



Tunneling into emergent topological matter

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Princeton University**

Outline

- **Emergent topological matter**
- **State-of-the-art STM technique**
- **Proof-of-principle methodology**
- **More to discover**

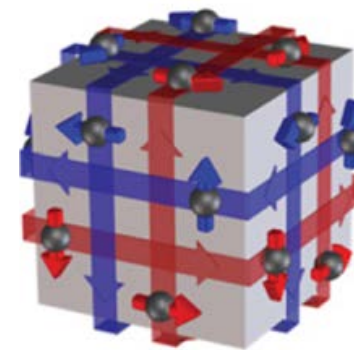
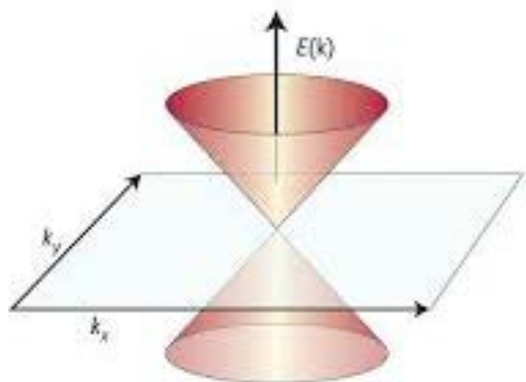
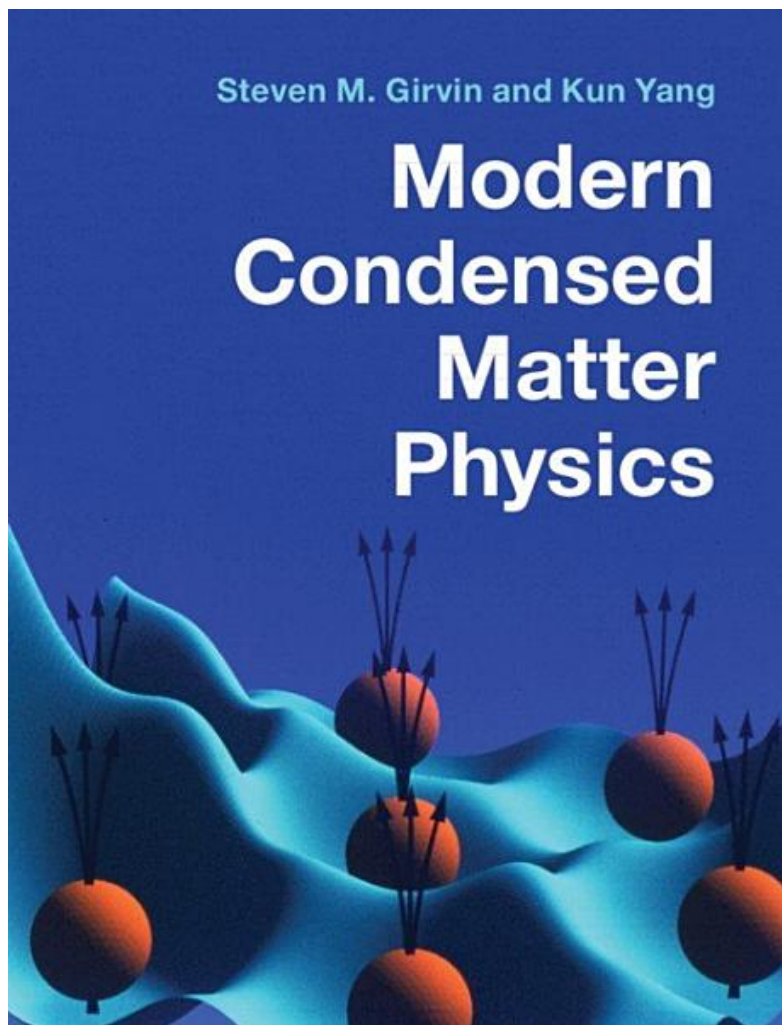
Topological matter

Quantum topology

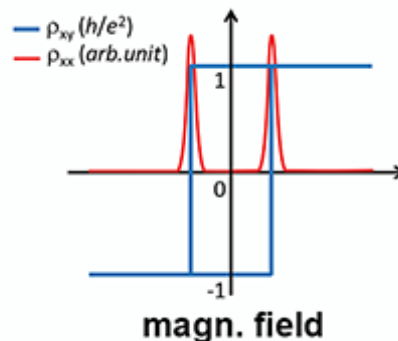
Topological quantum materials

Topological fermions (Dirac, Weyl...)

Symmetry protected
bulk-boundary correspondence



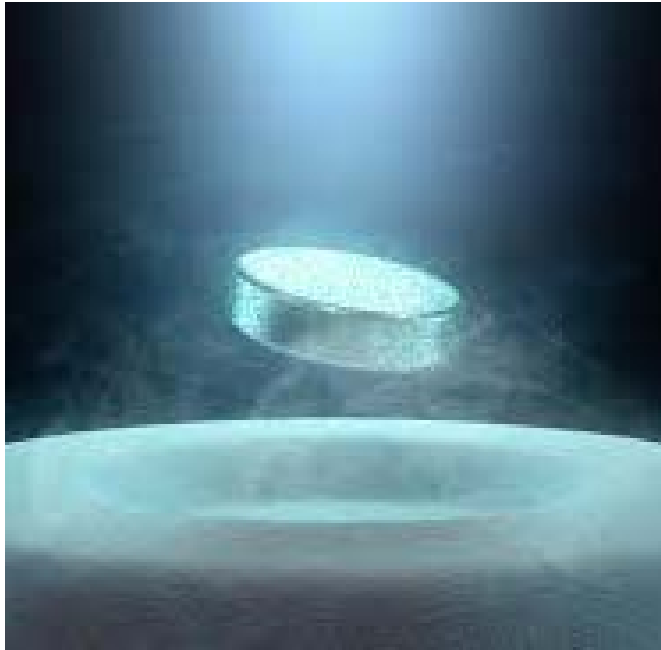
Quantized electronic excitations



- J.E. Avron, et al. Phys. Today (2003)
- F.D.M. Haldane. RMP (2017)
- M.Z. Hasan, C.L. Kane. RMP (2010)
- X.L. Qi, S.C. Zhang. RMP (2011)
- B. Keimer, J.E Moore. Nat. Phys. (2017)
- N.P.Armitage, E.J. Mele, A. Vishwanath. RMP (2018).
- K. He, Y. Wang, Q.K. Xue, ARCM (2018)

Emergent topological matter with strong interaction

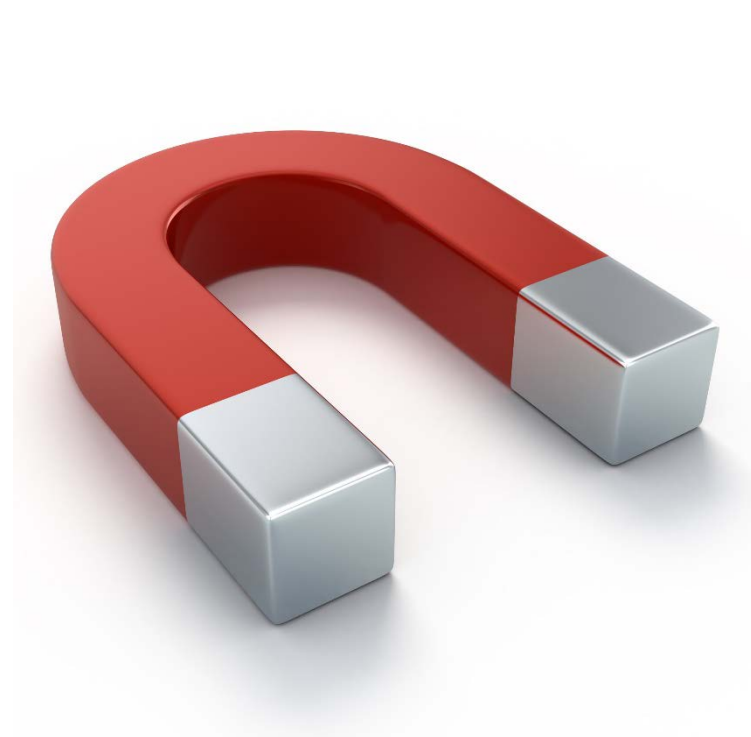
Superconductivity



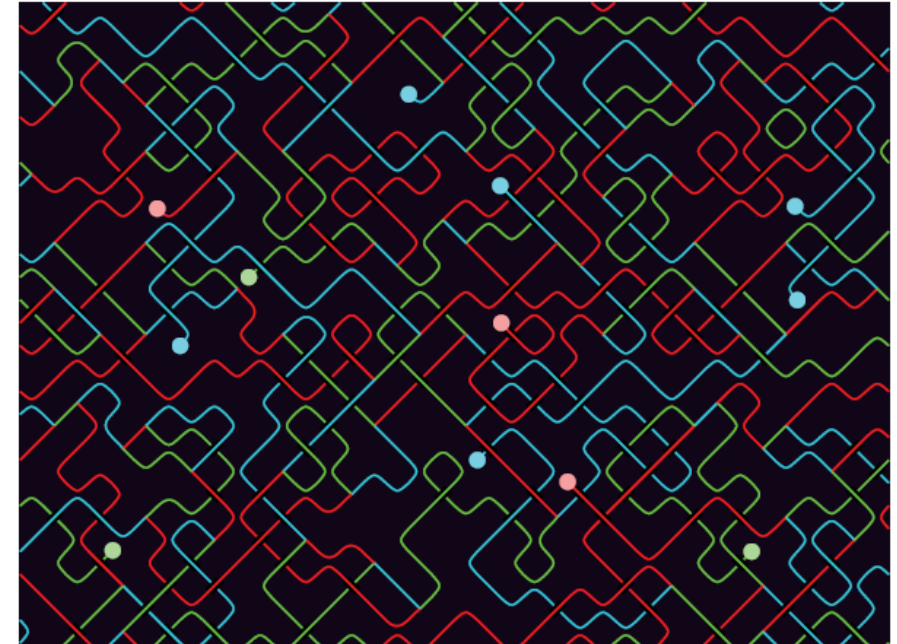
Correlated electrons

- P. W. Anderson. Science (1972)
- E. Dagotto. Science (2005)
- A. Fert. RMP (2008)
- B. Keimer, S. Kivelson, M. Norman, M. Uchida, J. Zaanen. Nature (2015)

Magnetism



Topological order; many-body entanglement

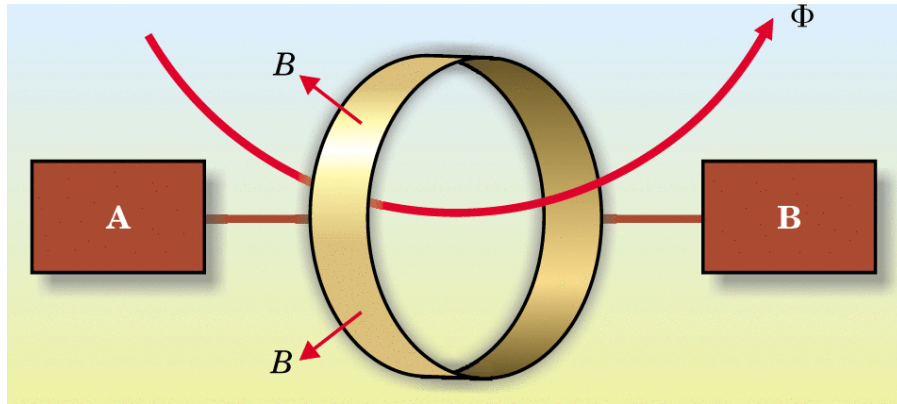


- S. Sachdev. Rep. Prog. Phys. (2019)
- X.G. Wen. Science (2019)

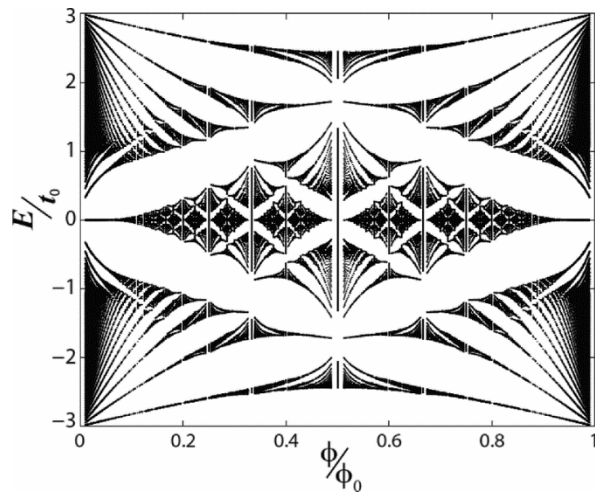
B field as strong perturbation for emergent topological matter

Quantum magnetic flux h/e ; quantum Hall conductance ne^2/h (n is the Chern number)

Laughlin's quantum pump

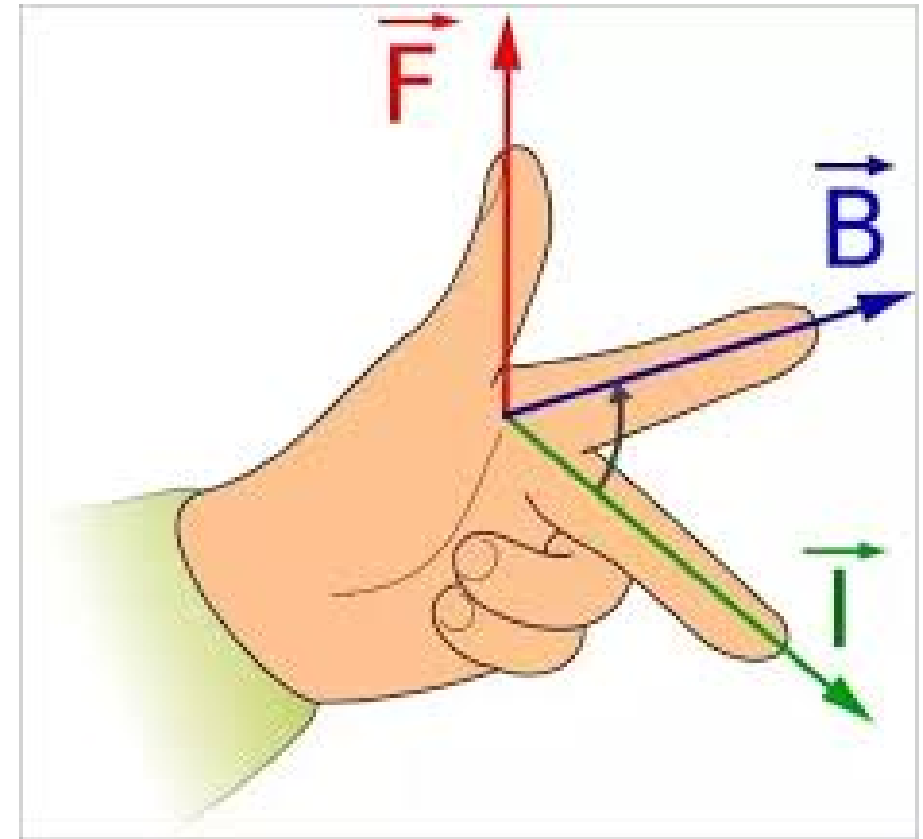


Hofstadter butterfly



R.B. Laughlin.
RMP (1999)

