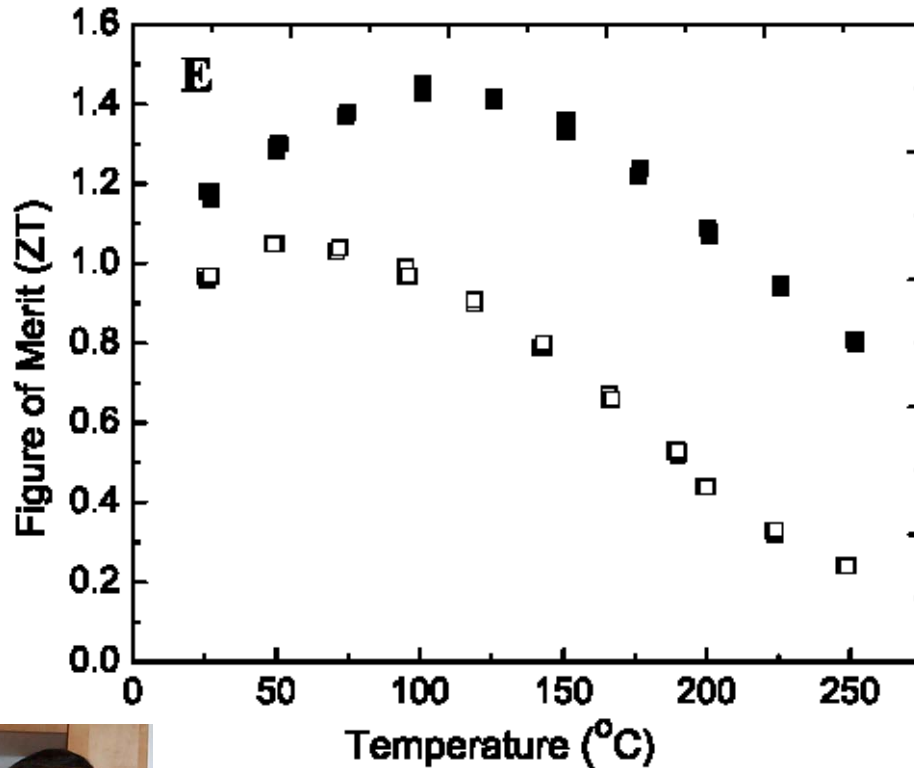
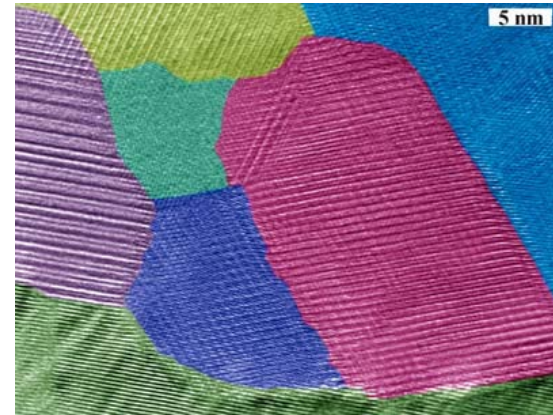
Interfaces that Scatter Phonons but not Electrons



Superlattices



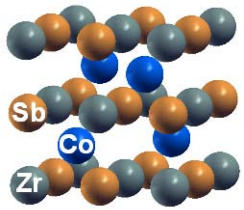
Nanostructured Thermoelectric Materials



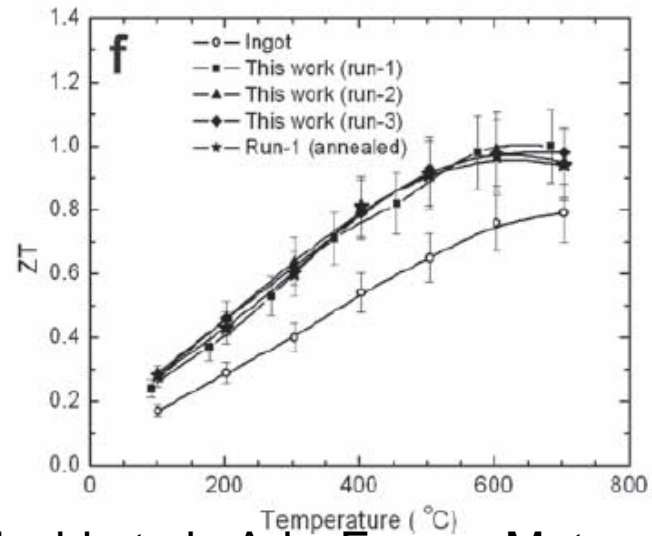
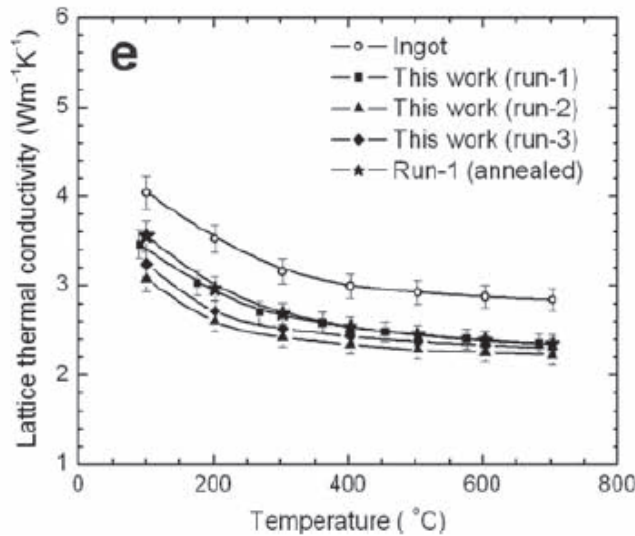
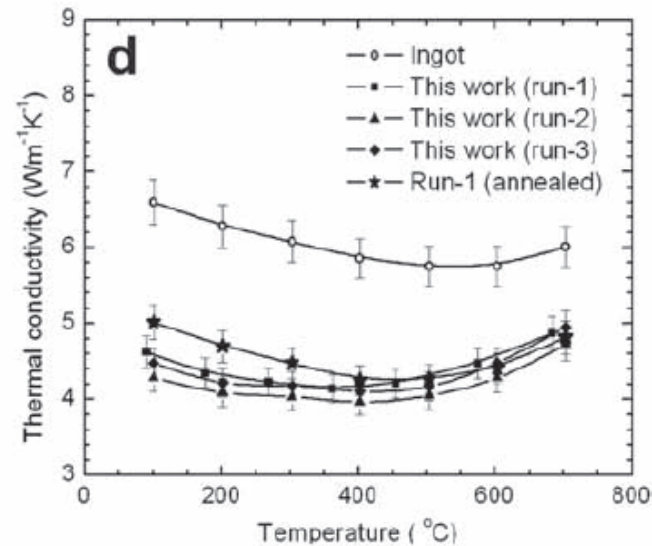
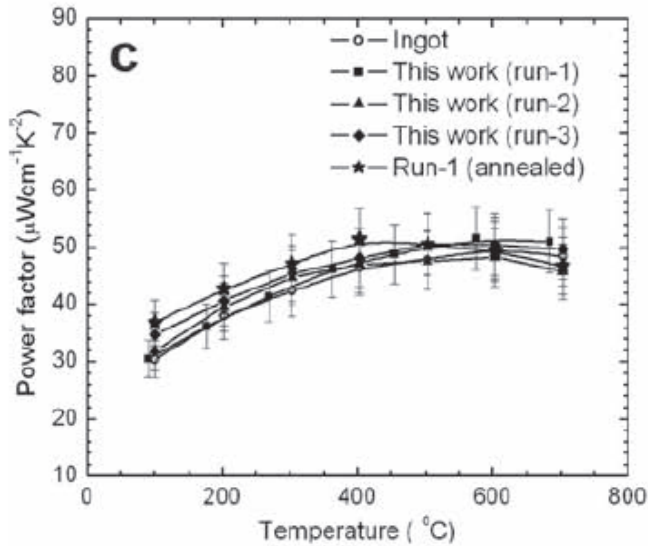
Poudel et al. Science, v. 320, p. 634, 2008



Engineering Group



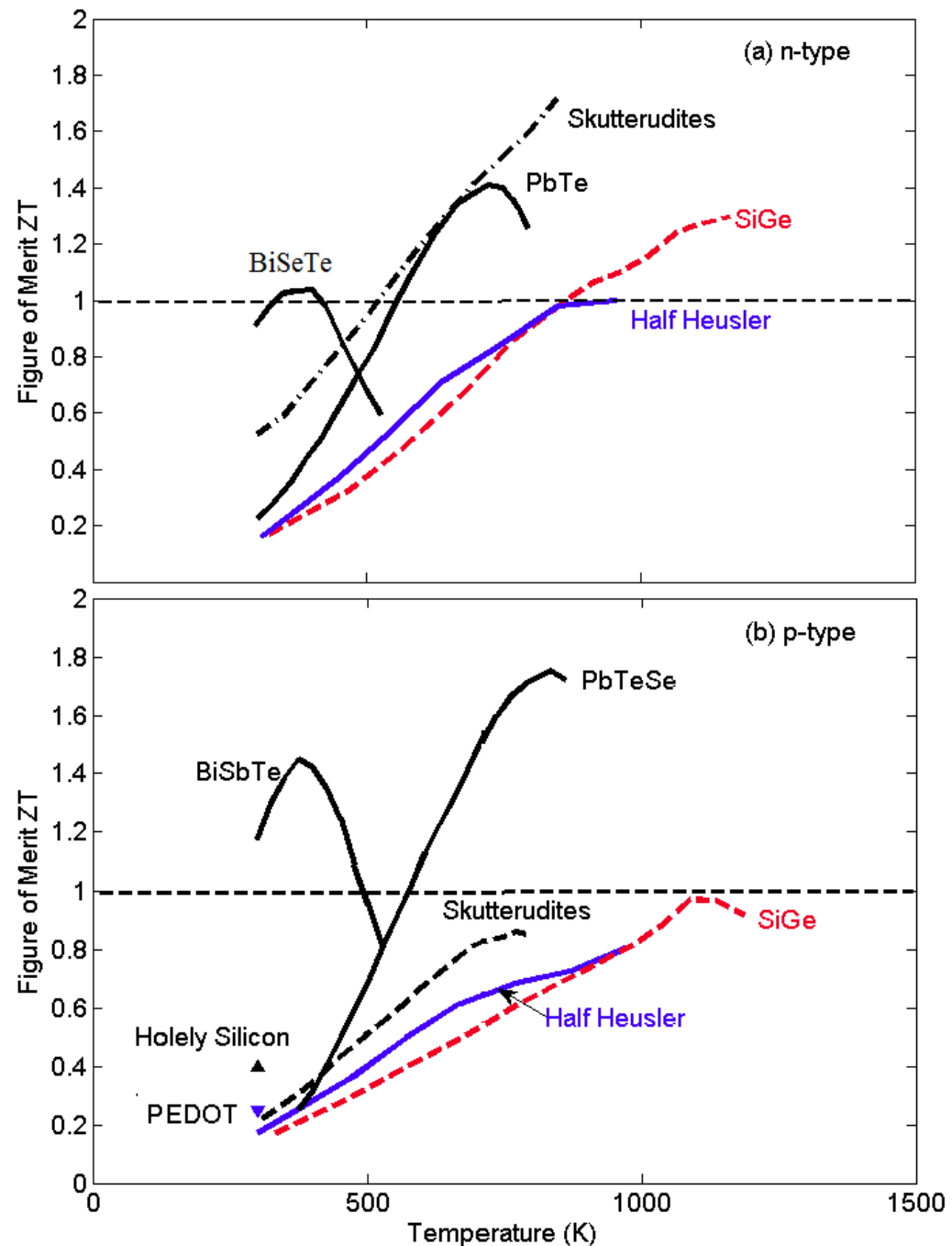
Half-Heuslers



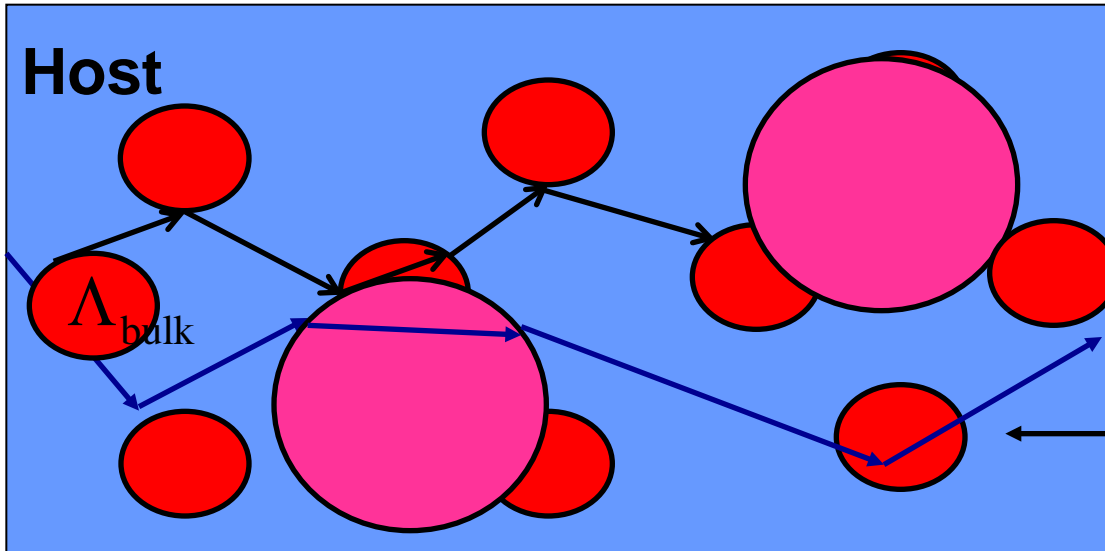
Joshi et al., Adv. Energy Mater., 1, 643, 2011.

Recent Progress in ZT

Zebarjadi et al., Energy & Env. Sci., 5, 5147, 2012



Phonon Engineering

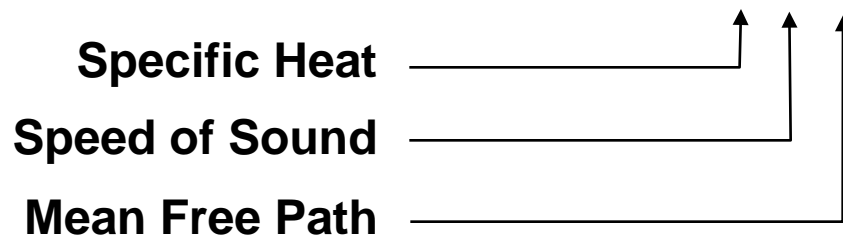


$$\Lambda_{\text{nano}} < \Lambda_{\text{bulk}}$$

Nanoparticles

Thermal Conductivity

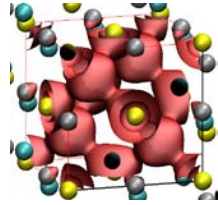
$$k = \frac{1}{3} \int C_{\omega} v_{\omega} \Lambda_{\omega} d\omega = \frac{1}{3} C v \Lambda$$



First-Principles Simulation

First Principle (DFT) calculations

$$i\hbar \frac{\partial \psi}{\partial t} = H \psi$$



e-band, e-DOS



Seebeck,
e-conductivity



ph-band, ph-DOS



- Density functional perturbation theory
- **Real space approach**

Broido et al., APL,
91, 231922, 2007;

Anharmonic Interatomic force

$$V = V_0 + \sum_i \Pi_i u_i + \frac{1}{2!} \sum_{ij} \Phi_{ij} u_i u_j + \frac{1}{3!} \sum_{ijk} \Psi_{ijk} u_i u_j u_k + \frac{1}{4!} \sum_{ijkl} X_{ijkl} u_i u_j u_k u_l$$

Esfarjani et al.,
Physical Review B
84, 085204, 2011.



