

1. Plate glass casting

High-quality plate glass is cast with extremely flat surfaces by floating it on molten tin and letting it cool as the glass and tin flow down a gently inclined plane.

Data:

- Liquid glass entering the process:  $\rho = 3.2 \frac{\text{g}}{\text{cm}^3}$ ,  $\mu = 1.0 \frac{\text{N}\cdot\text{s}}{\text{m}^2}$ , layer thickness=1mm.
  - Liquid tin:  $\rho = 7.0 \frac{\text{g}}{\text{cm}^3}$ ,  $\mu = 3 \times 10^{-3} \frac{\text{N}\cdot\text{s}}{\text{m}^2}$ , layer thickness=1mm.
  - Inclined plane angle:  $2^\circ$ .
- (a) Write the general solution to the equation for momentum conservation down the inclined plane in the flow direction.
- (b) What is the interface boundary condition at the glass-tin interface?
- (c) Calculate the velocity distribution in both the glass and the tin. (Hint: measure distance in the tin from the bottom, and distance in the glass from the top surface.)
- (d) What are the maximum and average velocities in the glass and tin?
- (e) Comment on the Reynolds numbers in the glass and tin. Do you think flow will remain laminar in both layers?