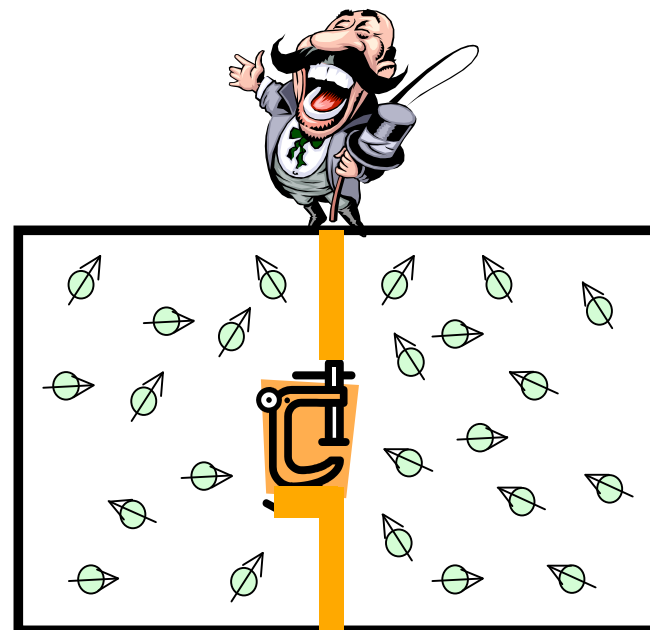
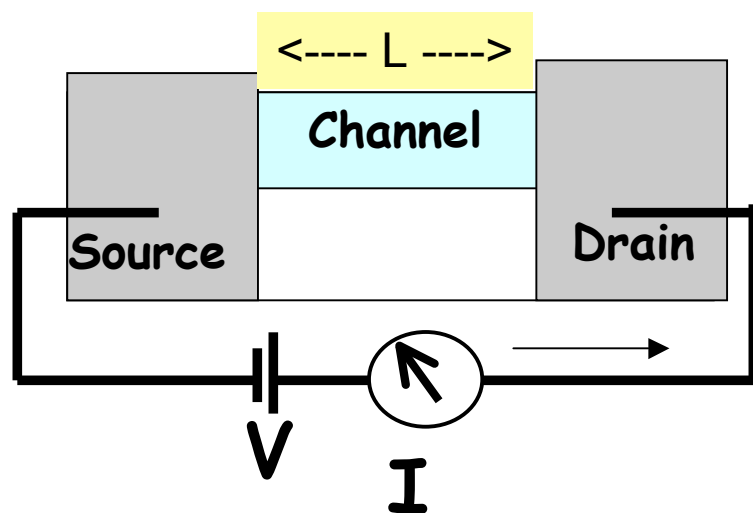


# Nanodevices & Maxwell's demon

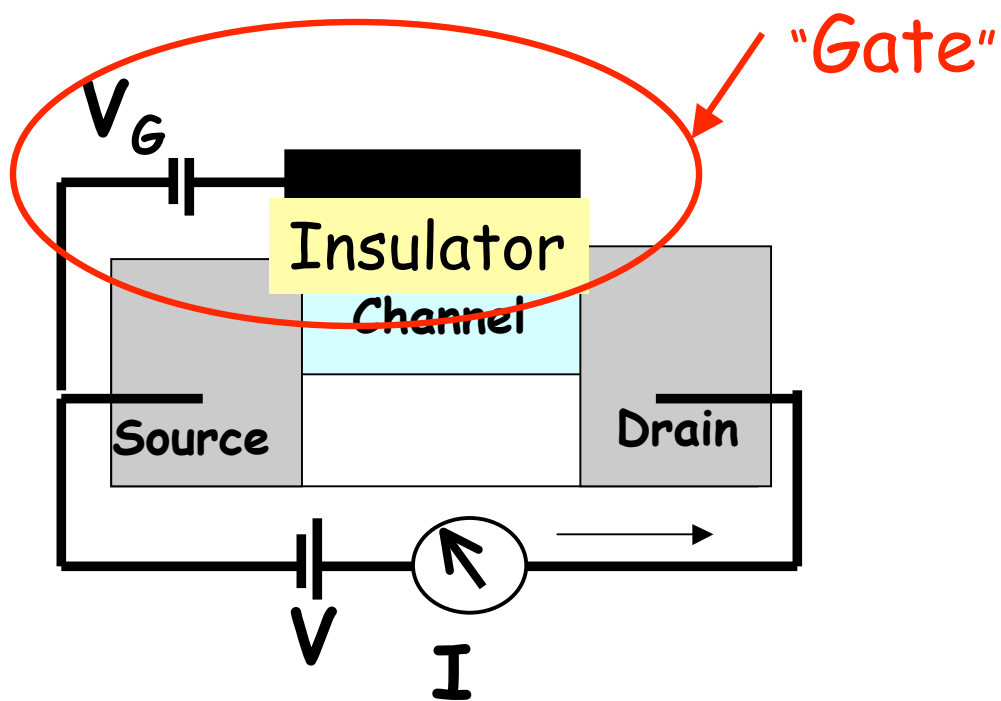


McCoy Lecture, Purdue  
September 26, 2006

# Nanodevices

&

# Maxwell's demon

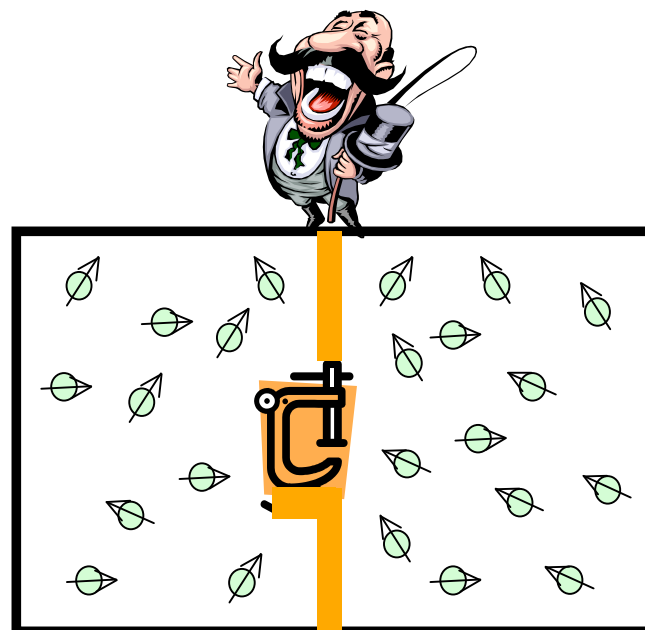
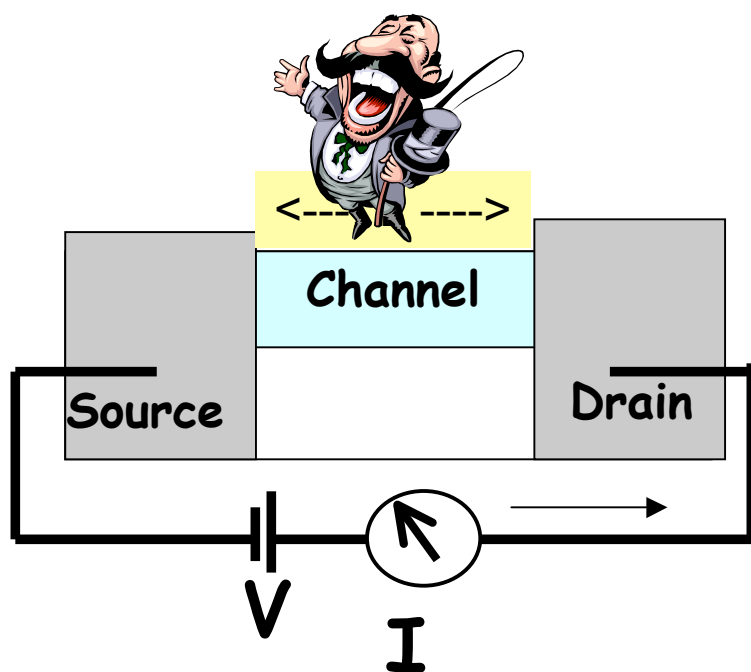


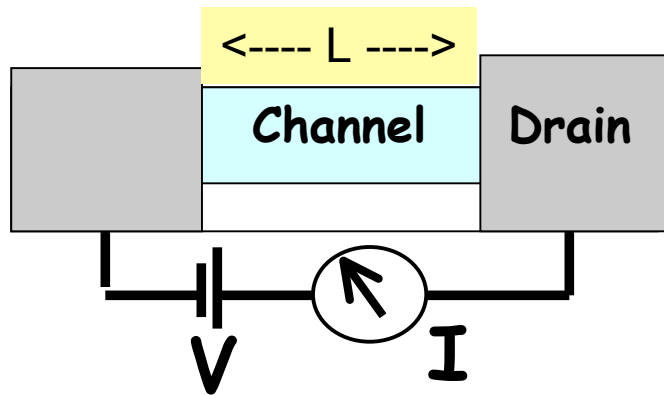
Transistor

# Nanodevices

&

# Maxwell's demon



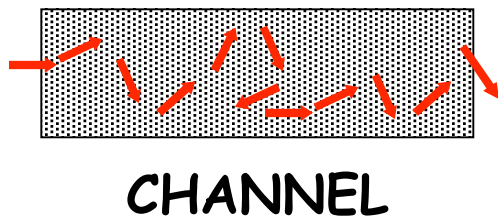
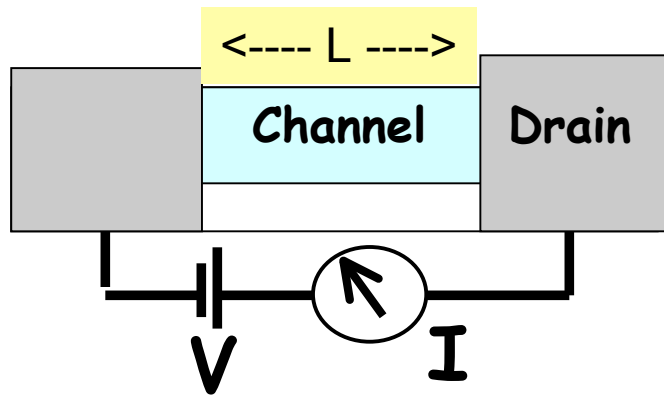


$$V = I R \quad \text{or} \quad I = V G$$

$$\text{Conductance, } G = 1/R$$

$$G = \sigma A / L$$

Conductivity



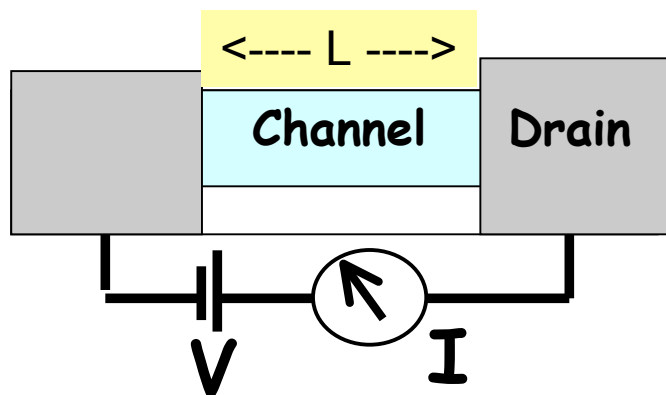
$$V = I R \quad \text{or} \quad I = V G$$

$$\text{Conductance, } G = 1/R$$

$$G = \sigma A / L$$

Conductivity

$$\sigma = q^2 n \tau / m$$



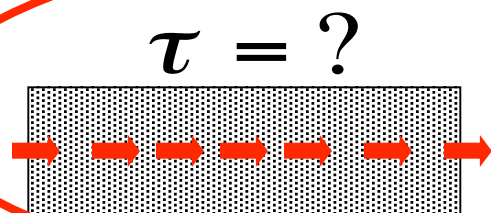
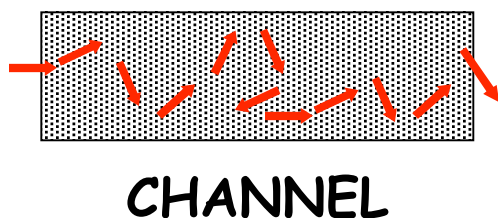
$$V = I R \quad \text{or} \quad I = V G$$

$$\text{Conductance, } G = 1/R$$

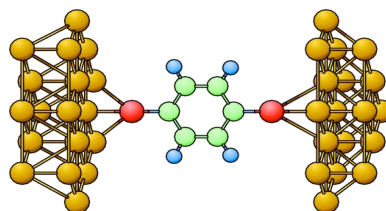
$$G = \sigma A / L$$

Conductivity

$$\sigma = q^2 n \tau / m$$



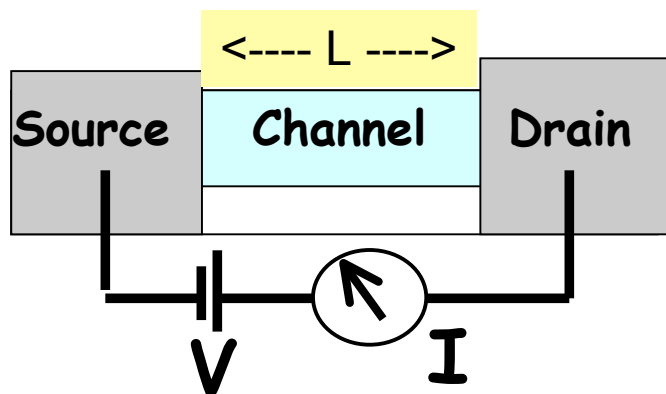
$$m = ? \quad n = ?$$



"Very complicated"

## Bottom-up View

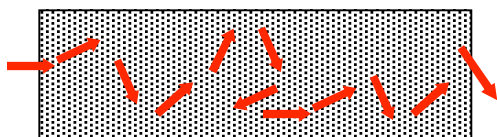
"Top"



Ohm's law

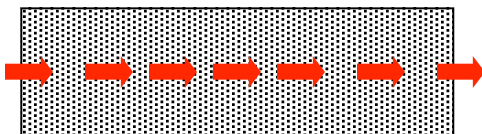
$$I = GV \quad , \quad G = \sigma A / L$$

