

ME 517: Micro- and Nanoscale Processes

Lecture 35: Surface Tension Microfluidics

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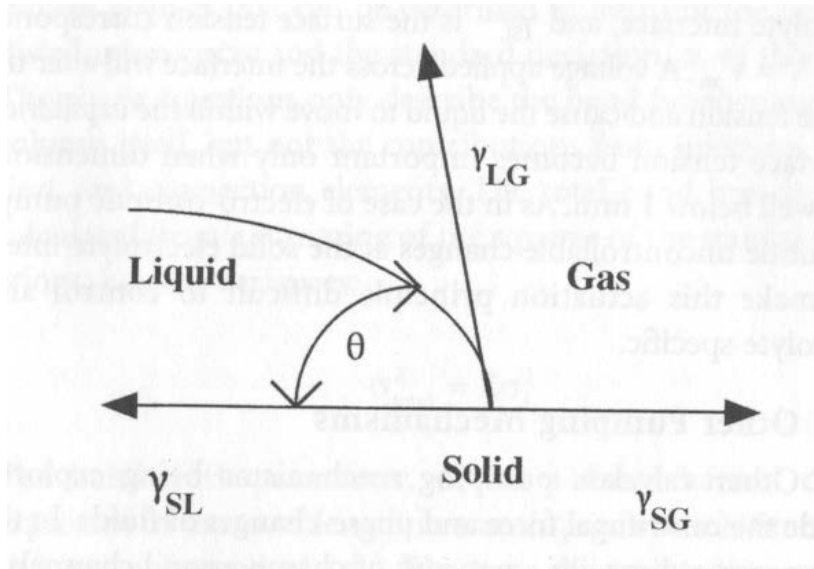
Spring 2014

Surface Tension Microfluidics

- Introduction to surface tension
- Thermocapillarity
- Electrowetting
 - Electrowetting on dielectric (EWOD)
 - Open opto-electrowetting (O-OEW)
 - Electrowetting + particle manipulation

Surface Tension Basics

Surface tension (γ) is the increase in energy as the surface area increases.



Young's Equation

$$\gamma_{SL} + \gamma_{LG} \cos \theta = \gamma_{SG}$$

Hydrophilic ($0^\circ < \theta < 90^\circ$)

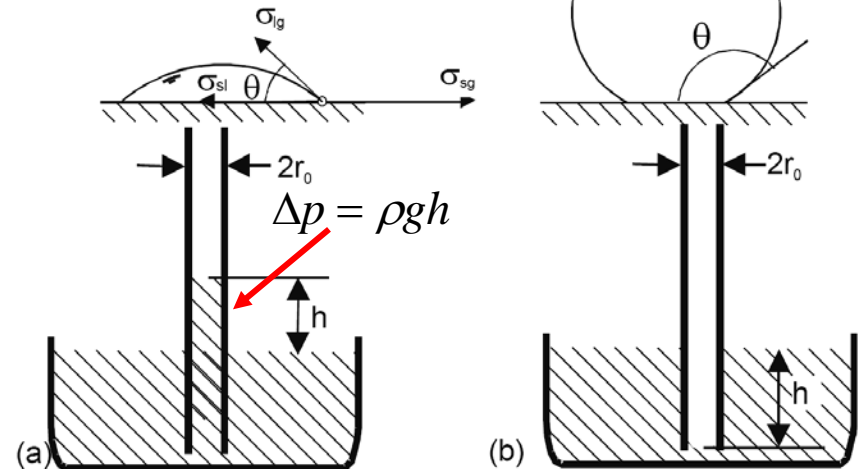
Hydrophobic ($90^\circ < \theta < 180^\circ$)

$$\Delta p = \frac{2(\gamma_{SG} - \gamma_{SL})}{r} = \frac{2\gamma_L \cos \theta}{r}$$

