



A Single Atom Transistor: The Ultimate Scaling Limit – Entry into Quantum Computing

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ESSxxRC 2020 Quantum Tutorial Gerhard Klimeck



The Ultimate Scaling Limit Entry into Quantum Computing

Why?



Inspired Modeling

What is it?

How to model this new world?

Where to study this?



Thanks to





Research Group @Purdue @NASA JPL 1998-2003 @Texasulnstruments 1994-1998











Collaborators:

Michelle Simmons, Sydney Lloyd Hollenberg, Melbourne Alan Seabaugh, Notre Dame

Intel Roadmap

Innovation Enabled Technology Pipeline Our Visibility Continues to Go Out ~10 Years





© Gerhard Klimeck http://www.chlpworks.com/media/wpmu/uploads/blogs.dir/2/files/2012/08/Intel22nmPMOSfin.jpg





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Roadmap of finite atoms!



Roadmap of finite electrons!



Quantum Dot Research





FinFETs with finite electrons



- How should one think about
- finite number electron transport?

• Each device has a specific fingerprint => Metrology of As vs P impurities

FinFETs with finite electrons



Source

150

HOW

Gate

D-H

E∔

С

(Na) (NA)

0.1

100





nature

1CS

Gate-induced quantum-confinement transition of a single dopant atom in a silicon FinFET

G. P. LANSBERGEN¹*, R. RAHMAN², C. J. WELLARD³, I. WOO², J. CARO¹, N. COLLAERT⁴, S. BIESEMANS⁴, G. KLIMECK^{2,5}, L. C. L. HOLLENBERG³ AND S. ROGGE¹

¹Kavli Institute of Nanoscience, Delft University of Technology, Lorentzweg 1, 2 ²Network for Computational Nanotechnology, Purdue University, West Lafayette ³Center for Quantum Computer Technology, School of Physics, University of Me ⁴InterUniversity Microelectronics Center (IMEC), Kapeldreef 75, 3001 Leuven, B ⁵Jet Propulsion Laboratory, California Institute of Technology, Pasadena, Califo *e-mail: G.P.Lansbergen@tudelft.nl

- finite number electron
- Each device has a specific fingerprint => Metrology of As vs P impurities

The single-atom transistor

Presentation Outline

- Why?
 - Continuum invalid
 - => finite atoms/electrons
- What is it?
 - Coulomb diamond
 - How is it built?
 - Results
- How to model this?
 NEMO
- Where to study this?
 nanoHUB.org











"The I-V curve of atomic transistors"



Experimental Data



A single-atom transistor, M. Fuechsle et.al. *Nature Nanotechnology, 2012*





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CENTRE FOR QUANTUM COMPUTATION & COMMUNICATION TECHNOLOGY

AUSTRALIAN RESEARCH COUNCIL CENTRE OF EXCELLENCE

A designed single electron transistor! • Gerhard Klimeck How did we get there?

Experimental Efforts: STM Lithography

Objectives

- Precise donor placement
- Place "many" donors in ultra-scaled region

Scanning Tunneling Microscopy

- Device surface imaging
- Control/pattern at atomic scales

Eagler et al, Nature (1990)

- Densely P δ-doped Si (Si:P) device
 - Doping control ~ 5x10⁻¹⁰(m)
 - Up to 1/2.9ML (1 P atom per every 2.9 Si atoms)

Fabricating single ML thick P doped planes using STM lithography



Ruess et al., Nano Lett. (2004) Picture edited



Si:P System

- Densely Phosphorus δ -doped Si (Si:P) device
 - » Thin densely P doped layer in low-doped/intrinsic Si bulk
 - » Electrons strongly confined in P doped layer





Single Impurity Outline



RDUE © Gerhard Klimeck



2-D Doping Plane (1A): Semi-metallic Property

Objective

 Explain metallic property of 1/4ML doped 2-D Si:P layer

Approach

- Supercell, 2-D periodic BC
- Dispersion at charge neutrality

Results

- Donor-bands in Si gap
- Non-zero DOS near EF
- Semimetal \rightarrow DOS Fluctuation
- Agree with previous studies
- Our approach:
 - → Much larger systems!