$\gamma \equiv \text{escape rate}$



$$G = (q^2 / h) (\pi D \gamma)$$

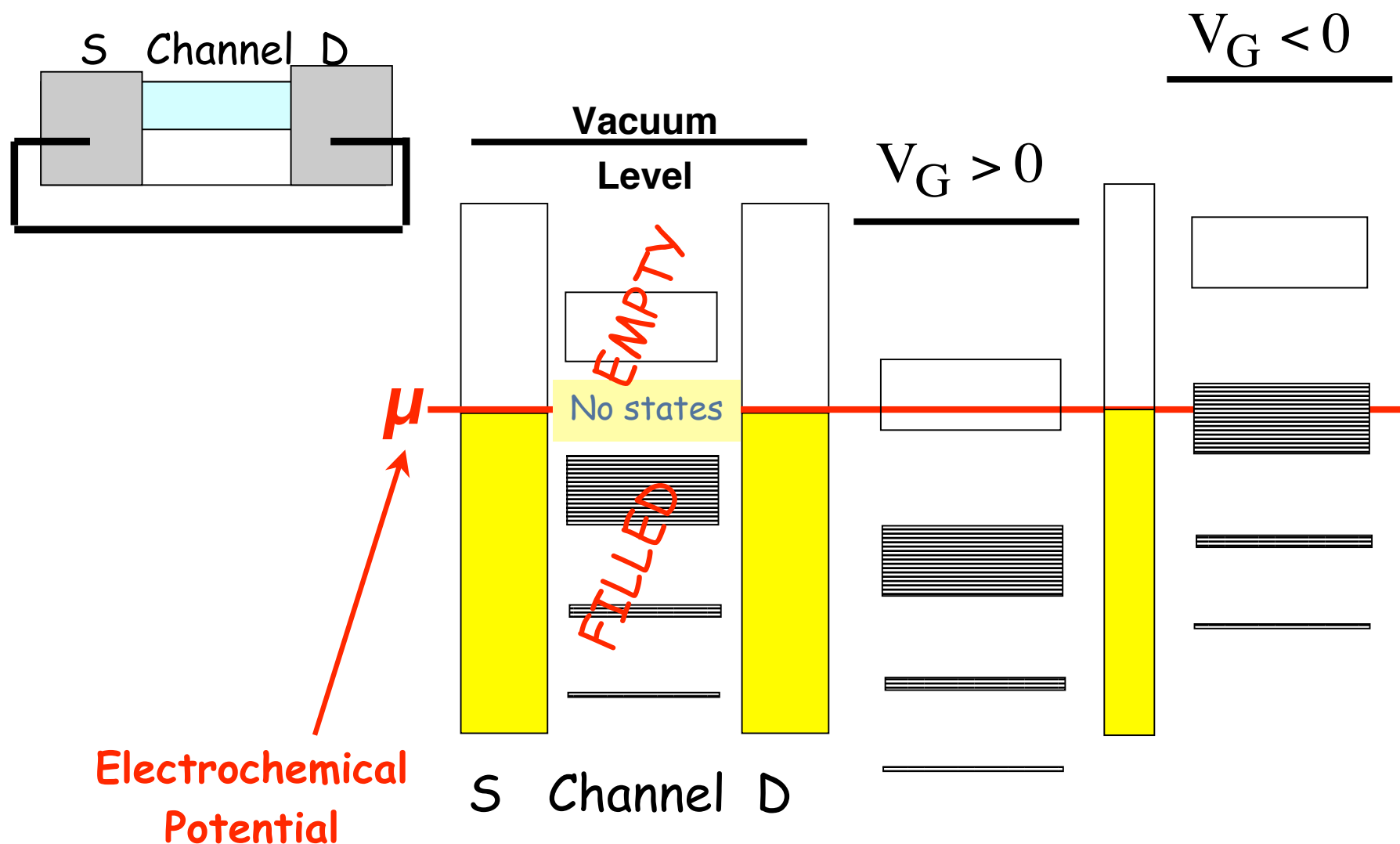
CHANNEL



$$G = \underbrace{(q^2 / h)}_{1 / 25.8 \text{ K}\Omega}$$

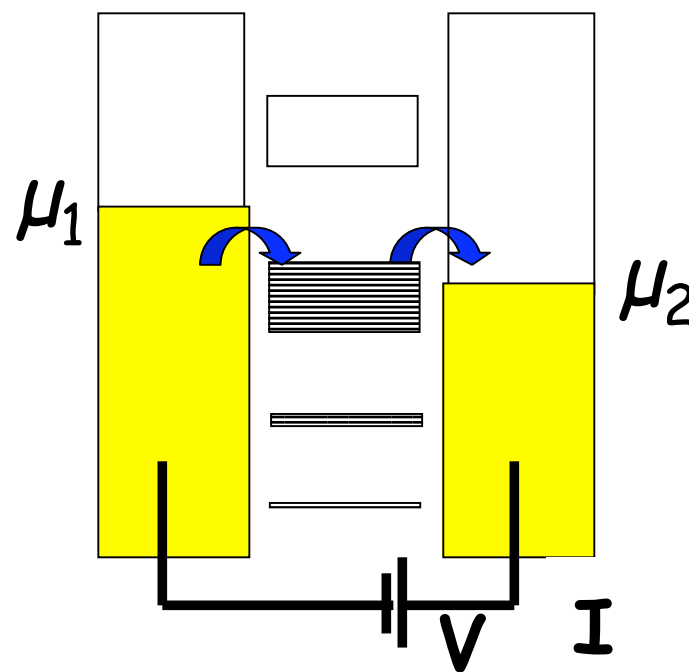
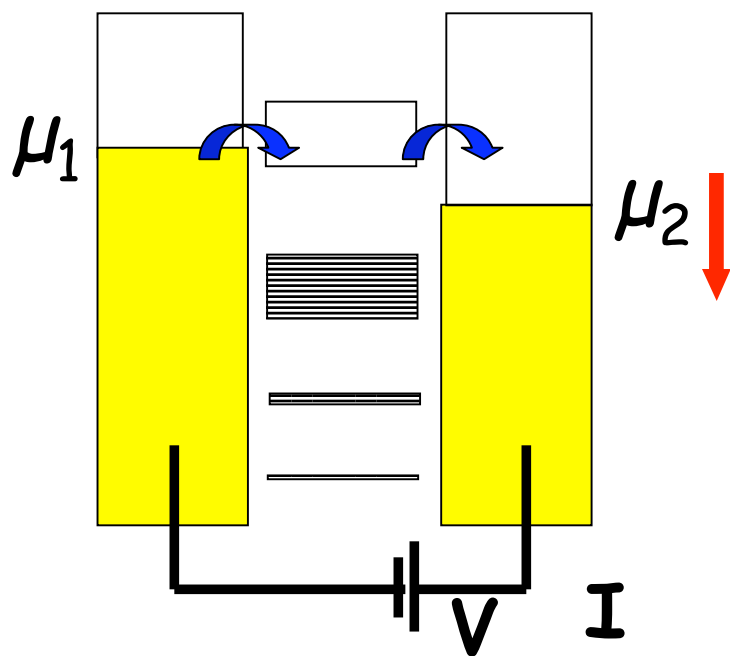
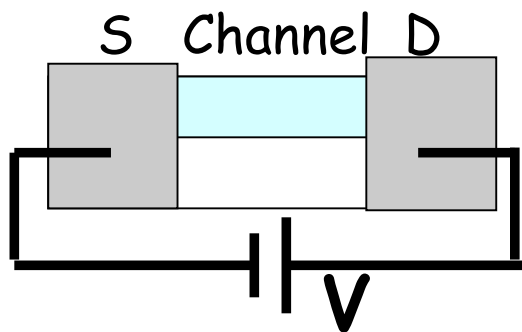
"Bottom"

# Equilibrium Energy Level Diagram



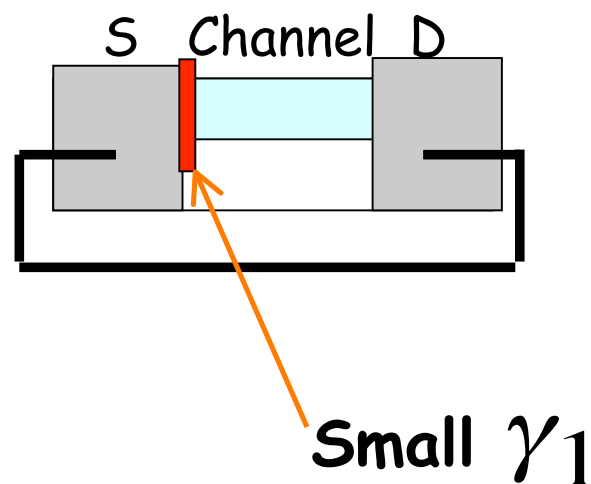
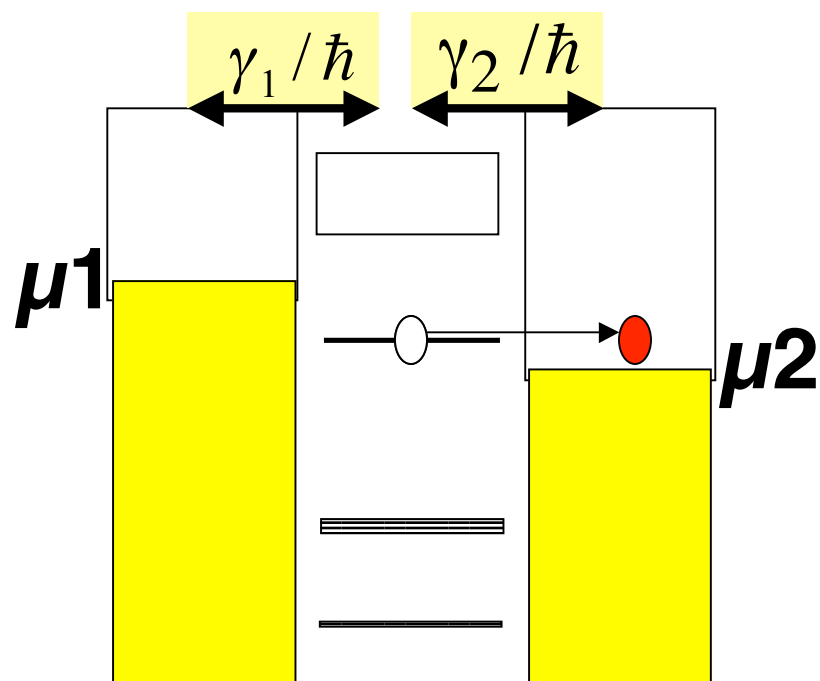


# What makes electrons flow?

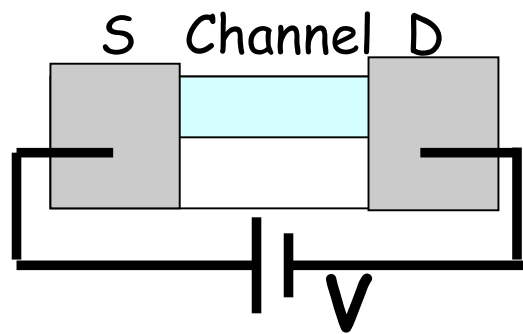


$\gamma / \hbar$  : *Escape Rate*

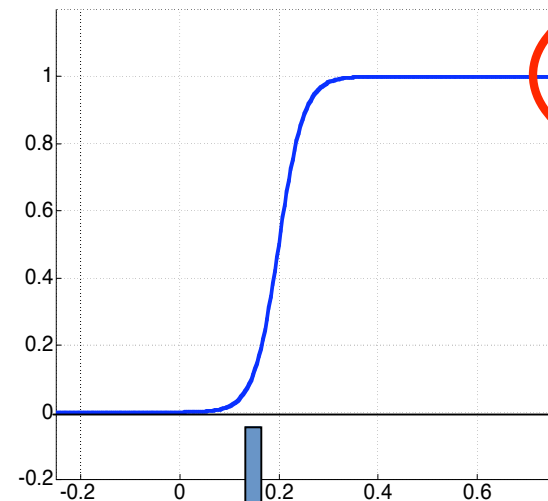
$\gamma$  has dimensions of energy



# Current through a very small conductor

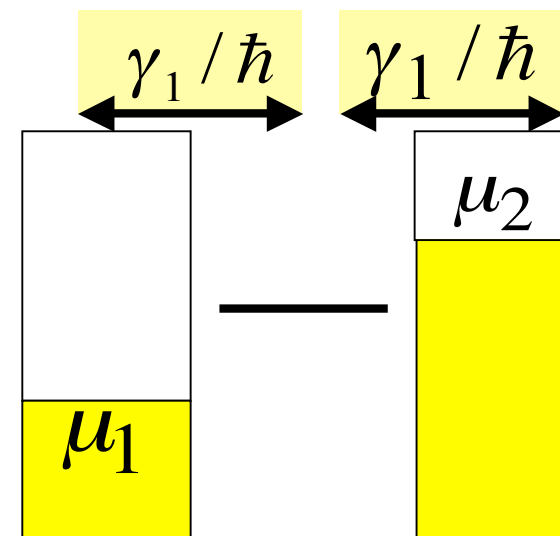
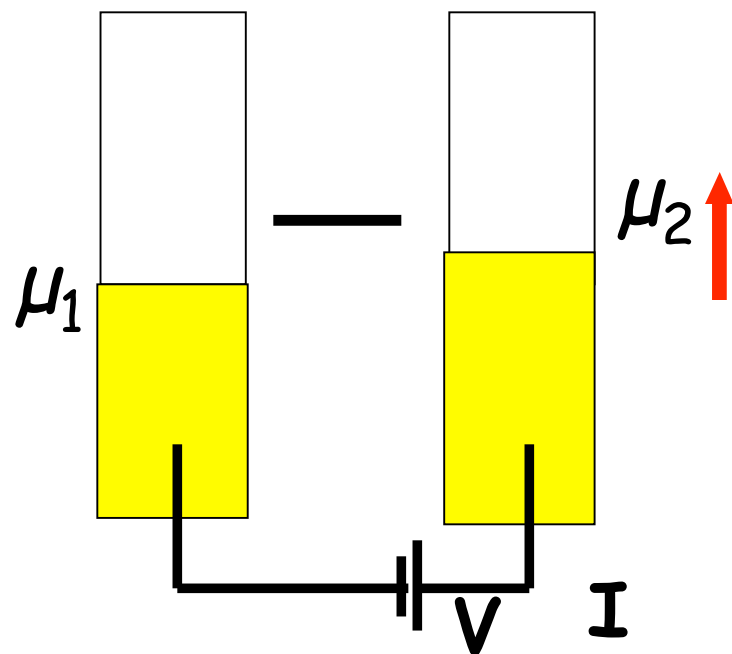


