



NEEDS

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**The deployment and evolution of the first  
NEEDS-certified model**  
*MIT virtual source compact model for silicon  
nanotransistors*

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*Thanks: Prof. Dimitri Antoniadis, MIT*



NEW YORK UNIVERSITY





NEEDS

NANO-ENGINEERED ELECTRONIC  
DEVICE SIMULATION NODE[NEEDS HOME](#)[ABOUT US](#)[RESOURCES](#)[CONTACT US](#)[NEEDS TEAM](#)

# Nano-Engineered Electronic Device Simulation Node

*NEEDS has a vision for a new era of electronics that couples the power of billion-transistor CMOS technology with the new capabilities of emerging nano-devices and a charter to create high-quality models and a complete development environment that enables a community of compact model developers.*

*NEEDS Team: Purdue, MIT, U.C. Berkeley, and Stanford.*

[REGISTER NOW](#) for the May 11-12 NEEDS annual meeting and workshop.

NEWEST COMPACT MODEL RELEASE: UCSB 2D Transition-Metal-Dichalcogenide (TMD) FET model 1.0.0. [See Compact Models Page](#)

NEEDS announces the public release of [Berkeley MAPP](#), a MATLAB-based platform for prototyping compact models and simulation algorithms.

GET STARTED ON COMPACT MODELING: Take Colin McAndrew's [online workshop](#).

For presentations on these device technologies by experts in the field, see the NEEDS Seminar Series on “Emerging Transistor Technologies.”



SEMINARS, COURSES, ETC.

NEEDS Seminar Series,  
nanoHUB-U and more



NEEDS is a resource for nanoelectronics supported by the [National Science Foundation](#) and by the [Semiconductor Research Corporation](#).

[needs.nanohub.org](https://needs.nanohub.org)

# NEEDS compact model development

## Compact models

*NEEDS is charged to develop compact models for a very wide variety of novel nanodevices. A set of carefully chosen compact models that encompass a wide variety of nanodevice physics is being developed to provide concrete guidelines for how compact models can be grounded in fundamental physics and detailed simulations and then carefully validated by experiments. Developing these models also provides a “laboratory” for addressing formulational, numerical, and convergence issues that arise for compact models. The models developed will provide the community with a library of high-quality and tested models, provide NEEDS with a set of case studies and examples, and drive the development of the NEEDS compact model development platform.*

NEEDS models are licensed with the Compact Model Council (CMC) Standard license as described in the following document – [CMC\\_Standard\\_license.pdf](#) (155 KB) and follow the CMC recommendations for [versioning](#).

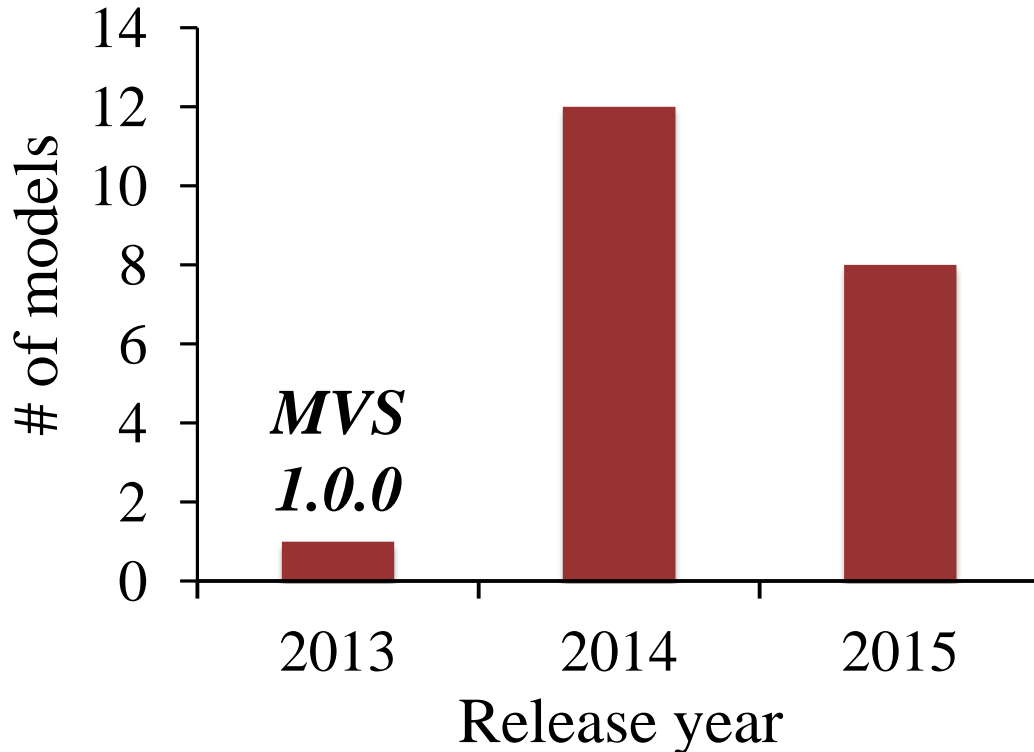
### **NEEDS model releases will include:**

- Matlab version for downloading
- Verilog-A version for downloading
- Manual (with a complete list of equations used and procedures to calibrate the

- A list of compact models for nanoscale devices available to download.
- Total number of models till date: 20
- Models from NEEDS member universities: 12/20 (60%)

# NEEDS model release history

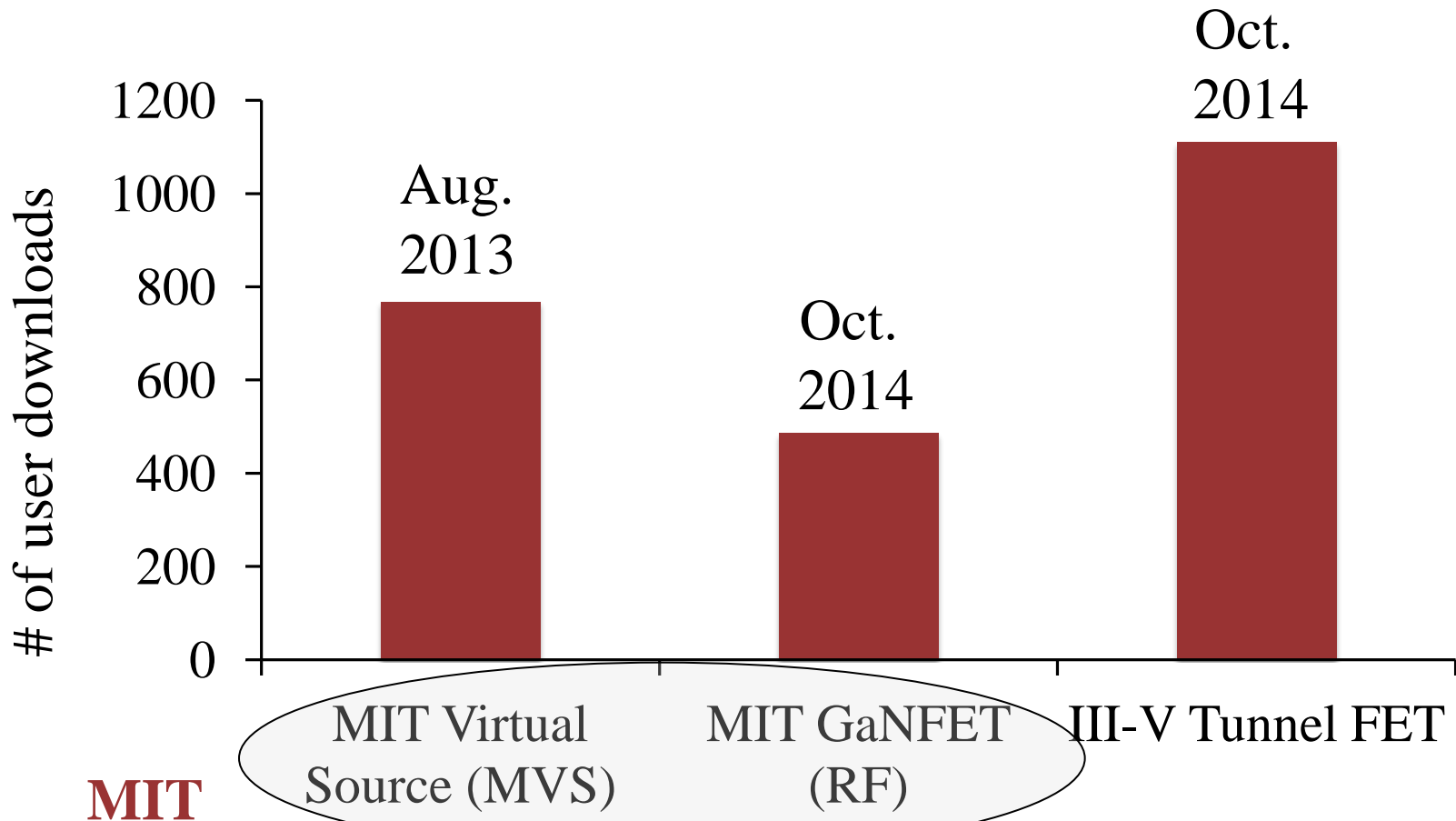
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## Upcoming models