(1A) Int'l Workshop for Comp. Elec. (2009) IEEE NANO (2010)





3D→2D→1D projection of Si [100] nanowire





Donor bands are observed below the Si bulk band gap

» Conduction band minimum of Si bulk \rightarrow 0(eV)





Donor bands are observed below the Si bulk band gap

» Conduction band minimum of Si bulk \rightarrow 0(eV)





Donor bands are observed below the Si bulk band gap

» Conduction band minimum of Si bulk \rightarrow 0(eV)





Band-Projection: A comparison to Si UTB



39 Klimeck tools:Classroom use:- >71,000 users>11,000 students- >2.3 million simulations>64 universities





Single Impurity Outline





Band projection in [100] Si:P wires

• 3D→2D→1D projection of Si [100] nanowire





Band projection in [110] Si:P wires

• $3D \rightarrow 2D \rightarrow 1D$ projection of Si [110] nanowire





Band Projection in [100]/[110] Si:P Quantum Wire





1-D Nanowire (2A): Semi-metallic Property

Objective

- Experiment: Ohmic conduction
- Explain metallic property of 1/4ML doped Si:P nanowire

Approach

- Supercell, 1-D periodic BC
- Dispersion at charge neutrality

Remark

Expensive computation.
 → compared to 2-D Si:P plane

Results

- Donor bands : 6 modes
- Non-zero DOS near EF
- Semimetal → DOS Fluctuations
 (2A) IEEE Silicon Nanoelectronics Workshop (2010)

121 * 124 * 2 = 30,008 atoms





Single Impurity Outline

AAAS

1) Si:P Doping Plane (2-D)

- 1A) Semi-metallic property
- 1B) Sensitivity to doping disord

121 * 8 = 968 atoms

2) Si:P Nanowire (1-D)

- 2A) Semi-metallic property
- 2B) Modulation of channel conductance
- 2C) Resistance-limit of Si Nanowire
- 2D) Sensitivity of resistance to doping disorder

121 <u>* 124 * 2 = 30,008 atoms</u>

3) Single-donor Quantum-dot (0-D)

- **3A) Channel Modulation**
 - → Single-electron transport

40 x 40 x 10 nm³ ~ 1million atoms

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Ohm's Law Survives to the Atomic Scale Science

B. Weber,¹ S. Mahapatra,¹ H. Ryu,²* S. Lee,² W. C. T. Lee,¹ G. Klimeck,² L. C. L. Hollenber

As silicon electronics approaches the atomic sc in size to the active device components. Maint

challenging because of the presence of confining surfaces and interfaces. We report






Results: Contact Modeling

Modeling of Si/P contacts

- Leads show *semi-metallic* behavior (non-zero DOS near E_F)
- Electrons strongly confined to leads (leads densely doped)





Potential Profile



Potential profile

- Thomas-Fermi calculation for potential landscape <u>without</u> ionized donor Klimeck et al, APL (1995) 40 x 40 x 10 nm³ ~ 1million atoms
- Donor potential
 - ✓ Empty state: Analytical Coulomb potential R.Rahman et al. PRL 2007, Lansbergen, Nature Physics, 4, 656 (2008)
 - ✓ Filled state: "Screened" potential by an electron from self-consistent simulation









Equilibrium Electrostatics















Gate Modulation of Channel state (theory vs. experiment)

- Close match of transitions points (D+ to D0 at 0.45V, D0 to D- at 0.72V)
 Comparison: Experiment (70.4V and ~0.8V)
- Close match of charging energy: U= 46.3meV
 Comparison: Experiment Charging energy Ec= ~47+2meV
- Gate lever-arm: Theory U/ΔVg = 0.11, Comparison: Experiment Ec/ ΔVg = 0.15

Gate Modulation of Channel state (theory vs. experiment)

- Results explain extension of Coulomb Diamond into D- (two-electron) regime
- Weak channel barrier at second transition point (~ 13 meV)
- Channel electrons no longer confined for Vg greater ~ 1V

(Ongoing) Calculation of Coulomb Diamond

Objective:

 Construct a coulomb diamond of the single donor QD device.

Problems:

- Understand the "full" coulomb diamond measured at T=4K considering:
 - \checkmark DOS of Si:P wire leads.
 - \checkmark Excited single donor states.
 - \checkmark Inelastic scattering for the transport.