Scattering calculation

$$W_{i \rightarrow f} = \frac{2\pi}{\hbar} \left| \langle f | V | i \rangle \right|^2 \rho$$

Molecular dynamics simulations

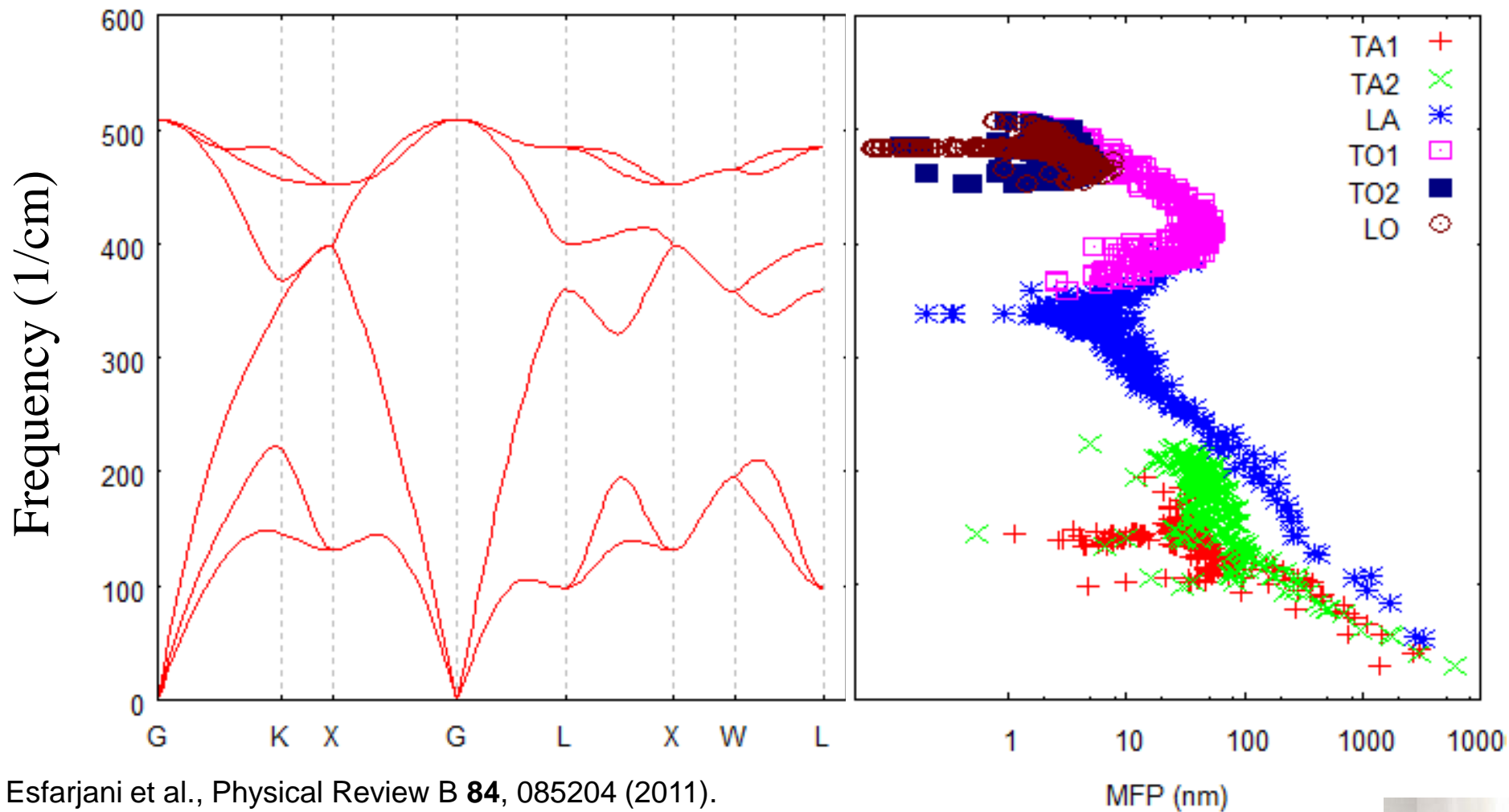
$$m_i \frac{d^2 \mathbf{r}_i}{dt^2} = -\nabla V$$

Alloy effects



Thermal conductivity + mean free path (mode-dependent)

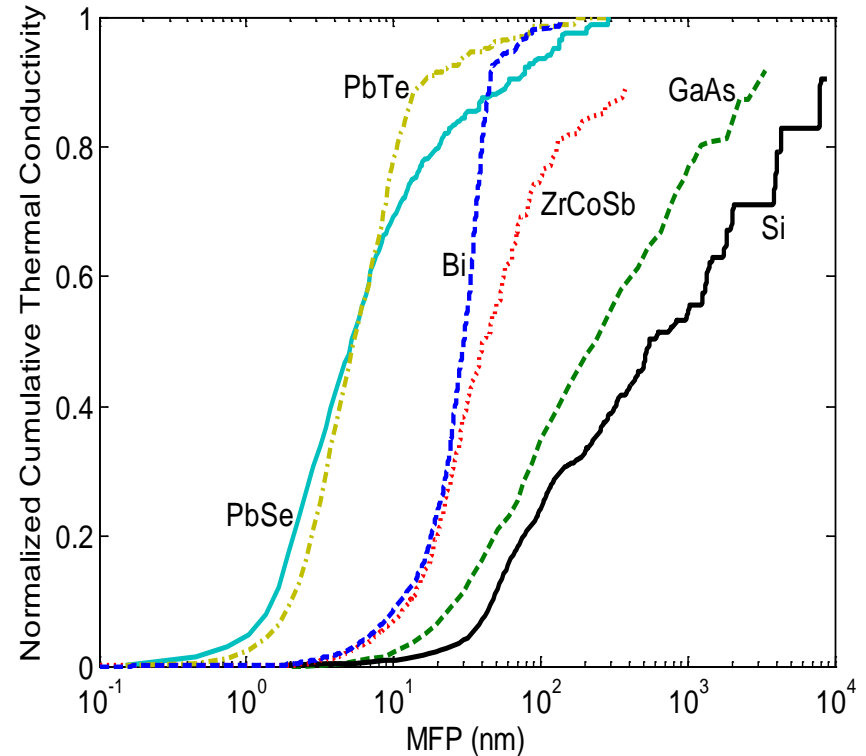
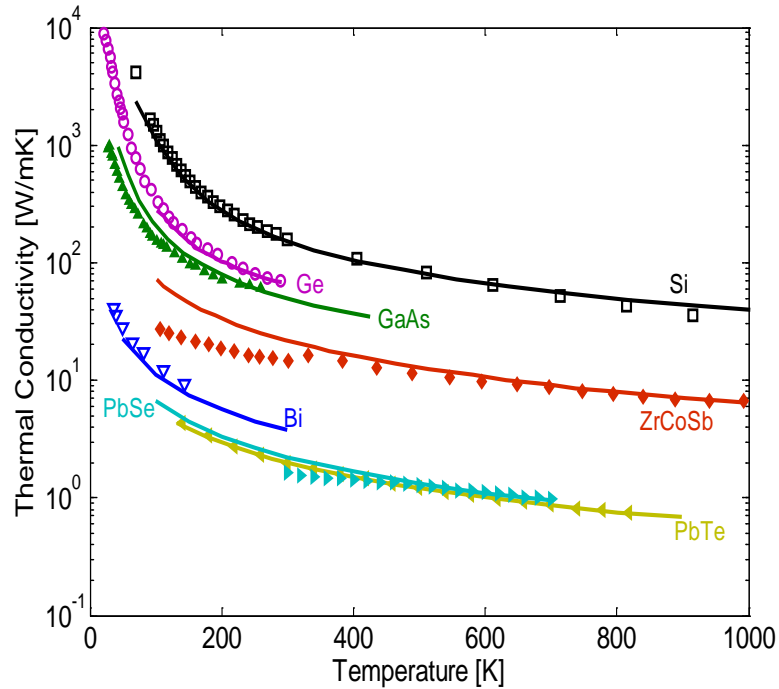
Phonon Mean Free Path in Si at 300 K



Esfarjani et al., Physical Review B **84**, 085204 (2011).



Results from First-Principles Simulation



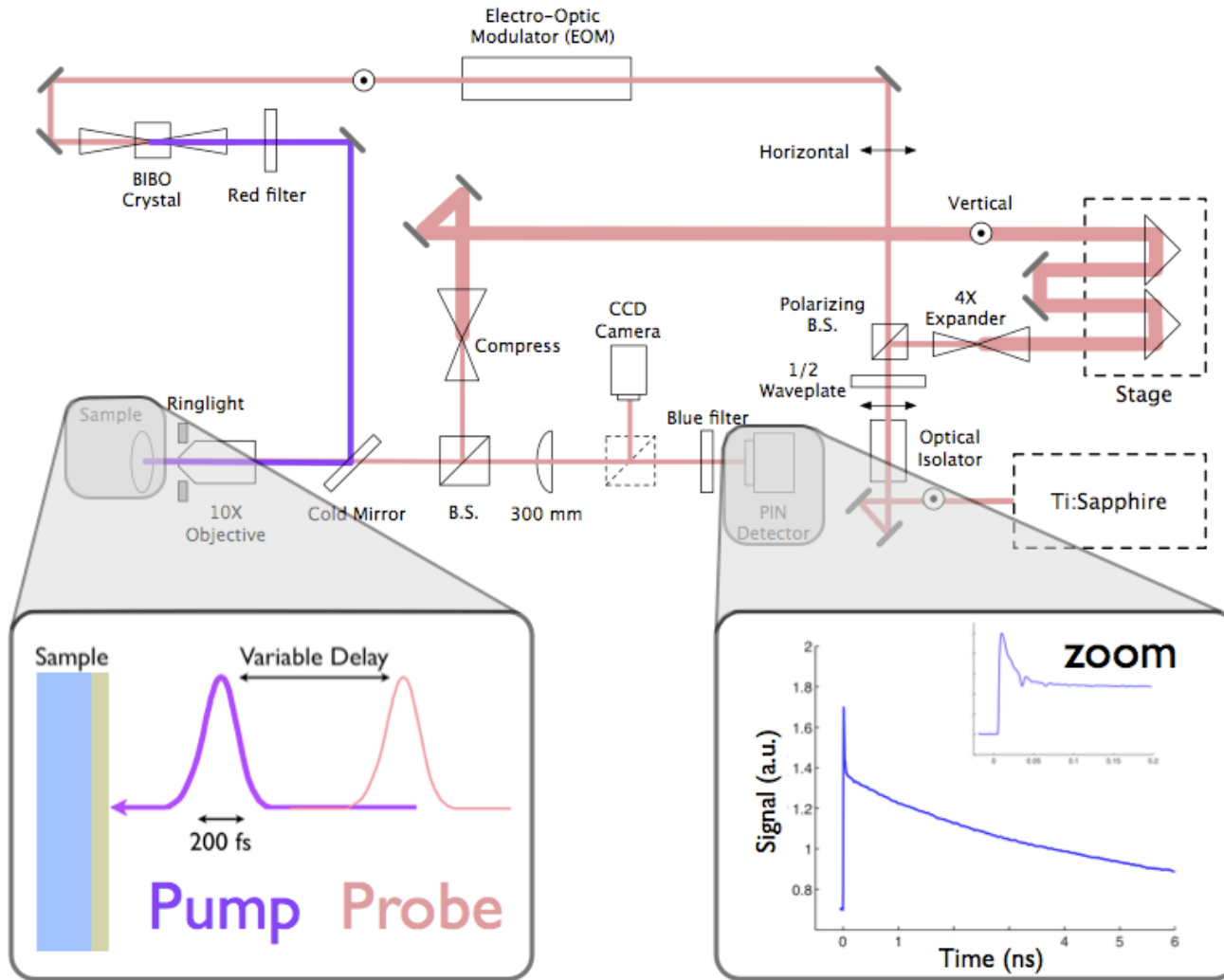
- Esfarjani et al., Phys. Rev. B 84, 085204 (2011).
Shiomi et al., Phys. Rev. B 84, 104302 (2011).
Takuma et al., Phys. Rev. B 85, 155203 (2012).
Tian et al., Phys. Rev. B 85, 184303 (2012).
Zebarjadi et al., Energy & Env. Sci, 5, 5047 (2012)