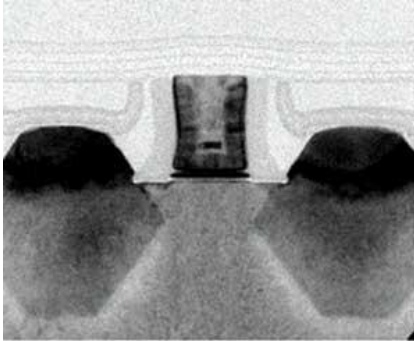
- Thermoelectric device
- Phase change memory
- Steep Subthreshold FETs
- NEMS Relay
- Optical modulator
- 45 nm CMOS SOI RF

# NEEDS compact models: top user downloads



# This presentation focuses on

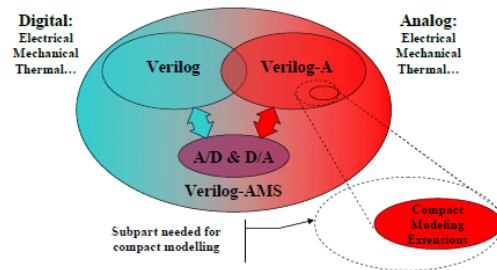
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## I. MVS model

- Nanotransistor basics
- Model formulation
- Experimental verification
- Mathematical issues

12  
min



## II. Model deployment on nanoHUB

- Process and requirements
- Current status
- Future goals

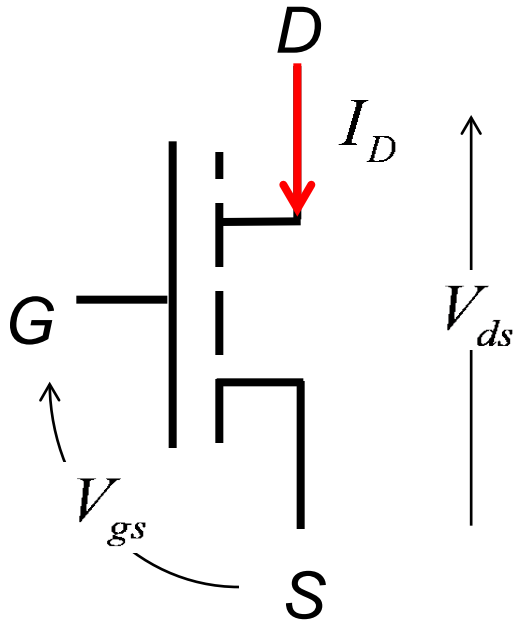
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**PART I**  
**MIT Virtual Source Model For**  
**Nanotransistors**

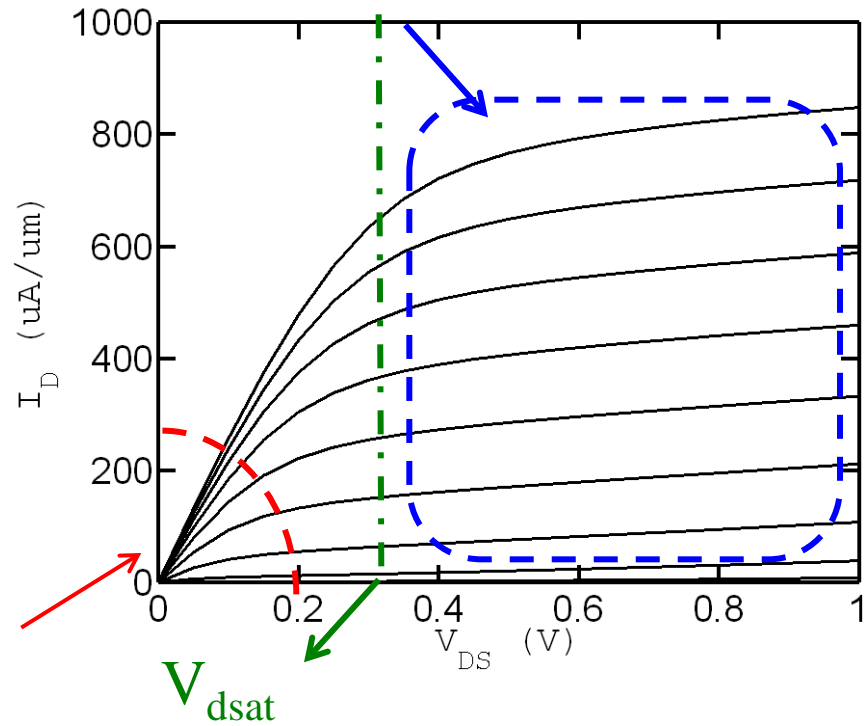
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# Textbook MOSFET $I$ - $V$ theory



gate-voltage controlled  
Resistor  
*a.k.a. linear region*

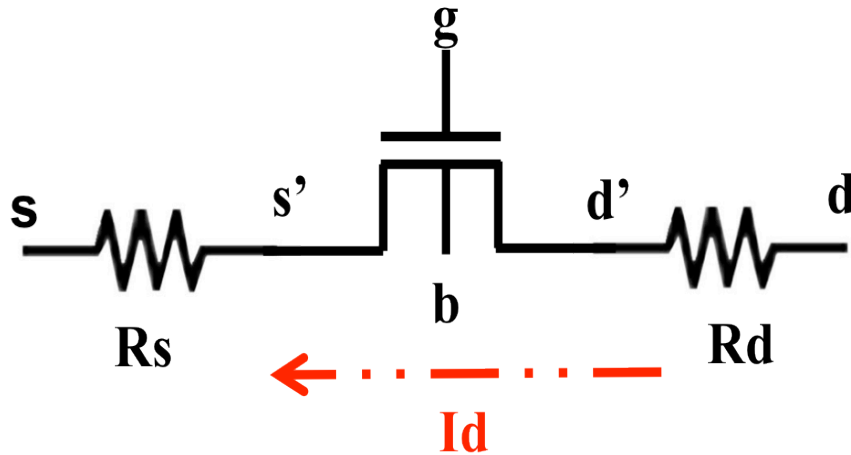
gate-voltage controlled  
current source  
*a.k.a. saturation*





# What is MVS model?

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## Currents

$$I_d = f(V_g, V_d, V_s, V_b)$$

$$I_g = I_b = 0$$

MIT Virtual Source (MVS) nanotransistor model gives *currents* and *charges* as functions of terminal voltages.

