

# PVLimits: PV thermodynamic limit calculator

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*Documentation*

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## 1 Introduction and tool summary

PVLimits software calculates the thermodynamic performance limits of single-junction (SJ) and multi-junction (MJ) solar cells. The user may choose the input spectrum (e.g., AM1.5G or Blackbody, distance from the Sun, concentration, etc.) and specify the parameters of the solar cell (temperature, bandgap, number of subcells in MJ cell etc.).

The calculations are based on detailed particle balance in the radiative limit: the absorbed solar photon flux ( $R_{in}$ ) is balanced by radiative recombination ( $R_{rad}$ ) and the carrier collection (electrical current,  $J$ ), as follows:

$$R_{in} = \frac{J(V)}{q} + R_{rad}(V).$$

Here,  $R_{in}$  (i.e., absorption flux) depends on the temperature of the ‘Sun’, the bandgap ( $E_g$ ) of the solar cell, and its distance from the Sun. The radiative recombination  $R_{rad}(V)$  depends on the temperature of the device,  $E_g$  and bias  $V$ . See refs. [1]–[5] for more details.

PVLimits has options to calculate the following:

1. Single junction PV:
  - a. J-V for a single bandgap
  - b. Eg-sweep: PV output parameters as a function of bandgap ( $E_g$ )
2. Multi-junction PV:
  - a. J-V for a given number of subcells ( $N$ ). The bandgaps are optimized accordingly
  - b. N-sweep: PV output parameters as a function of number of subcells ( $N$ ).

The usage of the tool is explained in the following sections.

## 2 Using the tool

### 2.1 Input

There are three parts in the input panel (see fig-1):

1. Simulation setup
2. PV inputs (simulation specific inputs)
3. Spectral input

We will discuss these three input parts in the following subsections.

### 2.1.1 Simulation setup

There are four simulation options as mentioned earlier:

1. Single junction PV:
  - a. J-V characteristics for a single bandgap
  - b. Eg-sweep: PV output parameters as a function of bandgap ( $E_g$ )
2. Multi-junction PV:
  - a. J-V characteristics for a given number of subcells ( $N$ ). The bandgaps are optimized accordingly
  - b. N-sweep: PV output parameters as a function of number of subcells ( $N$ ).

The image shows a software interface titled "PV thermodynamic limit calculator". It is divided into several sections:

- Simulation setup:** This section contains three dropdown menus: "Junction Type" (set to "Single Junction"), "Single Junction Options" (set to "J-V"), and "Multi Junction Options" (set to "J-V").
- Simulation specific input:** This section includes:
  - Bandgap:** A text input field with "Eg: 1.3eV".
  - V range:** Three input fields: "V min: 0V", "V max = Eg", and "V increment: 0.001V".
  - Binding energy of exciton:** An input field with "0eV".
  - Discontinuity at conduction band:** An input field with "0eV".
- Spectral input:** This section includes:
  - Sun Temperature:** A slider set to "5778K".
  - Device Temperature:** A slider set to "300K".
  - Solar Spectrum:** A dropdown menu set to "AM1.5G".
  - Distance from sun (unit: 1e9 m):** An input field with "150".
  - Cut-off energy (top filter):** An input field with "100eV".
  - Albedo,  $\rho$ :** An input field with "0".
  - Solar concentration factor:** An input field with "1".
  - Device angle restriction factor:** An input field with "1".