Chirality of electronic matter



D. E. Kharzeev. Annu. Rev. Nucl. Part. Sci. (2015)

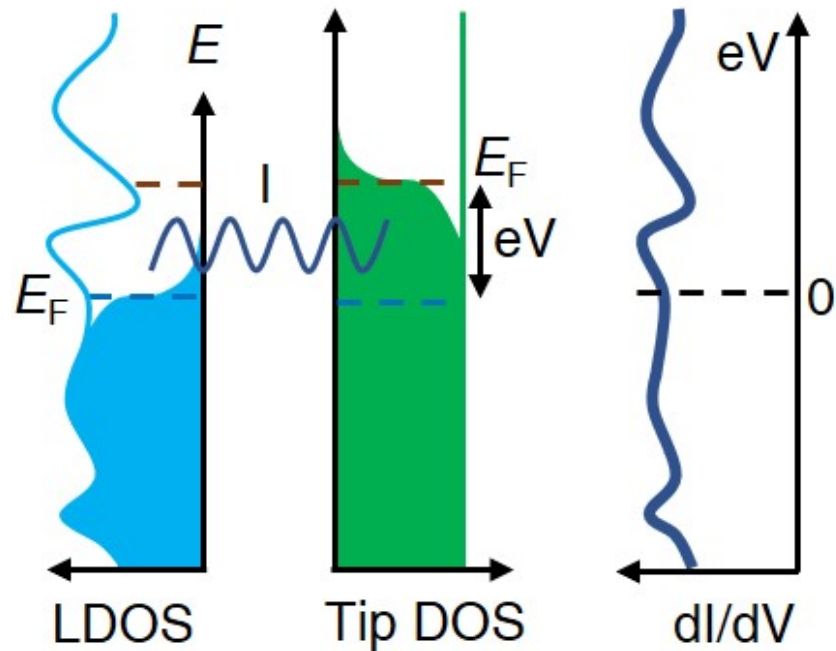
Outline

- Emergent topological matter
- State-of-the-art STM technique
- Proof-of-principle methodology
- More to discover

State-of-the-art STM technique

F. Hund, Z. Phys. (1927) J. R. Oppenheimer, Phys. Rev. (1928)
L. Nordheim, Z. Phys. (1927). W. Schottky, Z. Phys. (1931)

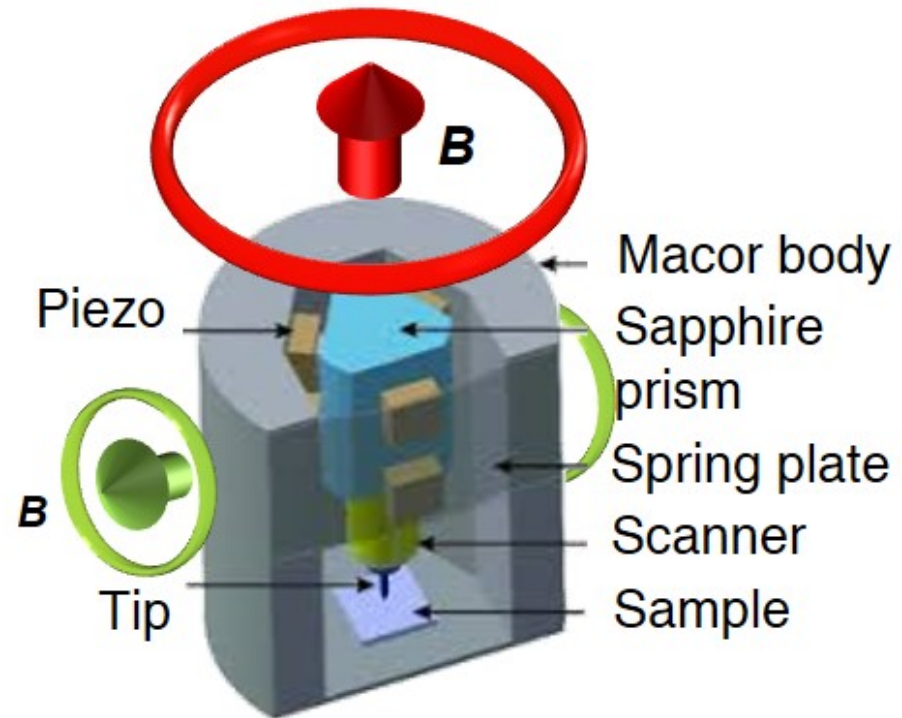
Quantum tunneling principle



J. Tersoff, D.R. Hamann. PRB (1985)

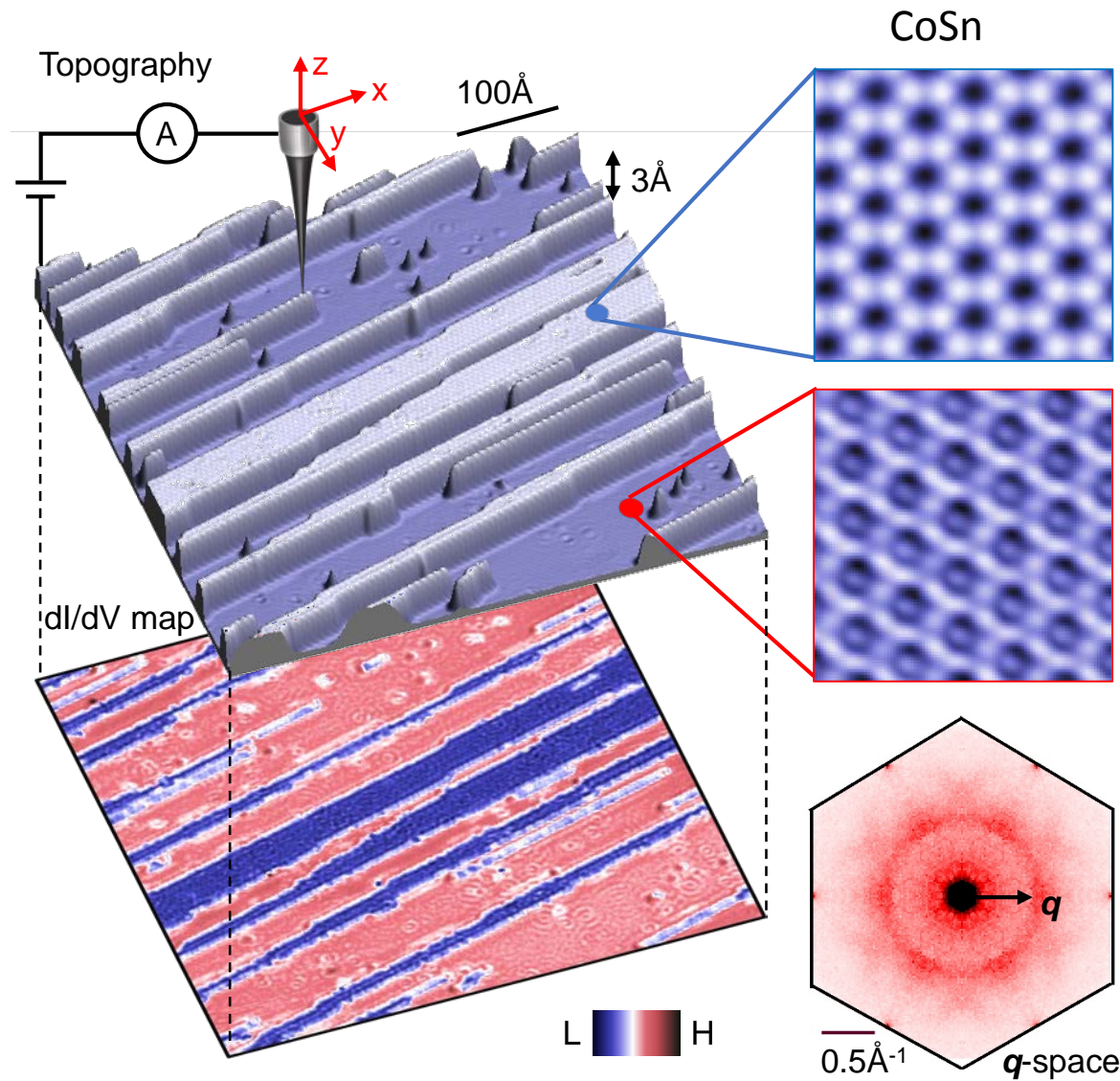
B. Voigtländer, Scanning Probe Microscopy. (Springer, 2015)

Pan-STM under a vector magnetic field



S. H. Pan. International Patent (1993)

STM data structure



Topography (Atomic resolution)

dI/dV spectrum (Sub-meV resolution)

dI/dV map

Quasi-particle interference (QPI)

O. Fischer. Rev. Mod. Phys. (2007)

R. Wiesendanger. Rev. Mod. Phys. (2009)

J. E. Hoffman. Reports Prog. Phys. (2011)

A. R. Schmidt, J.C. Davis et al. New Journal of Physics (2011)

A. Gyenis, A. Yazdani et al. New Journal of Physics (2016)

H. Zheng, M. Z. Hasan. Advances in Physics X (2018)

Comparison with other techniques in probing topological matter

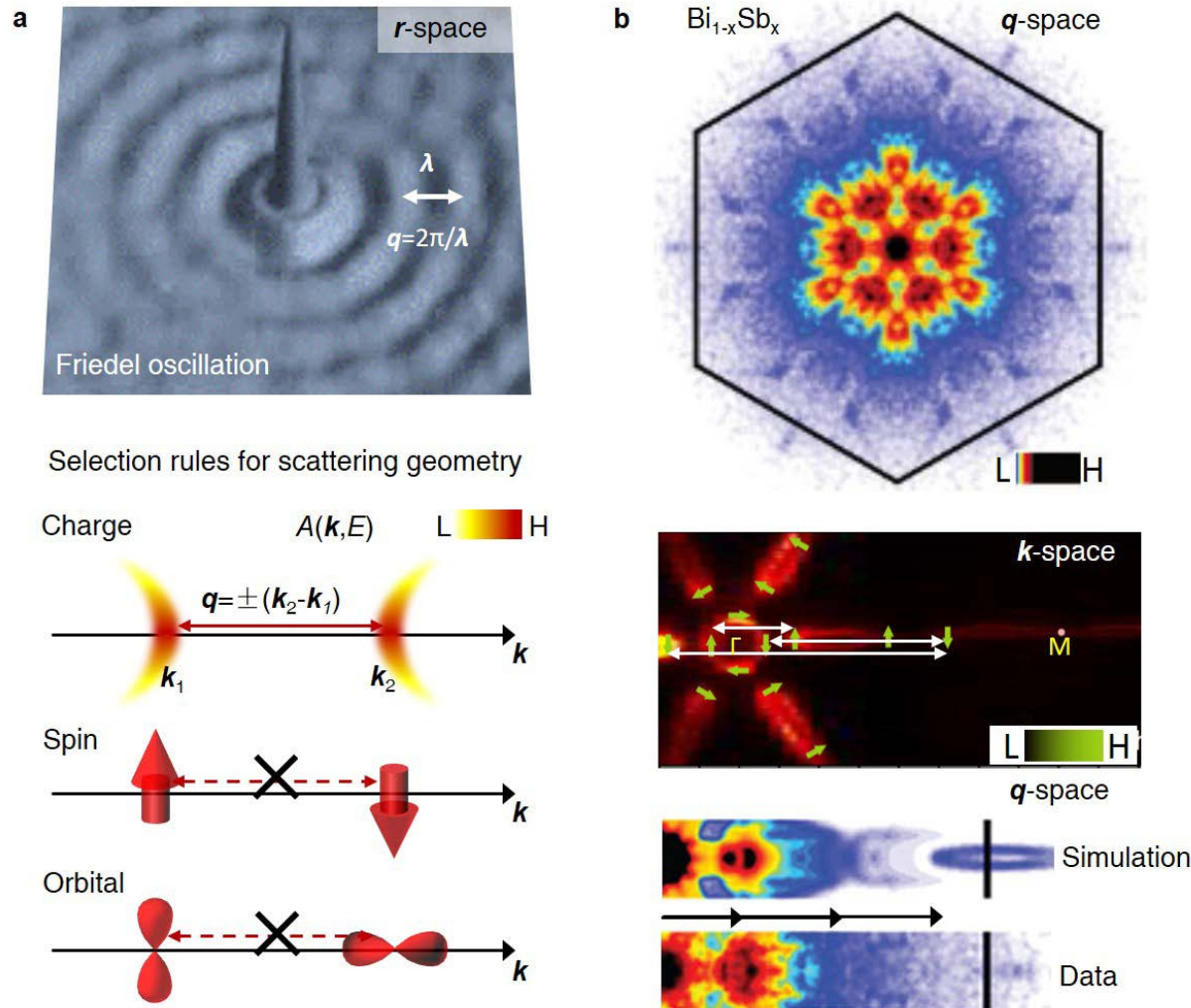
Technique	STM	ARPES	Magneto-transport
Key parameter	Local density of states	Spectral function	Conductivity tensor
Variables	Location; energy; magnetic field; magnetic or nonmagnetic tip; gating; temperature.	Momentum; energy; photon wavelength; photon polarization; spin polarization; gating; temperature.	Vector magnetic field; Landau level sequence; pressure; electrical field; gating; Temperature.
Unique aspects	Probing the scattering geometry; sub-meV energy resolution; Landau quantization; edge state; detecting zero modes.	Band crossing; spin/orbital-momentum locking and texture; probing both 2D surface and 3D bulk band structures.	Electron mobility; chiral anomaly; anomalous Hall; Hall quantization; thermal conductivity etc.
Connection with(in) scanning tunnelling microscopy	Correspondence between single defects, vortices and local density of states; correspondence between (bulk) energy gap and edge states.	Correspondence to momentum integrated photoemission signal; energy gaps; charge/spin/orbital texture; band dispersion; inter/intra- band structure scattering.	Effective quasi-particle dispersion and Fermi surface geometry; magnetic field response; effective mass, Fermi velocity, and Fermi length; phase transition.
Limitation	Momentum resolution; atomically flat surfaces; probing surface states and surface-projected bulk states; thermal smearing from tip.	Spatial resolution; fresh and flat surface; occupied states; energy resolution; magnetic field.	No energy, spatial, momentum or spin resolution; extrinsic scattering mechanism can contribute to the signal.