## Charges

$$Q_s = f_1(V_g, V_d, V_s, V_b)$$

$$Q_d = f_2(V_g, V_d, V_s, V_b)$$

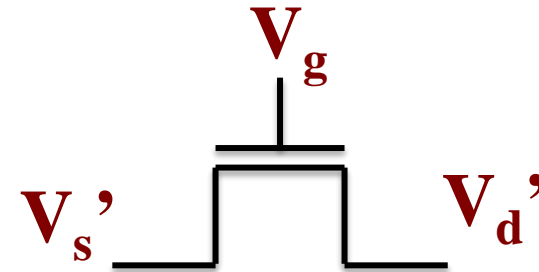
$$Q_b = f_3(V_g, V_d, V_s, V_b)$$

$$Q_g = -(Q_s + Q_d + Q_b)$$

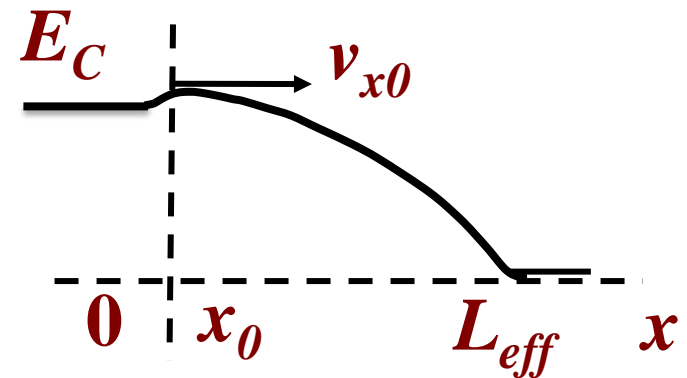
# MVS model: I-V characteristics

$$\frac{I_D}{W} = Q_{x_0} v_{x_0} F_{sat} \longrightarrow \text{Empirical function}$$

Charge at VS      Velocity at VS



- 10 fitting parameters.
- most of the parameters are physical and can easily be obtained through device characterization.
- describes quasi-ballistic **silicon, III-V and graphene devices.**



# MVS 1.0.0 model formulation

$$1) I_{DS} = WQ_{x0}(V_{GS}, V_{DS})F_{SAT}(V_{DS})v_{x0}$$

$$2) Q_{x0}(V_{GS}) = -C_{inv}m(k_B T/q) \ln\left(1 + e^{q(V_{GS} - V_T + \alpha(k_B T_L/q)F_f)/mk_B T}\right)$$

$$V_T = V_{T0} - \delta V_{DS}$$

$$3) F_{SAT}(V_{DS}) = \frac{V_{DS}/V_{DSAT}}{\left[1 + (V_{DS}/V_{DSAT})^\beta\right]^{1/\beta}}$$

$$4) V_{DSAT} = \frac{v_{x0}L}{\mu_{app}}$$

Only 10 parameters in this model:

$$C_{inv}, V_T, \delta, m, v_{x0}, \mu_{app}, L,$$

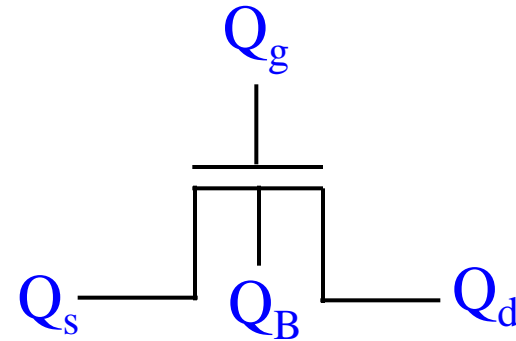
$$R_{SD0} = R_{S0} + R_{D0},$$

$$\alpha, \beta$$

# Charge partitioning/ Dynamic model

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- Charge partitioning tells us the charge associated with the various terminals in the transistor.
- **Transient analysis needs charges and inter-nodal capacitances.**
- In MVS, dynamic model is obtained self-consistently with the static transport model → **no additional fitting parameters.**



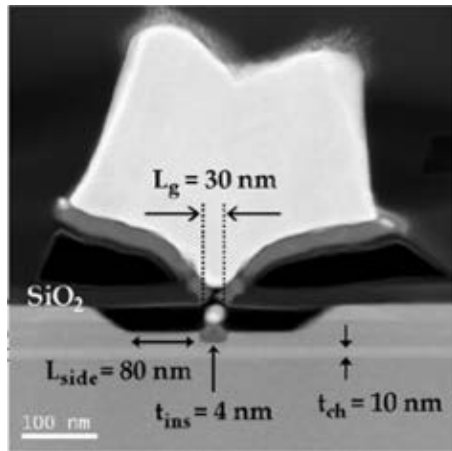
$$C_{ij} = -\frac{\partial Q_i}{\partial V_j} (i \neq j)$$
$$C_{jj} = \frac{\partial Q_j}{\partial V_j}$$

# References for MVS model equations

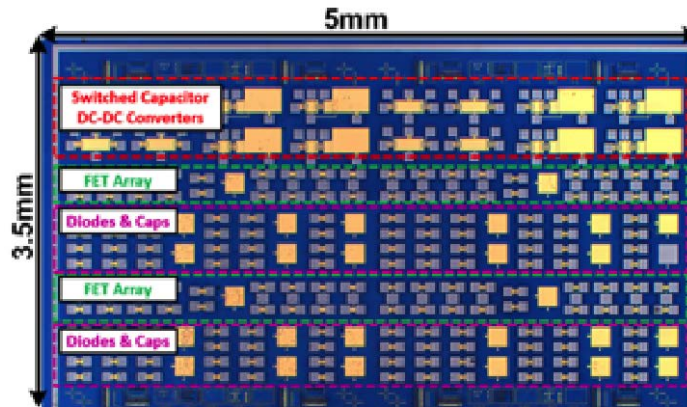
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1. A. Khakifirooz et al., “A simple semi-empirical short-channel MOSFET current-voltage model continuous across all regions of operation and employing only physical parameters,” IEEE Trans. Electron Devices, vol. 56, no. 8, **July 2009**.
2. L. Wei et al., “Virtual-source-based self-consistent current and charge FET models: from ballistic to drift-diffusion velocity-saturation operation,” IEEE Trans. Electron Devices, vol. 59, no. 5, **May 2012**.
3. S. Rakheja and D. Antoniadis, “MVS 1.0.1 Nanotransistor Model (Silicon),” <https://nanohub.org/resources/19684> (**Nov. 2013**)

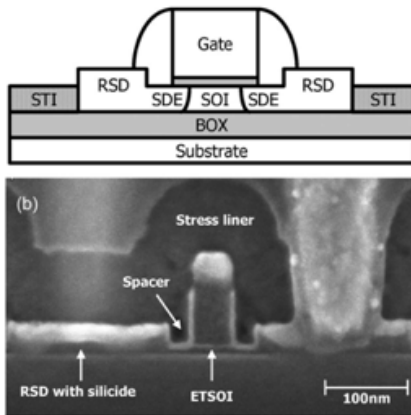
# MVS model verification with experiments



III-V HEMT  
(Intel & MIT)

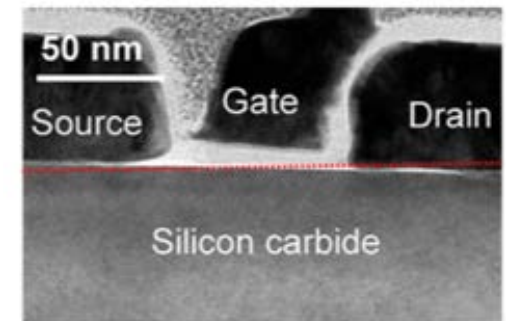
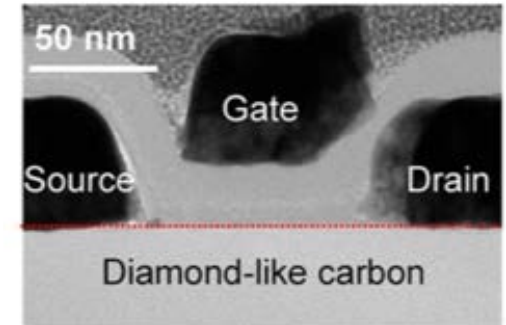


(MIT) Test chip fabricated using CVD grown  $\text{MoS}_2$



Si ETSOI  
(IBM)