$$\gamma_{\text{water}} = 72.8 \text{ mN/m}$$

$$r = 10^{-6} \text{ m}$$

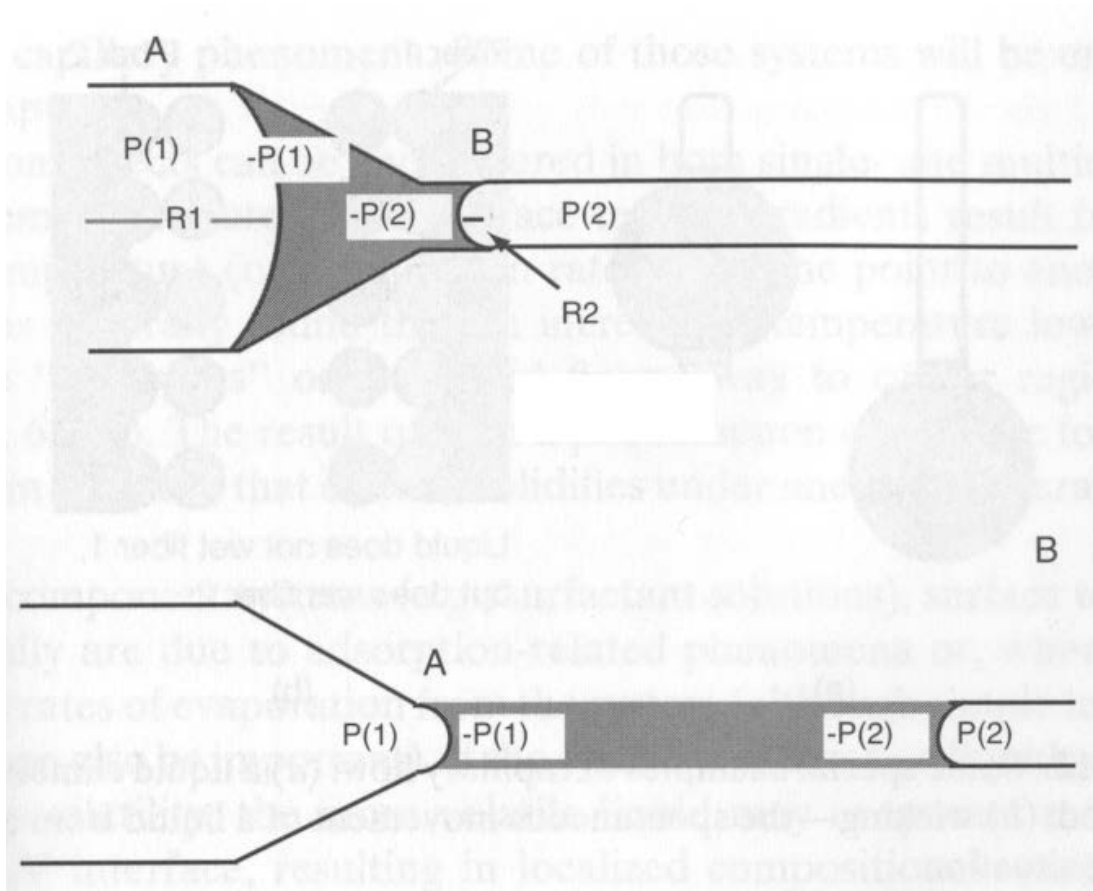
$$\Delta p \sim 100 \text{ kPa or 1 atm}$$



Capillary force driven pumping: (a) hydrophilic; and (b) hydrophobic.

Surface Tension Basics

Capillary tube wetting



Unstable

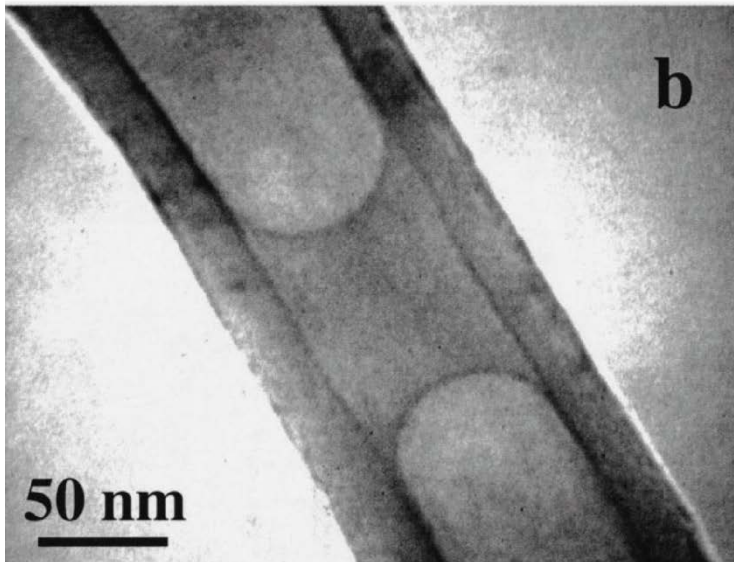
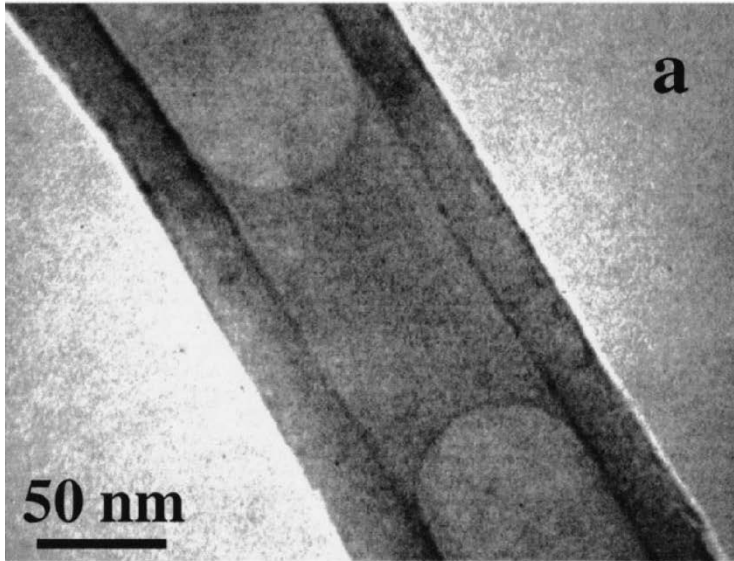
Stable = Stuck!