Approach:

 Rate-equation formalism coupled with tight-binding Schrödinger-Poisson solver.

in the Coulomb-blockade regime

Gerhard Klimeck,* Roger Lake,[†] and Supriyo Datta Purdue University, School of Electrical Engineering, West Lafayette, Indiana 47907-1285

Garnett W. Bryant

U.S. Army Research Laboratory, Microphotonic Devices Branch, Adelphi, Maryland 20783-1197 (Received 28 March 1994)

Starting from a rate-equation model proposed by Beenakker, we calculate current-voltage charannumentais and communication mention in a start with the last of the start of the

PHYSICAL REVIEW B

(Ongoing) Calculation of Coulomb Diamond

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 Construct a coulomb diamond of the single donor QD device.

Problems:

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Impurity Excited States

a)

Quantum Transport Theory With Coulomb Blockade, Excited States, Lead DOS

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Quantum Transport Theory With Coulomb Blockade, Excited States, Lead DOS

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Single Impurity Outline

AAAS

Si

1) Si:P Doping Plane (2-D)

1A) Semi-metallic property 1B) Sensitivity to doping disord

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challenging because of the presence of confining surfaces and interfaces. We report

- 2) Si:P Nanowire (1-D)
- 2A) Semi-metallic property
- 2B) Modulation of channel conductance
- 2C) Resistance-limit of Si Nanowire
- 2D) Sensitivity of resistance to doping disorder

3) Single-donor Quantum-dot (0-D)

3A) Channel Modulation → Single-electron trans

nature nanotechnology

Will briefly explain a tA single-atom transistor

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Martin Fuechsle¹, Jill A. Miwa¹, Suddhasatta Mahapa Oliver Warschkow¹, Lloyd C. L. Hollenberg³, Gerhard

A multi-scale modeling procedure 2. Potential profile 1. Contact modeling Semi-classical potential profile • Atomistic modeling on the leads Superpose w. donor potential Charge-potential self-consistency • Semi-metallic, DOS profile [110] G1-G2 cut Si bulk Ec (meV) **G2** Si:P Gate 0.05 100 -0.05 9nm -200 Fe Energy w.r.t. 251 meV -300 Single P 1.0 nm -3.65 110 Gi -2 0 ted by 5.5nm Distance from impurity, S-D cut (nm) 3. Charge filling Potential profile → Hamiltonian T = 4K3

- Compute eigenstates w.r.t $\rm E_{\rm F}$ at every $\rm V_{\rm G}$
- Transition, charging energy and gate modulation

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 NEMO
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 nanoHUB.org

Industrial Device Trends and Challenges

Observations:

NEM

- 3D spatial variations on nm scale
- Potential variations on nm scale
- New channel materials (Ge, III-V)

PURDUE Gerhard Klimeck

Questions / Challenges

- , Strain ?
- Quantization?
- Crystal orientation?
- Atoms are countable; does granularity matter? Disorder?
- New material or new device?

Assertions of importance

- High bias / non-equilibrium
- Quantum mechanics
- Atomistic representation
 - » Band coupling, non-parabolicity, valley splitting
 - » Local (dis)order, strain and orientation

Goal:

 Device performance with realistic extent, heterostructures, fields, etc. for new / unknown materials

Problems:

- Need ab-initio to explore new material properties
- Ab-initio cannot model nonequilibrium.
- TCAD does not contain any real material physics

Approach:

- Ab-initio:
 - Bulk constituents
 - Small ideal superlattices
- Map ab-initio to tight binding (binaries and superlattices)
- Current flow in ideal structures
- Study devices perturbed by:
 - Large applied biases
 - Disorder
 - Phonons

NEMO - Multi-Scale Modeling

A Journey Through Nanoelectronics Tools NEMO and OMEN

NEMO-1D

Yes
1D
~1,000
[100] Cubic, ZB
-
-
3 levels 23,000 cores

NEMØ5

	NEMO-1D	NEMO-3D
Transport	Yes	-
Dim.	1D	any
Atoms	~1,000	50 Million
Crystal	[100] Cubic, ZB	[100] Cubic, ZB
Strain	-	VFF
Multi- physics	-	
Parallel Comp.	3 levels 23,000 cores	1 level 80 cores