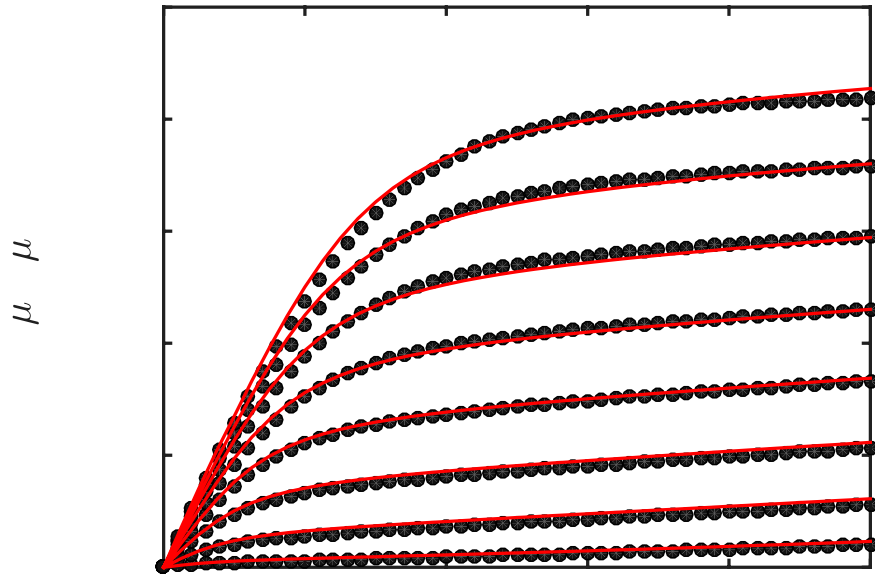
Graphene  
(IBM, Columbia, MIT)



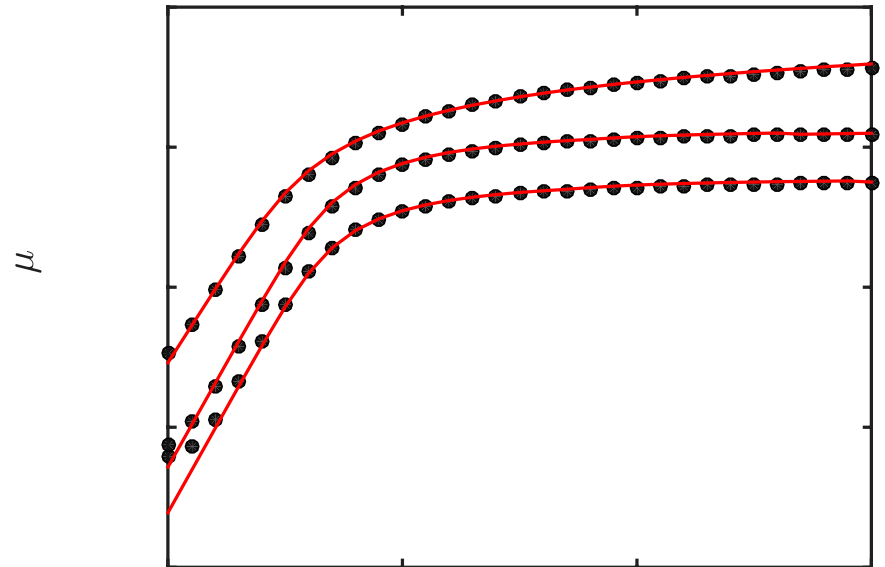
# Extremely thin silicon-on-insulator (SOI) (IBM, 2014)

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Output characteristics



Transfer characteristics



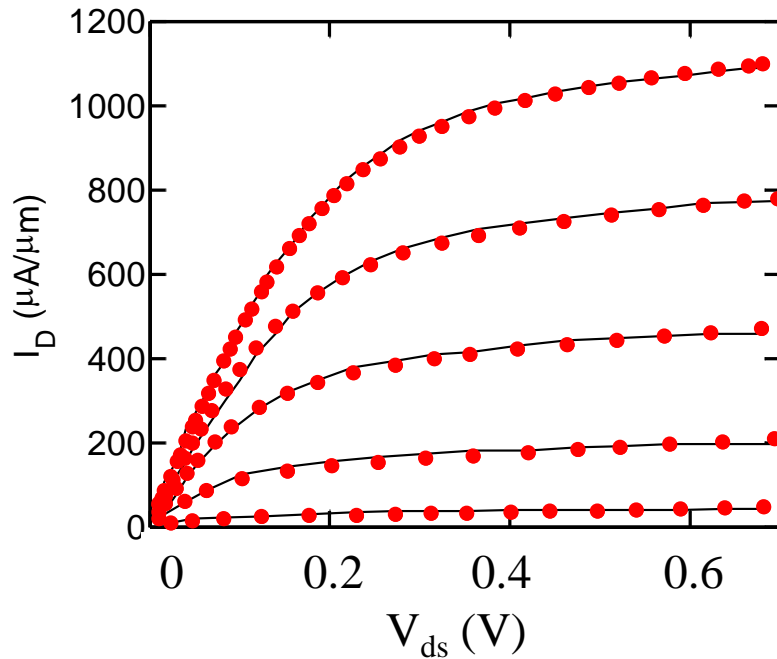
$$L_{\text{eff}} = 30 \text{ nm}$$

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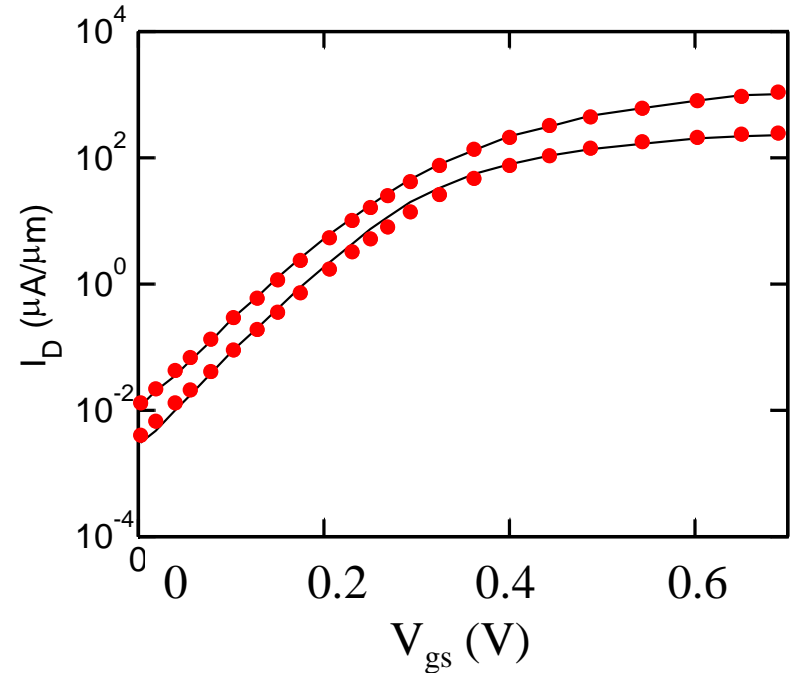
Symbols  $\rightarrow$  experiment  
Solid lines  $\rightarrow$  model