Proof-of-principle methodology

- Quasi-particle interference and Landau quantization
- Topological correspondence as a guideline for STM discovery
- Magnetic field control and engineering of topological matter
- Probing extreme local effect at the atomic scale

QPI method to probe scattering geometry

Early QPI method references: M. F. Crommie et al Nature, Science (1993). Y. Hasegawa et al PRL (1993). P. T. Sprunger. Science 275, 1764 (1997). L. Petersen et al. PRB (1998). J. E. Hoffman. et al. Science (2002).

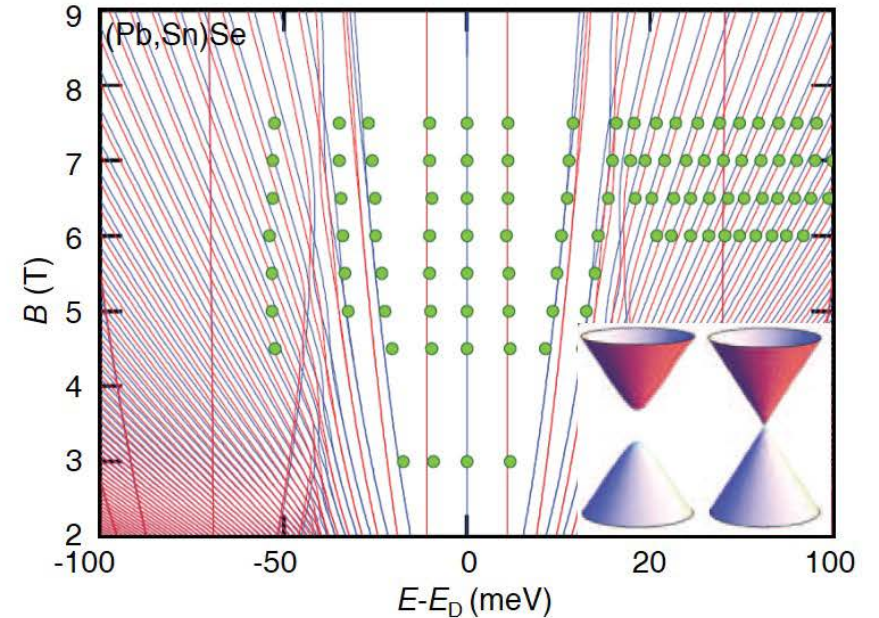
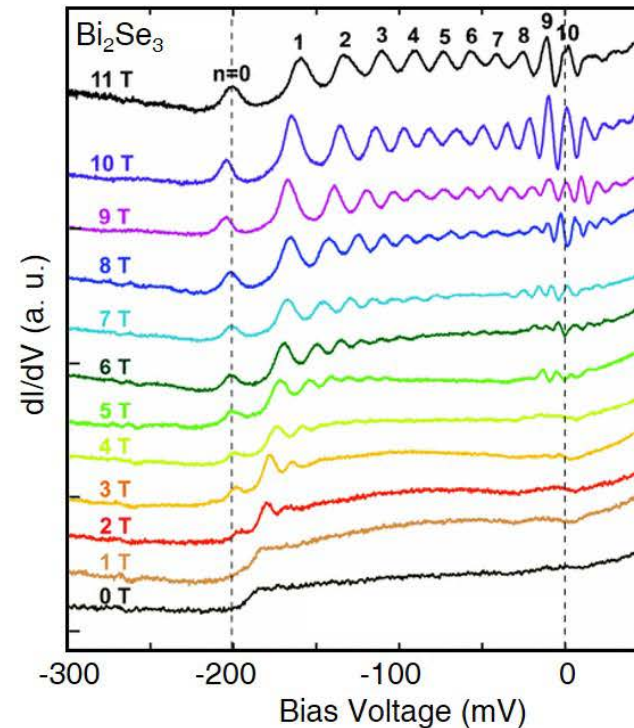
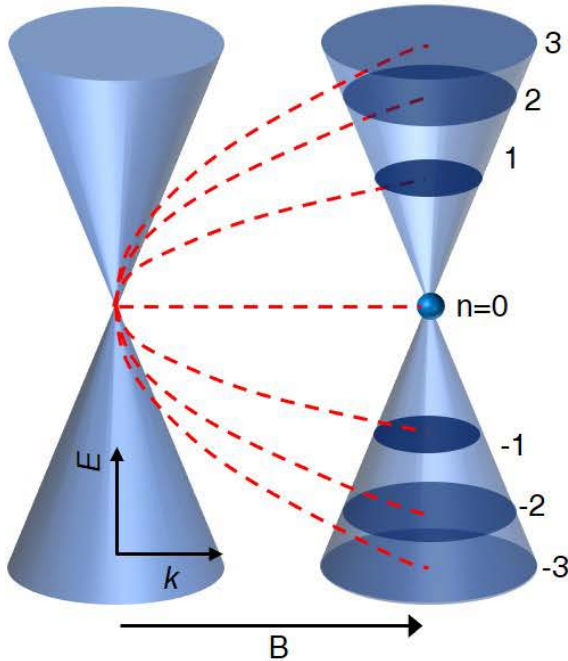


P. Roushan, A. Yazdani et al. Nature (2009); D. Hsieh, M.Z. Hasan et al. Nature (2008)

Landau quantization to detect topological fermions

Early references: J.W.G. Wildöer et al. PRB (1997). R Dombrowski et al. Applied Physics A (1998)
T. Matsui et al. PRL (2005). G.H. Li. et al. Nat. Phys. (2007). D. L. Miller. et al. Science (2009).

$$E_n = \text{sgn}(n)v\sqrt{2|n|e\hbar B}$$



P. Cheng, Q.K. Xue et al. PRL (2010). Y. Okada, V. Madhavan et al. Science (2013).

Transport Landau level quantization: Y. Xu, Y. P. Chen et al. Nature Phys (2014)

Proof-of-principle methodology

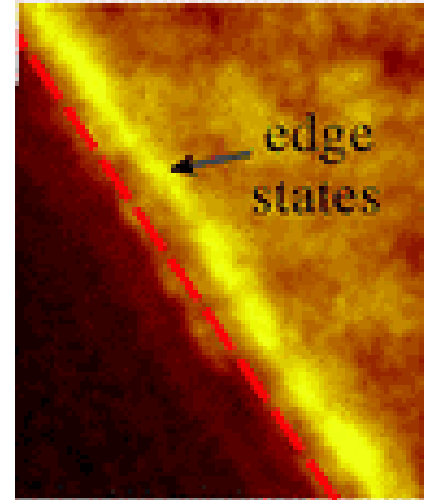
- Quasi-particle interference and Landau level quantization
- Topological correspondence as a guideline for STM discovery
- Magnetic field control and engineering of topological matter
- Probing extreme local effect at the atomic scale

Topological correspondence

Bulk-boundary correspondence

Chern number and edge states in the integer quantum Hall effect

Y. Hatsugai. PRL (1993)



Robust edge state in Bi

F. Yang, J.F. Jia et al. PRL (2012)

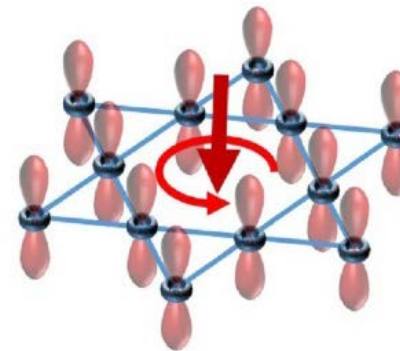
Wannier–Bloch correspondence

Maximally localized Wannier functions RMP (2012)

N. Marzari, A. A. Mostofi, J. R. Yates, I. Souza, D. Vanderbilt

Topological quantum chemistry Nature (2017)

Barry Bradlyn et al, C. Felser, M. I. Aroyo, B. A. Bernevig

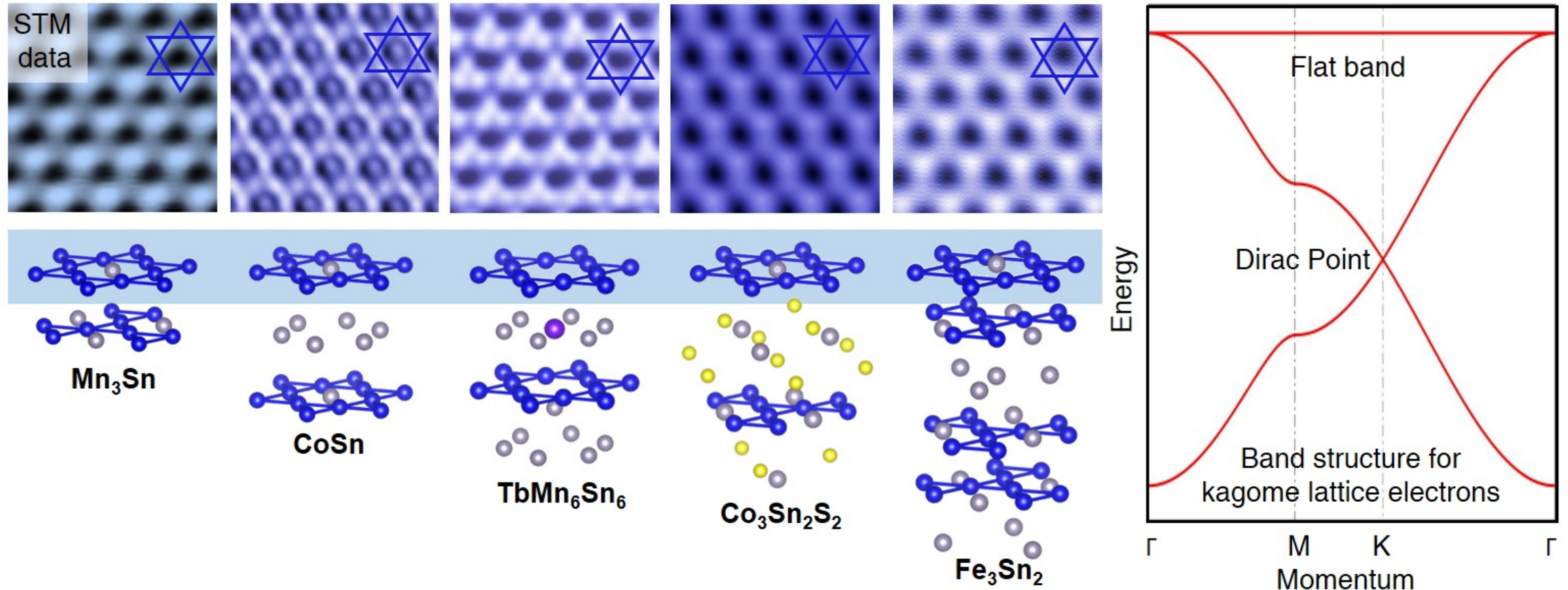


Orbital magnetism in $\text{Co}_3\text{Sn}_2\text{S}_2$

J-X Yin, M Z Hasan et al.
Nat Phys (2018)

Lattice geometry and topological correspondence

Unusual fermions arising from lattices with special geometry (honeycomb, kagome, Lieb, chiral lattice)



J.X. Yin, et al. Nature (2018). Z. Lin, et al. PRL (2018). Zhi Li, et al. Sci Adv (2018).

J. X. Yin, et al. Nat. Phys. (2019). N. Morali, et al. Science (2019). L. Jiao, et al. Phys. Rev. B (2019). S. Howard. Arxiv (2019).

J.X. Yin, et al. Nature (2020). S.S. Zhang, PRL (2020). J.X. Yin, et al. Nat. Commun. (2020).

J.X. Yin, et al. Nat. Commun. (2020). Y. Xing, et al. Arxiv (2020). Z. Guguchia, et al. Nat. Commun. (2020). Z. Liu, et al. Nat. Commun. (2020)

Quantum limit Chern magnetism in TbMn_6Sn_6

Theoretical concept for kagome Chern magnet:

F.D. Haldane PRL (1998).

C.L. Kane & E.J. Mele. PRL (2005).

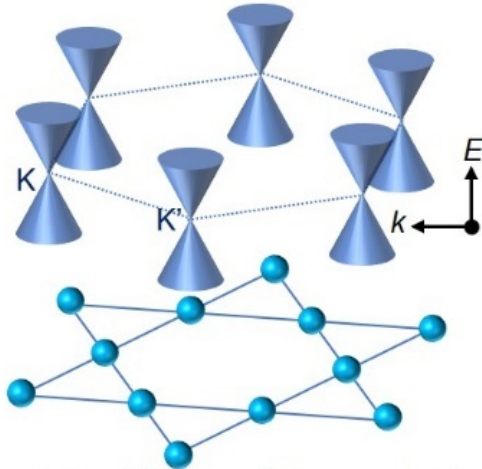
G.Xu, B. Lian, S.C. Zhang. PRL (2015).