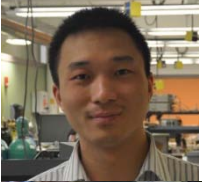
Group



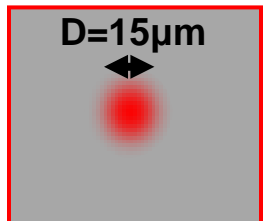
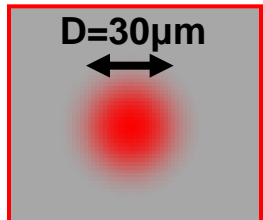
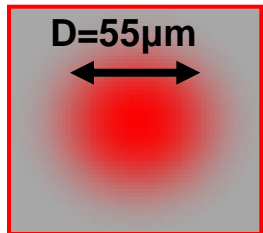
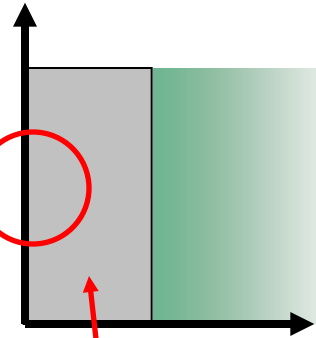
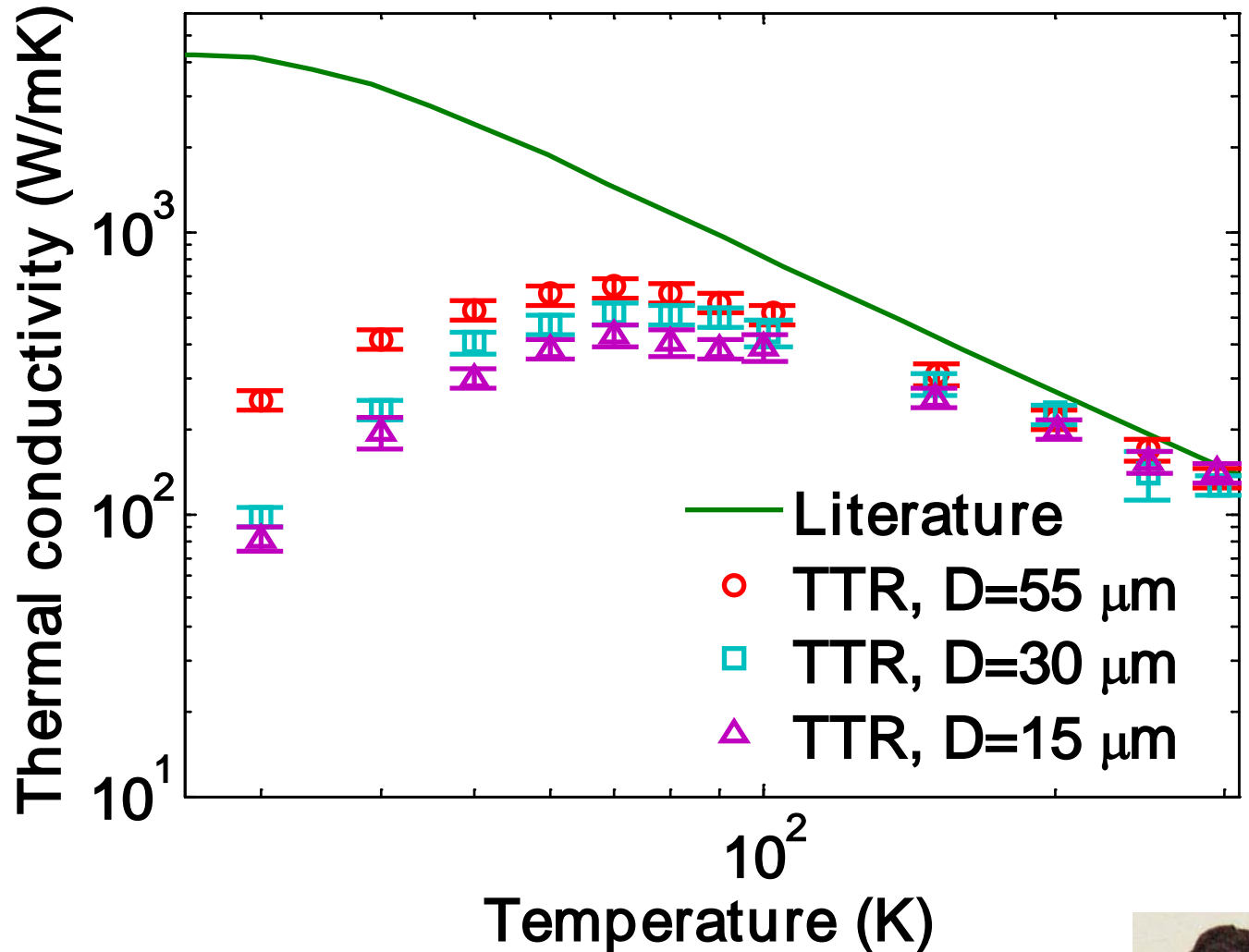
Thermal Conductivity Spectroscopy



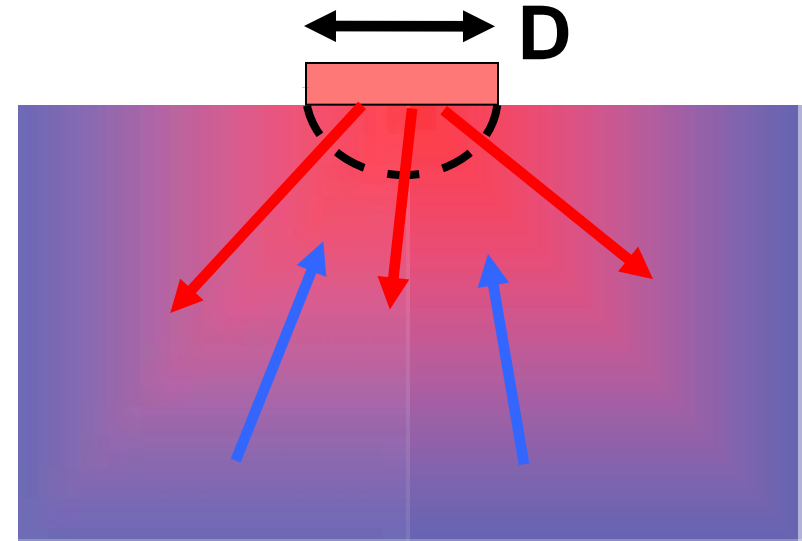
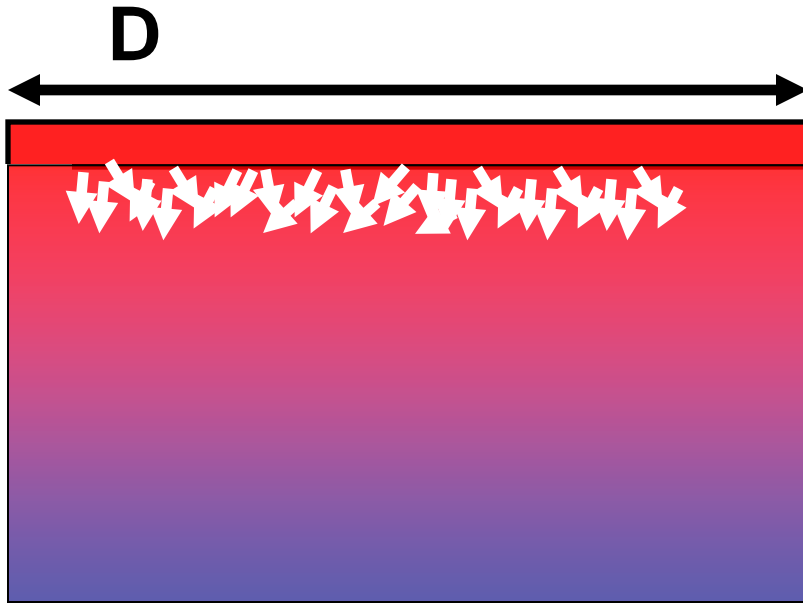
Schmidt et al. Review of Scientific Instruments, 79, 114902, 2008.



Experimental Results on Si



Effect of Quasi-ballistic Transport



Diffusive
Fourier's Law



Ballistic
Phonon radiation

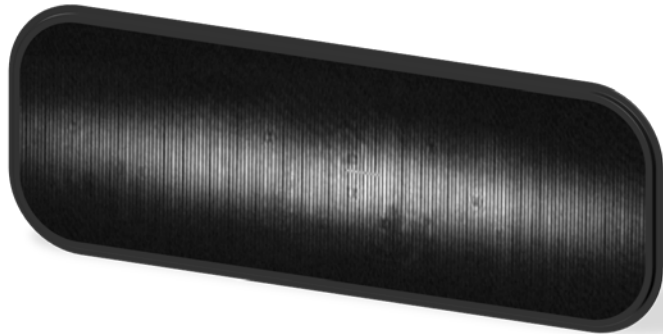
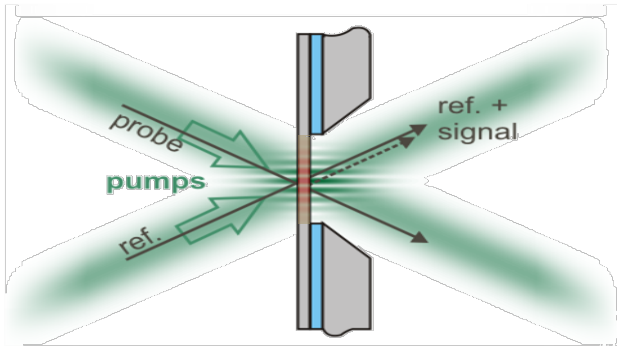
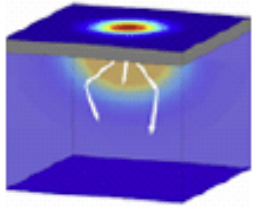
$$\frac{q_{B\omega}}{q_{D\omega}} \sim \frac{D}{\Lambda_{\omega}}$$

Ballistic heat flux is less than Fourier law prediction

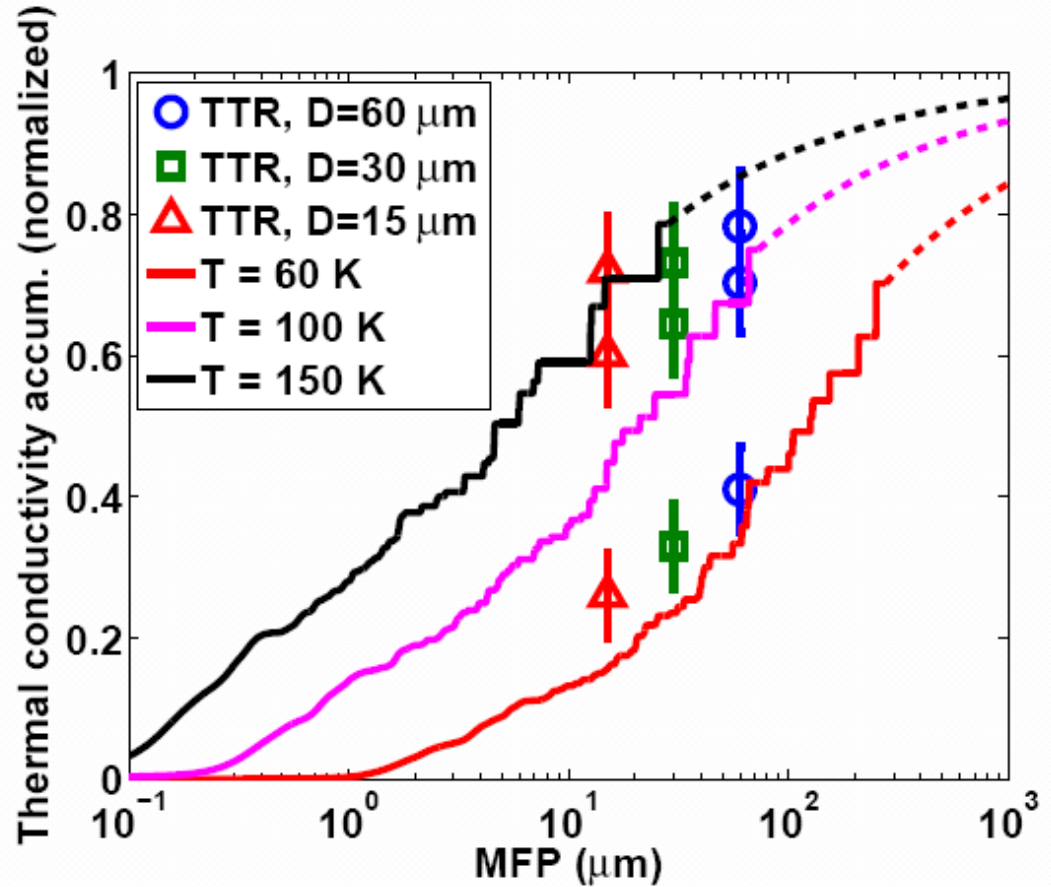
Chen, J. Heat Transfer, 118, 539, 1996

August 25, 2011

Thermal Conductivity Spectroscopy on Phonon MFP Distribution



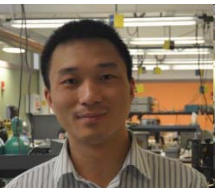
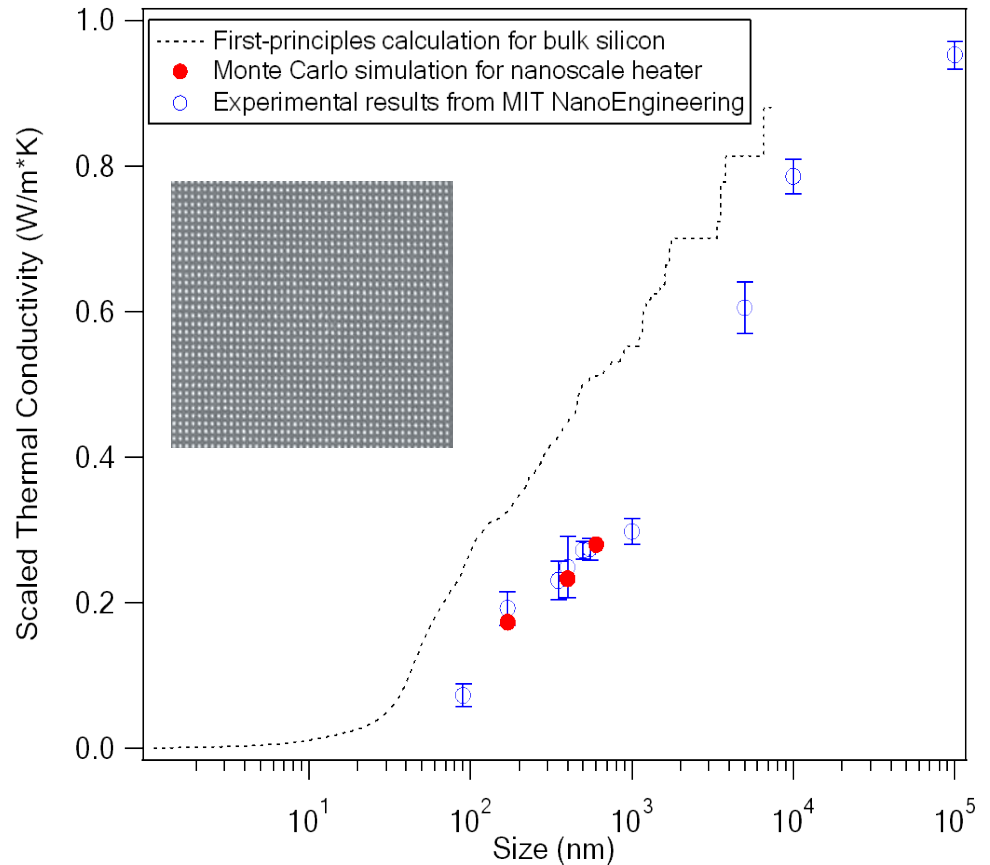
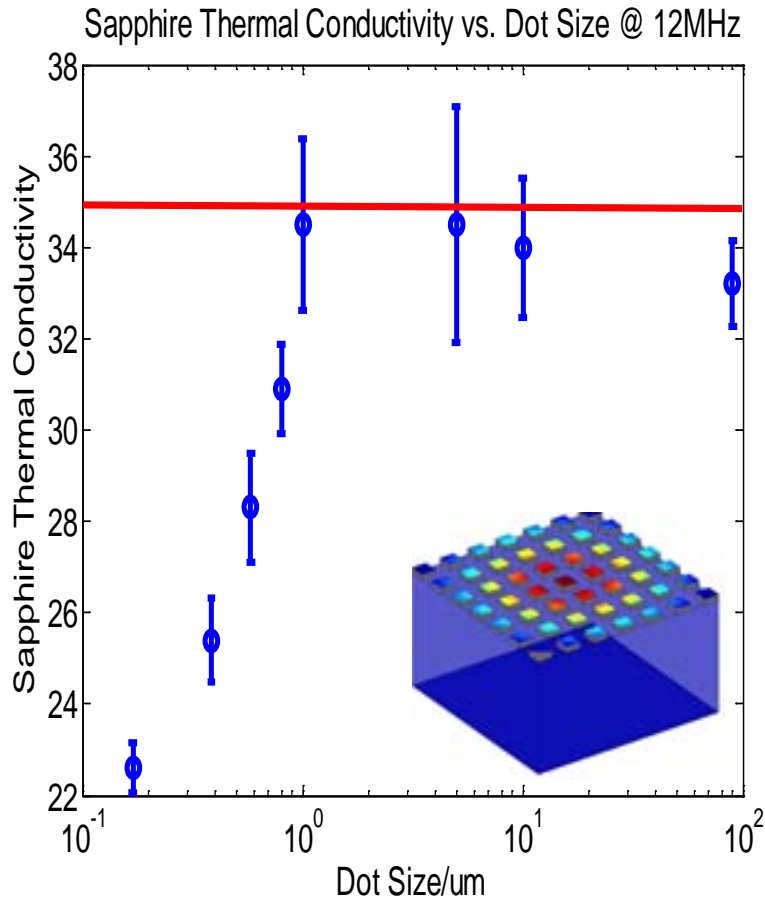
Johnson et al., submitted