# FinFET CMOS technology (Intel, 2014)

Output characteristics



Transfer characteristics



$$L_{eff} = 20 \text{ nm}$$

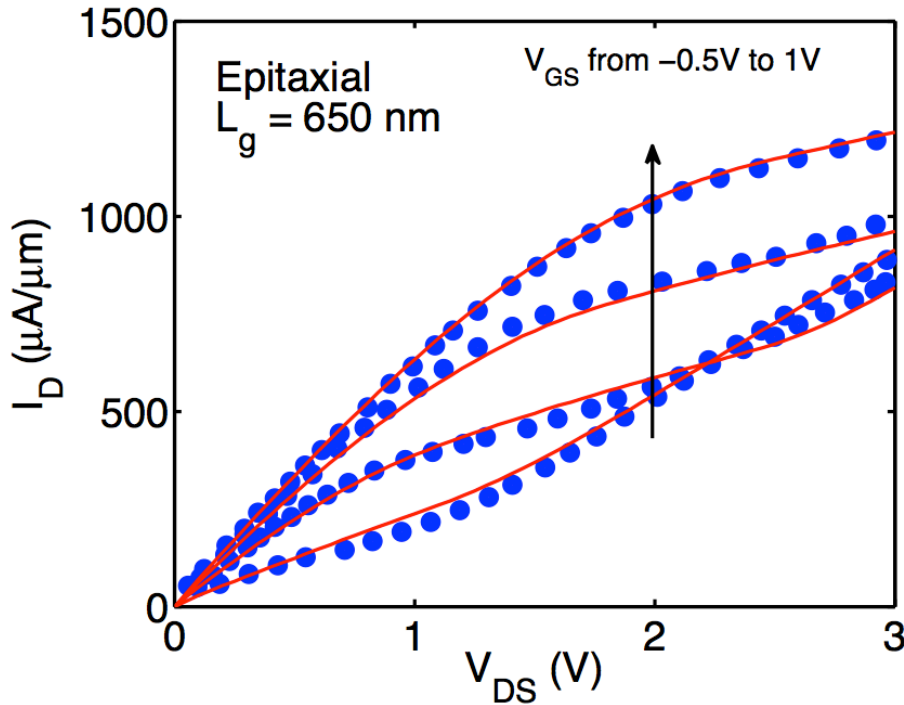
Symbols  $\rightarrow$  experiment

Solid lines  $\rightarrow$  model

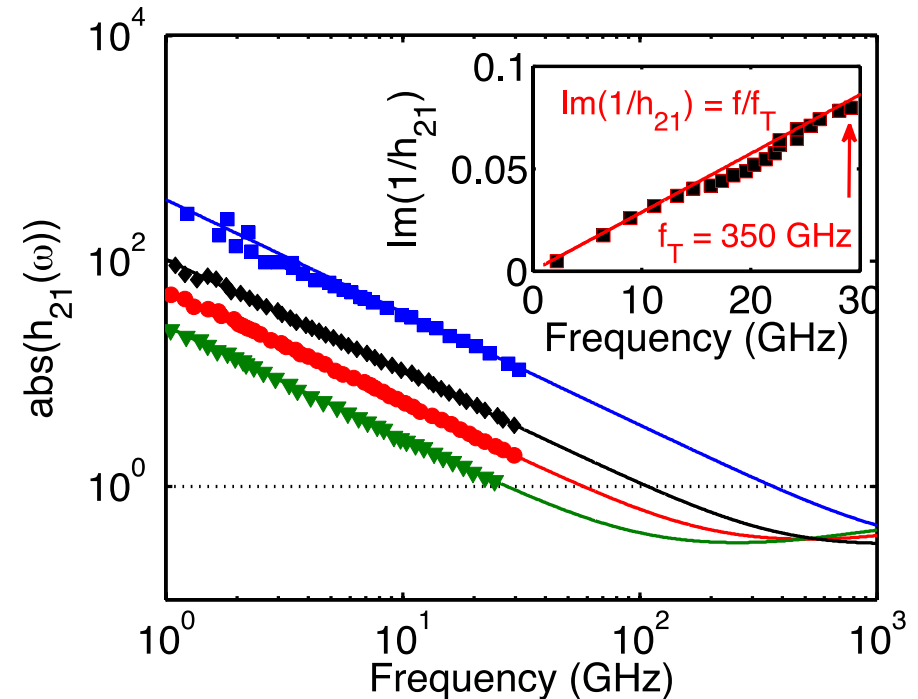


# Ambipolar graphene RF FETs

Output characteristics



Current gain versus freq.

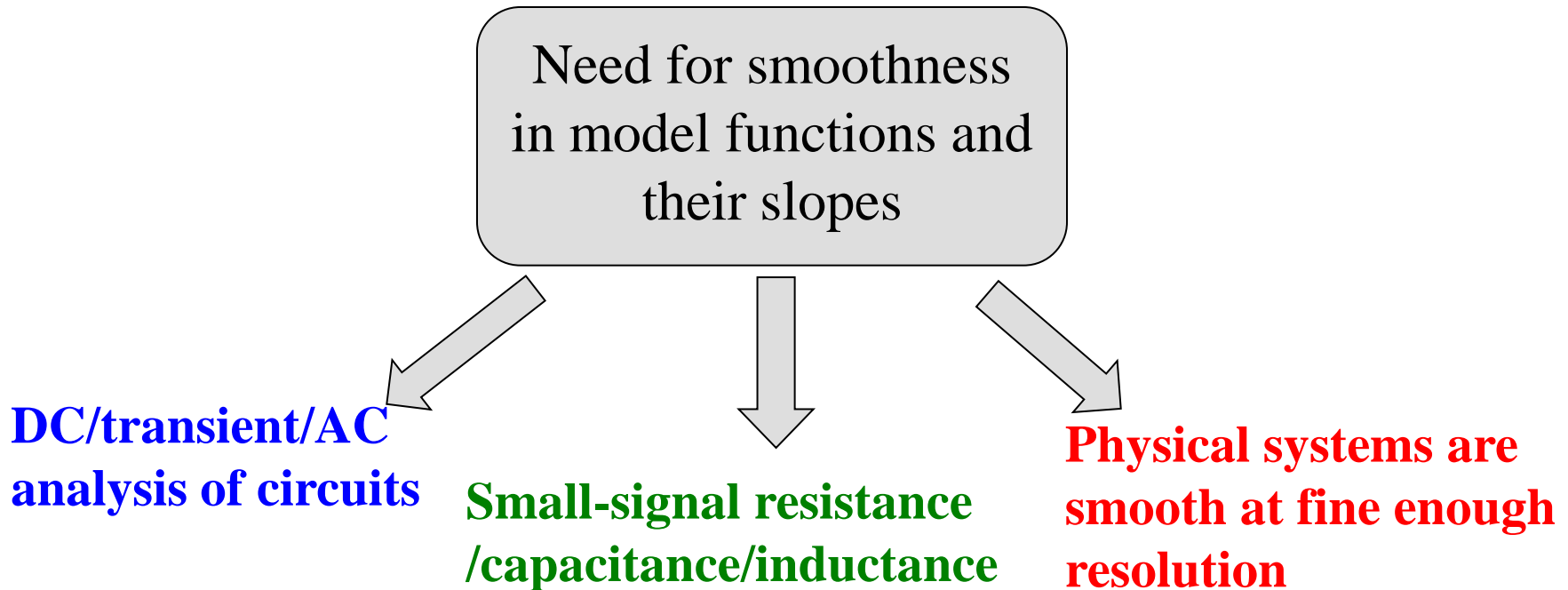


Epitaxial GFETs fabricated at IBM, 2013.