Normalized  
Current

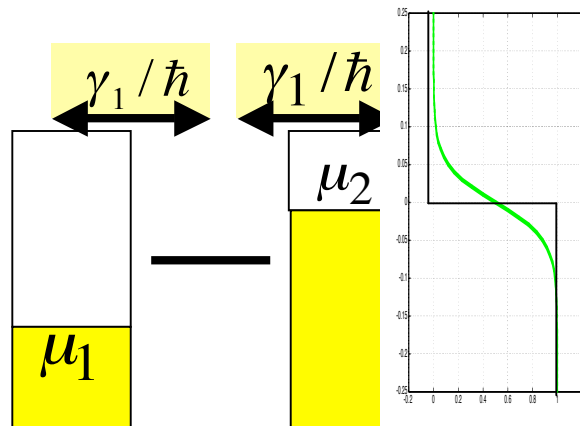


$$\frac{q\gamma_1}{2\hbar}$$

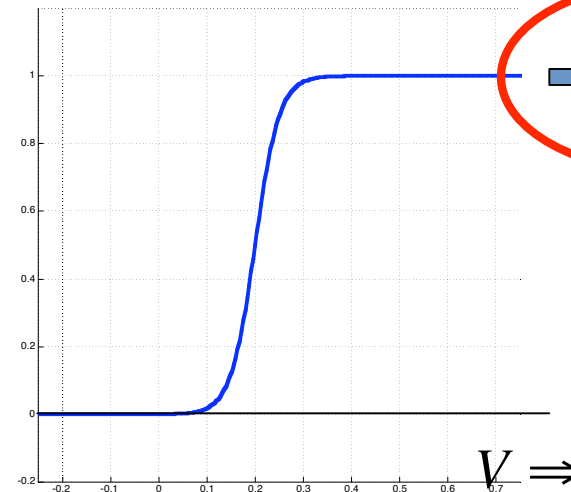
$V \Rightarrow$



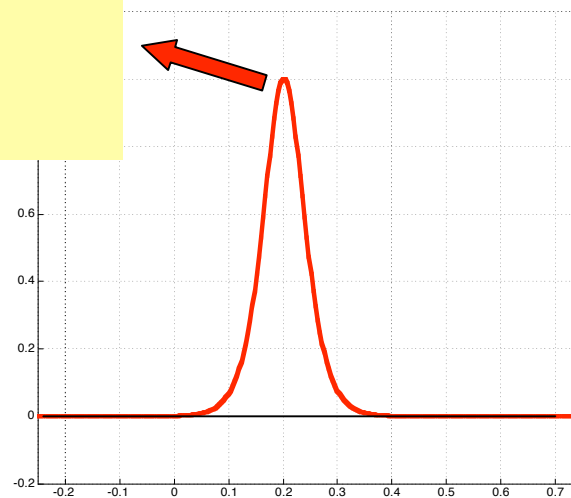
# Conductance quantum



Normalized  
Current

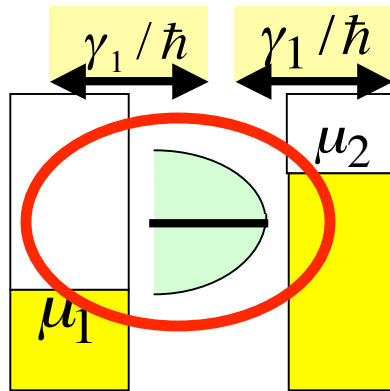


$$\frac{dI}{dV} \sim \frac{q\gamma_1/2\hbar}{4kT}$$

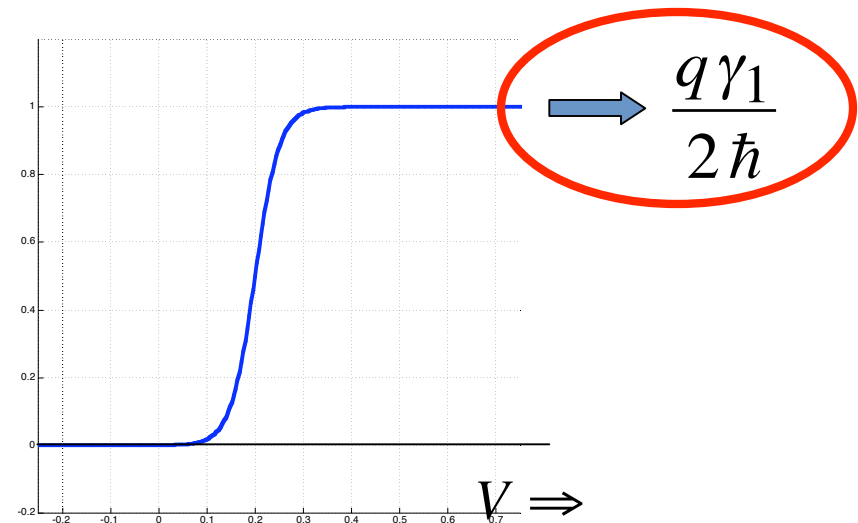


Normalized  
Conductance

# Conductance quantum



Normalized  
Current

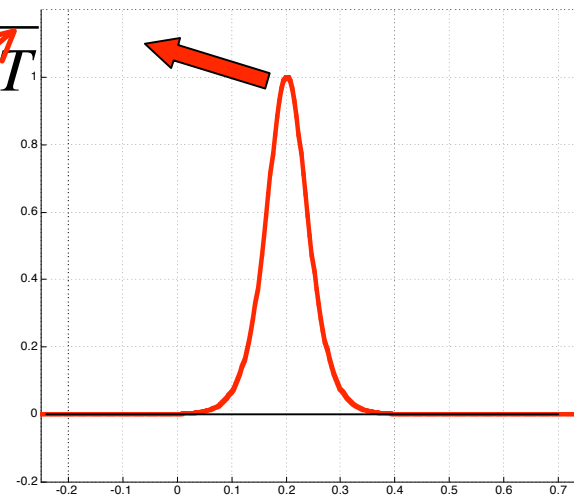


$$\frac{dI}{dV} \sim \frac{q\gamma_1/2\hbar}{2\gamma_1 + 4kT}$$

$$\sim q^2/4\hbar \quad \text{if} \quad \gamma_1 \gg kT$$

Conductance quantum

$$\sim q^2/2\pi\hbar \sim 1/25.8 \text{ K}\Omega$$

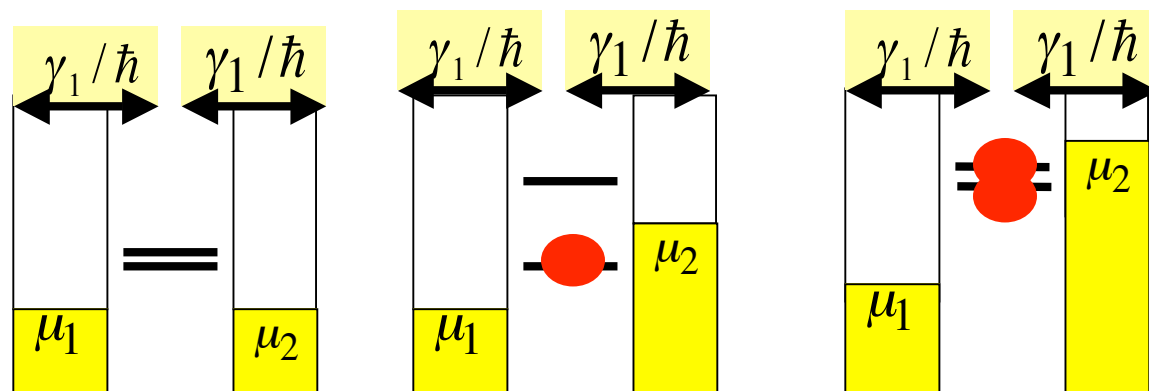


Normalized  
Conductance

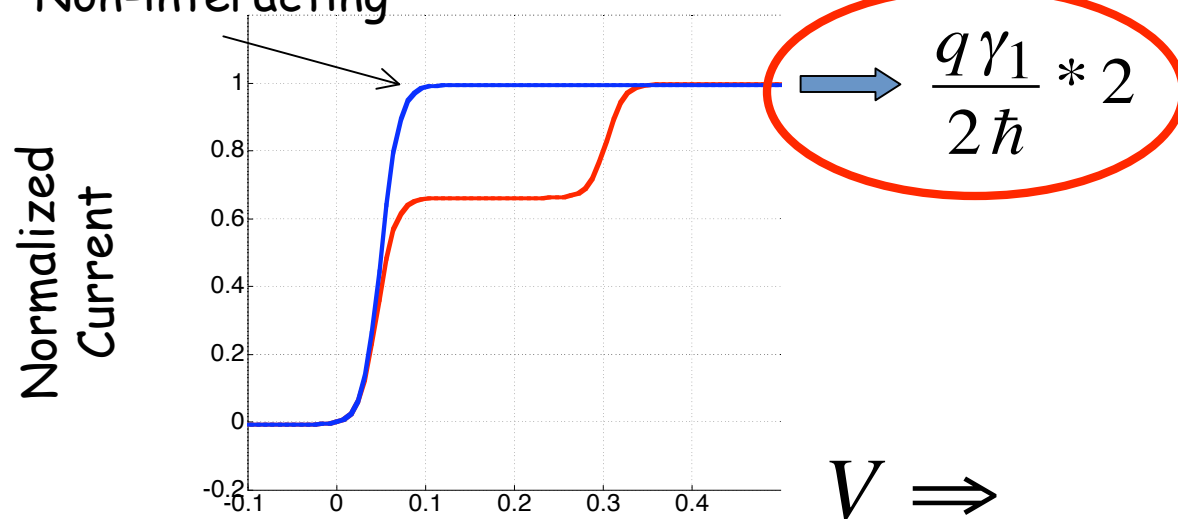
# Single electron charging

$U_0$  : Increase in potential due to SINGLE electron  
 $\gg \gamma, kT$

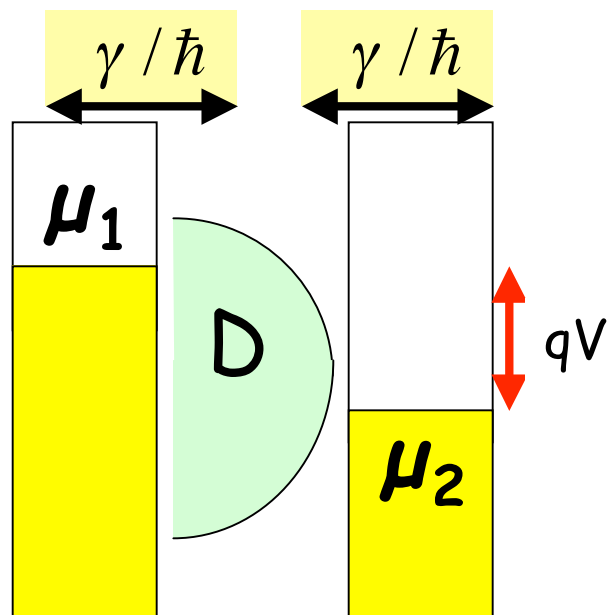
"Self-interaction Correction"



Non-interacting



# Conductance: The bottom line



$$I \sim \underbrace{\frac{q\gamma}{2\hbar}}_{\text{Current per state}}$$

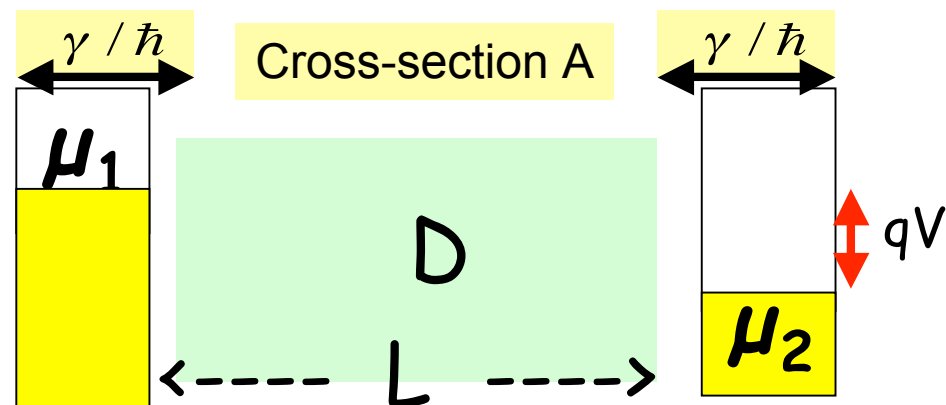
D: Density of states

$$\frac{I}{V} = \underbrace{\frac{q^2}{2\pi\hbar}}_{\text{Conductance Quantum}} \underbrace{\langle \pi D \gamma \rangle}_{\text{Transmission}}$$

# Ohm's Law

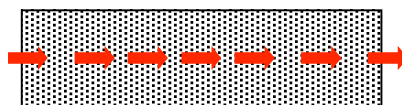
$$I/V = \frac{q^2}{2\pi\hbar} \langle \pi D \gamma \rangle$$

$$\frac{D}{\text{eV}} = \underbrace{N_0}_{\text{eV-m}^3} \underbrace{AL}_{\text{m}^3}$$