Known unknown

J.X. Yin, M.Z. Hasan et al. Nature (2020)

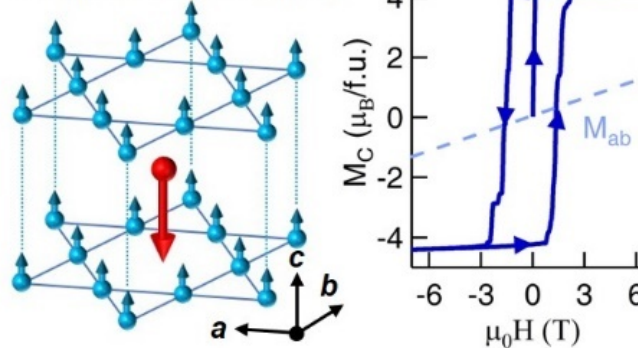
a Topological fermions in kagome lattice



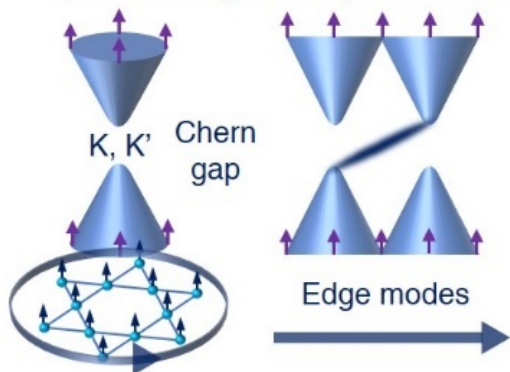
c Mn-kagome lattice ordering in RMn_6Sn_6



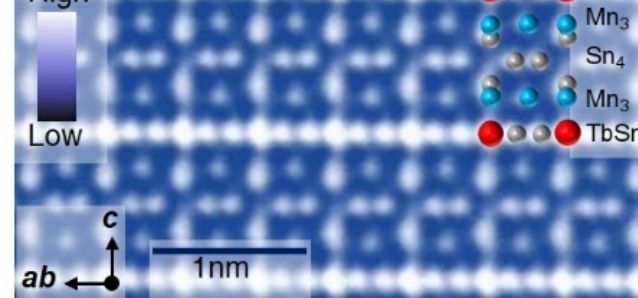
d Magnetism in TbMn_6Sn_6



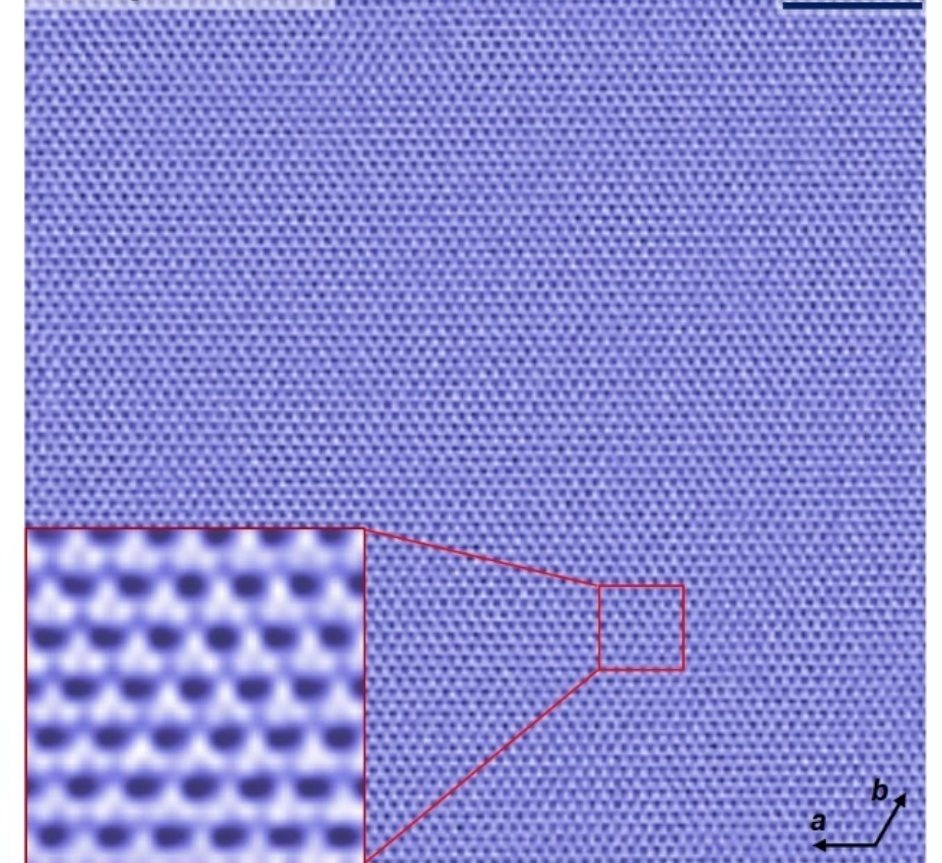
b Spin-orbit magnetic kagome lattice



e



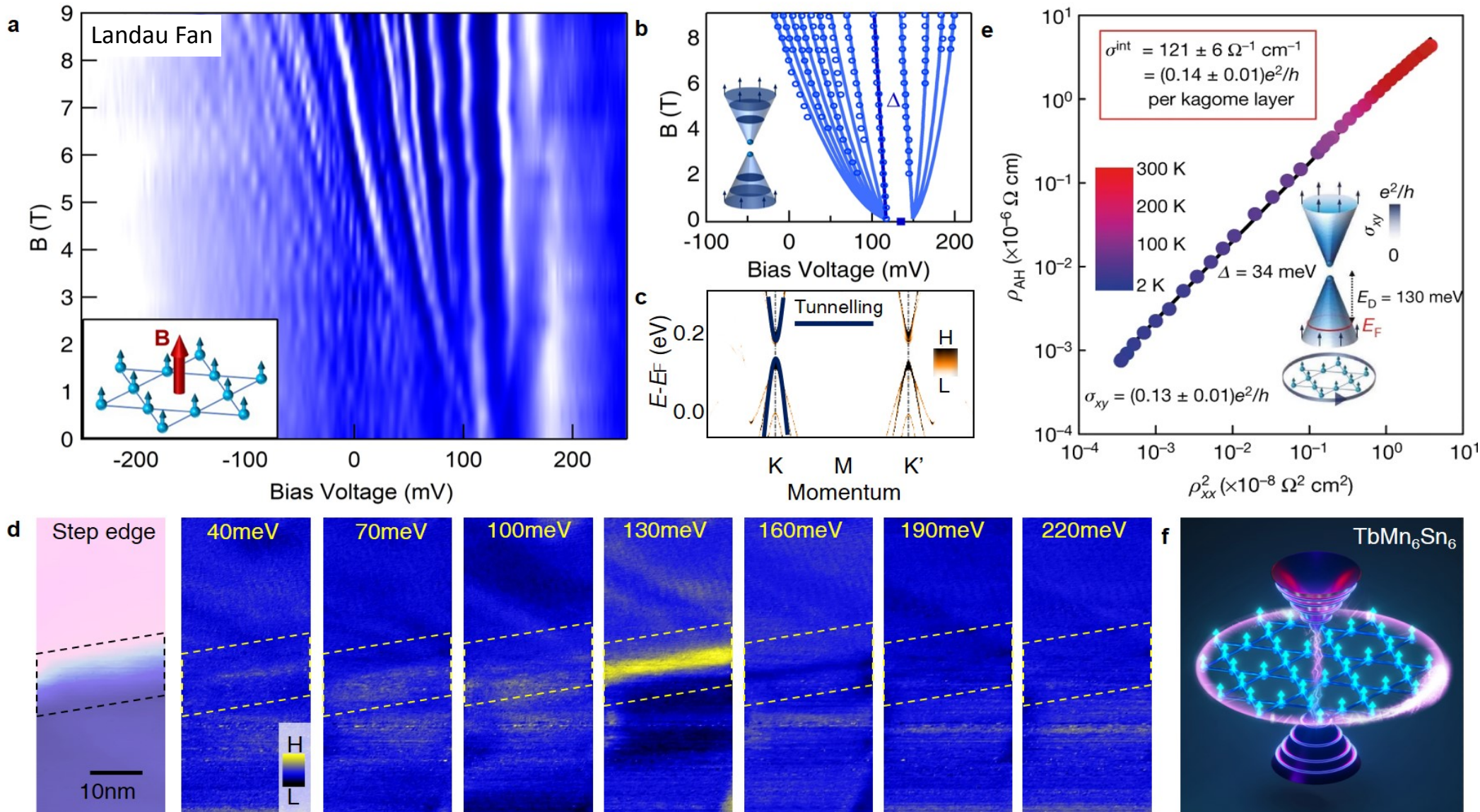
f Mn kagome surface



Bulk-boundary-Berry correspondence in Chern magnet

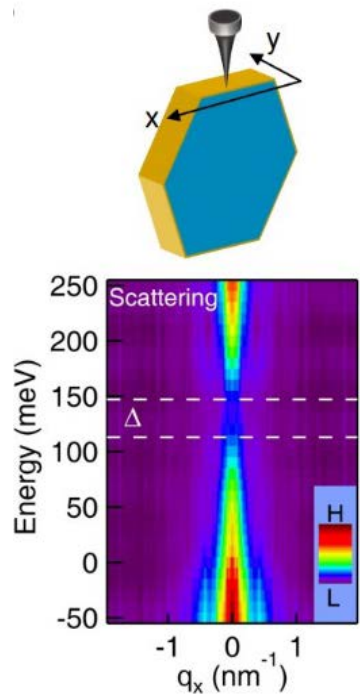
$$E_n = E_D \pm \sqrt{(\Delta/2)^2 + 2|n|e\hbar v^2 B} - \frac{1}{2}g\mu_B B$$

J.X. Yin, M.Z. Hasan et al. Nature (2020)

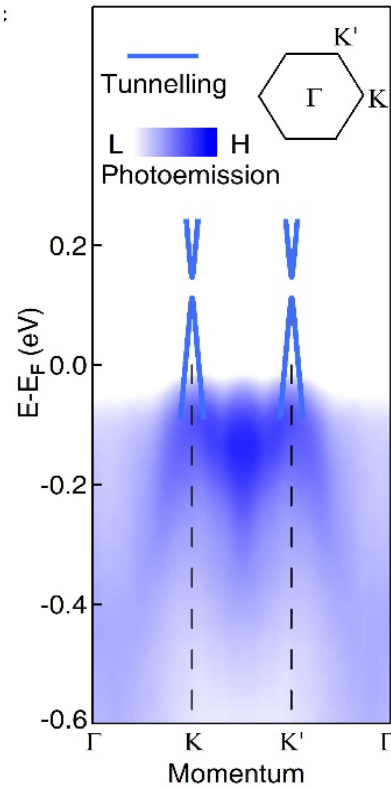


Additional features of Chern magnet

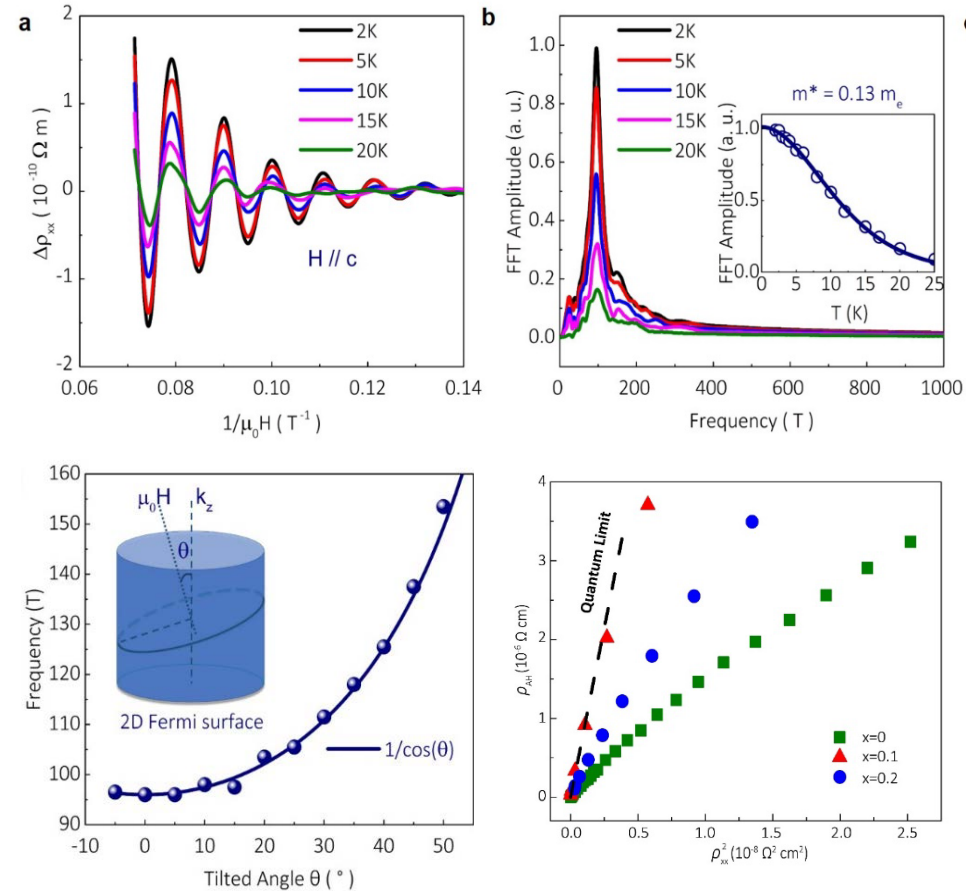
Side surface
QPI imaging



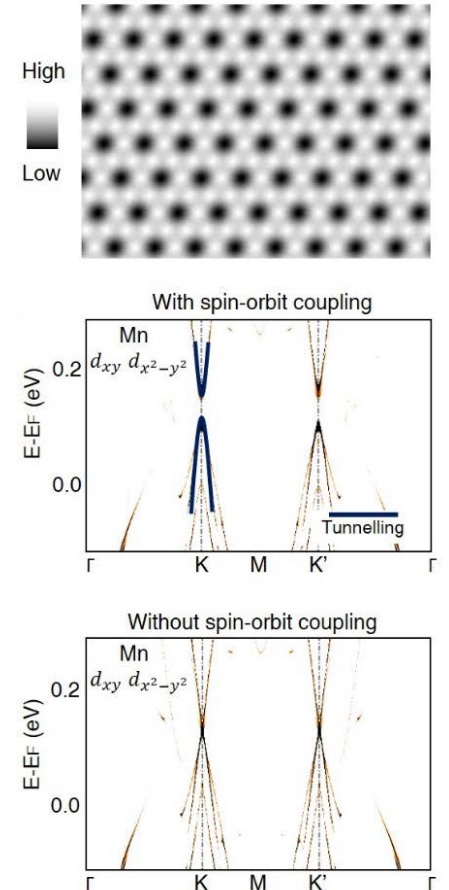
ARPES



Transport quantum Oscillations



First-principles



Proof-of-principle methodology

- Quasi-particle interference and Landau level quantization
- Topological correspondence as a guideline for STM discovery
- **Magnetic field control and engineering of topological matter**
- Probing extreme local effect at the atomic scale

Vector magnetic field STM

Early reference: H. F. Hess. et al. PRL (1992).