Minnich et al., PRL, 107, 095901, 2011



Pushing Down to Nanometer



Electron Transport

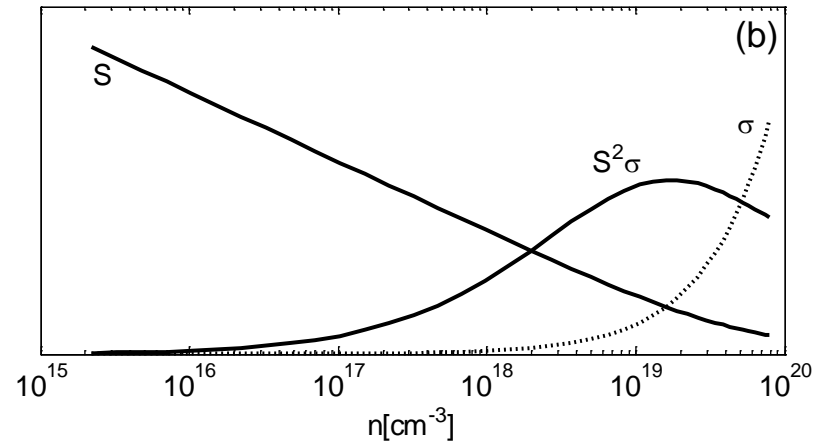
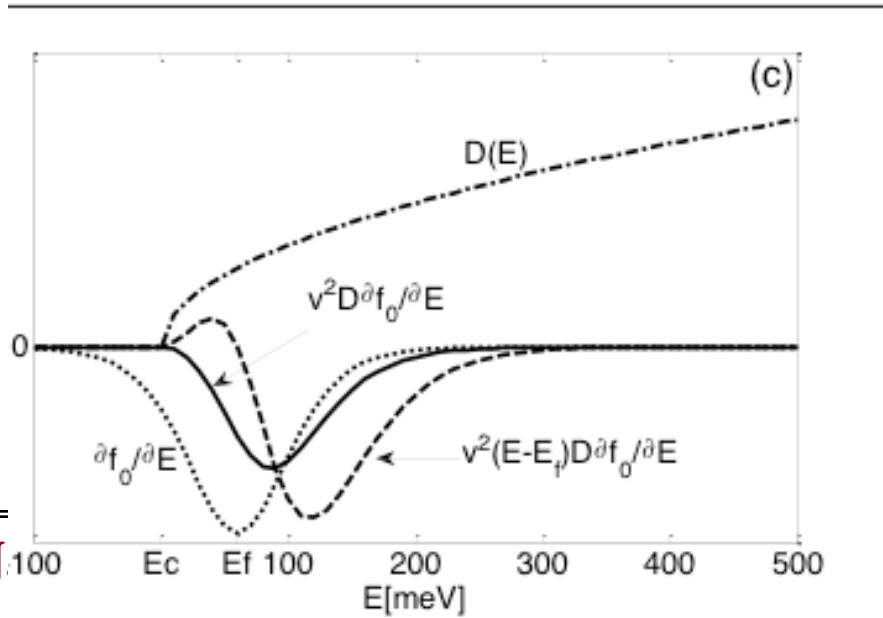
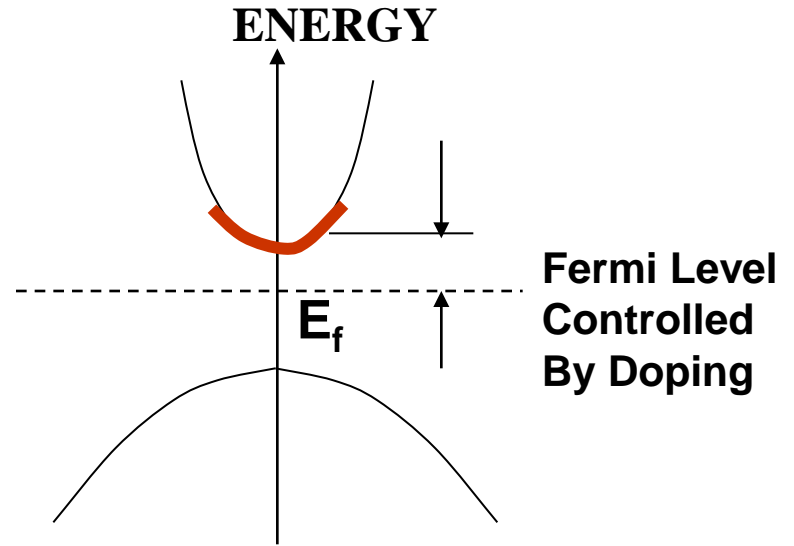
$$S = \frac{1}{q} \frac{\int (E - E_F) \sigma dE}{\int \sigma(E) dE} \propto \langle E - E_f \rangle$$

$$\sigma = \frac{q^2}{3} \int \tau v^2 D(E) (-\partial f_{eq} / \partial E) dE$$

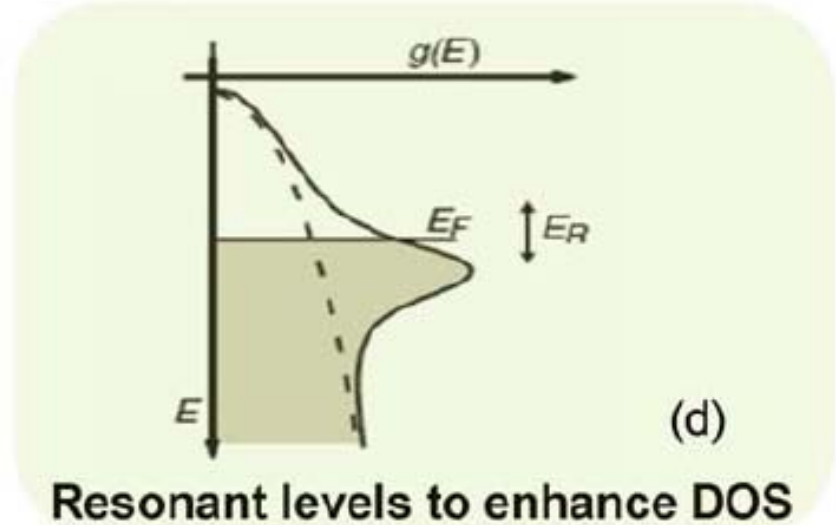
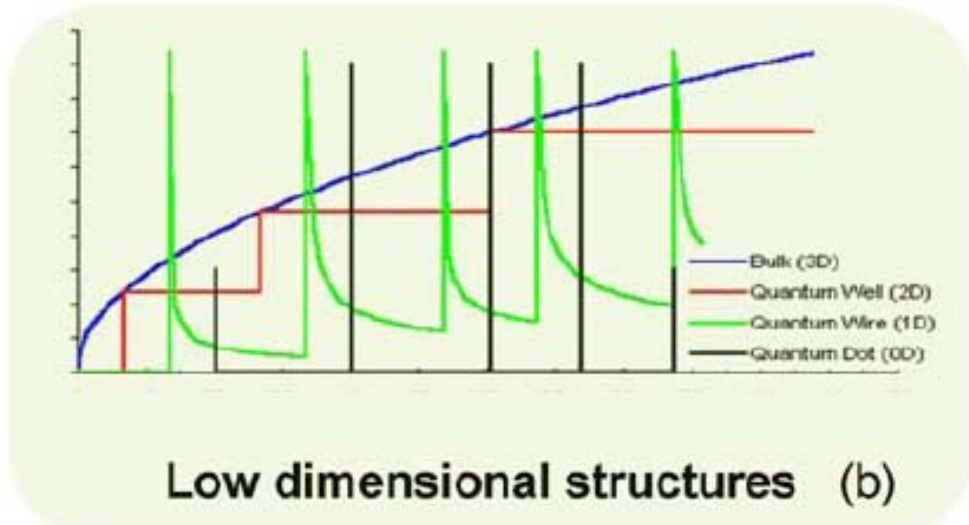
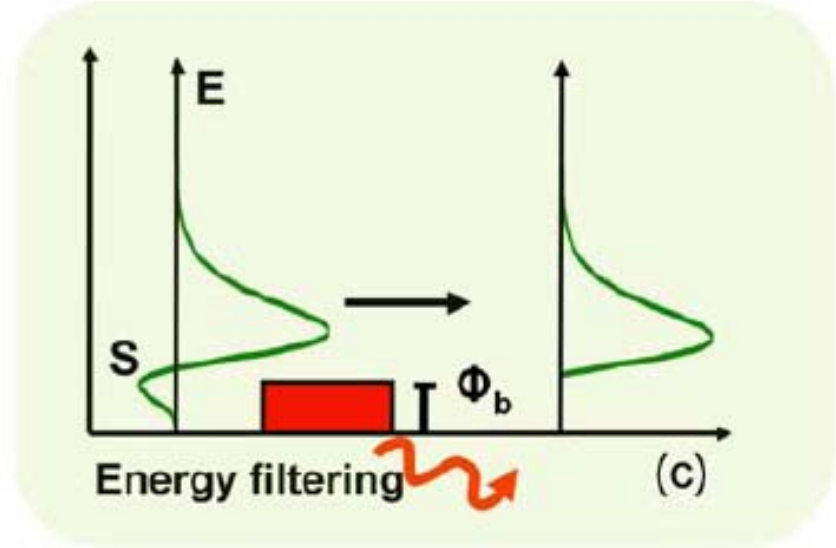
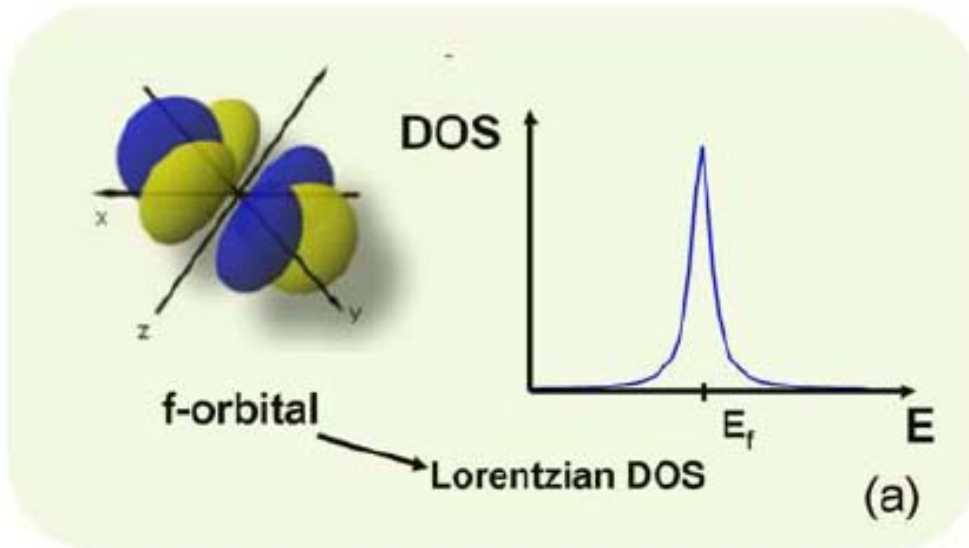
Relaxation
Time