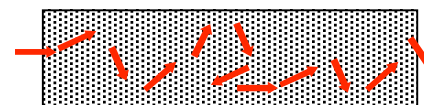
Can  
show  
that

Ballistic



$$\gamma \sim \frac{\hbar v}{L} \rightarrow D\gamma \sim A$$

Diffusive

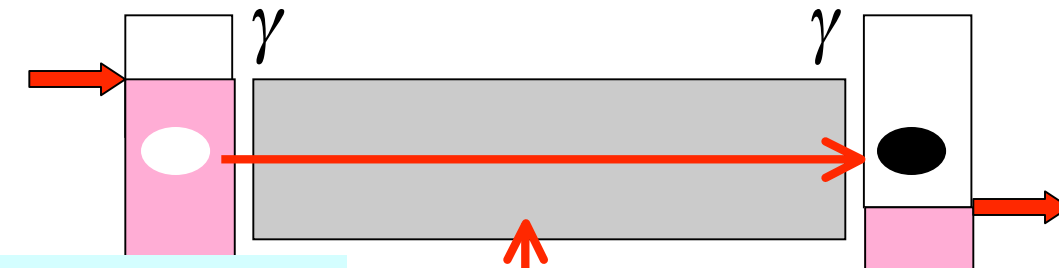
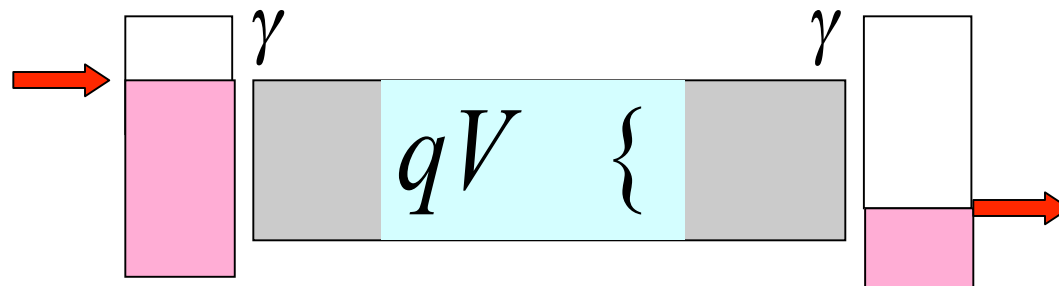
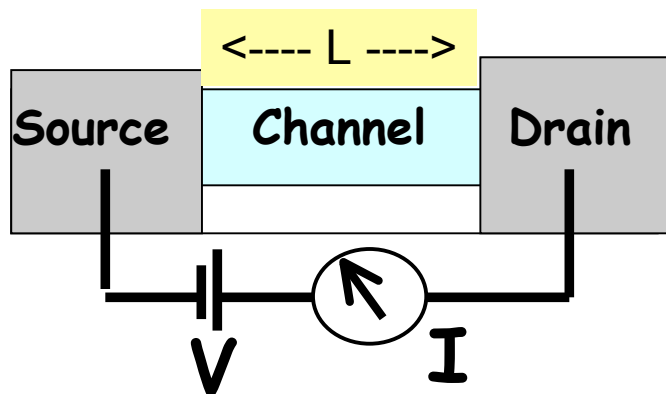


$$\gamma \sim \frac{2\hbar D}{L^2} \rightarrow D\gamma \sim A/L$$



# Where is the power dissipated ?

$$Power = V I$$



Dissipation

Dissipation

Contacts assumed  
to remain in equilibrium

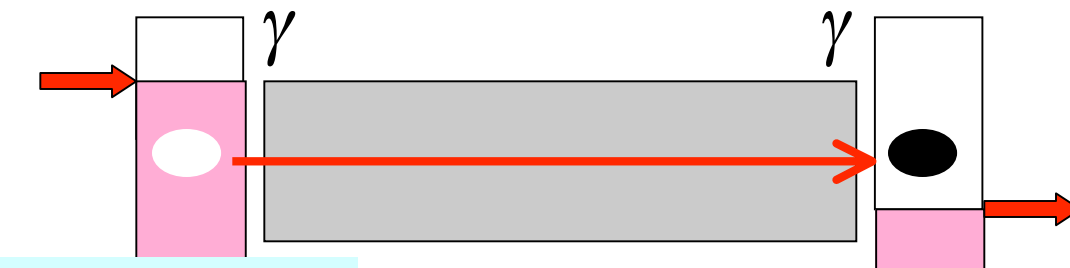
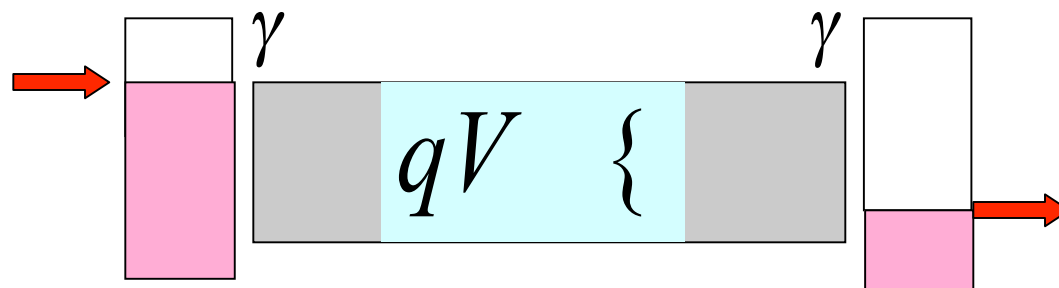
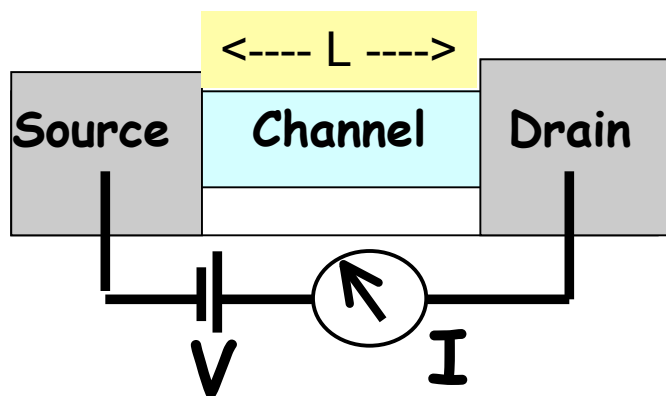
Thermodynamics

Newton's law  
Schrodinger equation

Dynamics

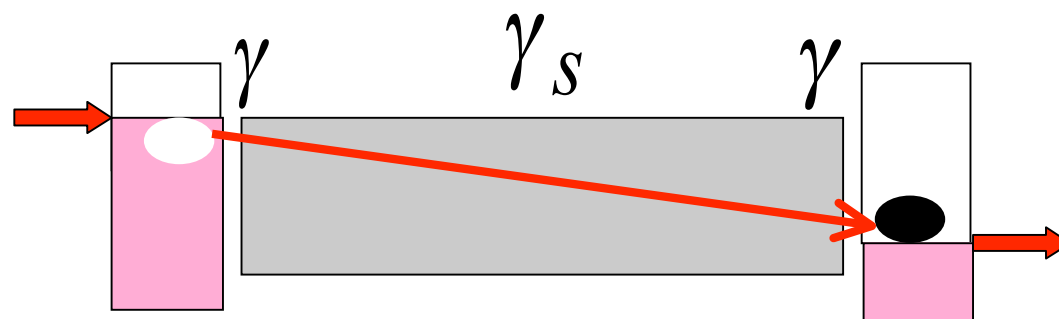
# Where is the power dissipated ?

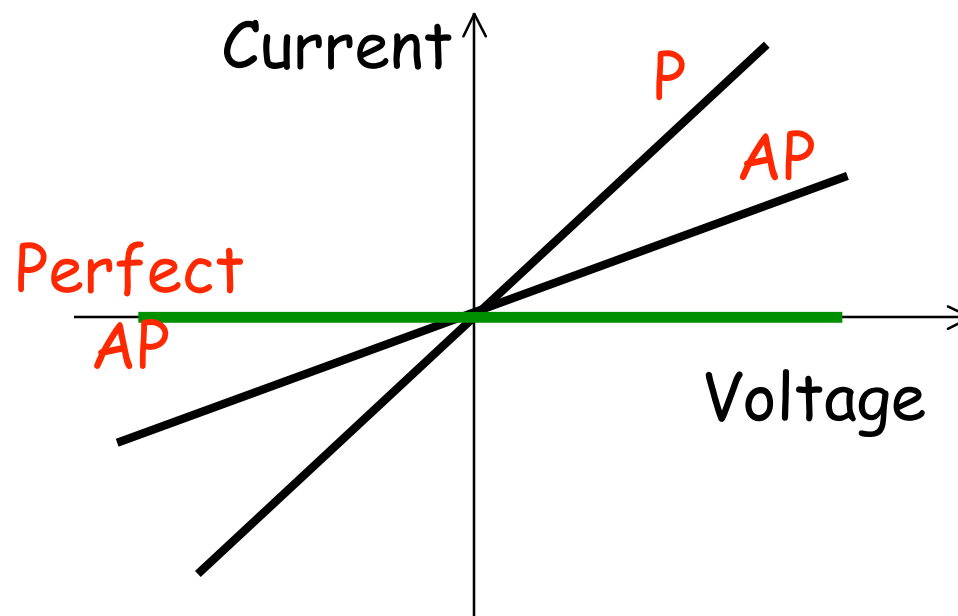
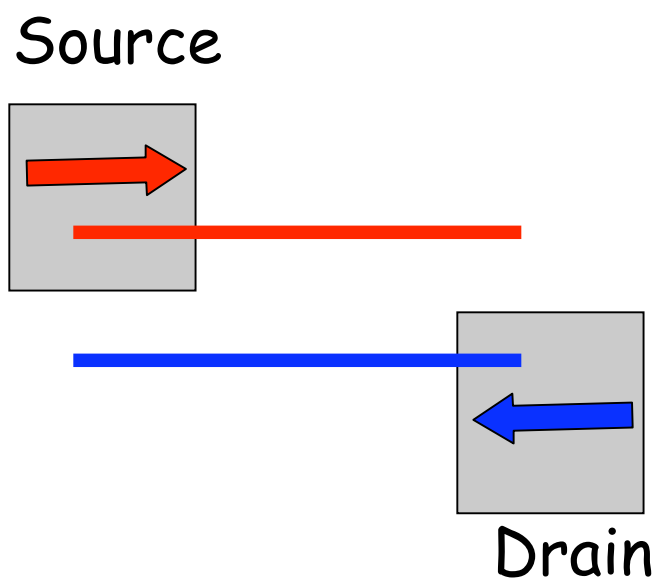
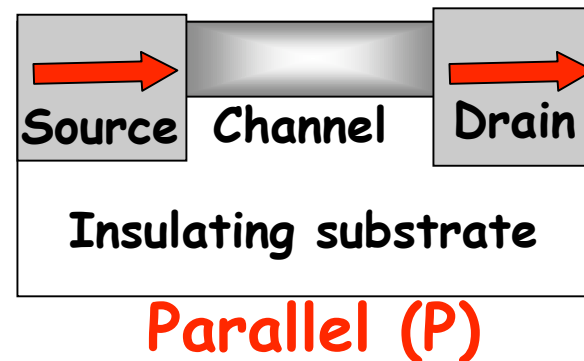
$$Power = V I$$



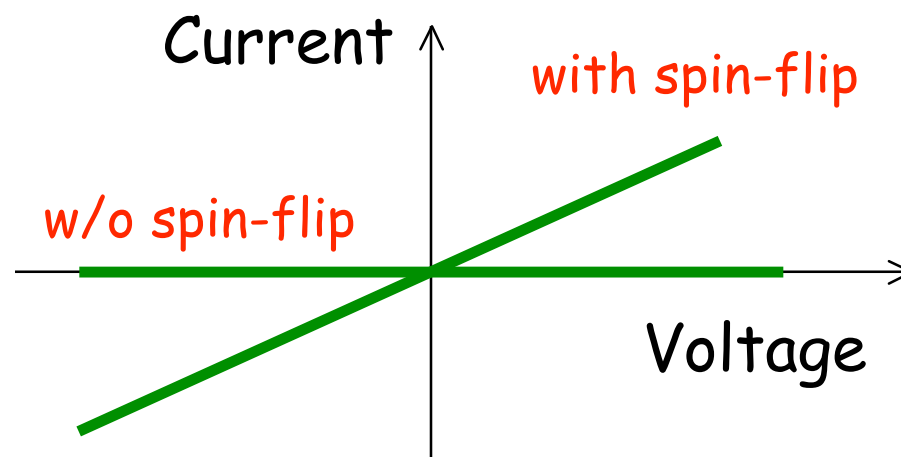
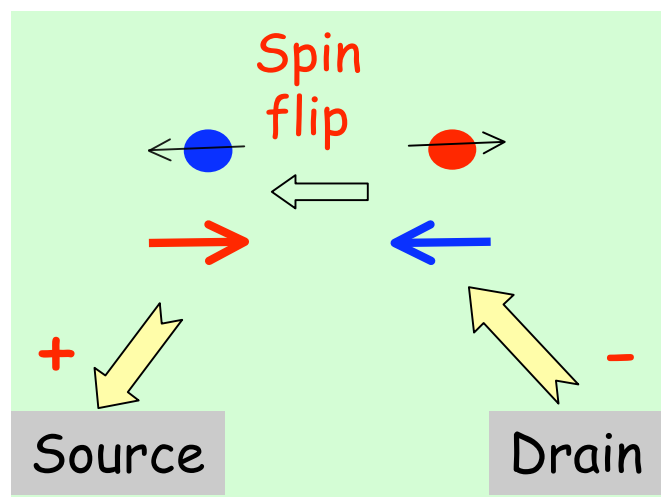
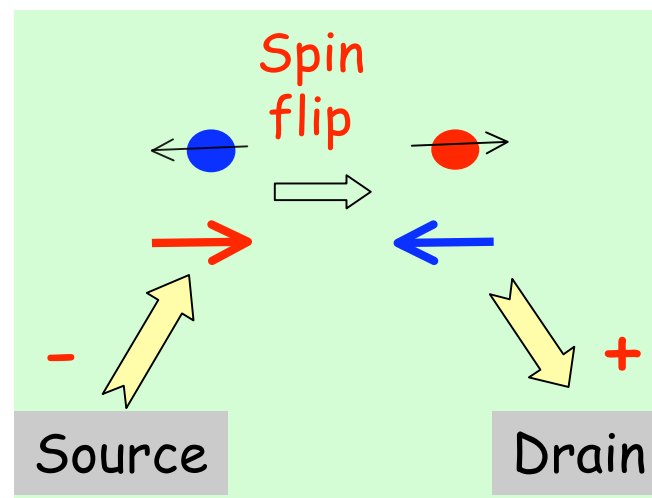
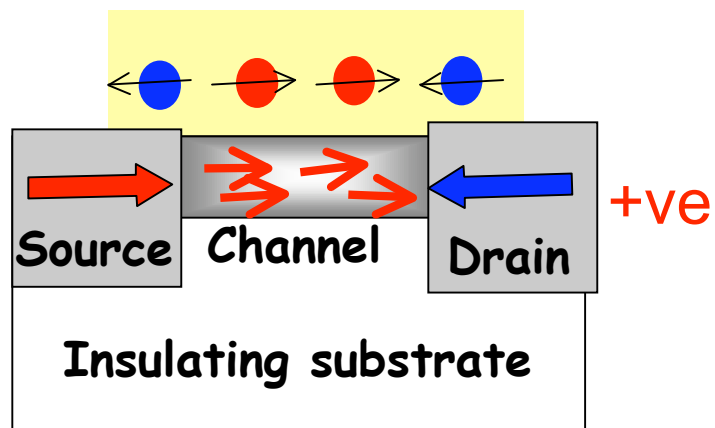
Dissipation