Princeton Work

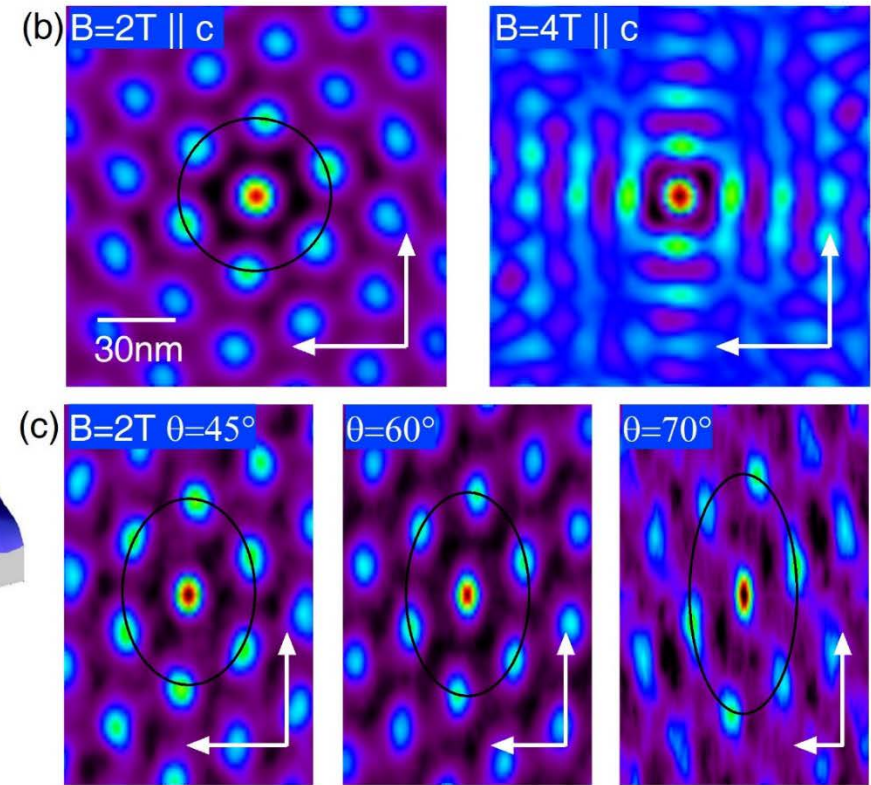
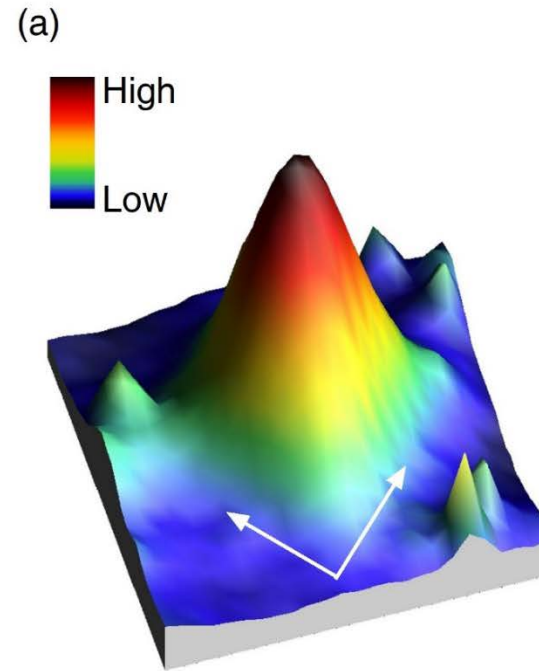
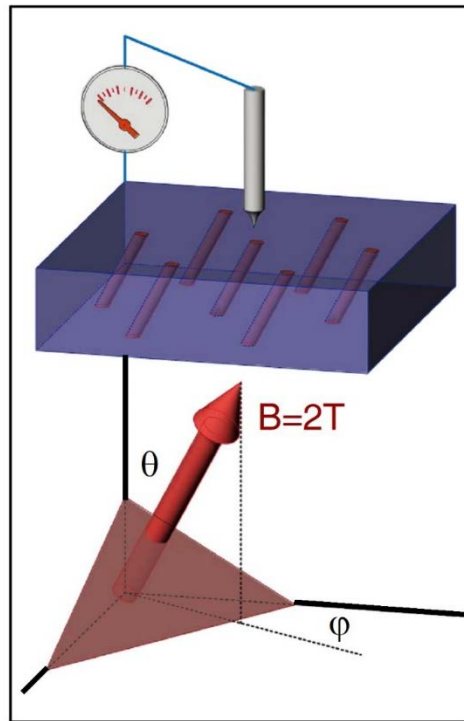
J.X. Yin, S.S. Zhang PRL (2019).

S.S. Zhang, J.X. Yin PRB (2019).

S.S. Zhang, J.X. Yin PRB (2020).

LiFeAs ($T_c=17\text{K}$)

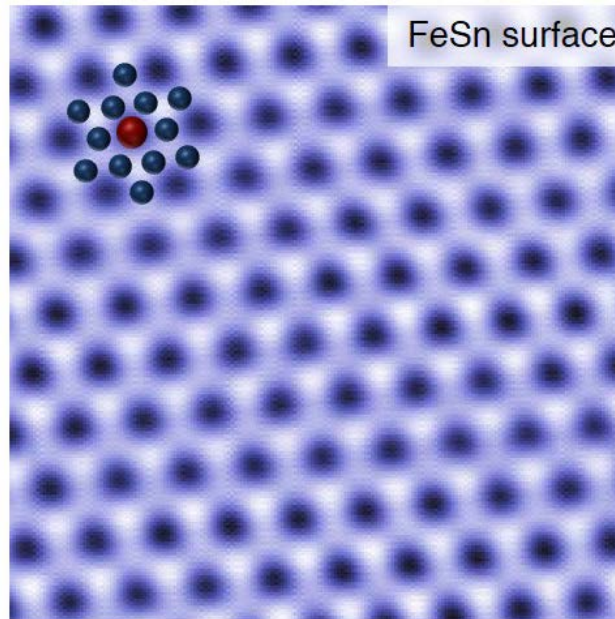
9-2-2T 380mK-77K



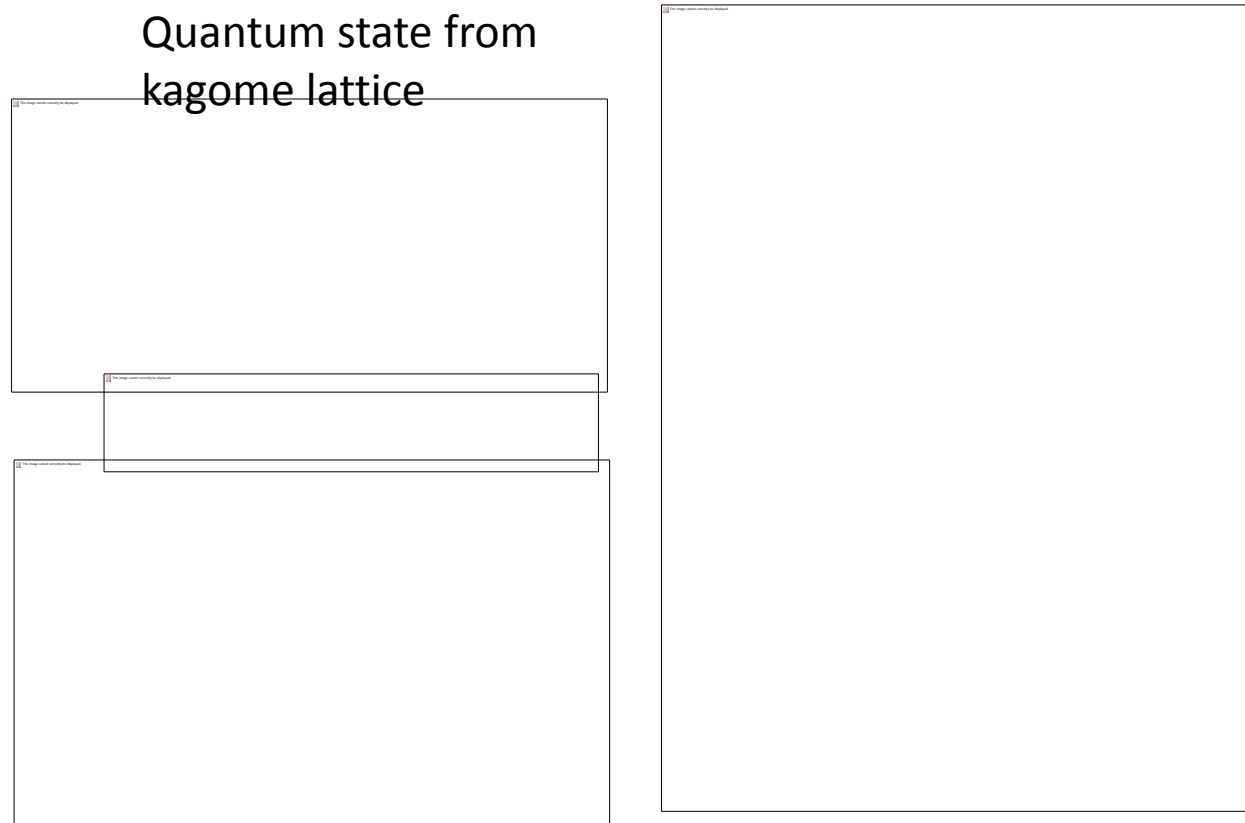
Giant spin-orbit tunability in topological magnet

Unknown unknown: How would a topological magnet response to vector magnetization?

Kagome magnet Fe_3Sn_2

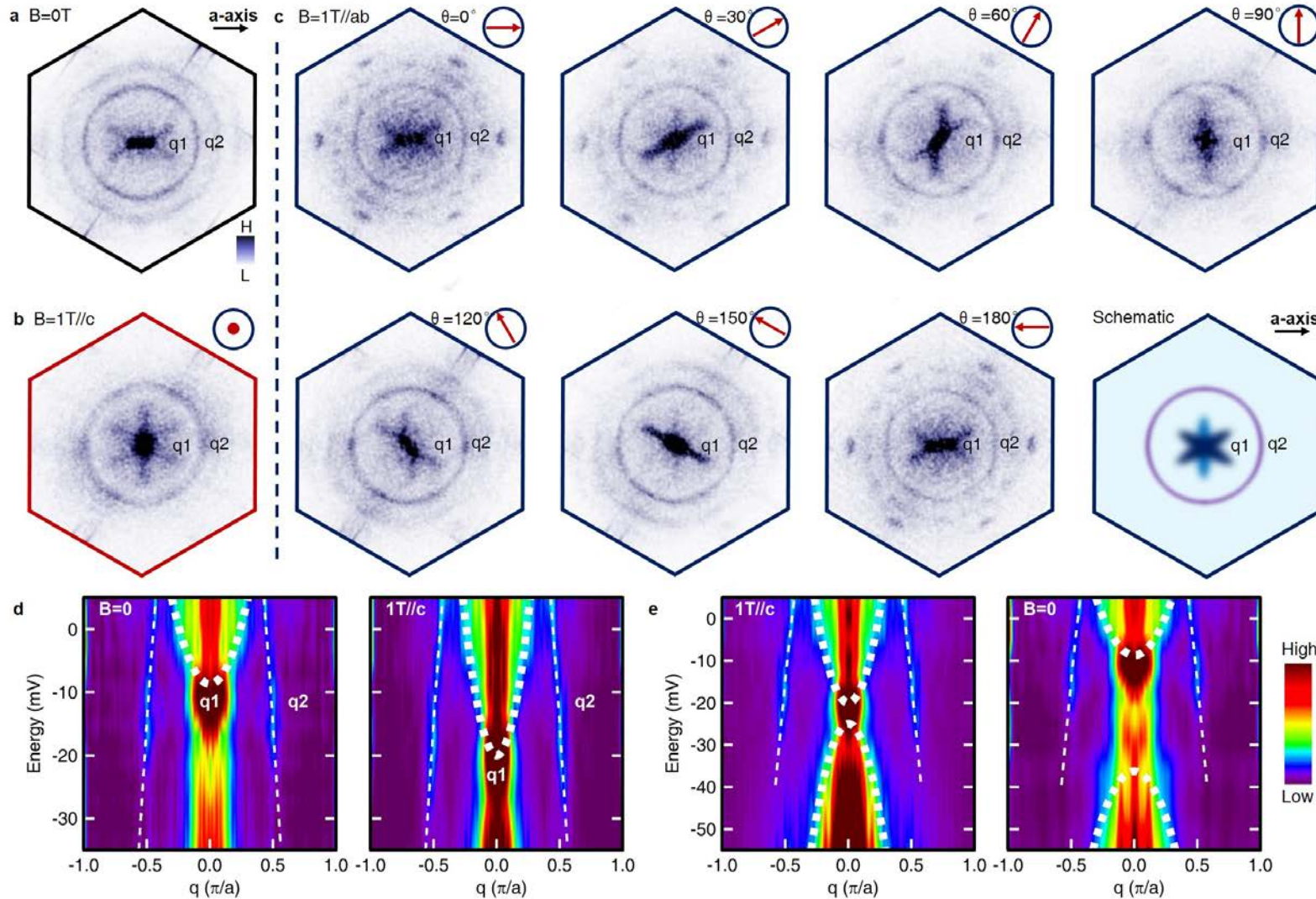


Quantum state from
kagome lattice

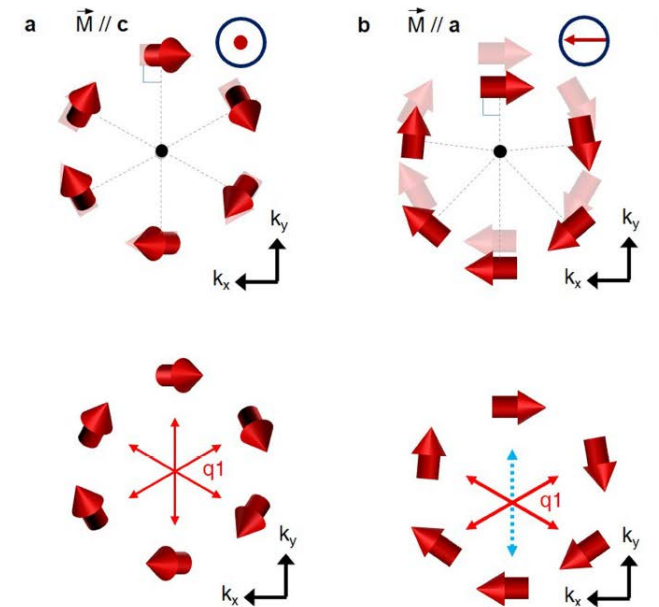


J X Yin, M Z Hasan et al Nature (2018)
Y Li, J M Tranquada et al PRL (2019)