Symbols  $\rightarrow$  experiment  
Solid lines  $\rightarrow$  model

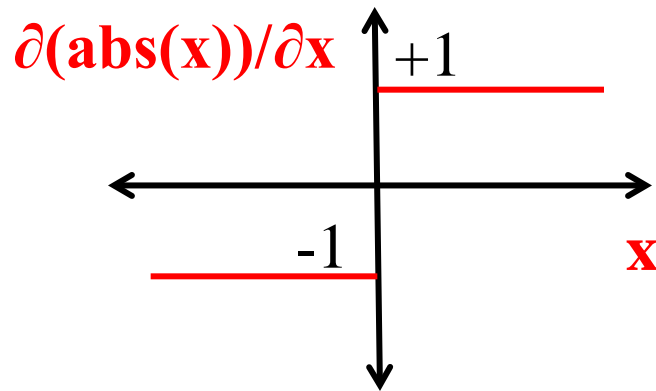
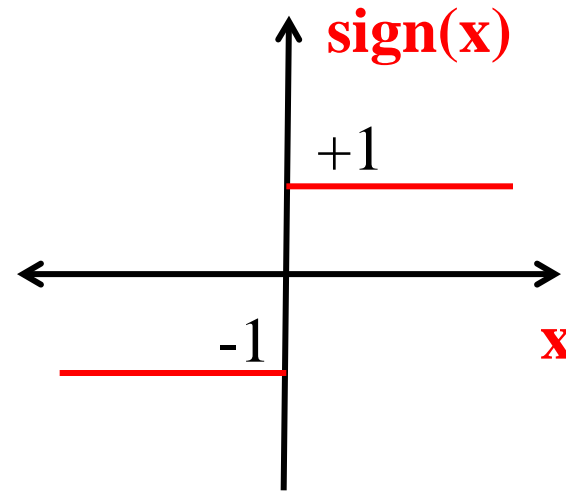
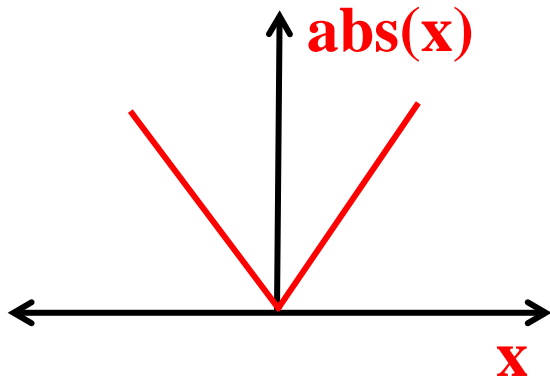
# Mathematical issues in writing compact models: “smoothness” is key

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*“A quick circuit simulation primer” <https://nanohub.org/resources/20610>*

# Example of non-smooth functions

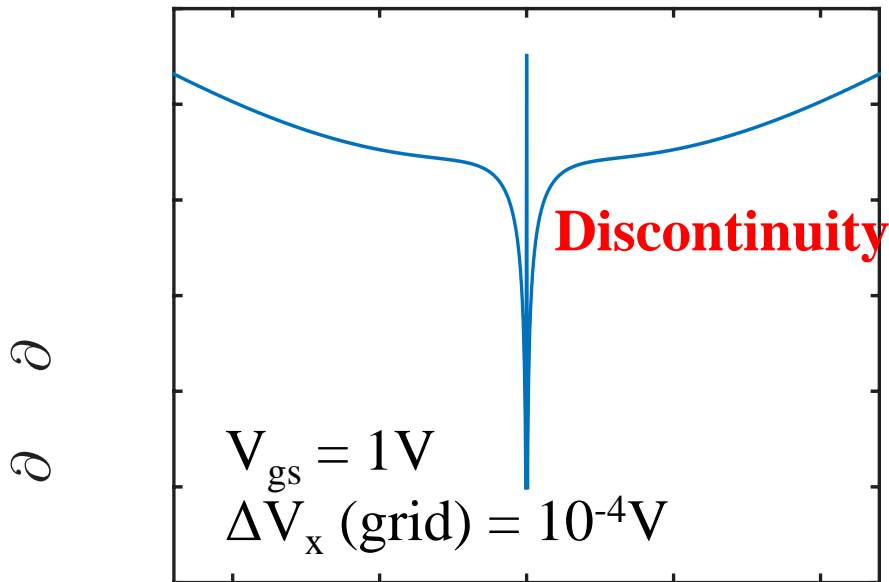


$$I_d = \text{type} \times \text{dir} \times \left( Q_{x0} v_{x0} F_{\text{sat}} \right)$$
$$\text{dir} = \text{type} \times \text{sign} \left( V_d - V_s \right)$$

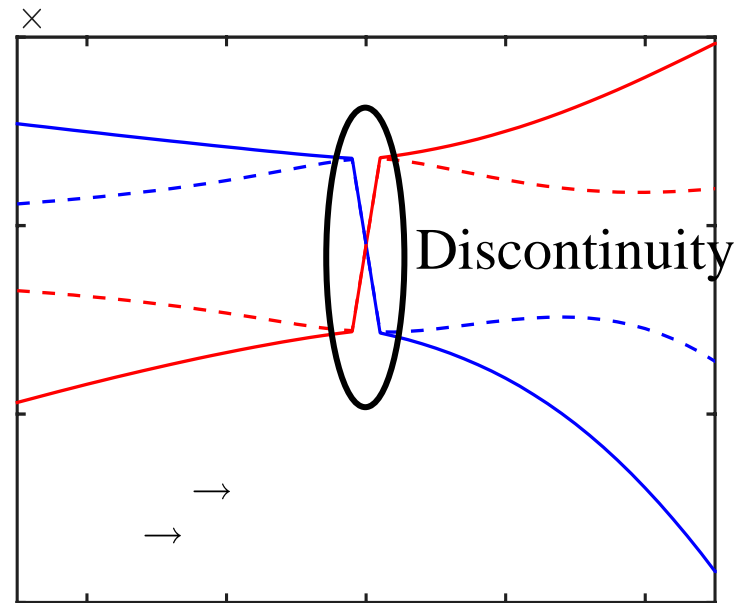
$$V_{ds} = \text{abs} \left( V_d - V_s \right)$$

# Problem areas in MVS model

Third derivative of current



Capacitance versus  $V_{ds}$



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**PART II**  
**MVS model deployment on**  
**nanoHUB**

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# MVS 1.0.1 package release snapshot

**MVS Nanotransistor Model (Silicon) 1.0.1**  
By [Shaloo Rakheja](#)<sup>1</sup>, [Dimitri Antoniadis](#)<sup>1</sup>  
*Massachusetts Institute of Technology (MIT)*

The MIT Virtual Source (MVS) model is a semi-empirical compact model for nanoscale transistors that accurately describes the physics of quasi-ballistic transistors with only a few physical parameters.

Listed in [Compact Models](#) | publication by group [NEEDS: Nano-Engineered Electronic Device Simulation Node](#)

**Version #**  
**Download bundle**

**Abstract**

**Model release components**

**Download Bundle**  
Additional materials available  
Version 1.0.1 - published on Oct 23, 2014  
doi:10.4231/D3H12V82S - [cite this](#)  
Last public release: 1.1.0  
Licensed under NEEDS Modified CMC License according to [these terms](#)

View most current public release [1.1.0] for latest usage information.  
0 citation(s)

**NEEDS: Nano-Engineered Electronic Device Simulation Node**

**See also**  
[III-V Tunnel FET Model](#)  
[FET pH Sensor Model](#)  
[Ambipolar Virtual Source](#)

Model Release Component	Bundle
<a href="#">MVS Nanotransistor Model (Silicon) 1.0.1 Verilog-A</a>	(VA   16 KB)
<a href="#">MVS Nanotransistor Model (Silicon) 1.0.1 Benchmarks</a>	(ZIP   122 KB)
<a href="#">MVS Nanotransistor Model (Silicon) 1.0.1 Model Exerciser</a>	(ZIP   8 KB)
<a href="#">MVS Nanotransistor Model (Silicon) 1.0.1 Parameter Extractor in MATLAB</a>	(ZIP   14 KB)
<a href="#">Experimental Data from Intel 32 nm and 45 nm N-type devices</a>	(ZIP   3 KB)
<a href="#">MVS Nanotransistor Model (Silicon) 1.0.1 Manual</a>	(PDF   7 MB)
<a href="#">License terms</a>	