Dissipation

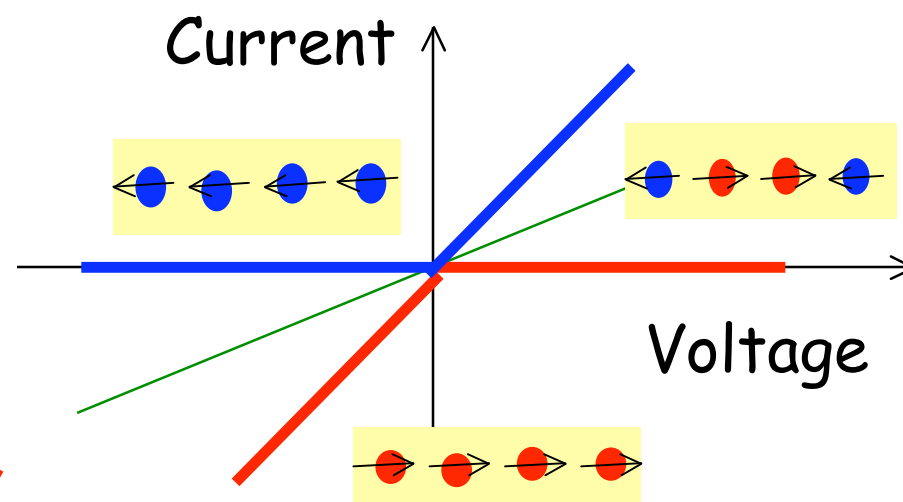
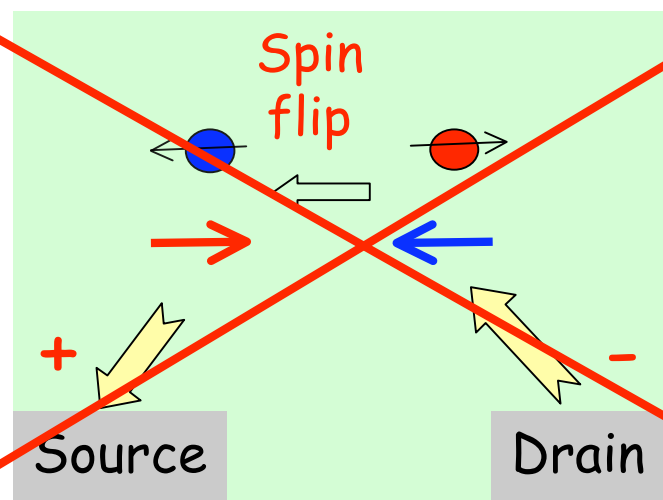
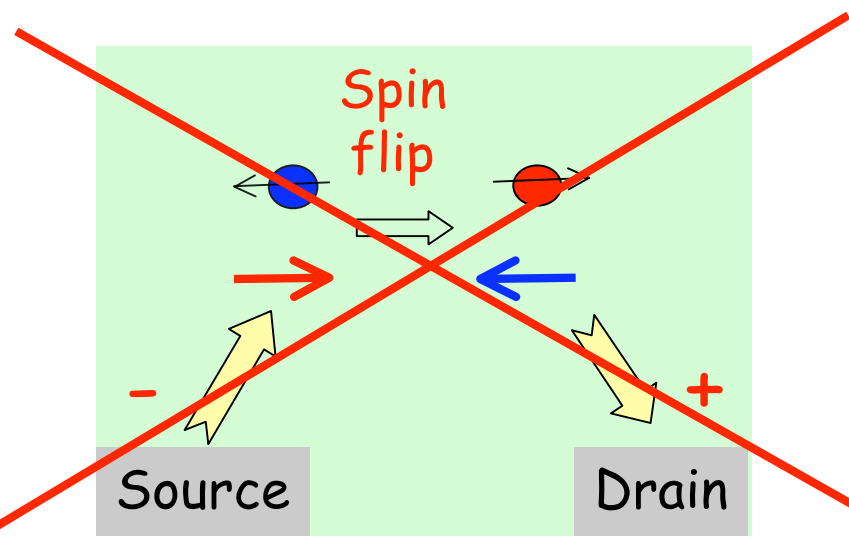
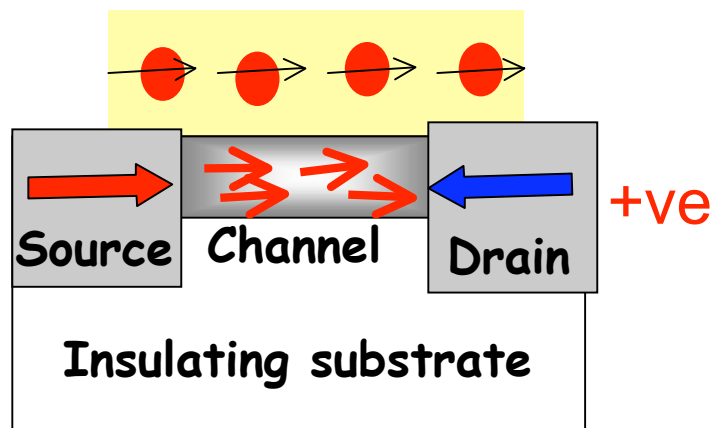




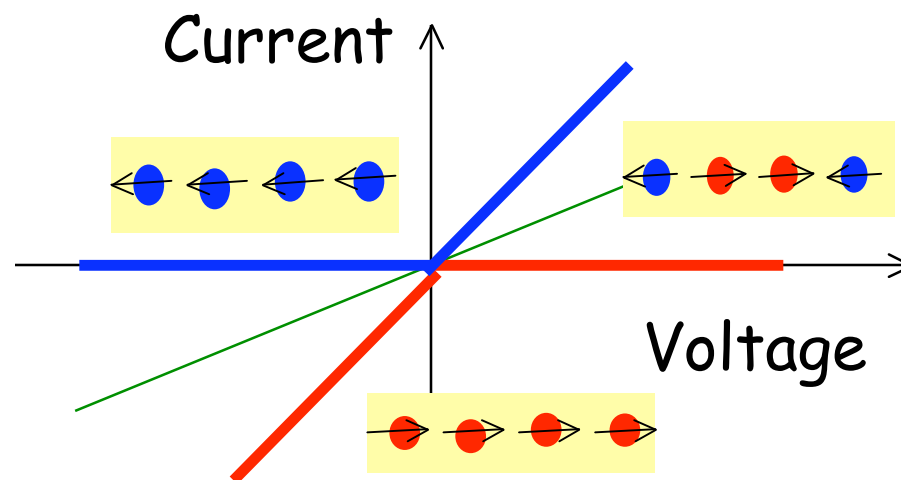
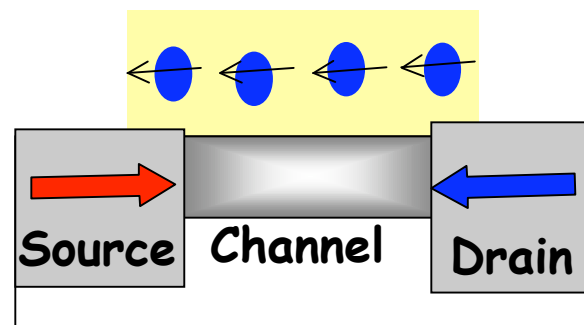
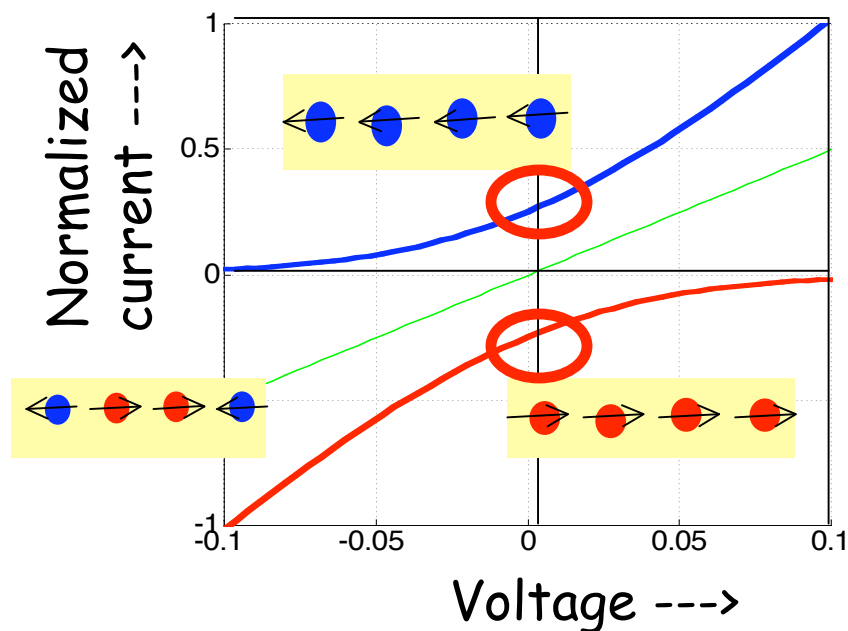
# Perfect AP with Spin-flip Impurities



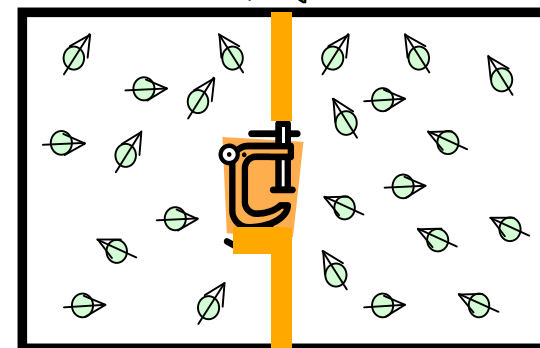
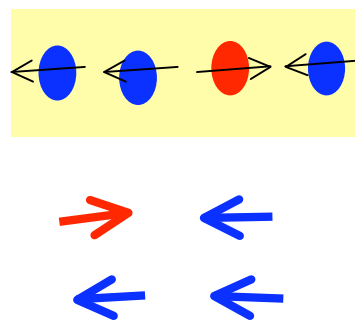
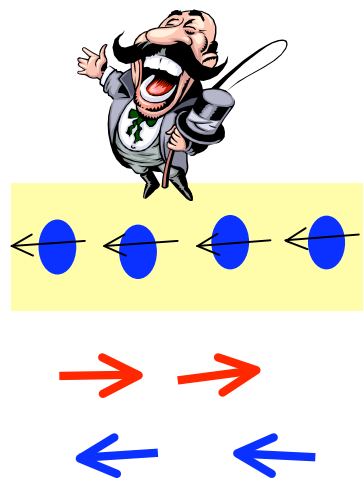
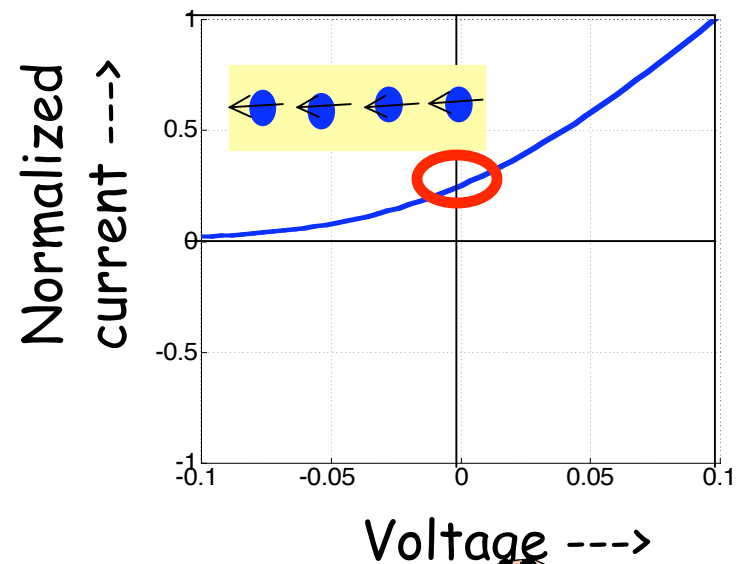
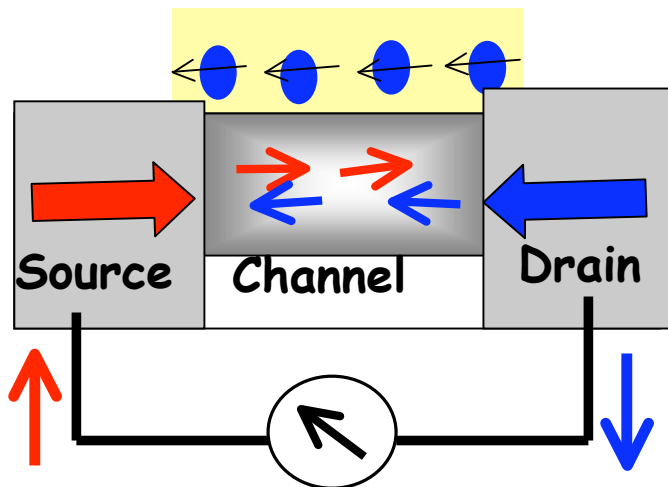
# Perfect AP with Spin-polarized gate

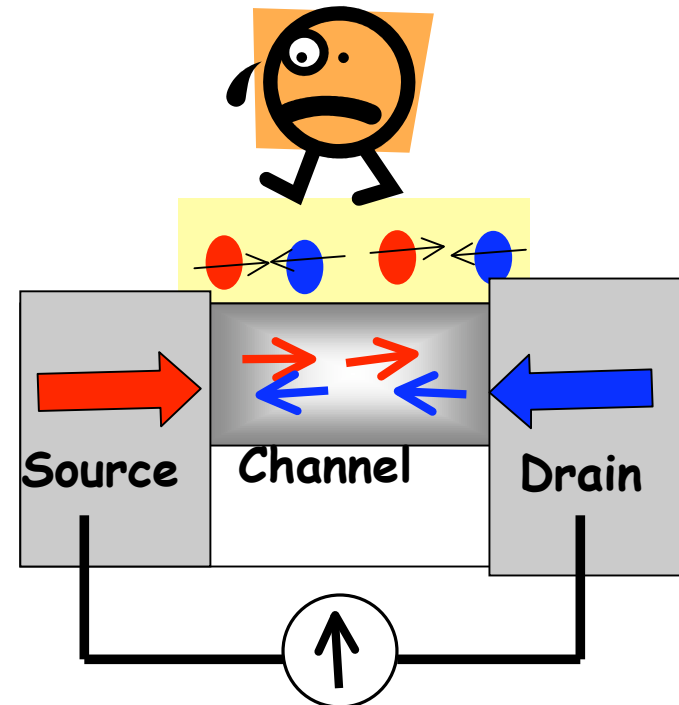
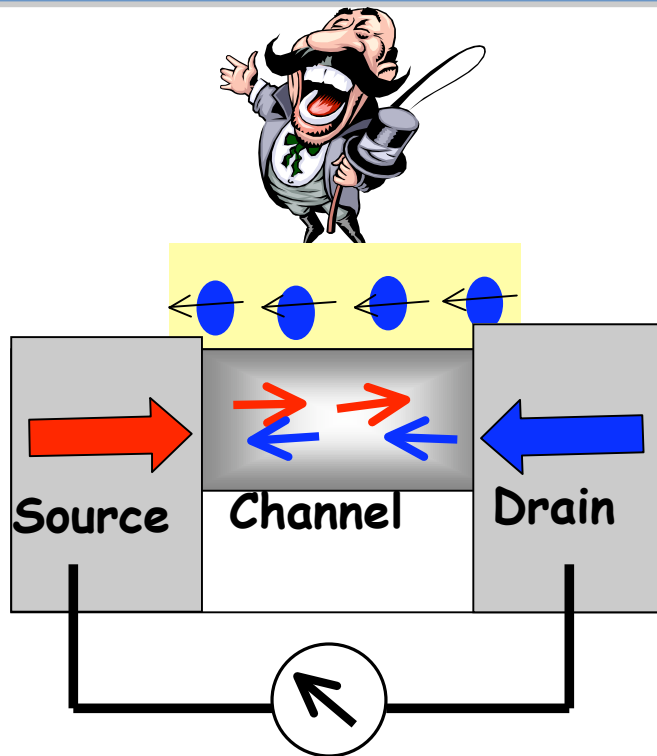