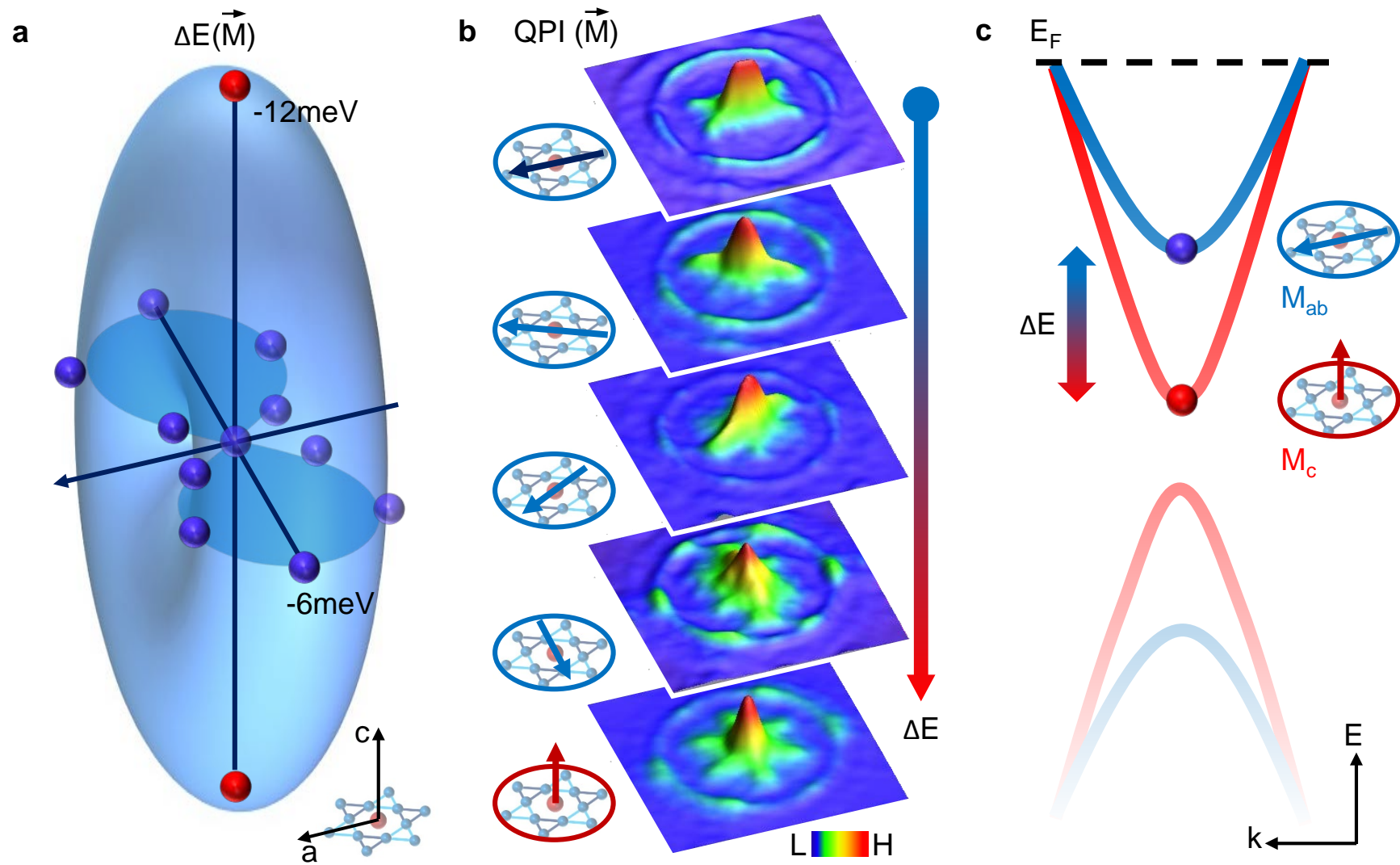
Vector field controlled scattering symmetry



QPI anisotropy $\sim \cos^2 \theta$
 θ is the in-plane angle with respect to the magnetization direction.
 By Lian Biao et al.



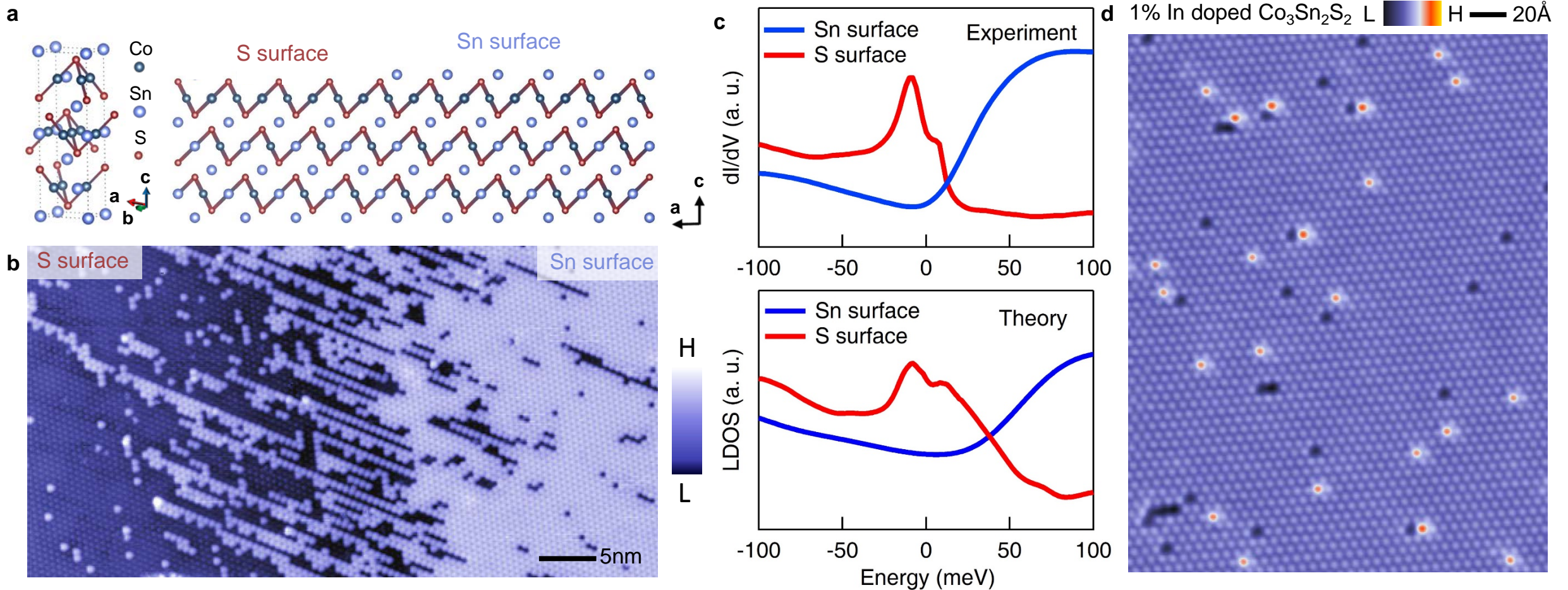
Spin-orbit tunability through vector field magnetization



Surface identification for $\text{Co}_3\text{Sn}_2\text{S}_2$

Crystalline symmetry and layer selective chemical marker

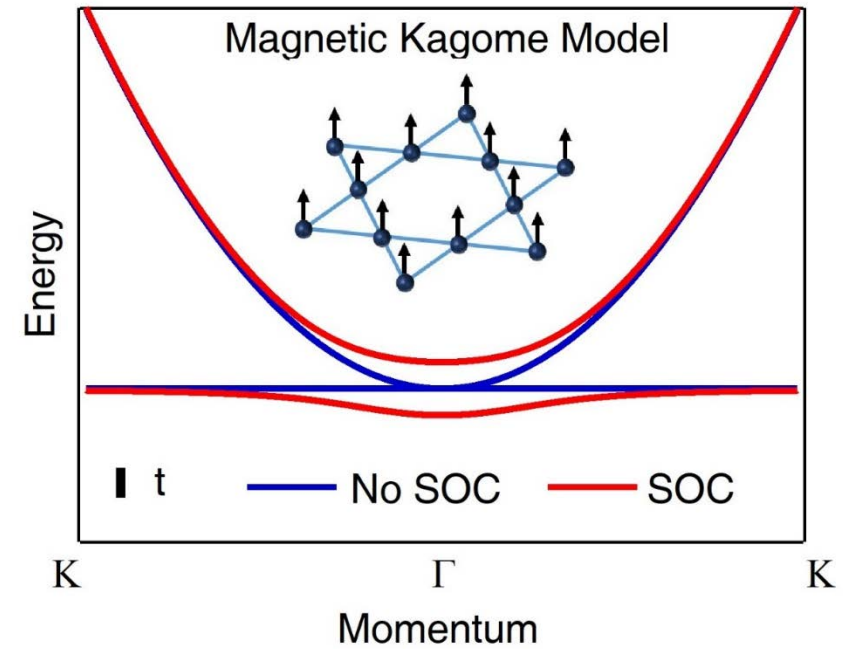
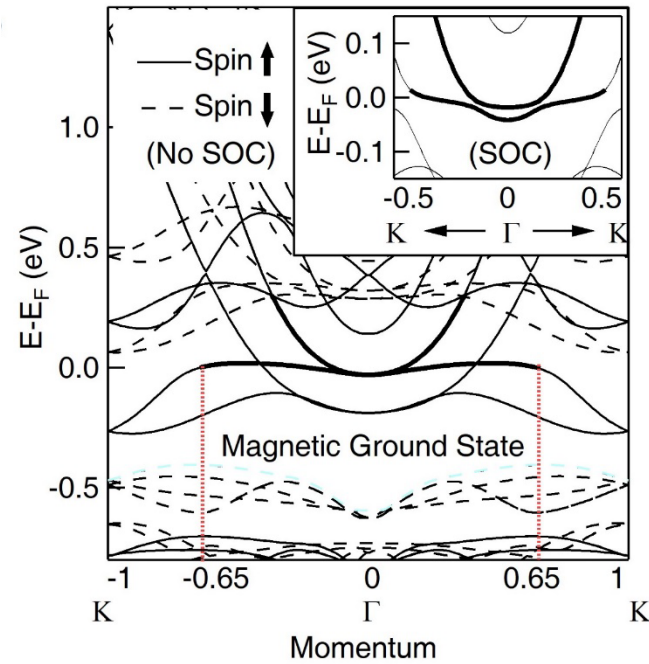
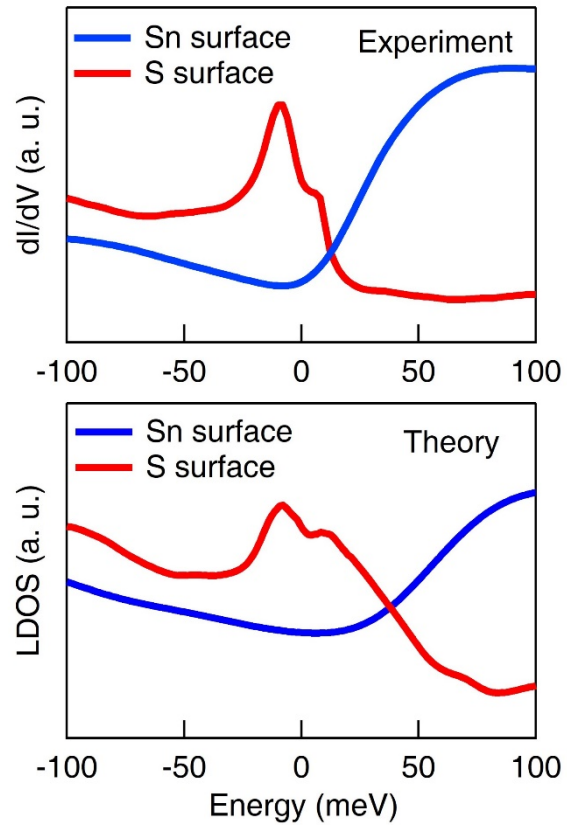
Early reference: A. Li, S.H. Pan et al. PRB (2019); P. Aynajian, A. Yazdani et al. Nature (2012)



J. X. Yin, M. Z. Hasan et al. Nat Phys (2019); J. X. Yin, M. Z. Hasan et al. Nat Commun (2020).

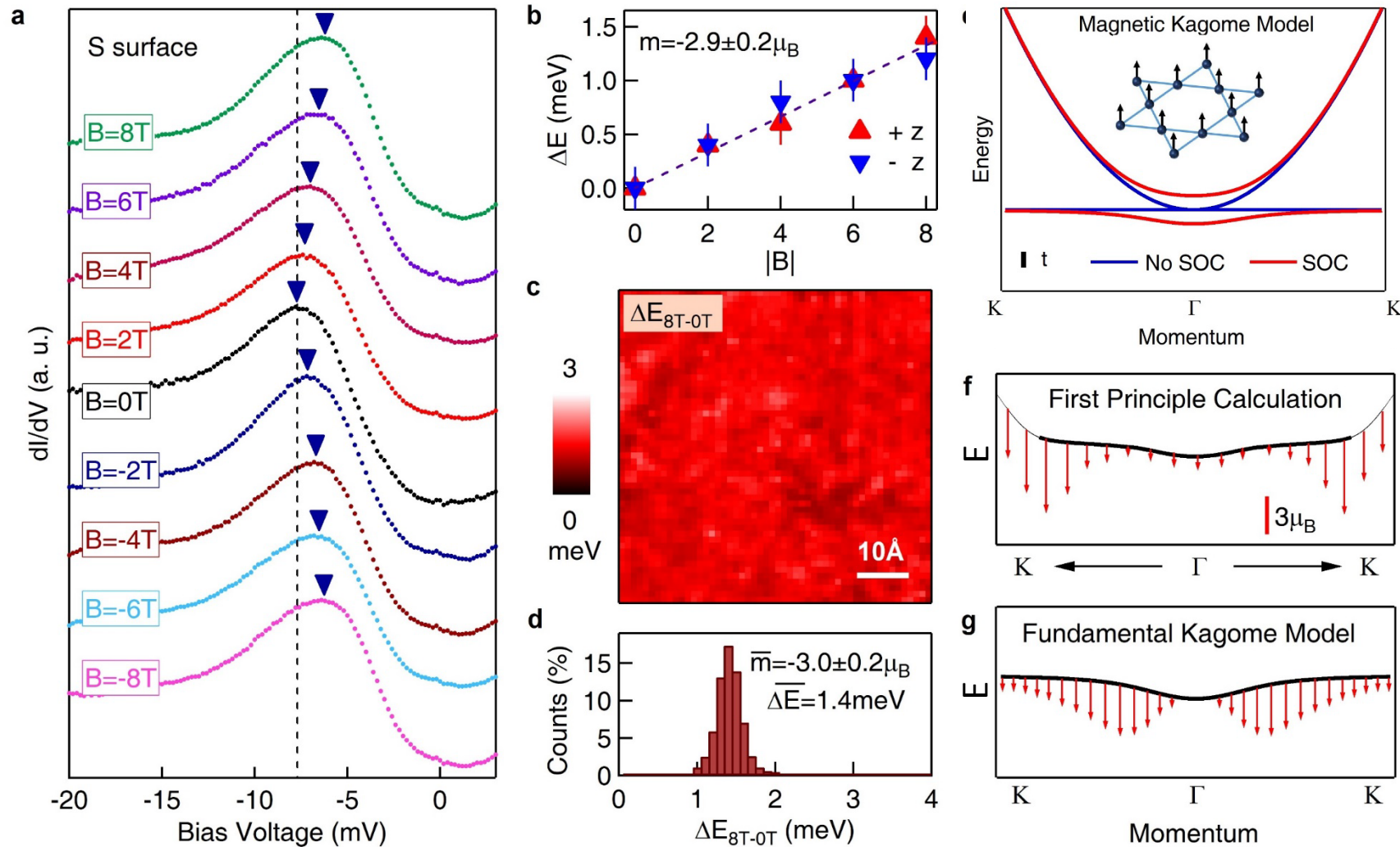
Kagome flat band in $\text{Co}_3\text{Sn}_2\text{S}_2$

J. X. Yin, M. Z. Hasan et al. Nat Phys (2019)



Negative flat band magnetism in $\text{Co}_3\text{Sn}_2\text{S}_2$

J. X. Yin, M. Z. Hasan et al. Nat Phys (2019)



Berry phase induced orbital magnetism: R. Karplus, J.M. Luttinger. PR (1954).