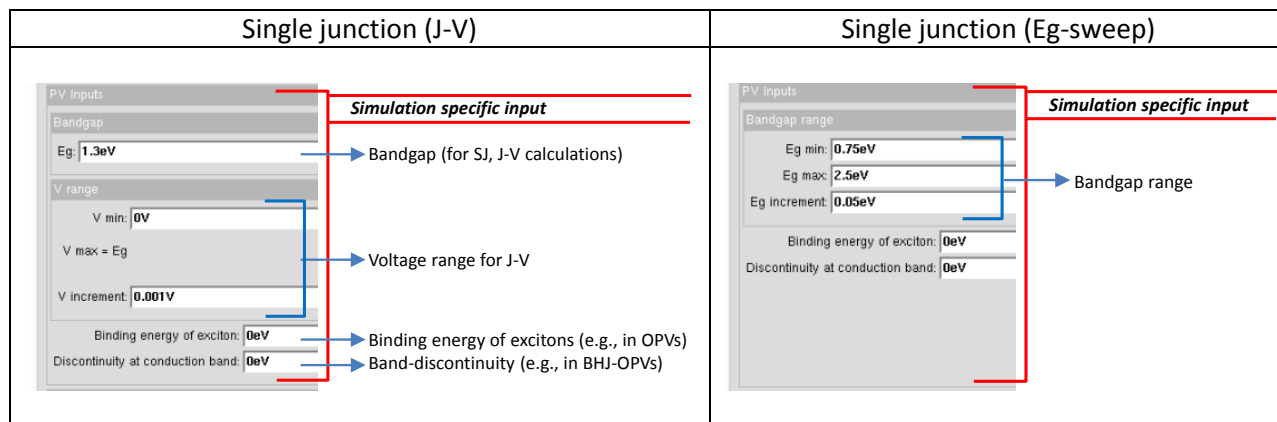
Red lines and arrows on the right side of the interface group these sections into three categories:

- Simulation setup:** Points to the three dropdown menus.
- Simulation specific input:** Points to the Bandgap, V range, Binding energy of exciton, and Discontinuity at conduction band fields. A text box next to it says "These set of inputs change based on the choice of simulation setup".
- Spectral input:** Points to the Sun Temperature, Device Temperature, Solar Spectrum, Distance from sun, Cut-off energy, Albedo, Solar concentration factor, and Device angle restriction factor fields.

Figure 1: Simulation setup and input parameter summary for PVLimits tool.

### 2.1.2 PV inputs

The input parameters available in this pane depend on the choice of simulation setup.



The binding energy of exciton is relevant for an excitonic solar cell (e.g., OPVs). The band-discontinuity restricts radiative emission primarily to the heterojunction (HJ) or the cross-gap. The thermalization and the band-discontinuity are assumed to provide energy for probable exciton dissociation in the system [6]. All the calculations for the single junction PV are based on refs [2], [6].

For the multi-junction simulations, the number of subcells (N) is the only input in this section. (NOTE: MJ solar cells simulated here are always bifacial, i.e., they emit from both front and back faces.)

### 2.1.3 Spectral input

The spectral input pane is the same for all the simulation setups. This input-set is briefly mentioned in Fig-1. The spectral input parameters are explained in more details in the following table:

Parameter	Default value	Comments
Sun temperature	5778 K	Temperature of the source (temperature can be changed for other systems, e.g., for thermo-photovoltaics). NOTE: keep at default while using AM1.5G.
Device temperature	300 K	
Spectrum	AM1.5G	[AM1.5G or ideal Blackbody]
Distance from sun	150 (*1e9m)	This is the distance from the source to the device. The distance will change the incident solid angle.
Cut-off energy [top filter]	100 eV	This allows a low-pass energy filter at the top. In a compound system, the high energy photons can be redirected for other applications.
Albedo, R	0	Range: [0, 1]. This is the effective scattered light from the surroundings to the back of the solar module
Concentration factor	1	Range: >0. For a concentrator PV, this factor is $\geq 1$ . However, for a cloudy day or lower intensity input, the simulator also allows concentrator factor of [0,1].
Angle restriction factor	1	The factor by which the emission solid angle is restricted.

(For some relevant distances from the sun see: <http://www.pveducation.org/pvcdrom/properties-of-sunlight/solar-radiation-in-space> )

## 2.2 Simulation Output

Once the simulation is done using a choice of input-sets, the results can be found from the drop-down list. Results can be compared for different sets of 'PV inputs' and 'Spectral inputs'. (NOTE: we recommend clearing the results before simulating a new 'Simulation setup').