# Current at zero voltage !!

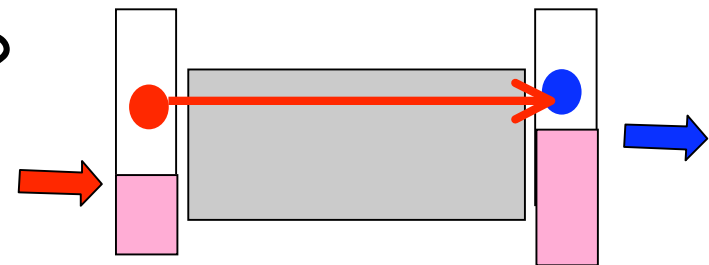


# Device to "demon"



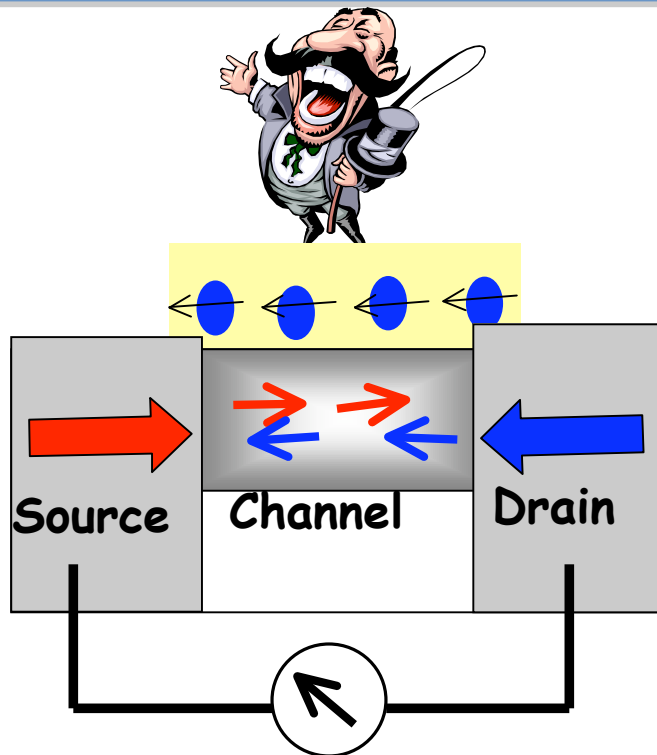


Where did the energy come from ?  
Answer: From the contacts



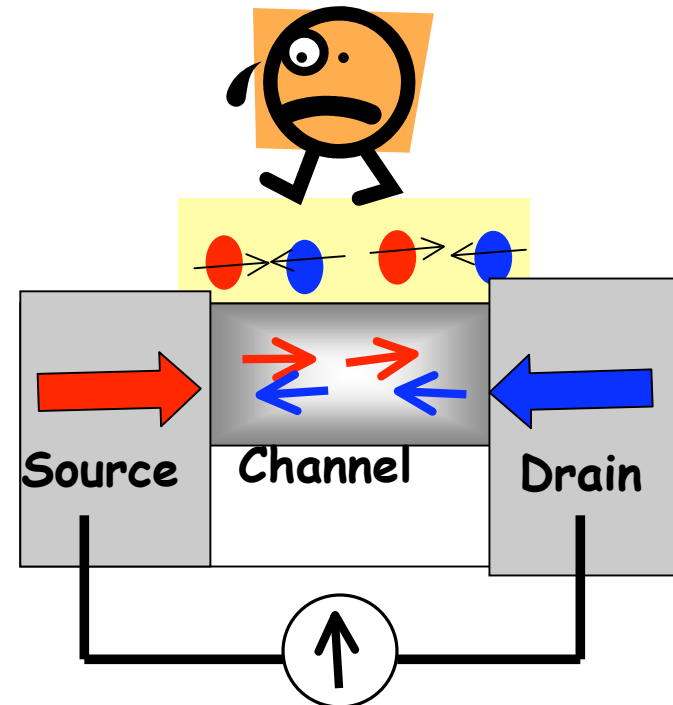


## Second law ?



$$S = 0$$

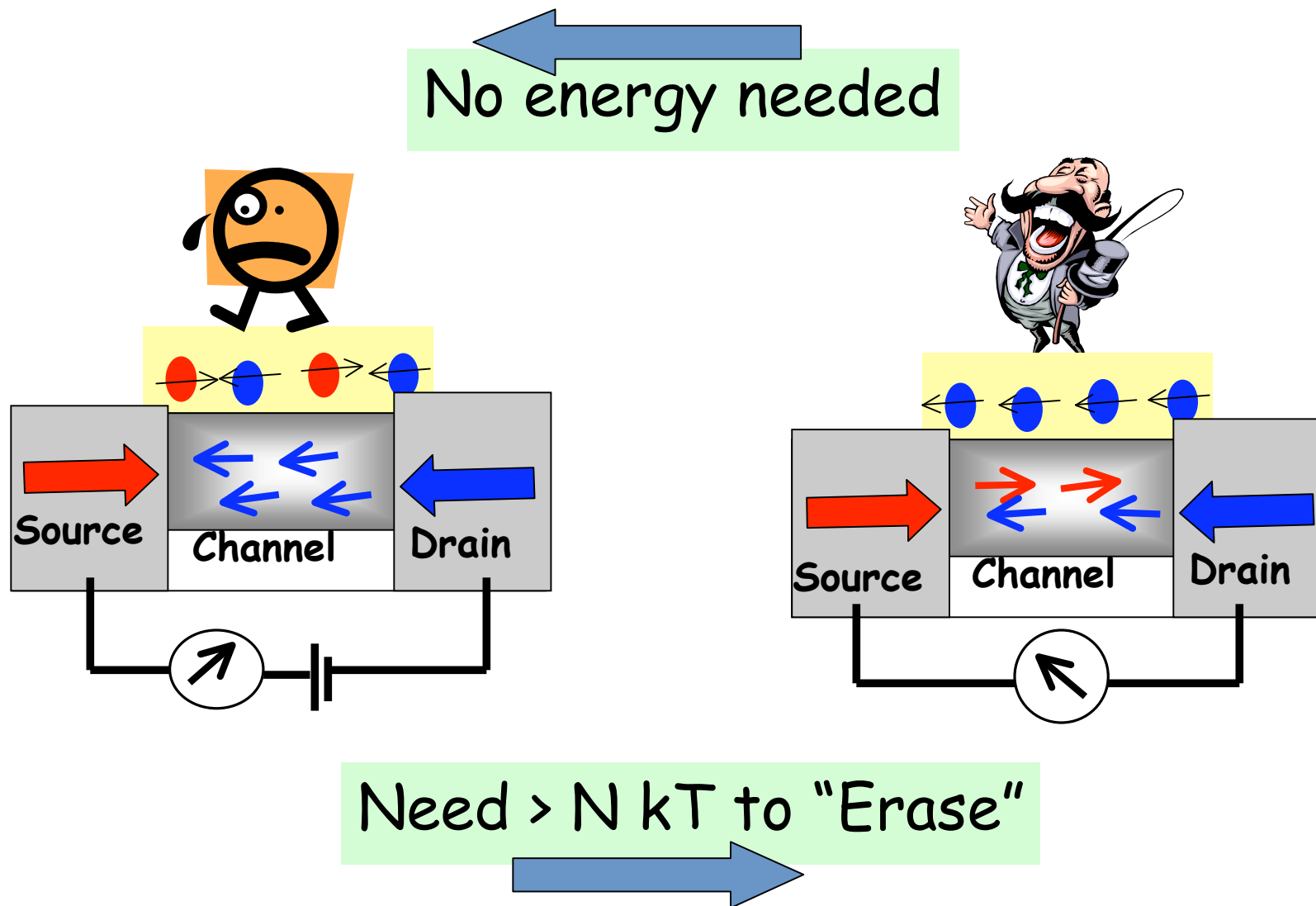
$$S = k \ln W$$



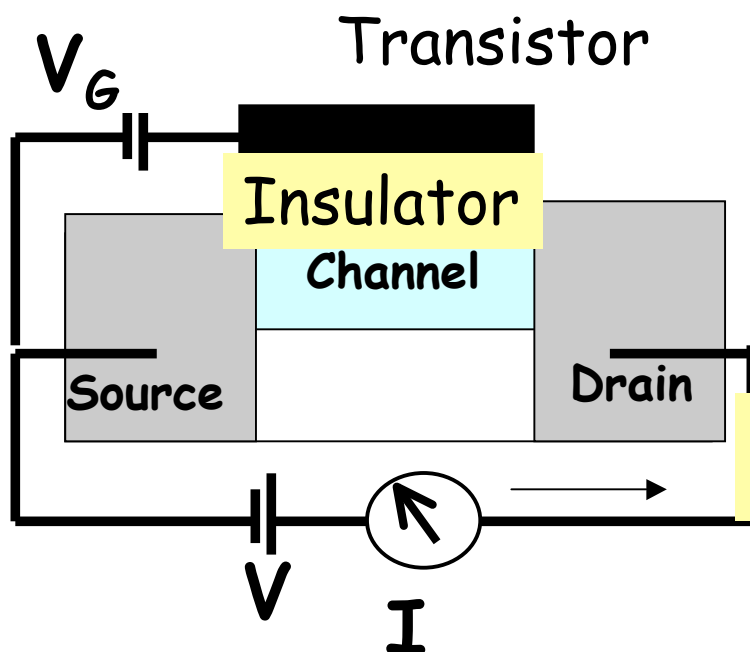
$$S = Nk \ln 2$$

Energy upto  $T\Delta S$  may be extracted

## Resetting the demon takes energy

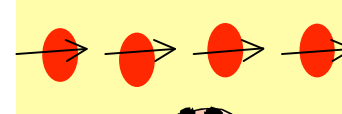
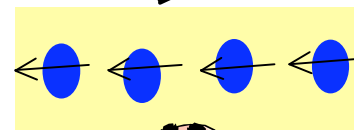
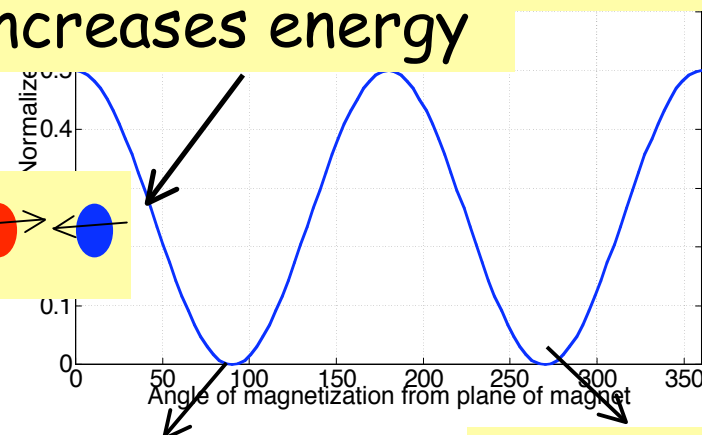


# Nanomagnets : Bistable demons

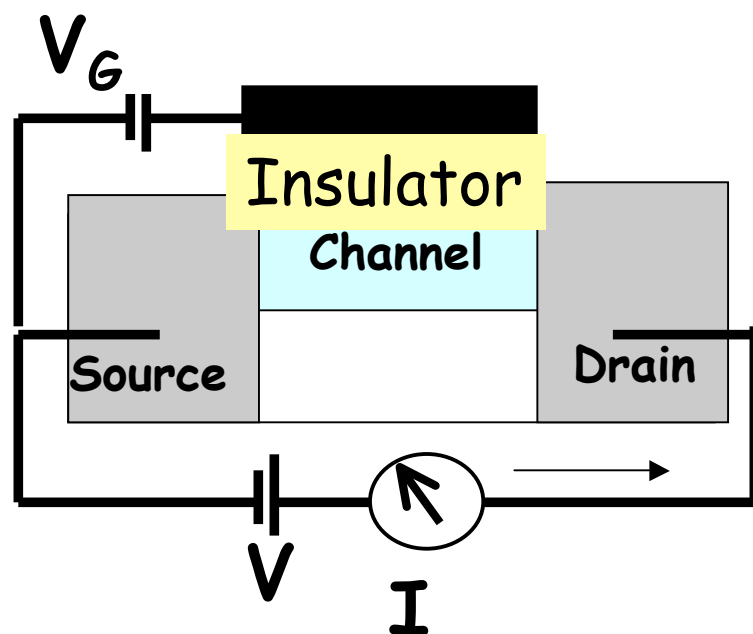


$$P = 10^4 \text{ electrons} \times (40 \text{ kT}) \times 10^9 \text{ Hz} = 1 \mu\text{W} / \text{switch}$$

Energy needed to switch from one other ?  
Flipping a spin increases energy



## Transistor



$$\begin{aligned}
 &P = 10^4 \text{ electrons} \\
 &\times (40 \text{ kT}) \\
 &\times 10^9 \text{ Hz} \\
 &= 1 \mu\text{W} / \text{switch}
 \end{aligned}$$

Nanoelectronics Research Initiative (NRI)