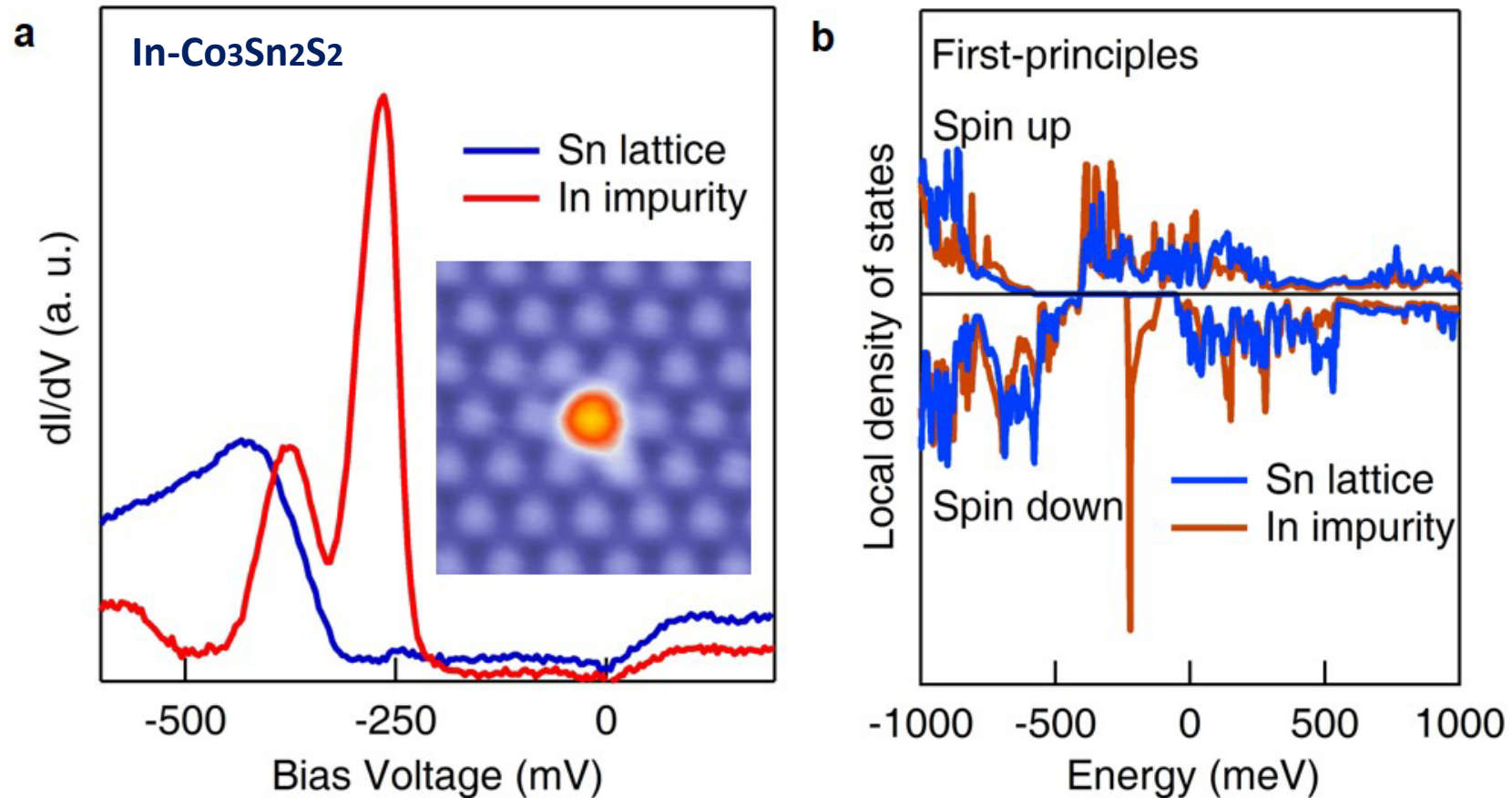
D. Xiao, M.C. Chang, Q. Niu. RMP (2010). D. Vanderbilt. Cambridge (2018).

Proof-of-principle methodology

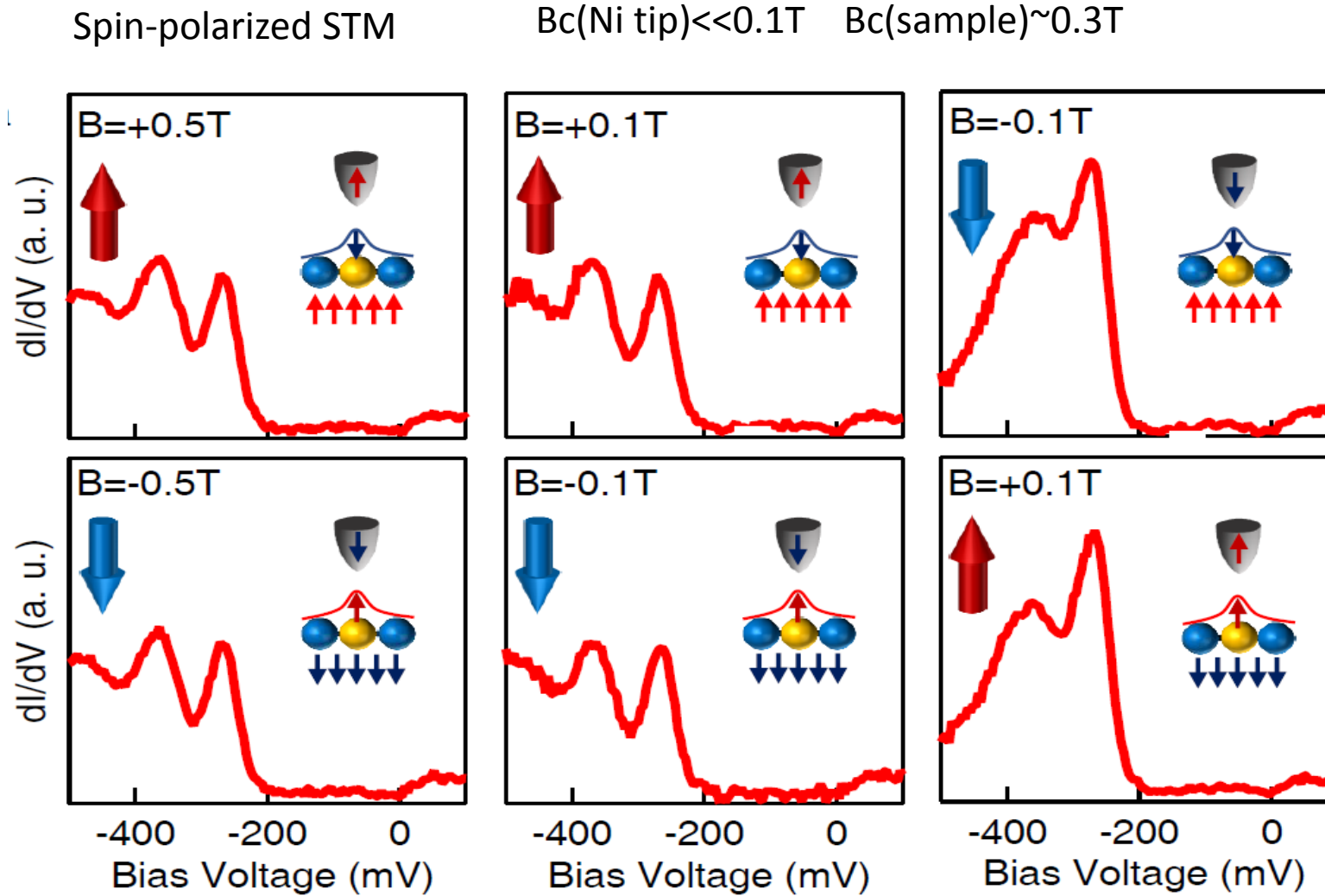
- Quasi-particle interference and Landau level quantization
- Topological correspondence as a guideline for STM discovery
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Spin-orbit quantum impurity in topological magnet

A nonmagnetic impurity can introduce spin-orbit coupled magnetic resonance in topological magnets



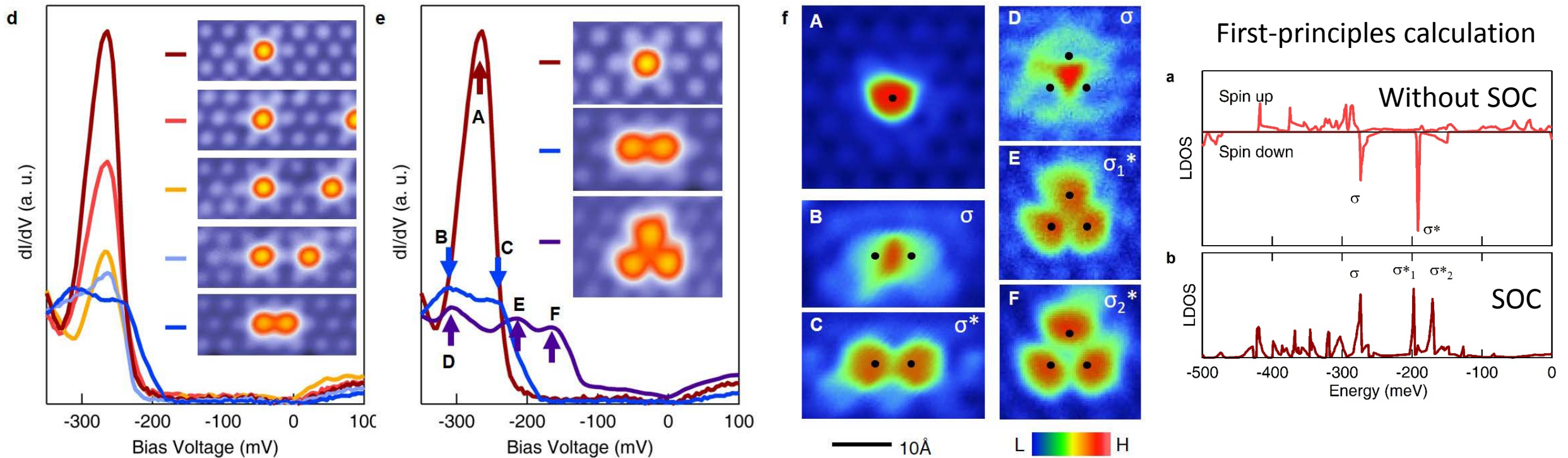
Spin-orbit quantum impurity in In-Co₃Sn₂S₂



J. X. Yin, M. Z. Hasan et al
Nat Commun (2020)

Spin-orbit quantum impurity in In-Co₃Sn₂S₂

A nonmagnetic impurity can introduce spin-orbit coupled magnetic resonance in topological magnets



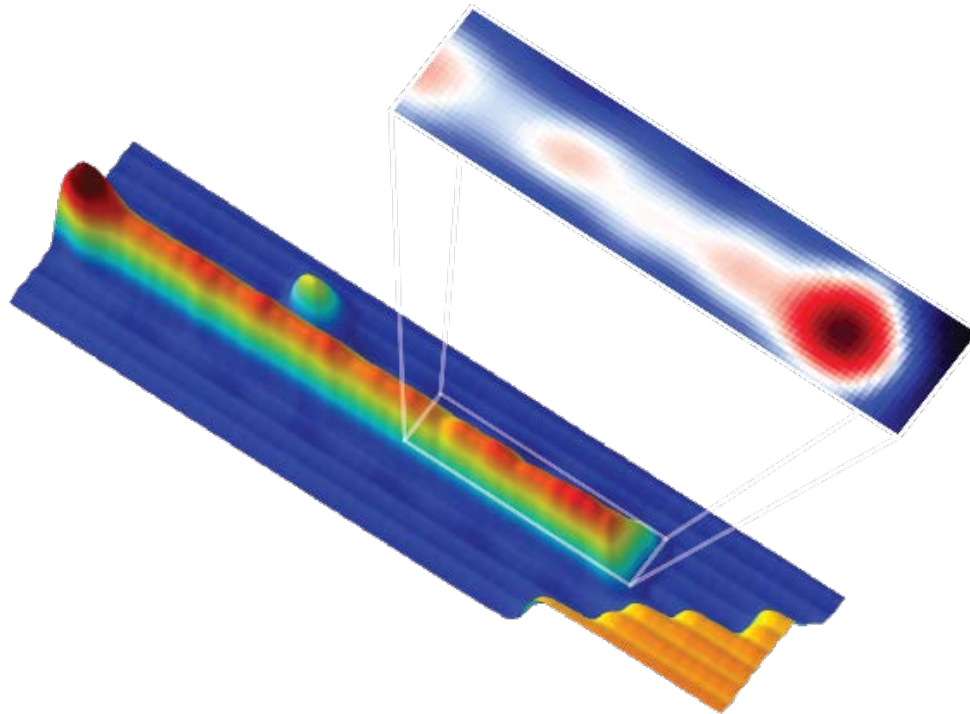
J. X. Yin, M. Z. Hasan et al
Nat Commun (2020)

Topological zero mode in artificial hybrid systems

Theory references: G. Moore, N. Read. Nucl. Phys. B (1991). G. E. Volovik. JETP Letters. (1999). A. Y. Kitaev. Phys.-Usp. (2001).