	NEMO-1D	NEMO-3D	NEMO3Dpeta
Transport	Yes	X.	-
Dim.	1D	any	any
Atoms	~1,000	50 Million	100 Million
Crystal [100] Cubic, ZB		[100] Cubic, ZB	[100], Cubic,ZB, WU
Strain	-	VFF	VFF
Multi- physics	-		
Parallel Comp.	3 levels 23,000 cores	1 level 80 cores	3 levels 30,000 cores

NFM@5

	NEMO-1D	NEMO-3D	NEMO3Dpeta	OMEN
Transport	Yes	-	-	Yes
Dim.	1D	any	any	any
Atoms	~1,000	50 Million	100 Million	~140,000
Crystal	[100] Cubic, ZB	[100] Cubic, ZB	[100], Cubic,ZB, WU	Any Any
Strain	-	VFF	VFF	-
Multi- physics	-			
Parallel Comp.	3 levels 23,000 cores	1 level 80 cores	3 levels 30,000 cores	4 levels 220,000 co

NEMØ5

NEMØ5	Core Code / Theory Development			
• NEMO-1D	(Texas Instruments '94-'98, JPL '98-'03)			
» Roger Lake, R. Chris Bo	wen			
• NEMO3D	(NASA JPL, Purdue, '98-'07)			
» R. Chris Bowen, Fabiano Oyafuso, Seungwon Lee				
 NEMO3D-peta 	(Purdue, '06-'11)			
» Hoon Ryu, Sunhee Lee				
• OMEN	(ETH, Purdue, '06-'11)			
» Mathieu Luisier				
• NEMO5	(Purdue, '09-'13)			
» 5 active professionals: M. Povolotsky, T. Kubis, J. Fonseca, B. Novakovic, R. Rahman, (formerly A. Ajoy, H-H Park, S. Steiger)				
23 active students: Ta Haume, Yu He, Ganesh Zhengping Jiang, Sungo Samik Mukherjee, Seun Sengupta, Saima Sharn	arek Ameen, James Charles, Junzhe Geng, Kaspar Hegde, Yuling Hsueh, Hesam Ilatikhameneh, Geun Kim, Daniel Lemus, Daniel Mejia, Kai Miao, Ig Hyun Park, Ahmed Reza, Mehdi Salmani, Parijat hin, Yaohua Tan, Archana Tankasala, Daniel			

Valencia, Evan Wilson,

Network for Computational Nanotechnology

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Compute Intensive: NEMO/OMEN

- 26 years developmentTexas Instruments
- •NASA JPL
- •Purdue
- Peta-scale EngineeringGordon Bell

ACM Gordon Bell Prize

Mathieu Luisier, Timothy B. Boykin, Gerhard Klimeck, Wolfgang Fichtner

Atomistic Nanoelectronic Device Engineering with Sustained Performances up to 1.44 PFlop/s

(e)

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- •Peta-scale Engineering
- •Gordon Bell
- •Science, Nature Nano

381 classes w/ 3,756 students 94 citations

Powers 8 Tools: team >28,600 Users >540,900 Simulation Runs
nanoHUB.org – always "on" New paradigms in global scientific knowledge transfer, publishing, and assessment

Who?

- > 2 million users annually
- > 1,800 contributors
- 172 countries

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• Faculty



StudentsIndustry practitioners

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- Faculty
- Students
- Industry practitioners

nanoHUB in a nutshell: translating traditional research to new paradigms in publishing, computing, research, & education

What ?

- 600+ nano-Apps in the cloud
- > 5,000 lectures and tutorials
- > 100 courses => MOOC

Cyberinfrastructure 24/7 operation with 99.4% uptime

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Research Impact: • nanoHUB tools now listed in WEB OF SCIENCE Google Scholar

- > 2,480 papers cite nanoHUB
- > 54,300 secondary citations
- h-index of 105

Educational Impact

- >54,800 students use tools in classrooms, >5,345 classes,
 >185 institutions
- Rapid curriculum change
 <6 months adoption rate

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Fundamental changes in approach or underlying assumptions

=> Existence Proofs

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The Ultimate Scaling Limit – Entry into Quantum Computing Gerhard Klimeck,

Director of nanoHUB.org, Purdue University, gekco@purdue.edu



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How to model this new world?

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Inspired Modeling

Why?