[Microdevice here](#)

[Water strider here](#)

Water in Carbon Nanotubes

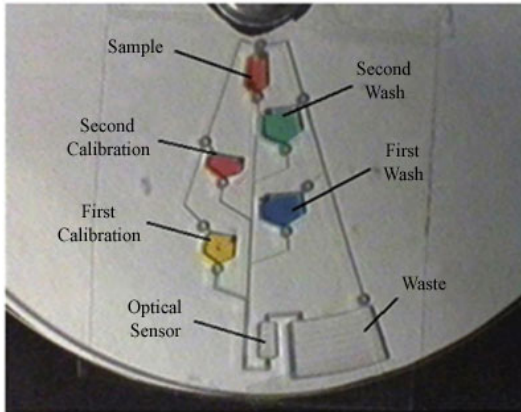
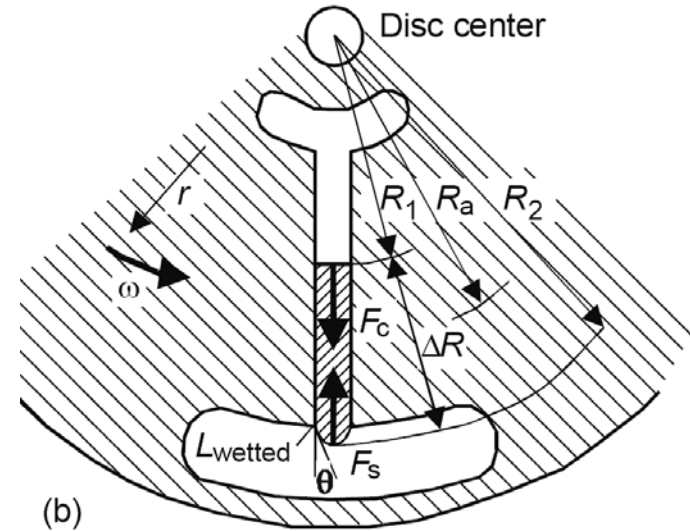
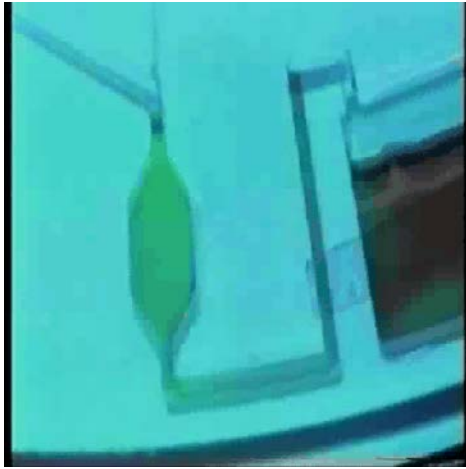
Megaridis, Phys. Fluids, Vol. 14, pp L5-L9, 2002



- Hydrothermally produced multi-wall carbon nanotube
- Water inside nanotube
- TEM micrographs of meniscus
- Water volume decreases from a to b upon heating
- Explanations:
 - Bubble expansion
 - Liquid evaporation
 - Thermocapillarity
- Results inconclusive

Surface Tension Valves

Lab-on-a-Disk: Marc Madou, UC-Irvine



Centrifugal Force:

$$\frac{dF_c}{dr} = \rho \omega^2 r$$

Surface Tension:

$$F_s = \frac{\sigma \cos \theta L_{\text{wetted}}}{A}$$

Burst Frequency:

$$f_b \geq \sqrt{\frac{\sigma \cos \theta}{\pi^2 \rho R_a \Delta R D_h}}$$

[Movie here](#)