Density
of States

Fermi-Dirac
Distribution

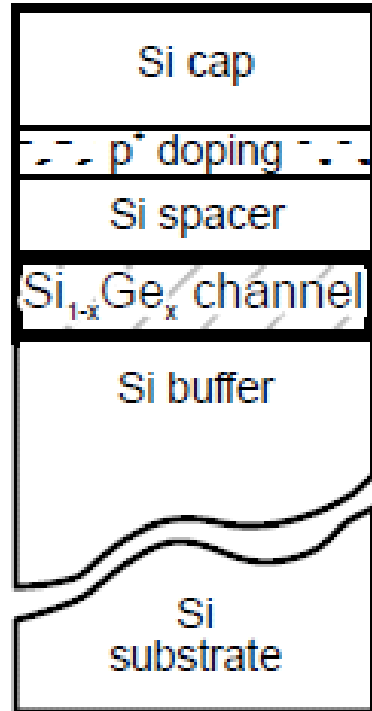


Electron Engineering



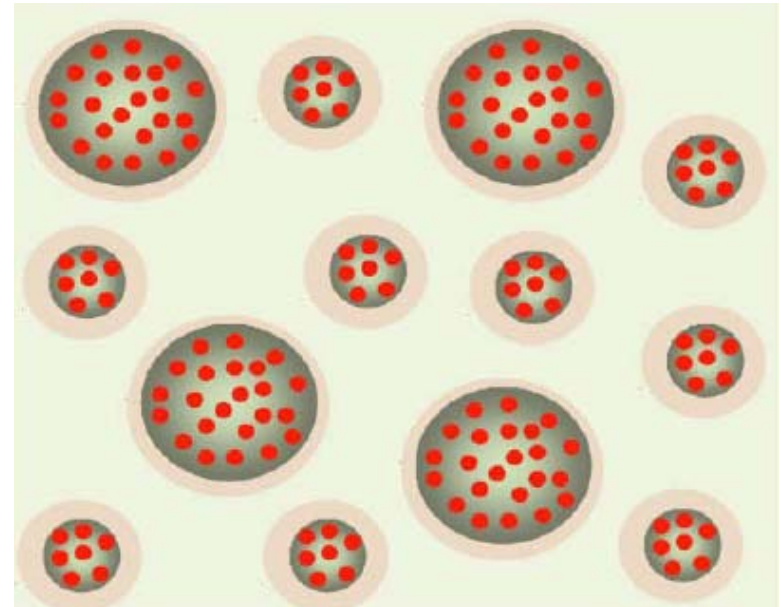
Modulation Doping

2D Thin-Films



Schaffler, Semicond. Sci. Tech. 12 1997

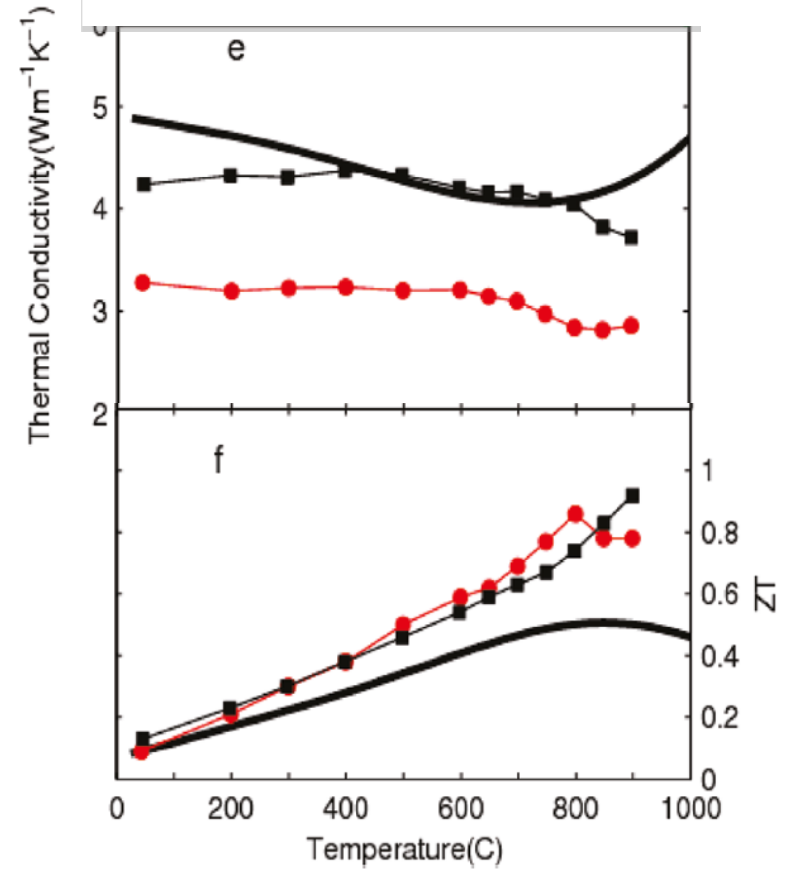
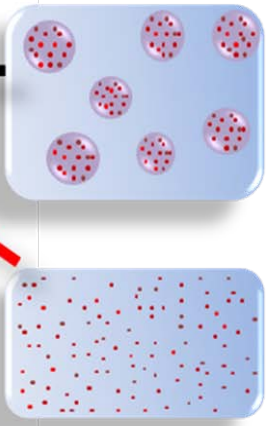
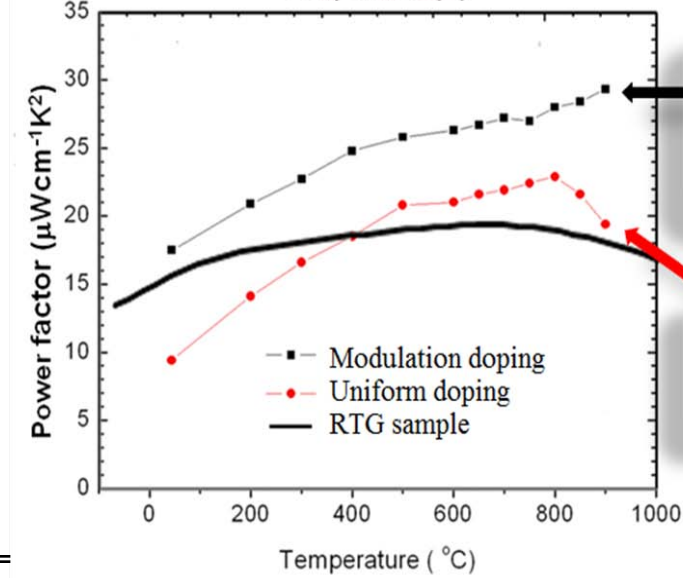
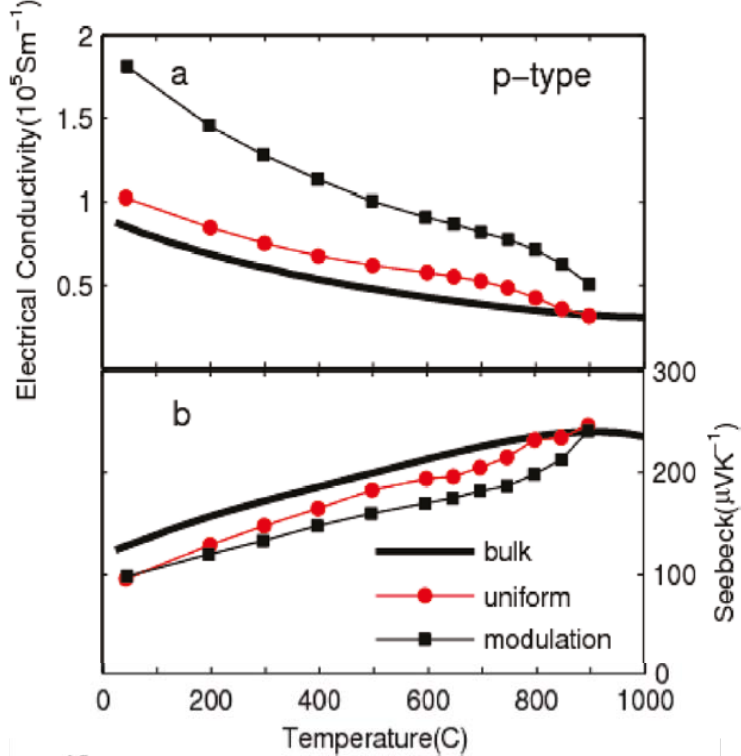
3D Bulk Nanostructures



Zebarjadi et al., Nano Letters, 11, 2225, 2011.

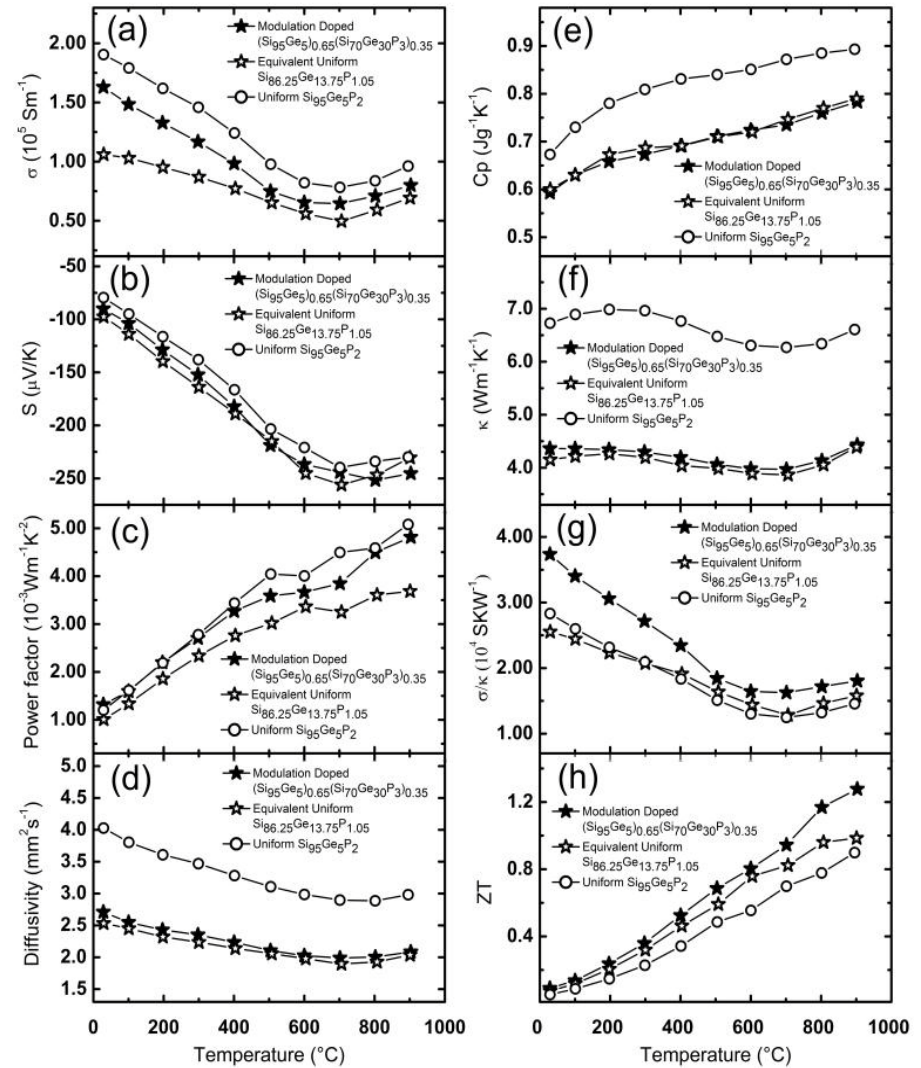
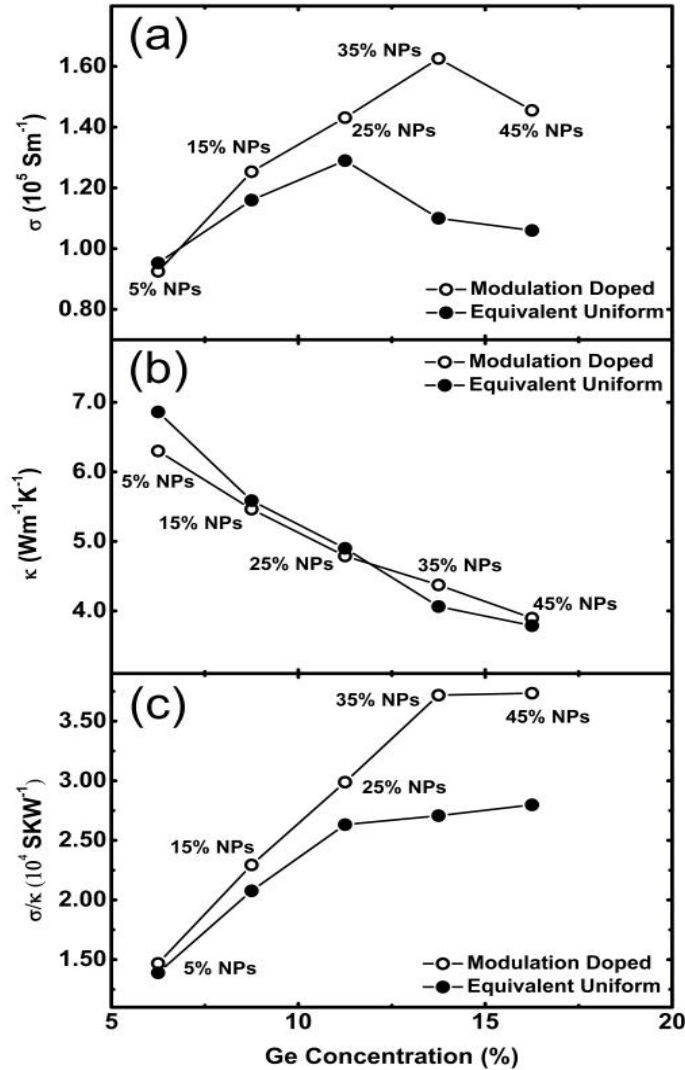


Modulation Doping



Zebarjadi et al., Nano Lett **11**, 2225-2230 (2011)

Concurrent Electron and Phonon Engineering

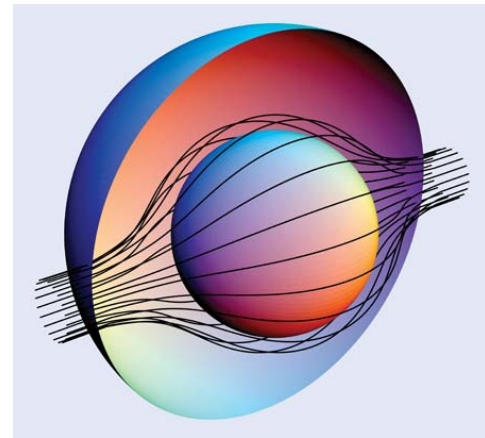


Yu et al., Nano Letters, 12, 2077 (2012).



en.wikipedia.org

Invisible Cloak

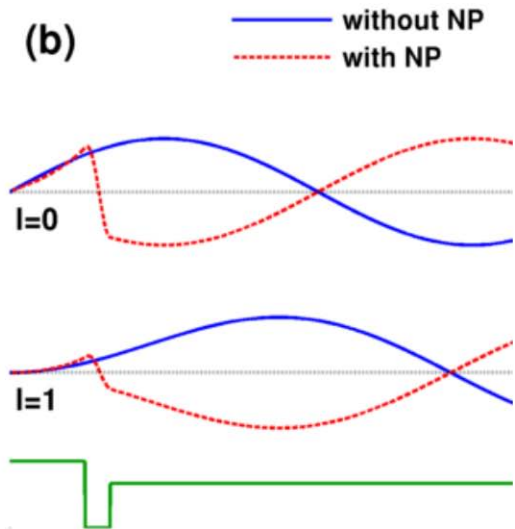
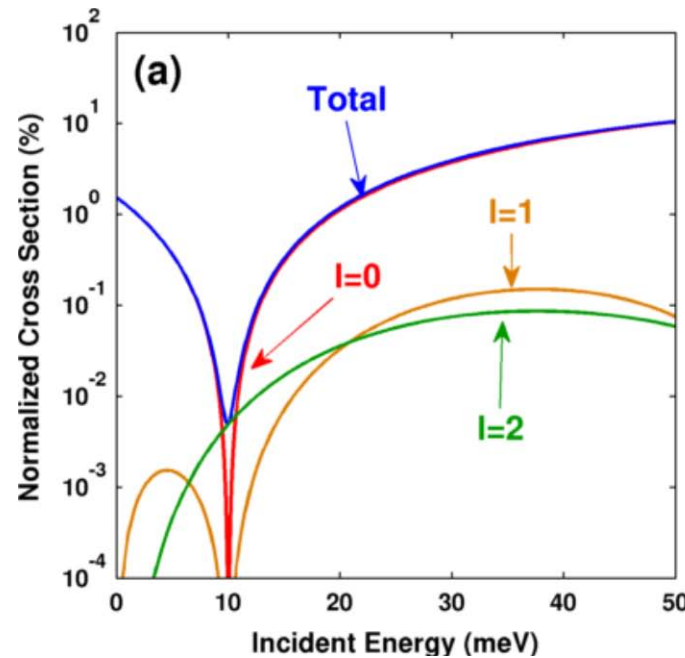
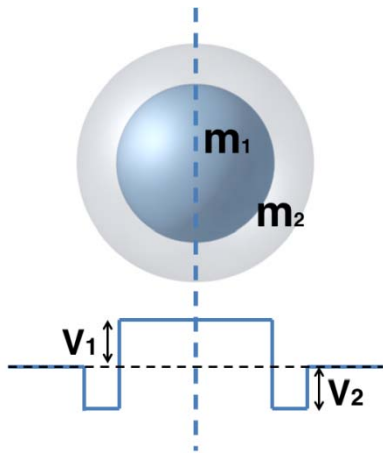
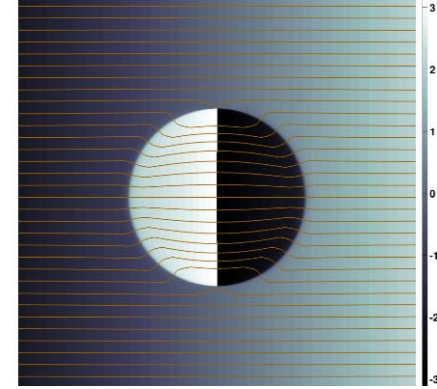


physicsworld.com

Invisible Particles

- Mott formula for the Seebeck coefficient:

$$S = \frac{\pi^2}{3} \frac{k_B}{q} k_B T \left\{ \frac{1}{D} \frac{dD(E)}{dE} + \frac{1}{\mu} \frac{d\mu(E)}{dE} \right\} \Bigg|_{E=E_F}$$