# MVS 1.0.1 release package contents on nanoHUB: 1/2

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## 1. MATLAB-related

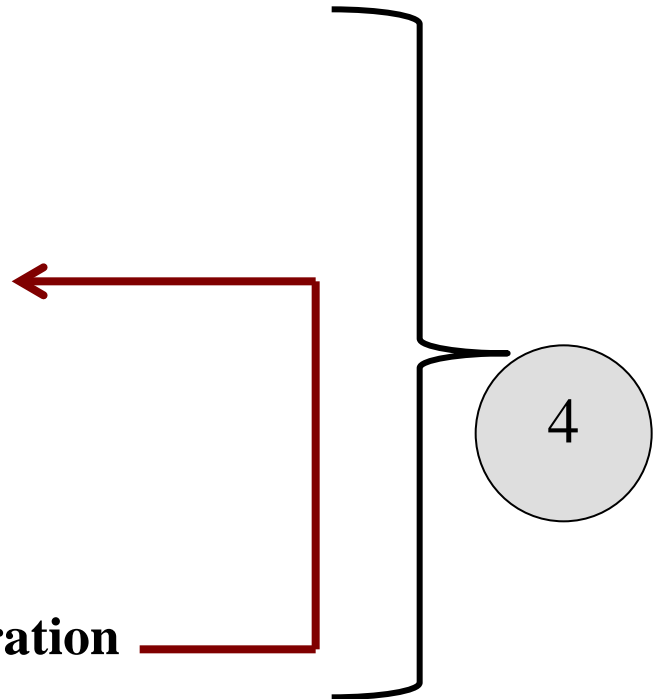
- i. Model implementation
- ii. Model exerciser
- iii. Numerical parameter extractor

## 2. Verilog-related

- i. Model implementation
- ii. Test-benches for simple circuits

## 3. Experimental data for model calibration

## 4. Model manual



# MVS 1.0.0 release package contents on nanoHUB: 2/2

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5. Update log (when a new version is released)
6. License agreement

*Link to the model on nanohub:*

<https://nanohub.org/publications/15>

*Wiki for model-release checklist:*

NEEDS → For Developers → First item on Resources



# Quick checklist for model release

Component	Associated files and/or requirements
<b>MATLAB</b>	<ul style="list-style-type: none"><li>• Model file</li><li>• Model exerciser</li><li>• Parameter extraction (analytical/non-linear)</li><li>• Readme file</li></ul>
<b>Verilog-A</b>	<ul style="list-style-type: none"><li>• Model file</li><li>• SPECTRE/HSPICE netlists for simple circuits</li><li>• Readme file</li></ul>
<b>Experimental data</b>	<ul style="list-style-type: none"><li>• Readme file for data format and references</li></ul>
<b>Model manual</b>	<ul style="list-style-type: none"><li>• Explaining all of the model equations</li><li>• Simulation results</li><li>• Extraction methodology</li><li>• Proper references</li></ul>

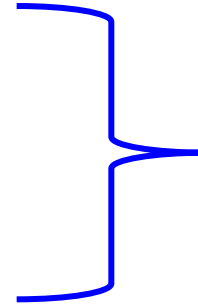
CMC license agreement  
+  
Update log (if needed)

# MVS-related seminars on nanoHUB

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- NEEDS Compact Model Release –  
Lessons Learned from MVS 1.0.0

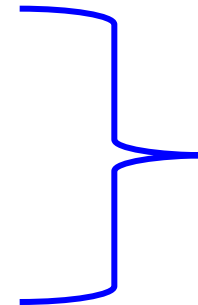
<https://nanohub.org/resources/20139>



Steps to follow  
when releasing  
your own  
compact model

- The MVS Nanotransistor Model:  
A Case Study in Compact Modeling

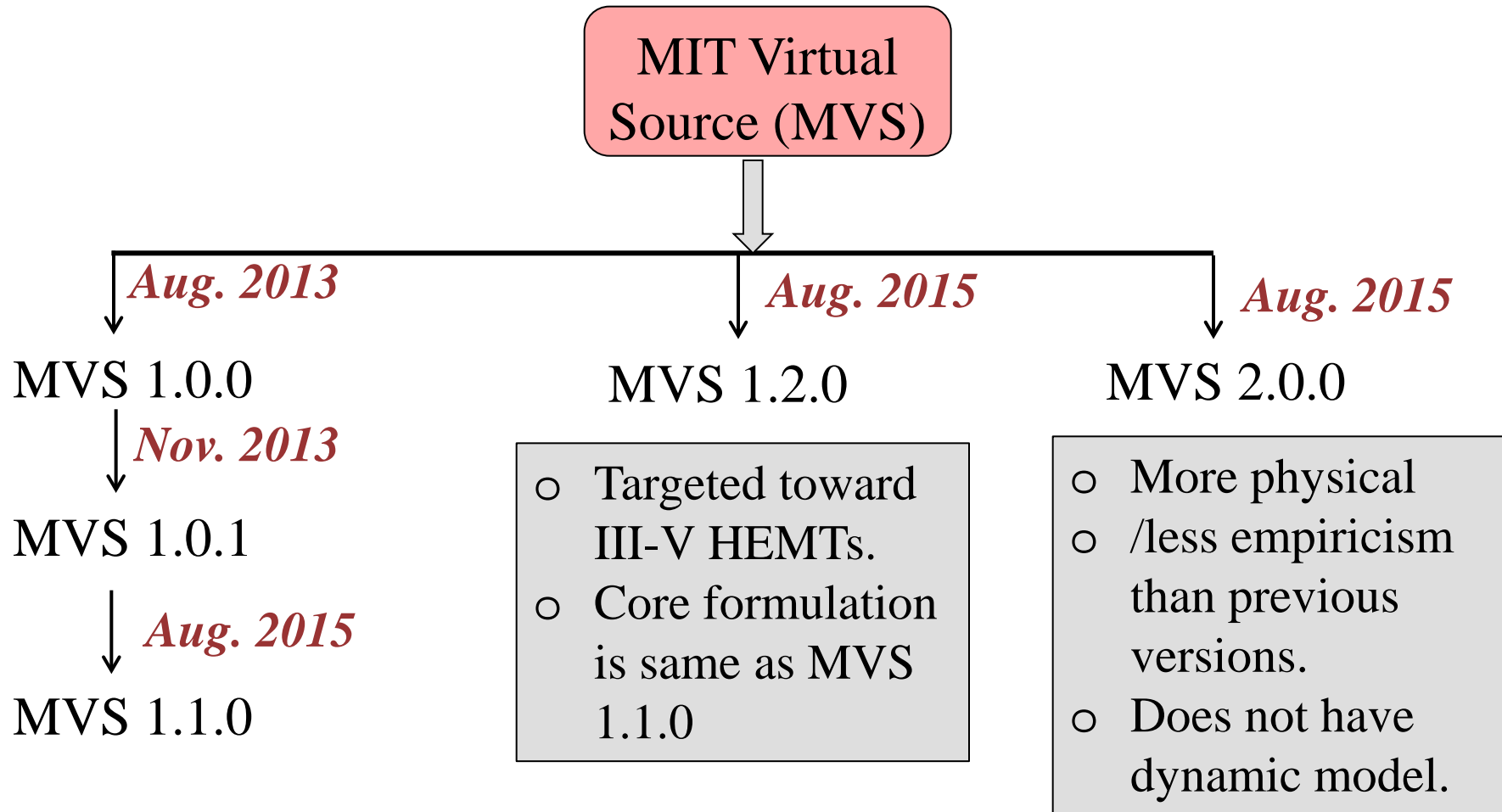
<https://nanohub.org/resources/21712>



Dealing with  
mathematical  
issues in compact  
models

# MVS model evolution

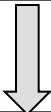
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# MVS model evolution

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MIT Virtual Source (MVS)



*Aug. 2013*

**MVS 1.0.0**

*Nov. 2013*

**MVS 1.0.1**

*Aug. 2015*

**MVS 1.1.0**

Original MVS model  
[2009, 2012]

# MVS 1.0.0 model evolution

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## Issues:

- Unused variables
- Hidden states
- Parameter range
- Indentation

## Issues:

- **Capacitance discontinuity**
- Better ways needed to fix some other numerical issues in VA

- While we fixed some existing bugs in MVS 1.0.1, the mathematical issues still exist.

# MVS model evolution

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MIT Virtual Source (MVS)

*Based on Landauer transmission theory*

*Accounts for non-equilibrium conditions in the channel*

*Non-linearity of access region resistances*

*Aug. 2015*

MVS 2.0.0

- More physical
- /less empiricism than previous versions.
- Does not have dynamic model.