Launched by SIA & NSF

Objective: Explore options for producing a low power switch

Mark Lundstrom

Ashraf Alam

Kaushik Roy

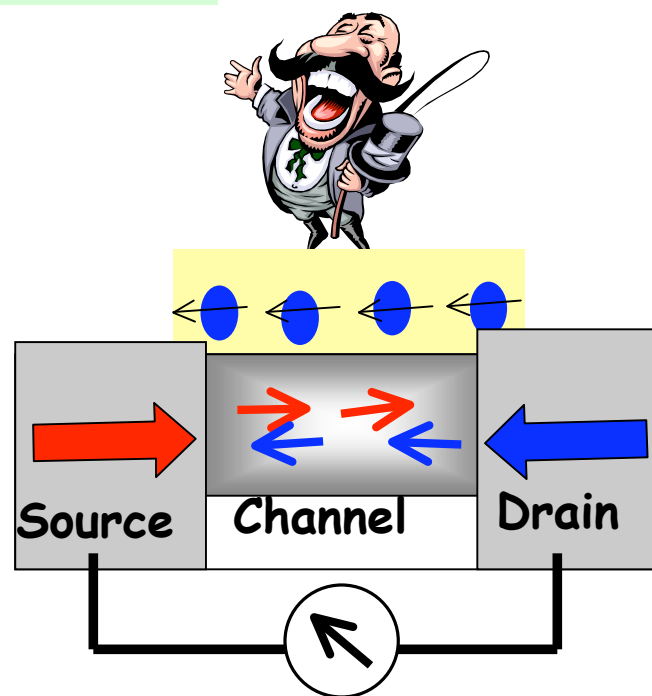
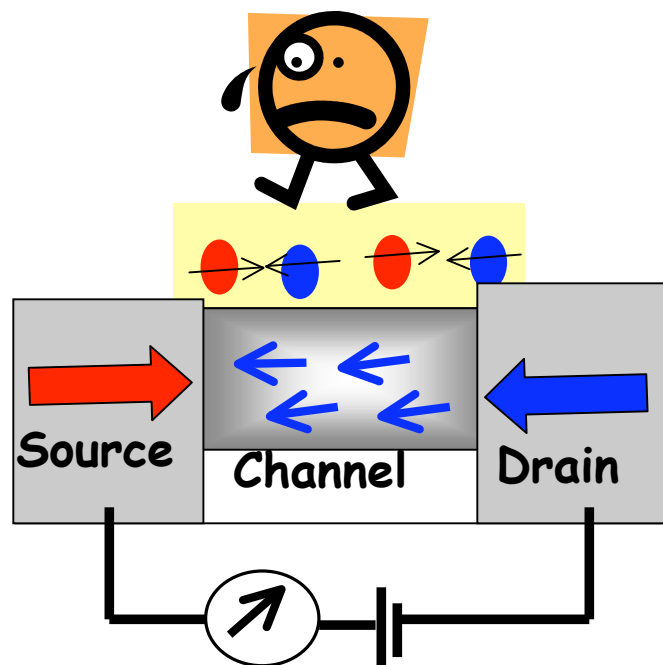
Gerhard Klimeck

# Why is the flow unidirectional ?

$$S = Nk \ln 2$$

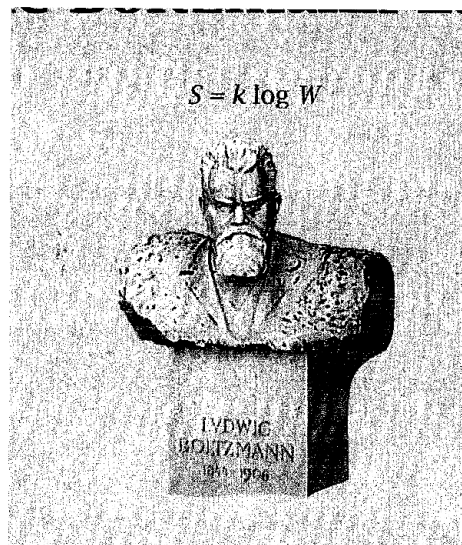
No energy needed

$$S = 0$$



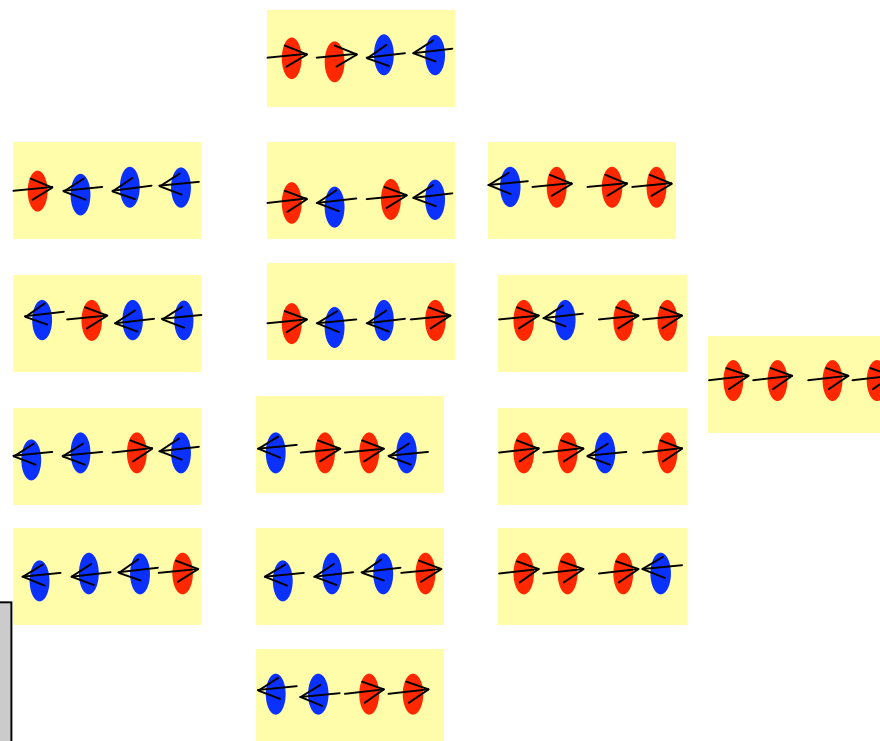
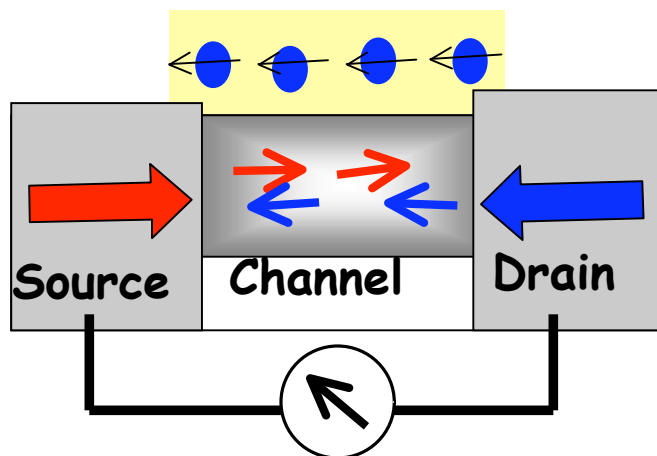
Need  $> N kT$  to "Erase"

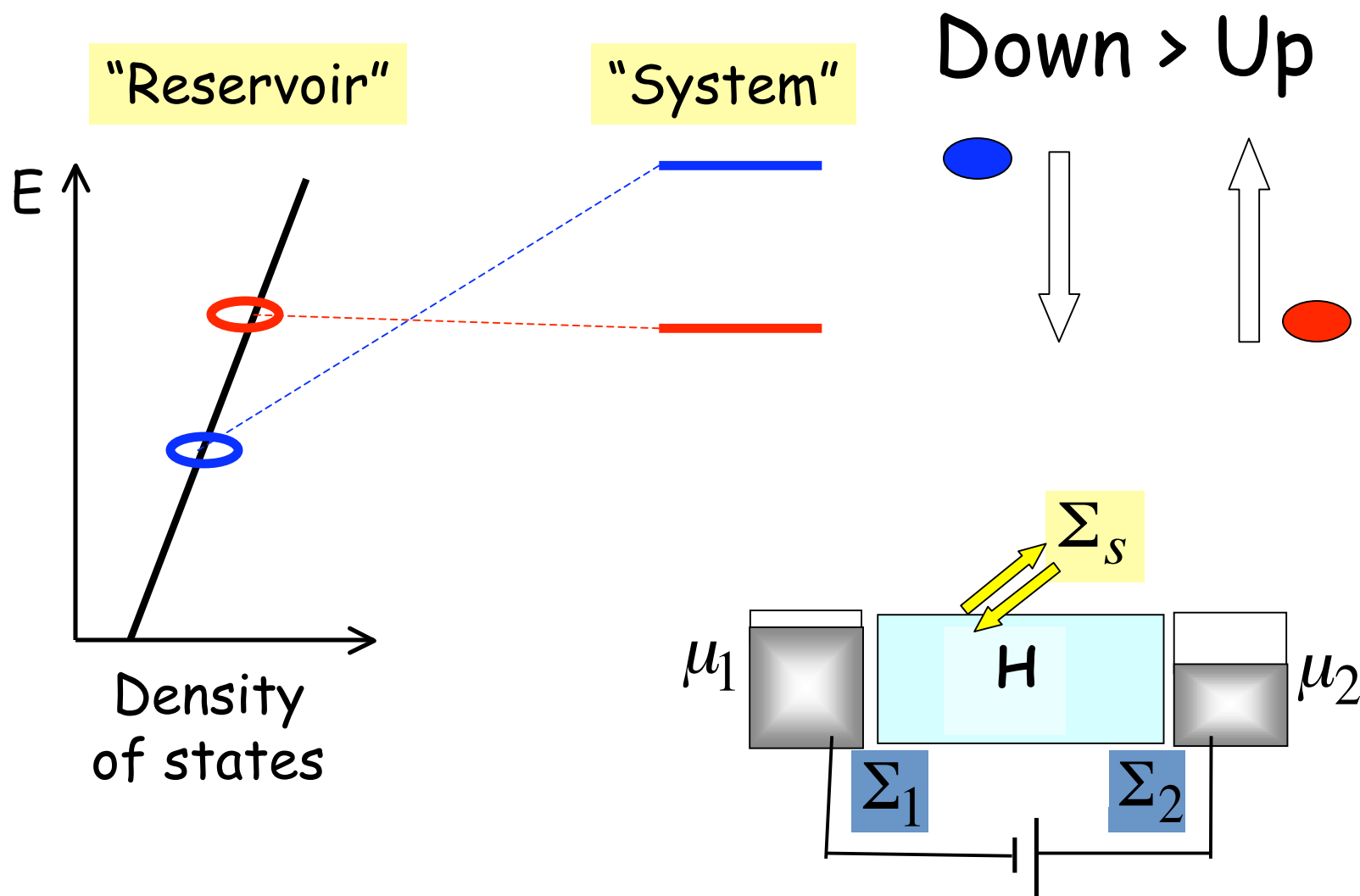
# Entropy as a driving force



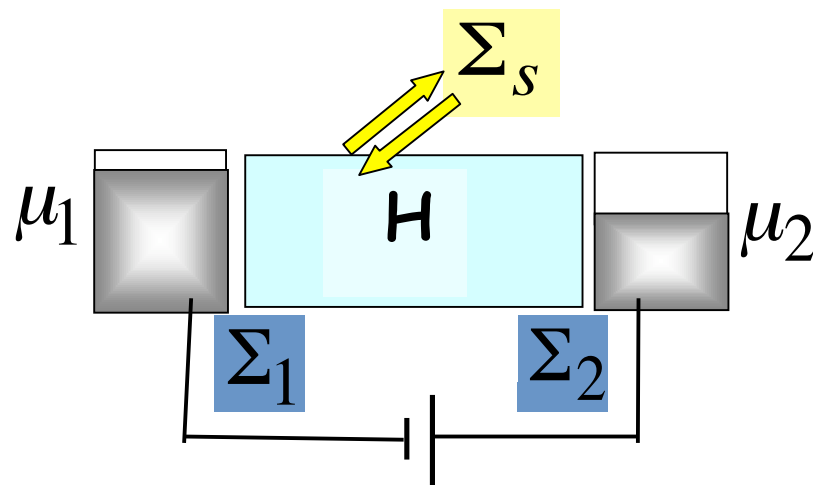
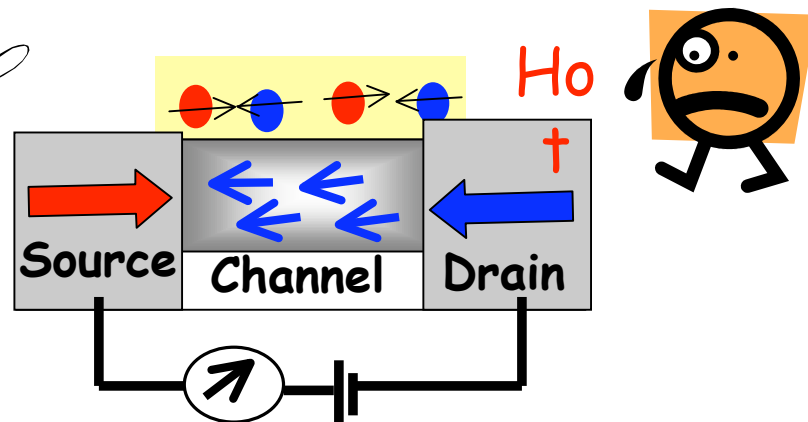
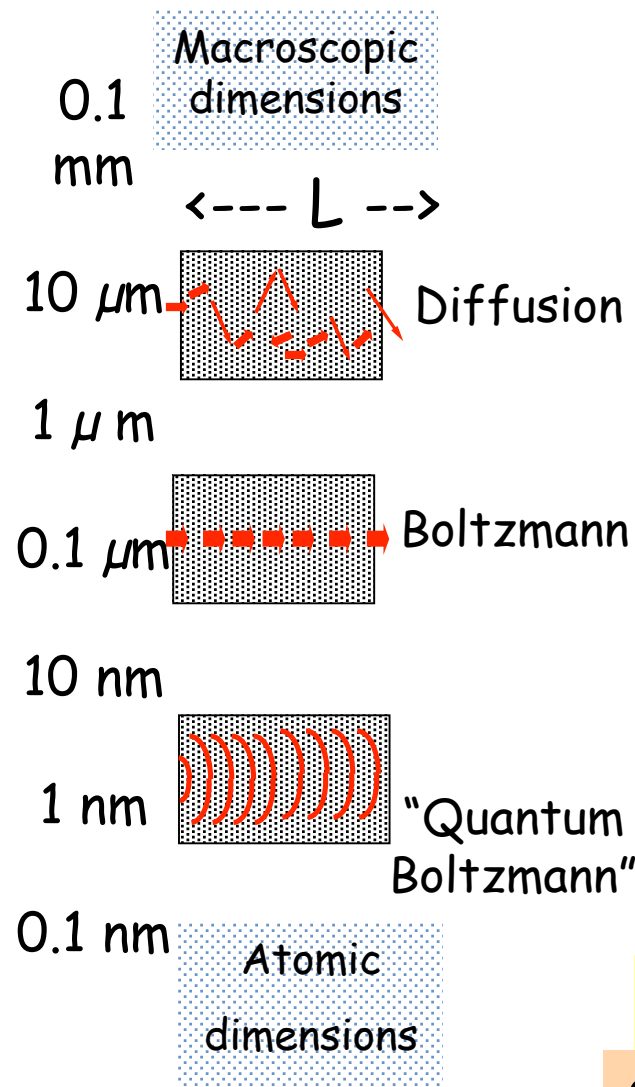
$$S = k \log W$$