B. Liao et al., Phys. Rev. Lett., 109, 126806, 2012



Application: From Micro Watts to Giga Watts

Vehicles



Power Plants



μW

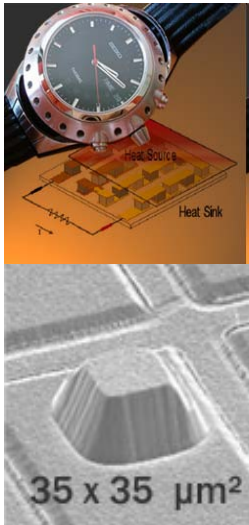
W

kW

MW

GW

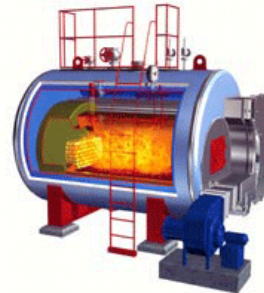
Sensors



Stove



Furnace



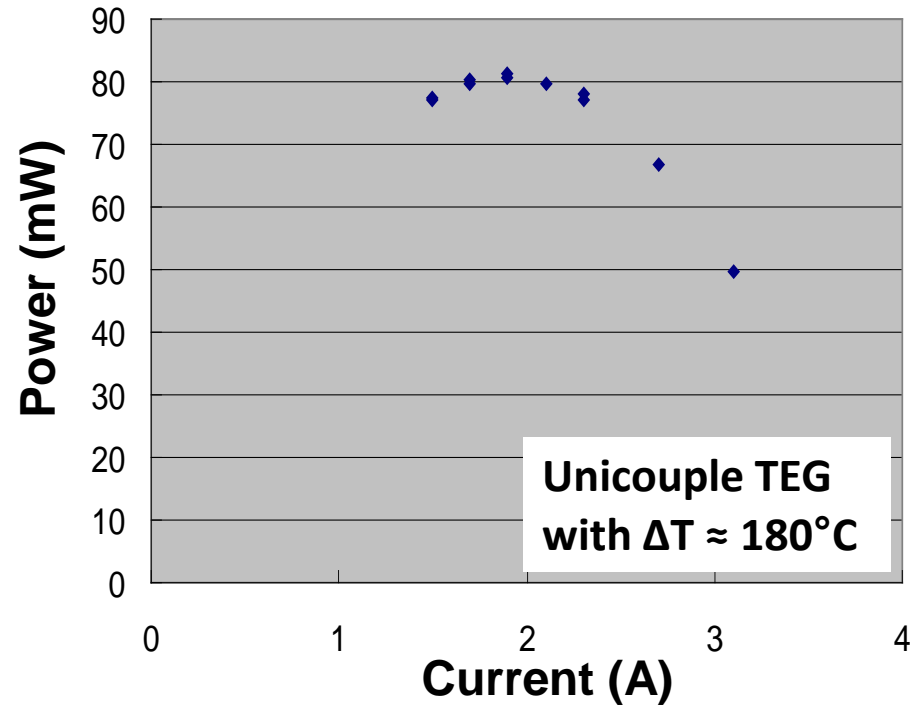
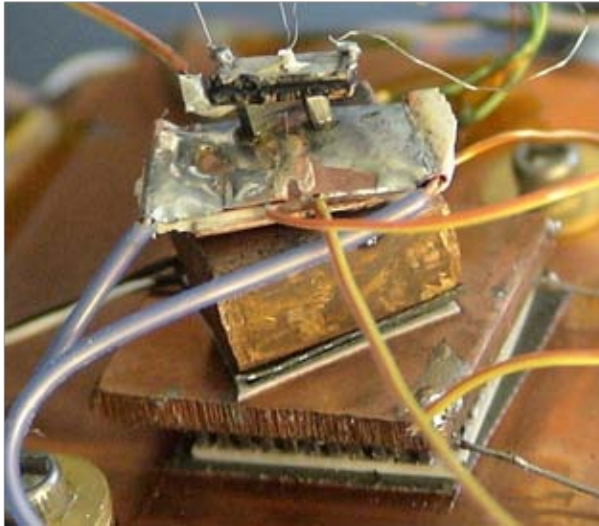
Solar



Industrial Waste Heat



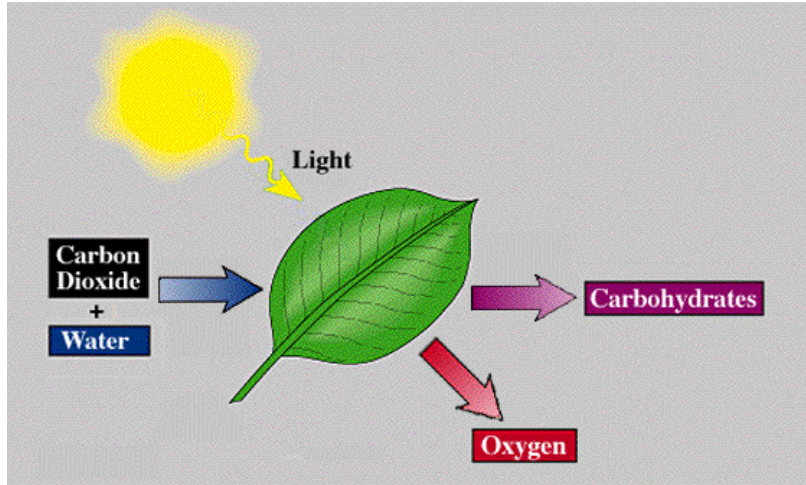
Power and Cost Example



- ❑ Dimensions of TE elements: 1.5mm x 1.5 mm x 1.6 mm
- ❑ Material cost per power output ≈ 0.1 \$/Watt
- ❑ Cost of TE material can be small relative to total system cost!

Solar Energy Utilization

Solar Fuel



http://www.phschool.com/science/biology_place/biocoach/photosynth/overview.html

Solar Heating



<http://www.global-greenhouse-warming.com/solar-hot-water.html>

Solar Electricity: PV



homesolarpvpanels.com

Solar Electricity: Thermal-Mechanical

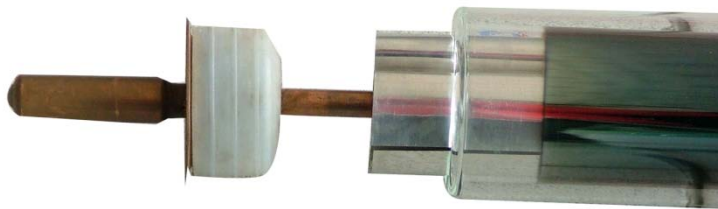


<http://www.treehugger.com/Solar-Thermal-Plant-photo.jpg>

Solar Hot Water Systems



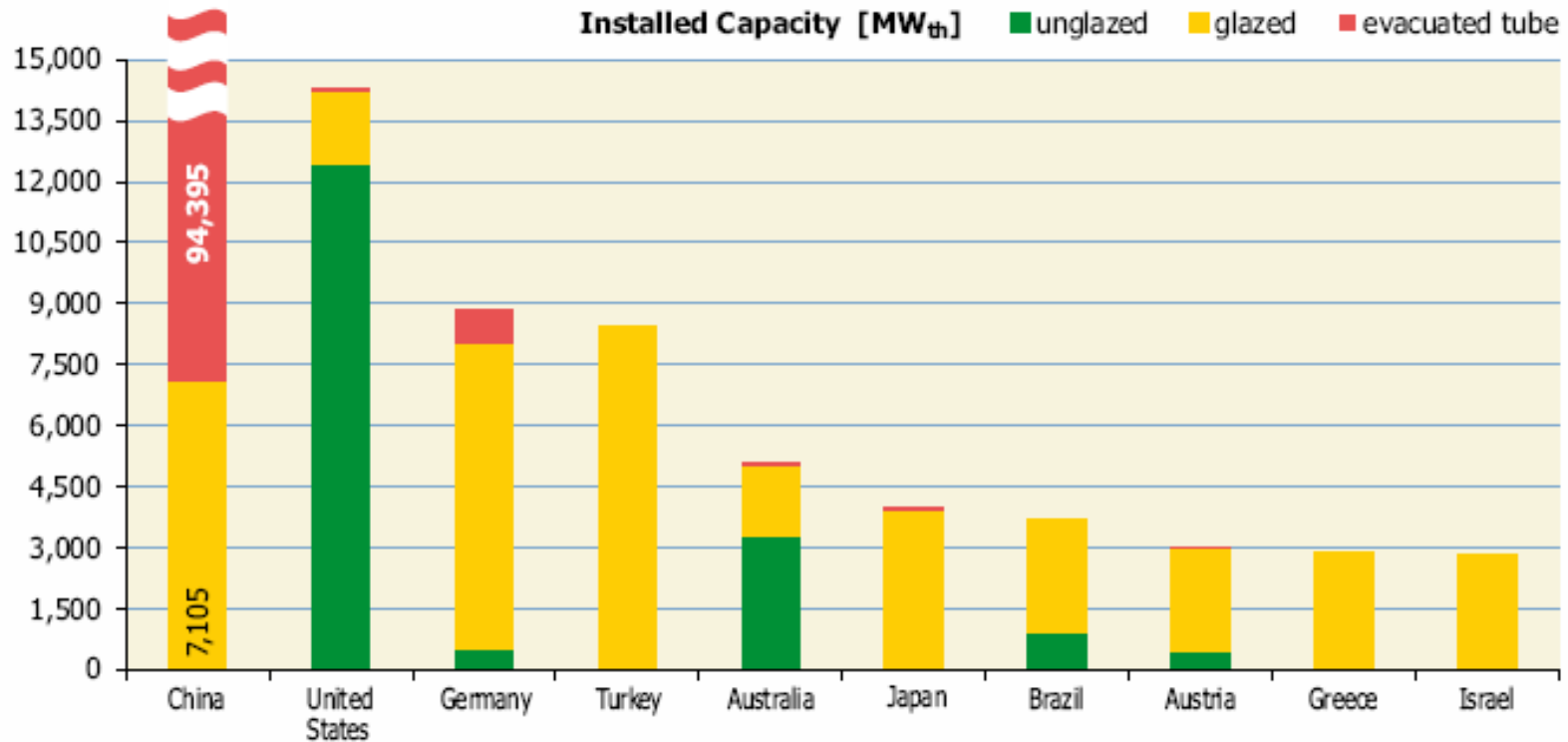
http://www.freewebs.com/solarwyse/solar_tubesspecs.html



<http://www.made-in-china.com>

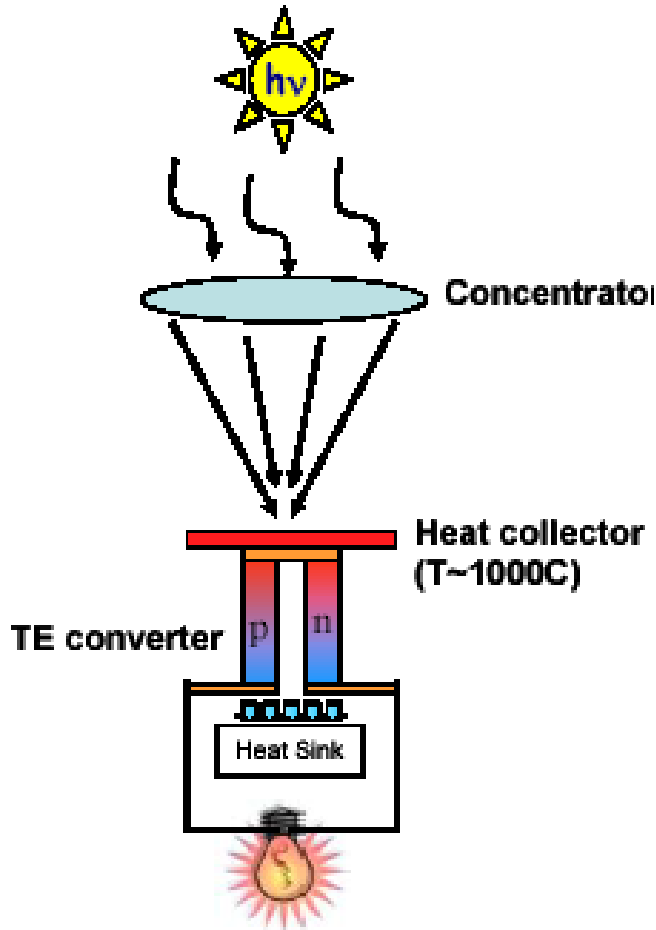


Solar Thermal Installed Capacity, 2009

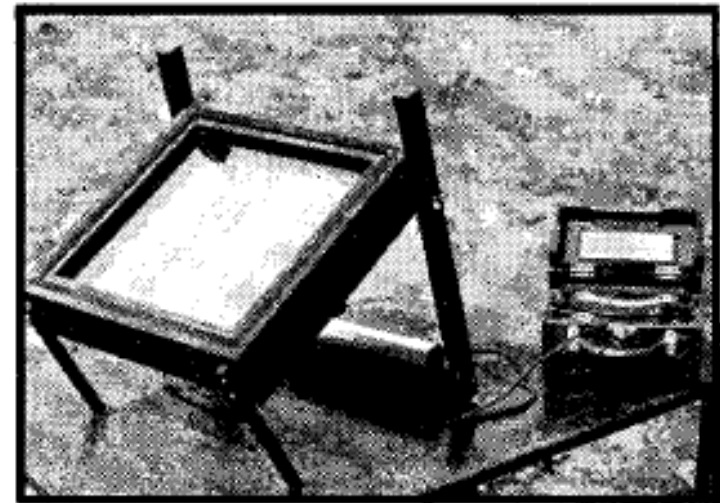


China in 2009, total of 134 Million m^2 Evacuated Tubes

Solar Thermoelectric Energy Conversion



- US Patent No. 389124:
E. Weston in 1888
- M. Telkes, JAP, 765, 1954



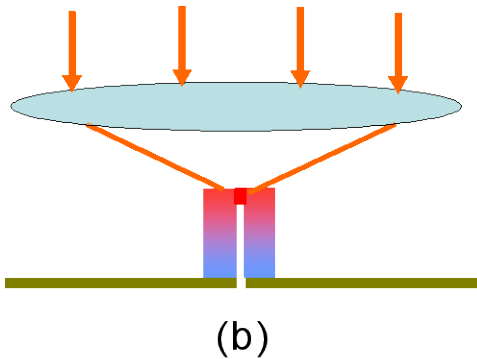
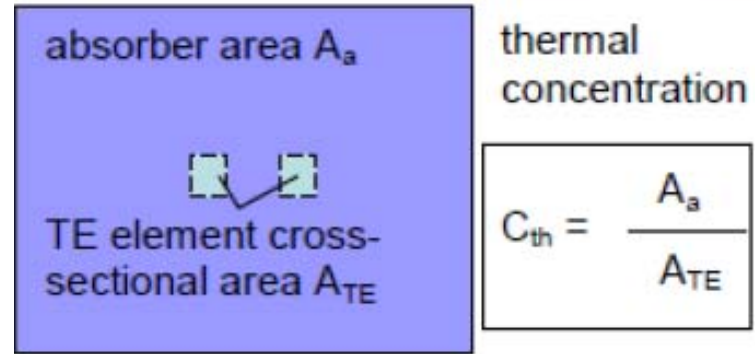
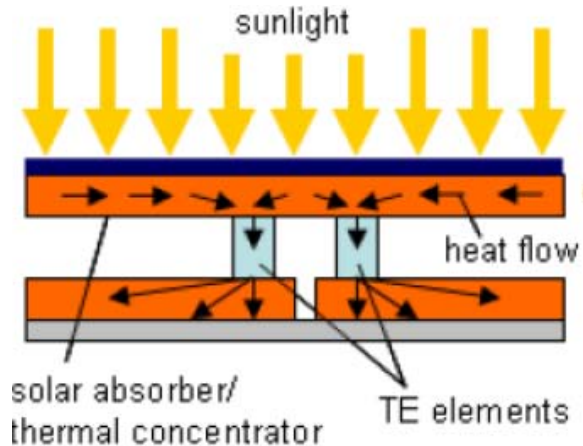
Efficiency: 0.63%