# MVS 2.0.0

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## MVS 2.0.0 provides two implementations:

- For III-V HEMTs which have degeneracy and gm-reduction under high drain current
- For Si ETSOI devices which operate under non degeneracy and do not have any gm-reduction.

MVS 2.0.0 provides **only static transport model**.

<https://nanohub.org/publications/74>

} Contains links to all other versions of MVS

## MVS Nanotransistor Model 2.0.0

By [Shaloo Rakheja](#)<sup>1</sup>, Dimitri Antoniadis<sup>1</sup>

Massachusetts Institute of Technology (MIT)

The MIT Virtual Source (MVS) model is a semi-empirical compact model for nanoscale transistors that accurately describes the physics of quasi-ballistic transistors with only a few physical parameters.

Listed in [Compact Models](#) | publication by group [NEEDS: Nano-Engineered Electronic Device Simulation Node](#)

About

Supporting Docs

Versions

Reviews

Wishlist

Questions

Citations

### Abstract

MVS 2.0.0 is an improved physics-based virtual source (VS) model to describe transport in quasi-ballistic transistors. The model is based on Landauer scattering theory and includes (i) degeneracy on thermal velocity and mean free path of carriers in the channel, (ii) drain-bias dependence of gate capacitance and VS charge including the effects of non-linear resistance of the extrinsic device region on gm-degradation at high drain currents in the channel.

Other MIT Virtual Source Models:

- [MVS 1.2 HEMT](#)

This version of the MVS model is specifically targeted toward III-V HEMT devices that show a reduction in the transconductance at high drain currents. The model includes a mechanical correction to the gate-channel capacitance.

Finally, the static transport model is supplemented with a charge partitioning model. As in the previous MVS model versions, we provide the drift-diffusion model (NVSAT) and blended quasi-ballistic charge model.

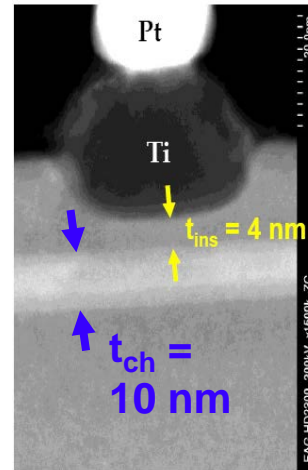
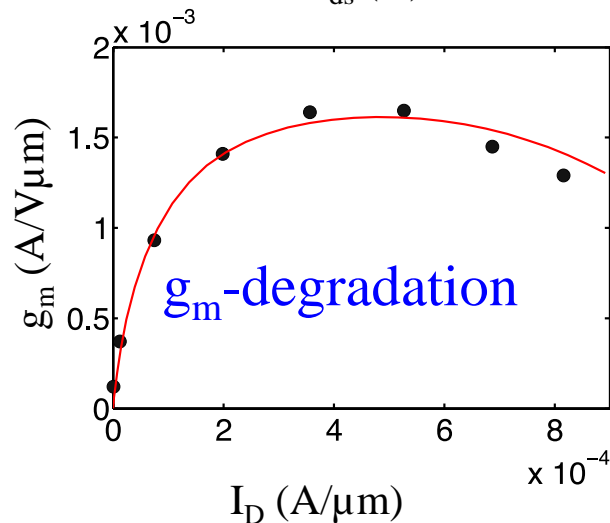
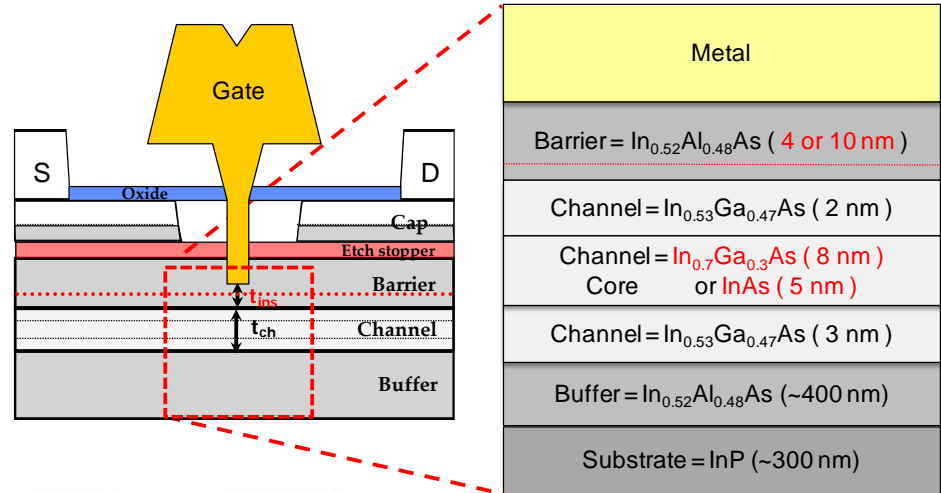
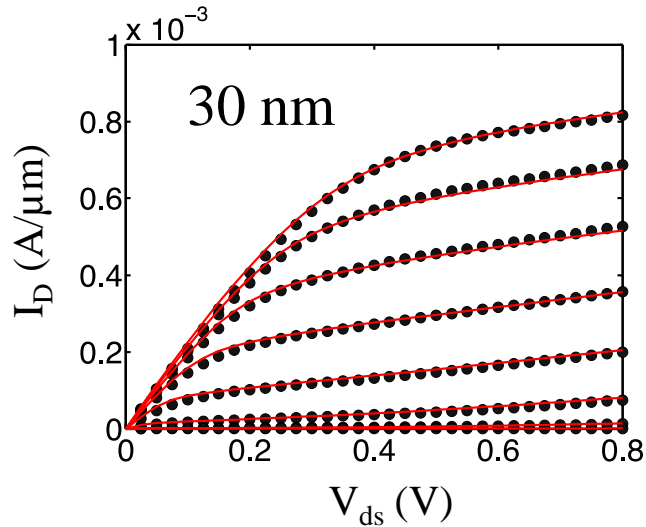
- [MVS 1.1 Silicon](#)

This version of the MVS model is specifically targeted toward silicon devices. It contains slightly more empiricism than the more detailed MVS 2.0, and it is based on compact models.

*Links to all MVS versions  
available on the same page*



# InGaAs HEMTs with MVS 2.0.0



- $L_{eff} = [30, 40, 60, 80, 130] \text{ nm}$
- Fabricated at MIT, 2009.

# Key references for MVS 2.0.0

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- S. Rakheja, M. Lundstrom, D. Antoniadis, “An Improved Virtual-Source-Based Transport Model for Quasi-Ballistic Transistors – Part I: Capturing Effects of Carrier Degeneracy, Drain-Bias Dependence of Gate Capacitance, and Non-linear Channel-Access Resistance,” **IEEE Transactions on Electron Devices, vol. 62, no. 9, pp. 2786-2793, Sep. 2015.**
- S. Rakheja, M. Lundstrom, D. Antoniadis, "An Improved Virtual-Source-Based Transport Model for Quasi-Ballistic Transistors – Part II: Experimental Verification,” **IEEE Transactions on Electron Devices, vol. 62, no. 9, pp. 2794-2801, Sep. 2015.**

# Summary- MVS nanotransistor models

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- Two VS Models (MVS-1 and 2) provide a progression of approximation accuracy to the Transmission Model suitable for any FET structure.
- Despite its simplicity MVS-1 provides a suitable tool for FET carrier transport benchmarking for technology assessment.
- MVS-2 is based on physically sound charge-control and transport models to allow quantitative analysis of band-structure characteristics.

# MVS future plans

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**Discontinuity ?**

MIT Virtual Source (MVS)

*Aug. 2013*

MVS 1.0.0

*Nov. 2013*

MVS 1.0.1

*Aug. 2015*

MVS 1.1.0

*Aug. 2015*

MVS 1.2.0

*Aug. 2015*

MVS 2.0.0

○ **Dynamic model**

○ **Current and capacitance discontinuity at  $V_{ds} = 0V$  ?**

**MVS 2.1.0**