The summary of the outputs are given below:

Output	Description
<b>Single junction J-V</b>	
Fraction of incident solar radiation	Output power and all the power loss components normalized to the net input solar power
J, Jopt vs. V	J-V curve (J in mA/cm <sup>2</sup> )
Simulation log	List of output parameters. NOTE: net solar illumination is the incident flux (before any concentration)
<b>Single junction Eg-sweep</b>	
Fraction of solar radiation	Output power and all the power loss components normalized to the net input solar power. See [2], [6] for details and physics.
Efficiency matrix	This is the set of values in the plot of 'fraction of solar radiation' or power budget. The first column is the bandgap Eg (eV). The subsequent columns contains the power components mentioned in the previous plot.
Efficiency vs Eg	
Jsc vs Eg	
Voc vs Eg	
FF vs Eg	
Voc, Vopt vs Eg	
Jsc, Jopt vs Eg	

Output	Description
<b>Multi-junction J-V</b>	
Jsc, J_fit vs Eg	Blue line: Jsc vs Eg. Red line: a straight line fit for Jsc vs Eg for 0.5 to 1.7eV. The fitting equation: $J_{sc} = J_{SUN} (1 - \beta \cdot E_g)$ . The fitting parameters are given in the simulation log
J, Jopt vs V	The J-V curve
Subcell index vs Eg	The bandgap sequence in the optimized tandem
Simulation log	Summary of output parameters
<b>Multi-junction N-sweep</b>	
Jsc, J_fit vs Eg	[explained as before]
Simulation log	Summary of output parameters
Eg vs no of subcells	This shows the optimized tandem bandgap-sets for N-subcells
Eg matrix	The bandgap values from the previous plot is given in this matrix
Normalized efficiency vs N	The output is normalized to 1-sun to find the normalized efficiency
Voc, Vopt vs N	
Jsc vs N	

### 3 Illustrative Example

#### 3.1 Single junction Eg-sweep

Input set: (Eg-sweep with AM1.5G illumination)

Junction Type: Single Junction  
 Single Junction Options: Eg-sweep  
 Multi Junction Options: N-sweep

**PV Inputs**

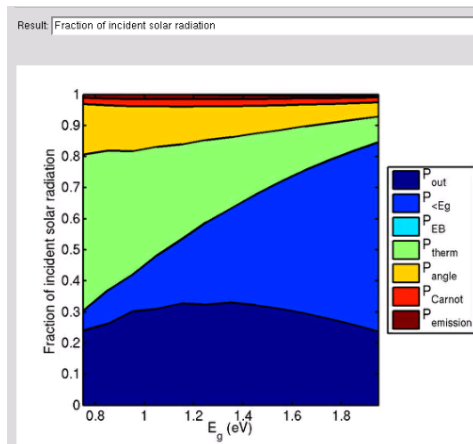
Bandgap range  
 Eg min: 0.75eV  
 Eg max: 2eV  
 Eg increment: 0.1eV

Binding energy of exciton: 0eV  
 Discontinuity at conduction band: 0eV

**Spectral Inputs**

Sun Temperature: 5778K  
 Device Temperature: 300K  
 Solar Spectrum: AM1.5G  
 Distance from sun (unit: 1e9 m): 150  
 Cut-off energy (top filter): 100eV  
 Albedo,  $\rho$ : 0  
 Solar concentration factor: 1  
 Device angle restriction factor: 1

Output sets: (power budget; for physics see [2], [6])