Heat Flux Consideration

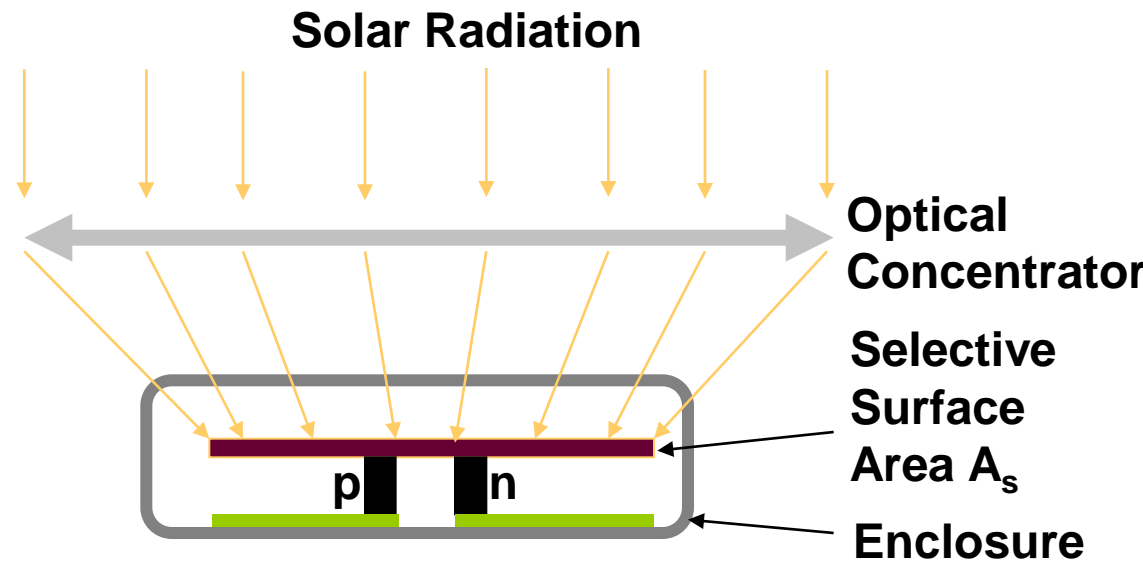
$$q = k \frac{\Delta T}{L} \approx 1 \frac{\text{W}}{\text{m} * \text{K}} \frac{100 \text{ K}}{\text{L}}$$

q=1000 W/m² (1 Sun); L=100 mm
q=100,000 W/m² (100 Sun); L=1 mm

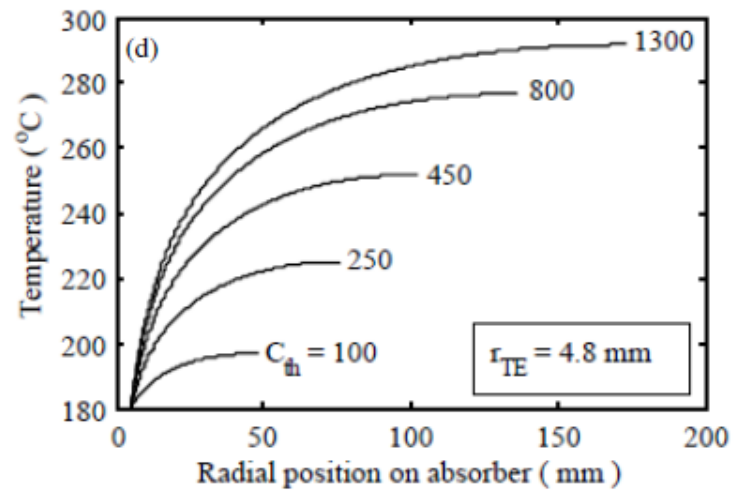
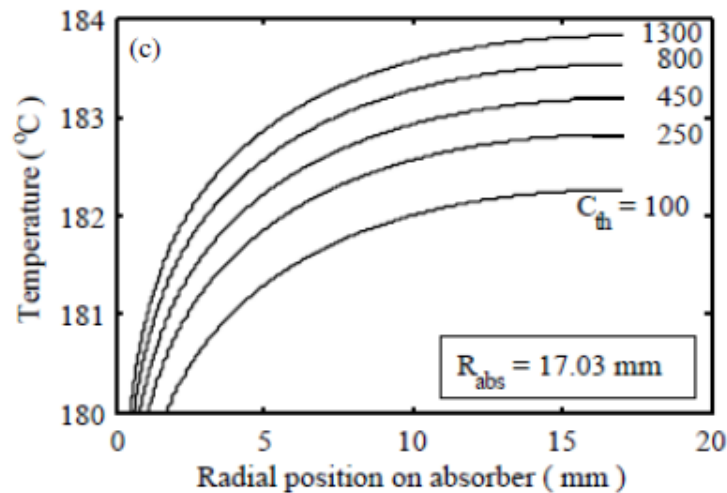
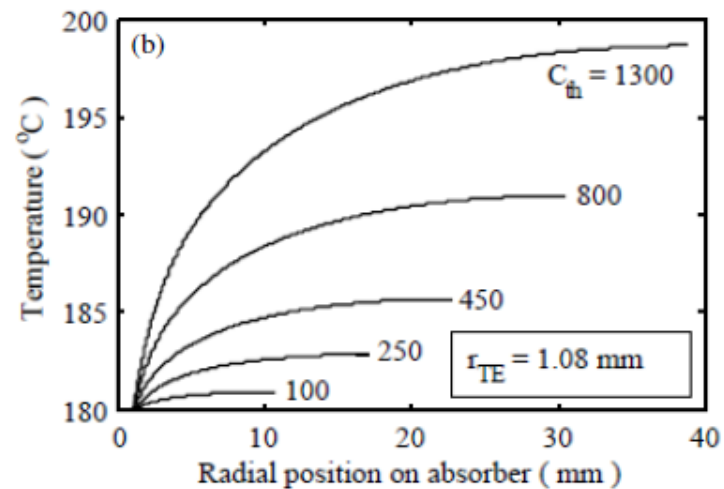
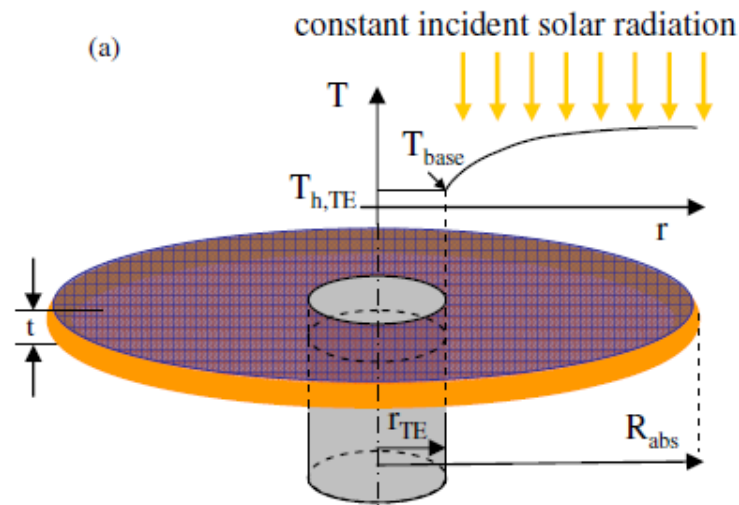
Possible Configurations



Optical Concentration



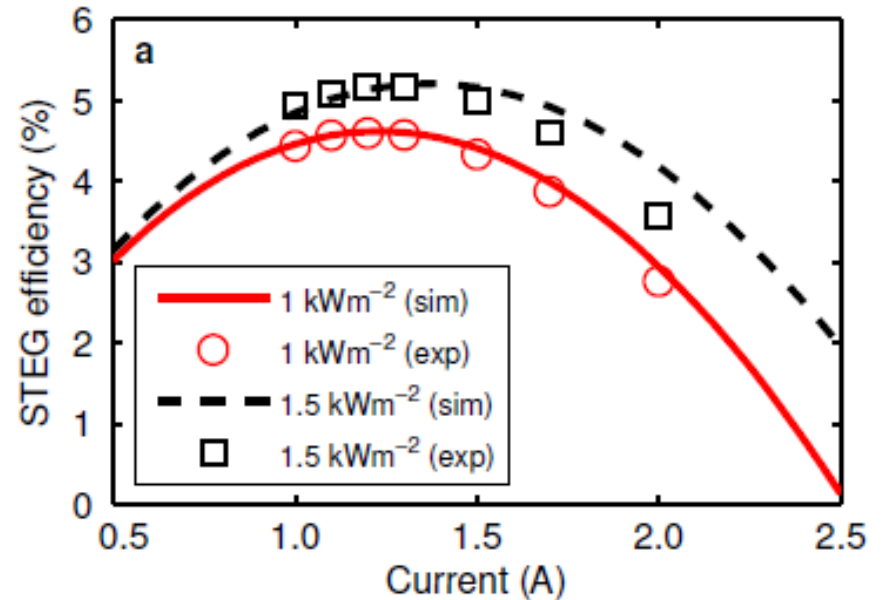
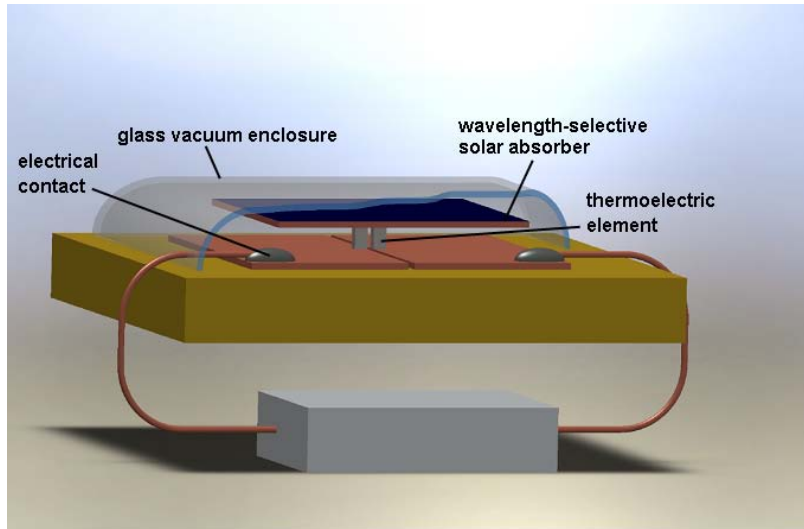
Thermal Concentration



Kraemer et al., Solar Energy, 86, 1338, 2012.

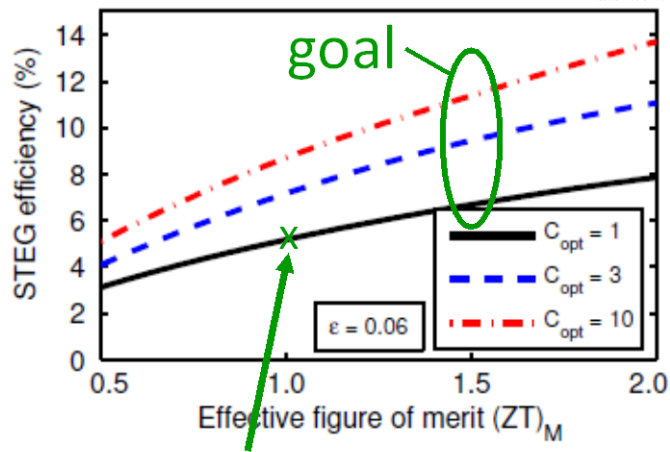
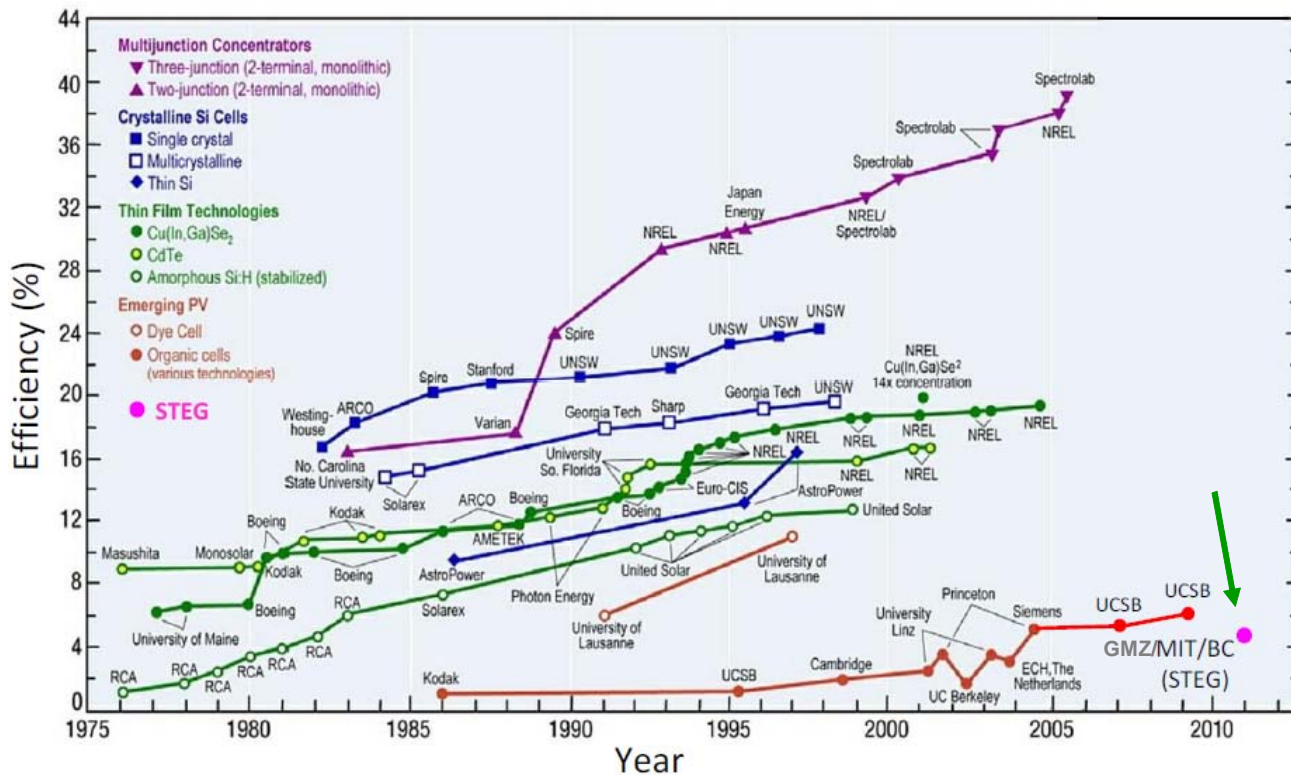