All  
"blue"





# Unified model for nanodevices

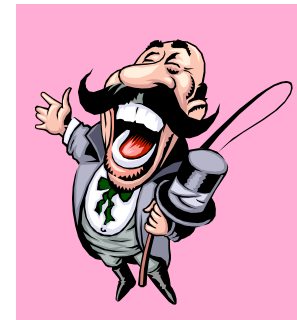
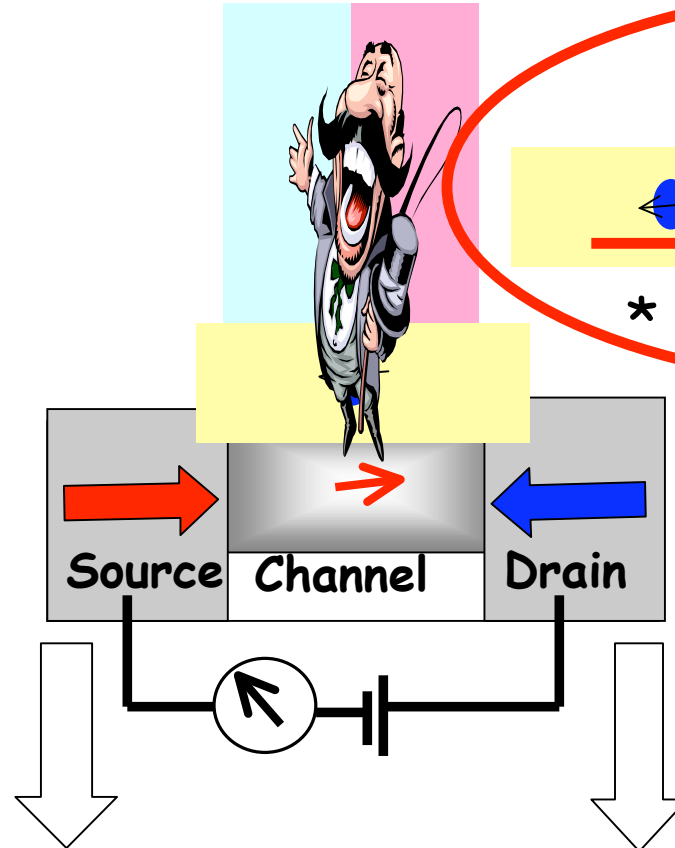
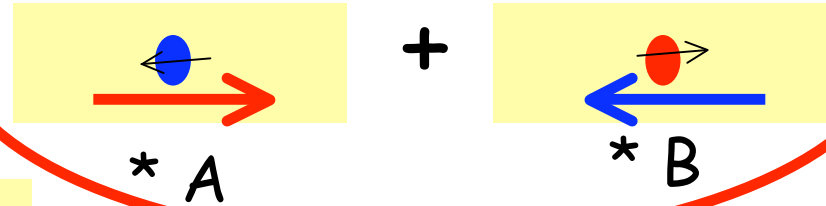


Nanowires, nanotubes, molecules ....  
Switches, energy conversion, cooling ...

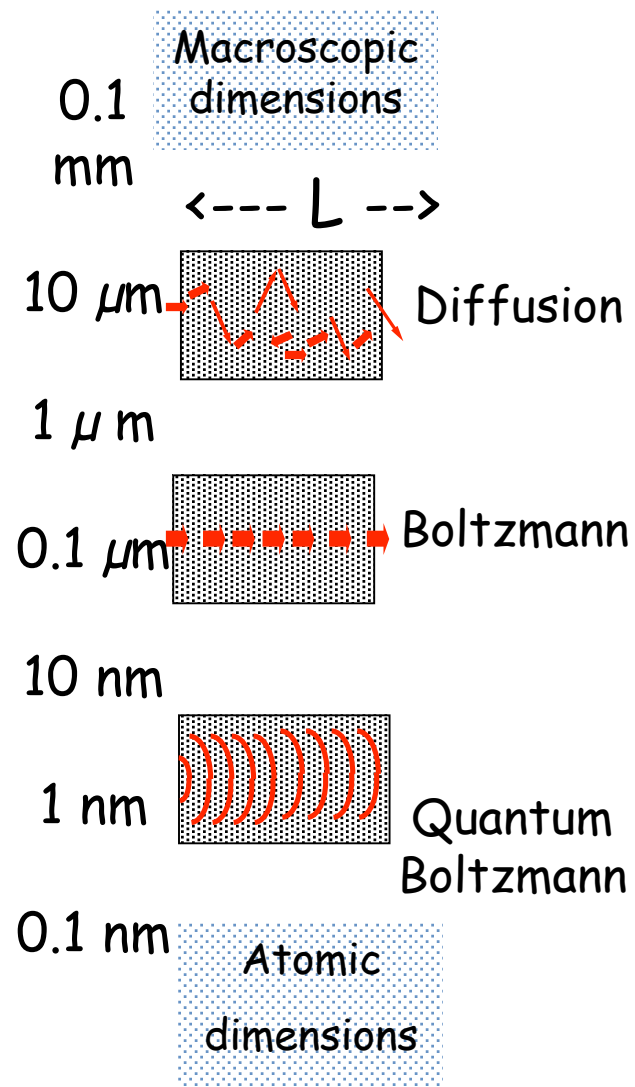


# Entangled "demon"

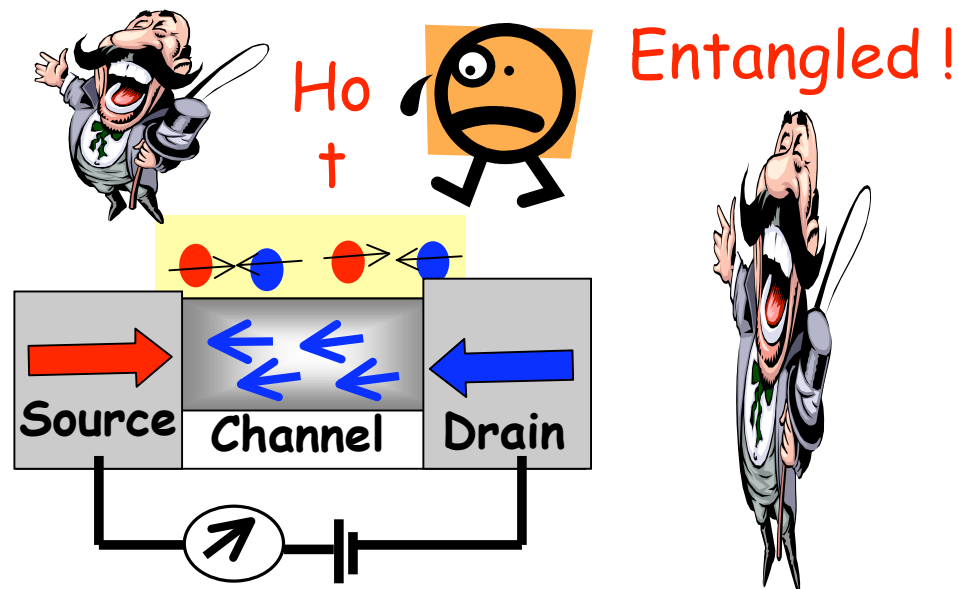
Entangled !



# "It is all about the contacts"



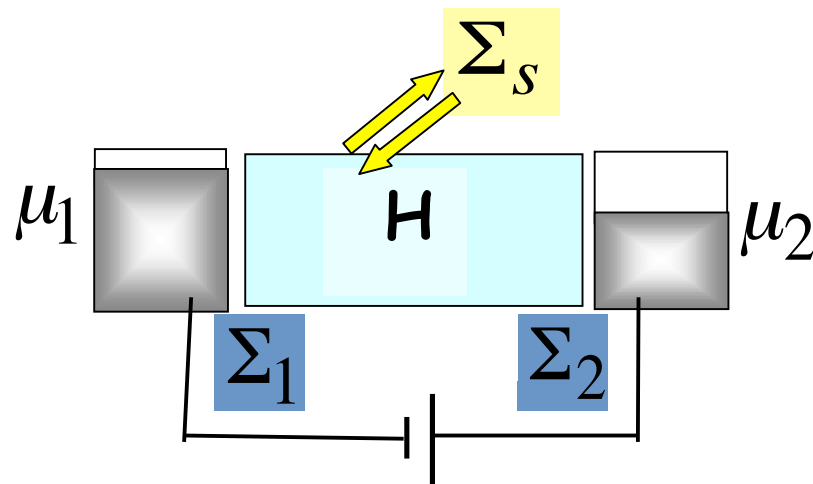
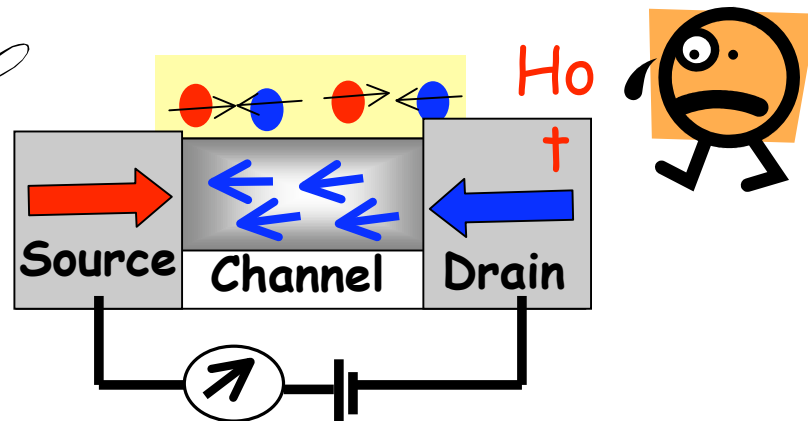
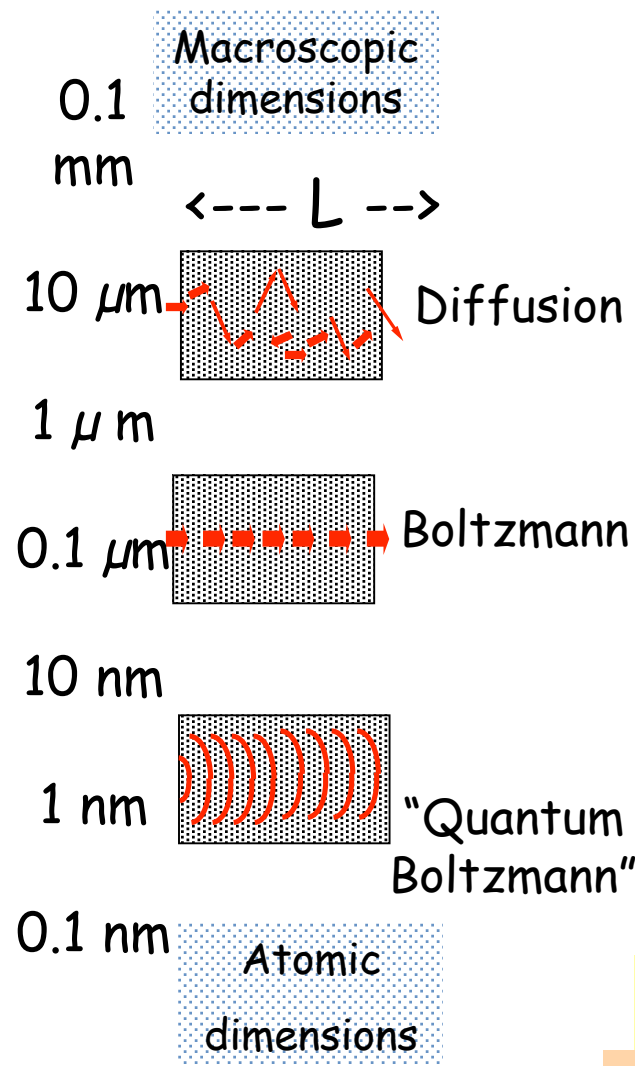
"Even simple things .. work .. in only one direction because it has some ultimate contact with the rest of the universe .."  
Feynman lectures, Vol.1, 46-8



Thanks to Purdue and  
to all my outstanding  
students and colleagues,  
supportive friends and family.

# Questions & Answers

# Unified model for nanodevices

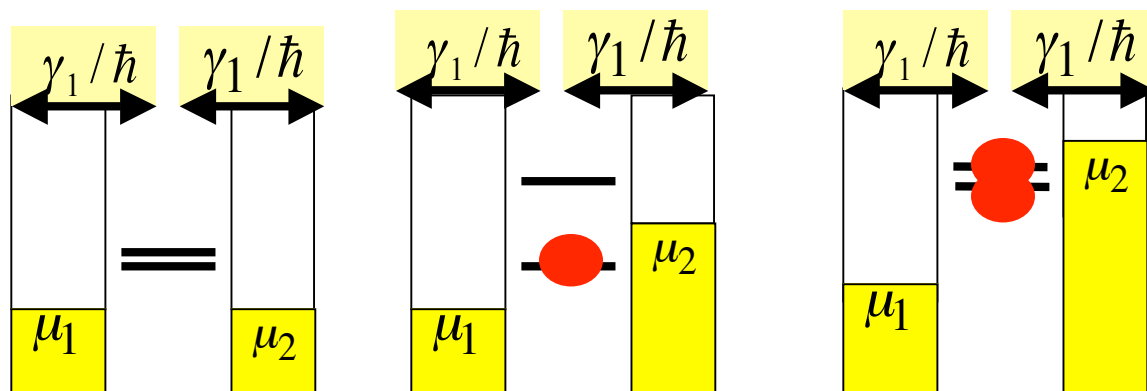


Nanowires, nanotubes, molecules ....  
Switches, energy conversion, cooling ...

# Single electron charging

$U_0$  : Increase in potential due to SINGLE electron  
 $\gg \gamma, kT$

"Self-interaction Correction"



Non-interacting