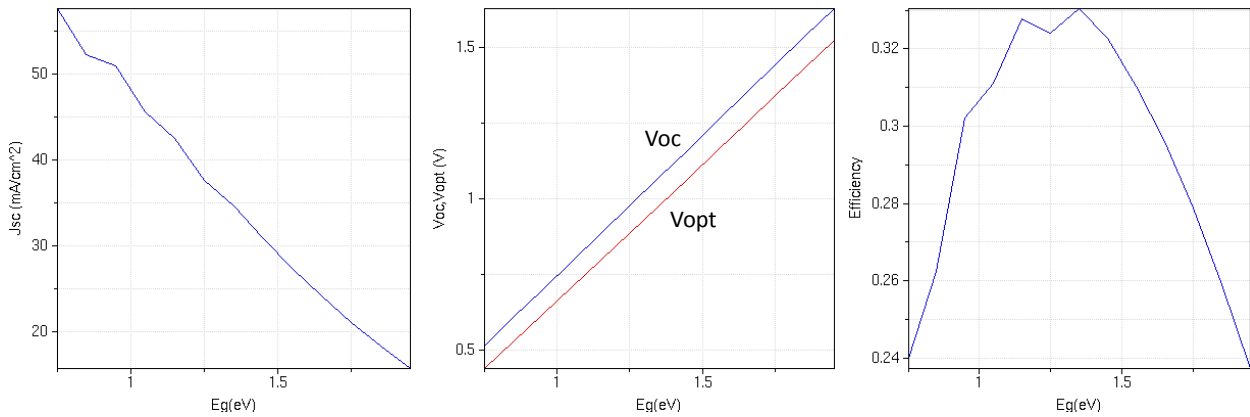


Result: Efficiency Matrix

0.7500	0.2400	0.0636	0.0000	0.5039	0.1614	0.0212	0.0234
0.8500	0.2625	0.1069	0.0000	0.4493	0.1471	0.0219	0.0213
0.9500	0.3020	0.1182	0.0000	0.3975	0.1446	0.0241	0.0201
1.0500	0.3110	0.1714	0.0000	0.3492	0.1303	0.0240	0.0168
1.1500	0.3277	0.2066	0.0000	0.3051	0.1218	0.0246	0.0149
1.2500	0.3241	0.2644	0.0000	0.2651	0.1082	0.0237	0.0132
1.3500	0.3306	0.3026	0.0000	0.2291	0.1000	0.0237	0.0120
1.4500	0.3226	0.3553	0.0000	0.1963	0.0894	0.0227	0.0104
1.5500	0.3105	0.4084	0.0000	0.1672	0.0792	0.0215	0.0096
1.6500	0.2961	0.4599	0.0000	0.1416	0.0700	0.0203	0.0082
1.7500	0.2788	0.5106	0.0000	0.1191	0.0614	0.0189	0.0073
1.8500	0.2591	0.5603	0.0000	0.0994	0.0535	0.0174	0.0061
1.9500	0.2375	0.6093	0.0000	0.0823	0.0460	0.0158	0.0049

Eg (eV)      Output,  $P_{out}$   
 Below Eg,  $P_{<Eg}$   
 Binding energy loss,  $P_{EB}$   
 Thermalization loss,  $P_{therm}$   
 Angle entropy,  $P_{angle}$   
 Carnot loss,  $P_{Carnot}$   
 Emission loss,  $P_{emission}$

Output sets: (Jsc, Voc, Vopt, efficiency)