Solar Thermoelectric Power Conversion

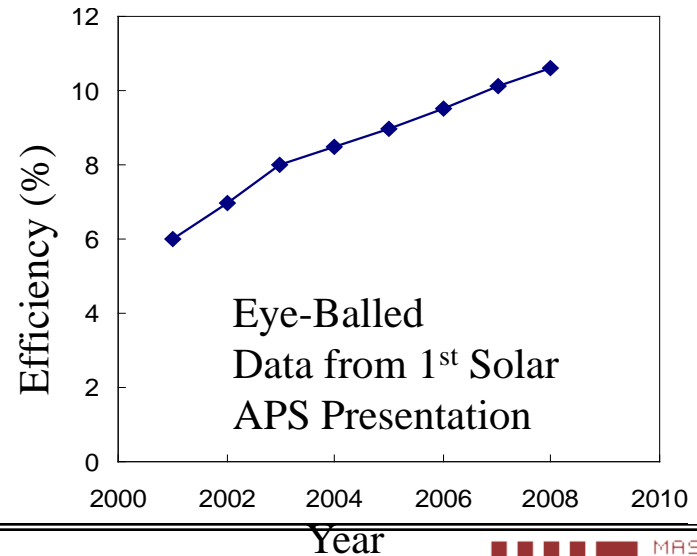


Kraemer et al., Nature Materials, 10, 523, 2011

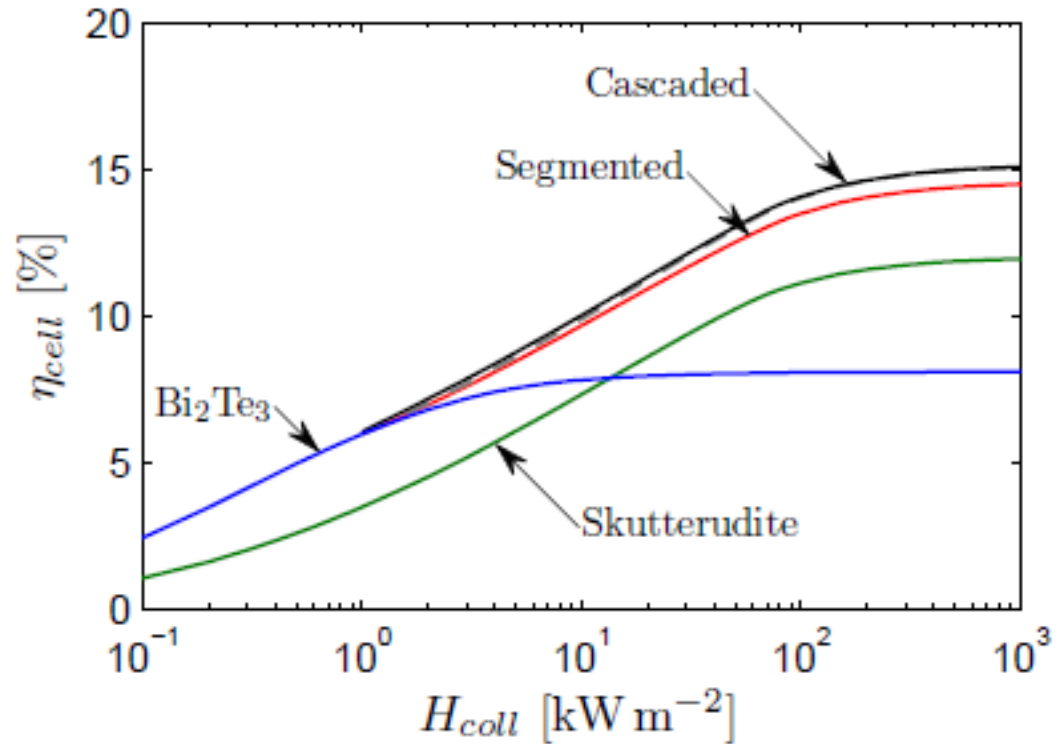
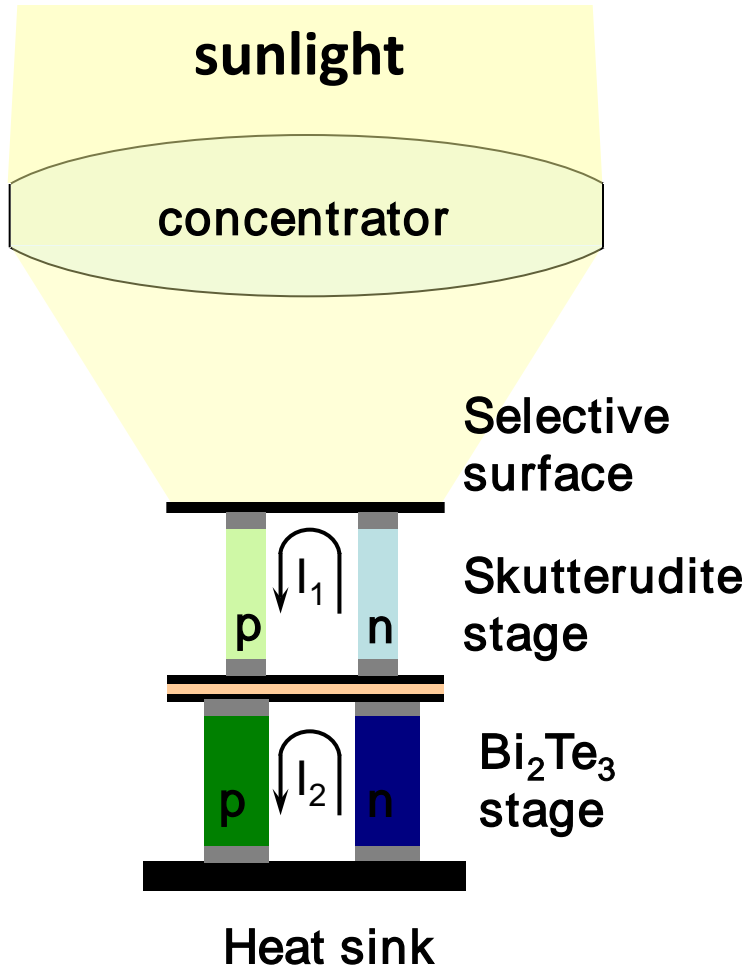




current state



Cascaded/Segmented STEGs

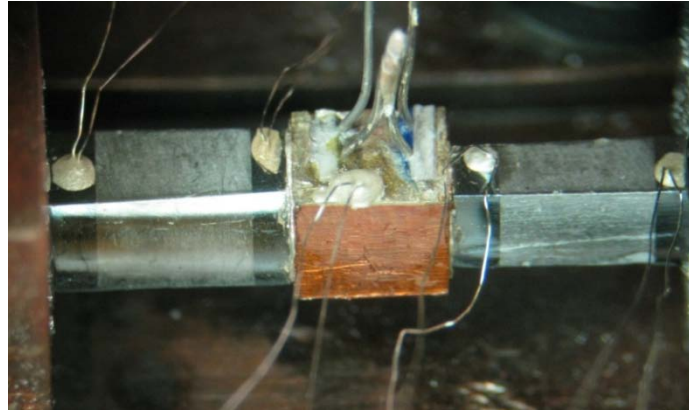


McEnaney, J. Appl. Phys., 110, 074502, 2011.

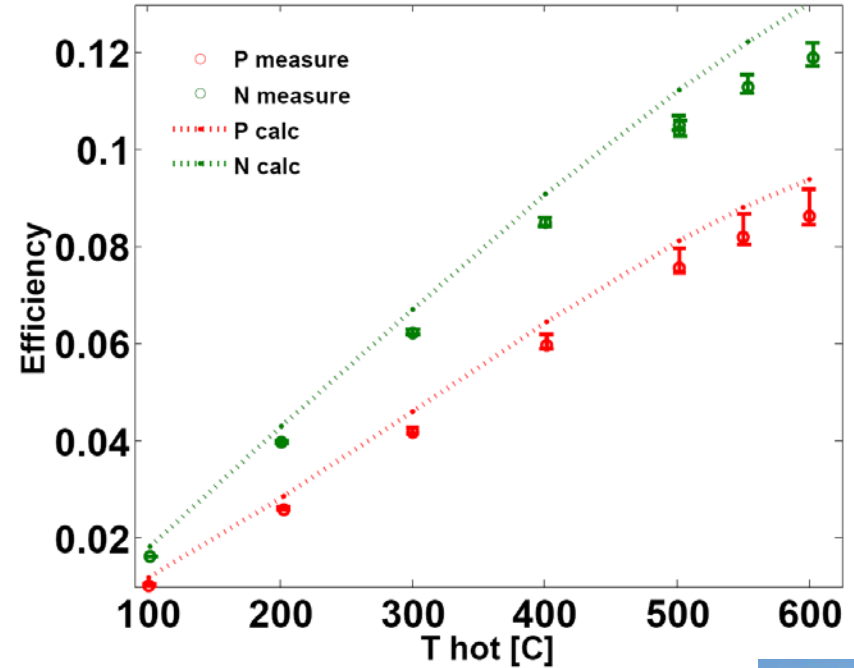
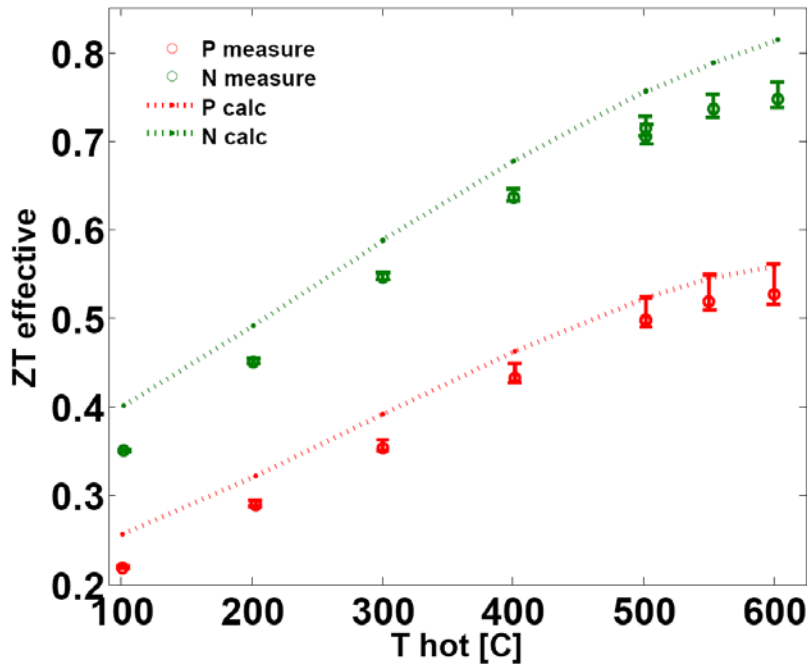


Skutterudites

N-type: $ZT_{\text{eff}} = .75$
P-type: $ZT_{\text{eff}} = .5$



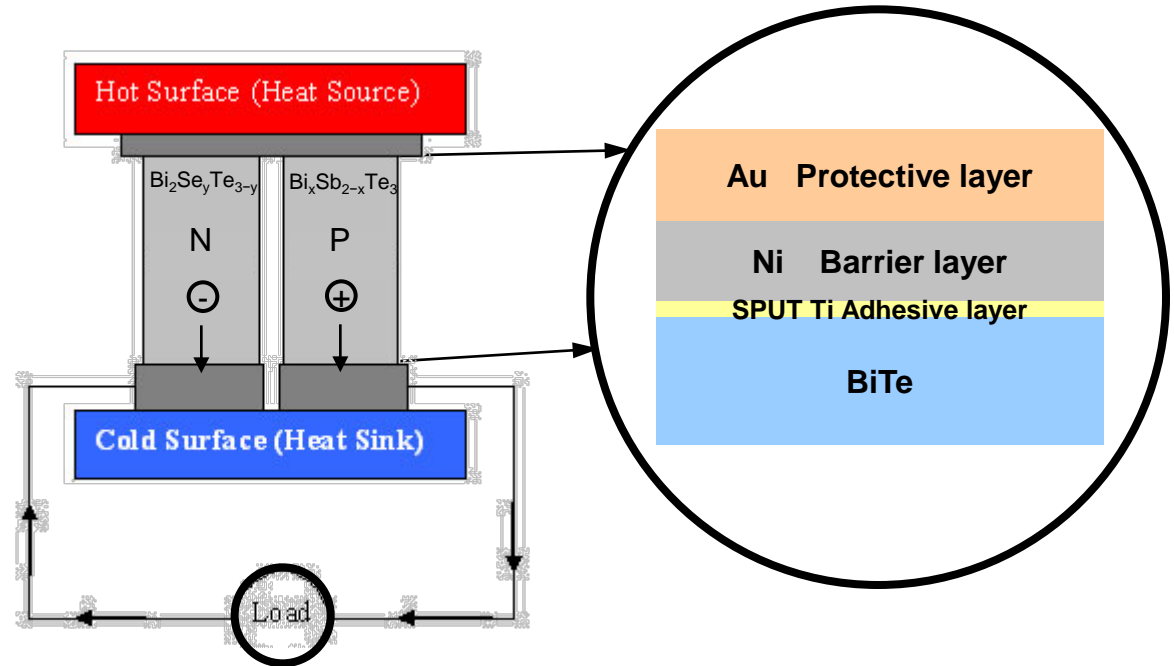
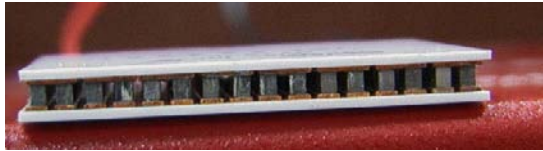
N-type: 12%
P-type: 8.5%
Pair: 9.1%



Muto et. al., Adv. Energy Materials, September, 2012.



Key Challenges in Devices



- Diffusion barriers
- Bonding strength
- Thermal stress
- Electrical contact resistance
- Thermal contact resistance

Summary

- Contra-properties in ZT: great challenges in understanding electron and phonon transport,
- Nanostructures provide new knobs to improve ZT, and significant progresses have been made in materials,
- Thermoelectric devices raise new challenges: thermal, mechanical, and electrical coupling,
- Ample room in system innovation, taking existing materials into real world.

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Gene Fitzgerald Group
Keith Nelson Group
David Singh Group**



**SOLID-STATE SOLAR-THERMAL
ENERGY CONVERSION CENTER**



**U.S. DEPARTMENT OF
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