### 3.2 Multi-junction N-sweep: (albedo, R=0.3)

**Junction Type:** Multi Junction

**Single Junction Options:** Eg-sweep

**Multi Junction Options:** N-sweep

**PV Inputs**

Multi Junction Subcell Number Range

**Nmin:** 1

**Nmax:** 7

Binding energy of exciton: 0eV

Discontinuity at conduction band: 0eV

**Spectral Inputs**

**Sun Temperature:** 5778K

**Device Temperature:** 300K

**Solar Spectrum:** AM1.5G

Distance from sun (unit: 1e9 m): 150

**Cut-off energy [top filter]:** 100eV

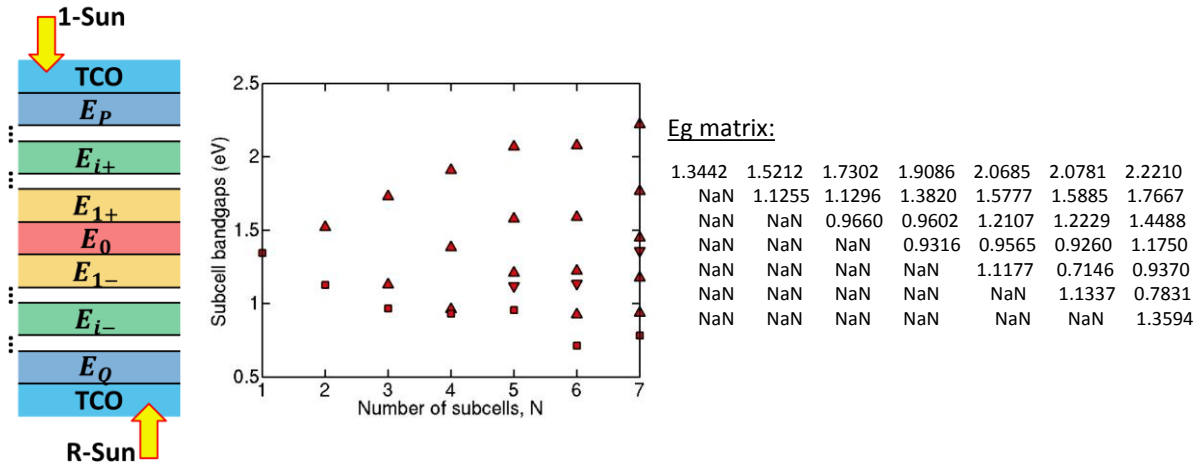
**Albedo, R:** 0.3

Solar concentration factor: 1

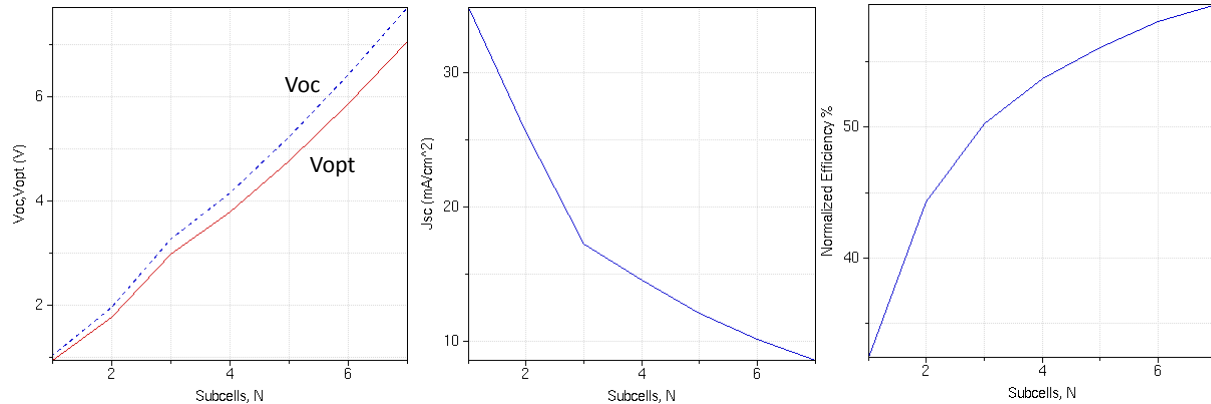
Device angle restriction factor: 1

Output sets: (optimized badgaps for tandem)

For conventional tandems, the bandgaps of the subcells always have decreasing values starting from top. However, for bifacial tandem there are sources from both sides—therefore, scanning from top to bottom subcells: top most subcell has the largest bandgap, then the bandgap reaches some minimum ( $E_0$ ) and then increases again. In the output plot for bandgaps vs number of subcells: the squares ( $\square$ ) mark  $E_0$ . The  $\Delta$  and  $\nabla$  markers represent bandgaps for the front  $\{i+\}$  (subcells on top of  $E_0$ ) and bottom  $\{j-\}$  (subcells below  $E_0$ ).



Output sets: ( $J_{sc}$ ,  $V_{oc}$ ,  $V_{opt}$ , efficiency)



## 4 References

- [1] W. Shockley and H. J. Queisser, "Detailed Balance Limit of Efficiency of p-n Junction Solar Cells," *J. Appl. Phys.*, vol. 32, no. 3, p. 510, 1961.



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- [3] M. A. Alam and M. R. Khan, "Fundamentals of PV efficiency interpreted by a two-level model," *American Journal of Physics*, vol. 81, no. 9, pp. 655–662, Sep. 2013.
- [4] M. R. Khan and M. A. Alam, "Thermodynamic limit of bifacial double-junction tandem solar cells," *Applied Physics Letters*, vol. 107, no. 22, p. 223502, Nov. 2015.
- [5] M. A. Alam and M. R. Khan, "A Markov Chain Approach for Defining the Fundamental Efficiency Limits of Classical and Bifacial Multi-junction Tandem Solar Cells," 2016.
- [6] M. R. Khan and M. . Alam, "Critical binding energy for exciton dissociation and its implications for the thermodynamic limit of organic photovoltaics," in *Device Research Conference (DRC), 2014 72nd Annual*, 2014, pp. 281–282.