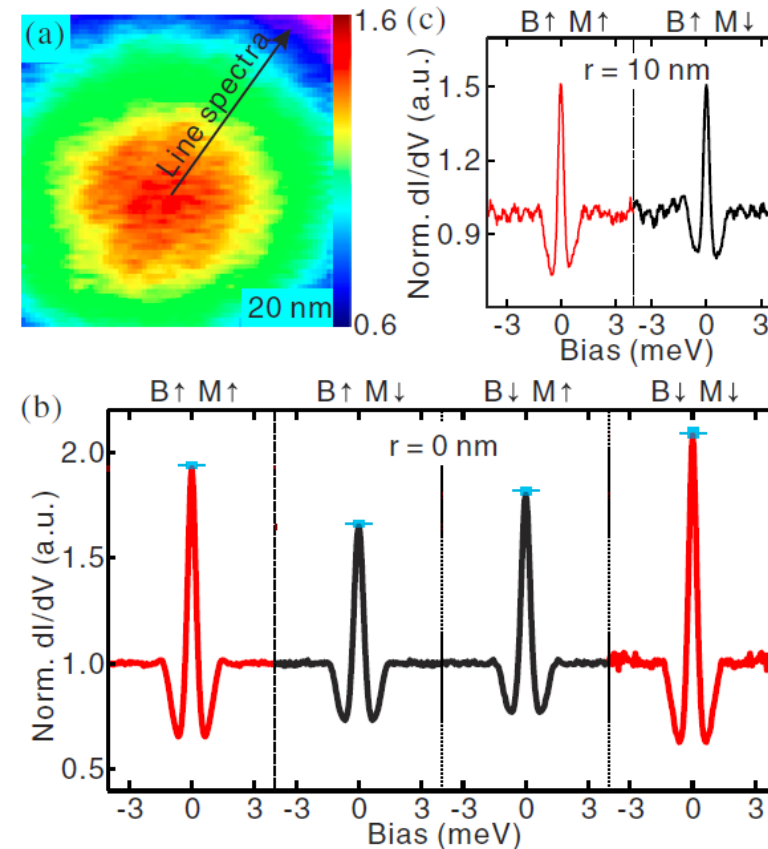
1D Chain

Ali Yazdani et al.



2D heterostructure

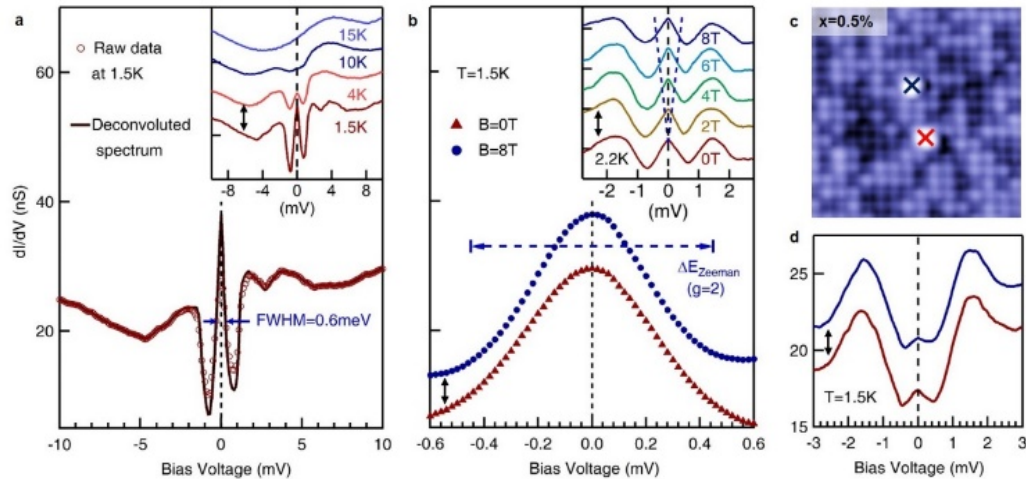
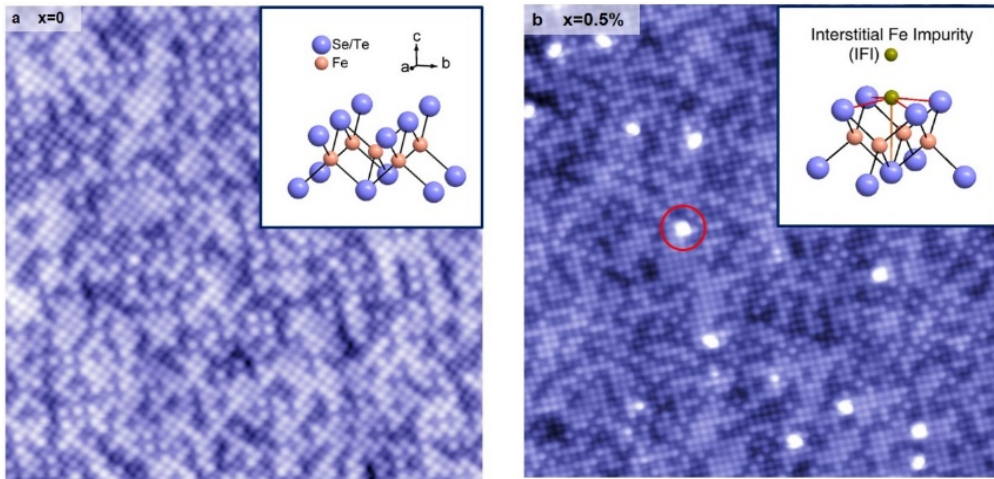
Jinfeng Jia et al.



Searching for naturally occurring topological zero mode

J X Yin, S H Pan, *et al* Nat. Phys. 2015

Majorana like robust zero mode



PHYSICAL REVIEW B **92**, 115119 (2015)

Topological nature of the FeSe_{0.5}Te_{0.5} superconductor

Zhijun Wang,^{1,2} P. Zhang,¹ Gang Xu,^{1,3} L. K. Zeng,¹ H. Miao,¹ Xiaoyan Xu,¹ T. Qian,¹ Hongming Weng,^{1,4} P. Richard,¹ A. V. Fedorov,⁵ H. Ding,^{1,4,*} Xi Dai,^{1,4,†} and Zhong Fang^{1,4,‡}

PHYSICAL REVIEW B **93**, 115129 (2016)

Topological characters in Fe(Te_{1-x}Se_x) thin films

Xianxin Wu,¹ Shengshan Qin,¹ Yi Liang,¹ Heng Fan,^{1,2} and Jiangping Hu^{1,2,3,*}

PRL **117**, 047001 (2016)

PHYSICAL REVIEW LETTERS

week ending
22 JULY 2016

Topological Superconductivity on the Surface of Fe-Based Superconductors

Gang Xu, Biao Lian, Peizhe Tang, Xiao-Liang Qi,^{*} and Shou-Cheng Zhang[†]

PHYSICAL REVIEW X **9**, 011033 (2019)

Quantum Anomalous Vortex and Majorana Zero Mode in Iron-Based Superconductor Fe(Te,Se)

Kun Jiang,^{1,2} Xi Dai,³ and Ziqiang Wang¹

¹Department of Physics, Boston College, Chestnut Hill, Massachusetts 02467, USA

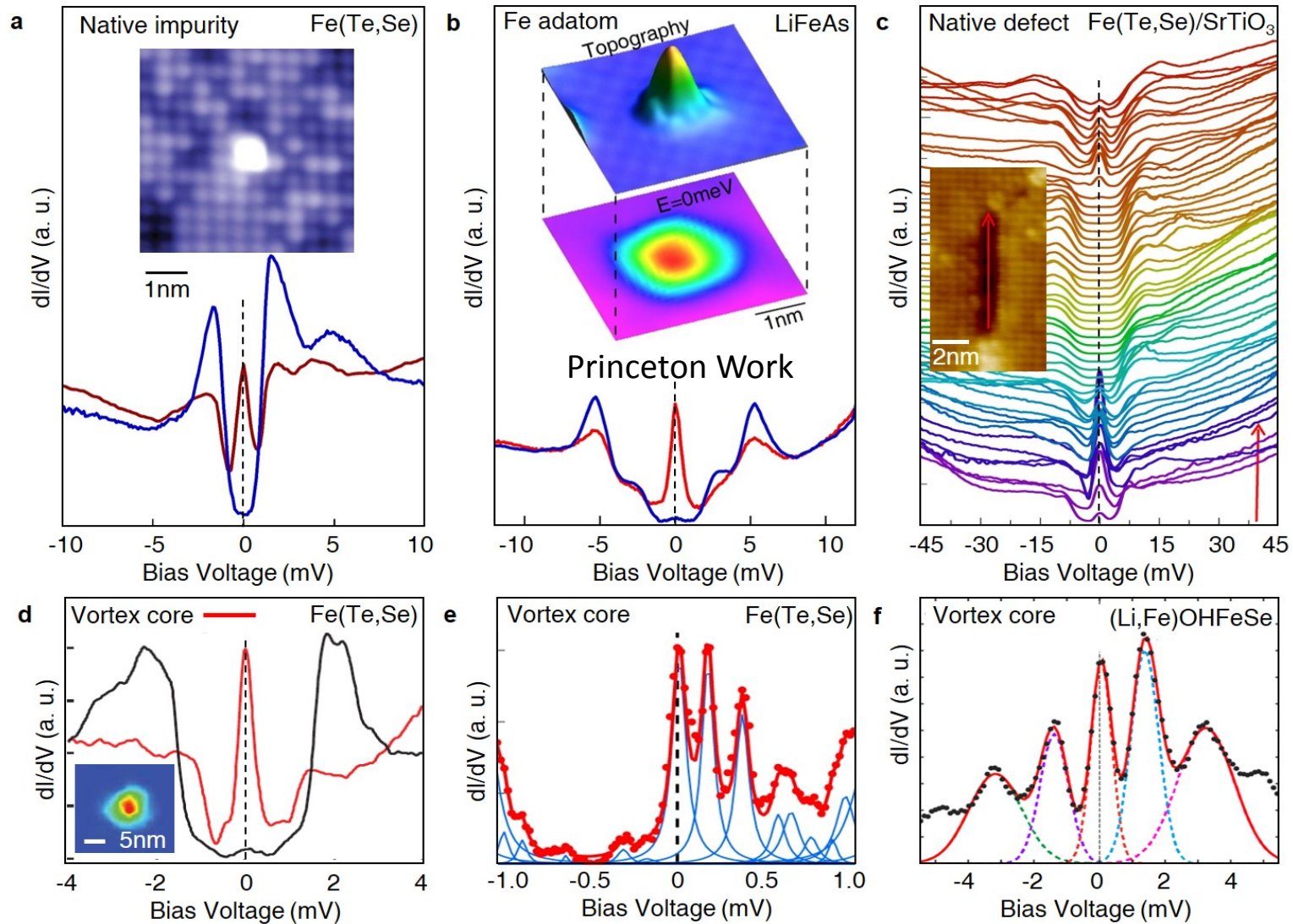
²Beijing National Laboratory for Condensed Matter Physics and Institute of Physics, Chinese Academy of Sciences, Beijing 100190, China

³Department of Physics, Hong Kong University of Science and Technology, Kowloon, Hong Kong

Spontaneous vortex formation and Majorana zero mode in iron based superconductor.

Recommended with a Commentary by Patrick A. Lee, MIT

Searching for naturally occurring topological zero mode



J.X. Yin, et al. Nat. Phys. (2015). S.S. Zhang, et al. PRB (2020). C. Chen, et al. Nat. Phys. (2020).
Z. Wang, et al. Science (2020). T. Machida, et al. Nat. Mater. (2019). Q. Liu, et al. PRX (2018).

Fundamental role of anion in iron-based superconductivity

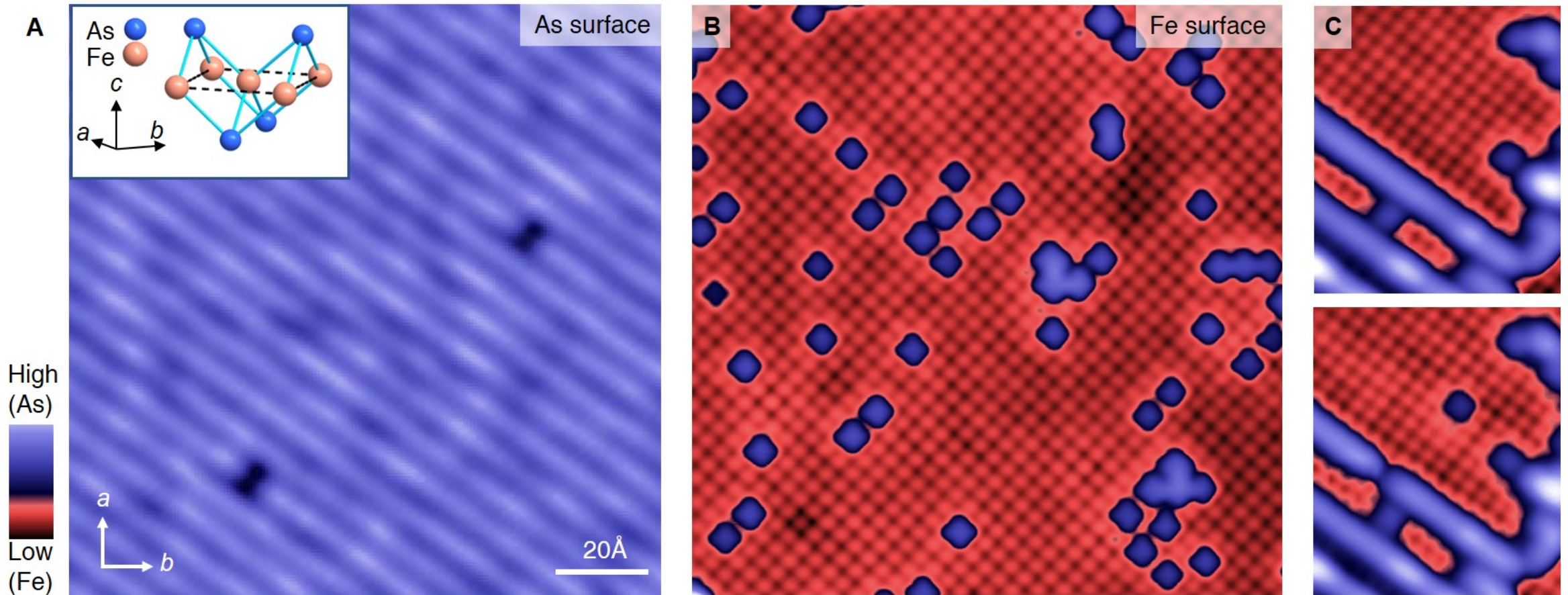
>100 cleaved $\text{Ba}_{0.4}\text{K}_{0.6}\text{Fe}_2\text{As}_2$ crystals ($T_c=38\text{K}$, experiments 2011~2015).

75% are disordered surfaces,

13% are Ba(K) surfaces, 11% are As surfaces,

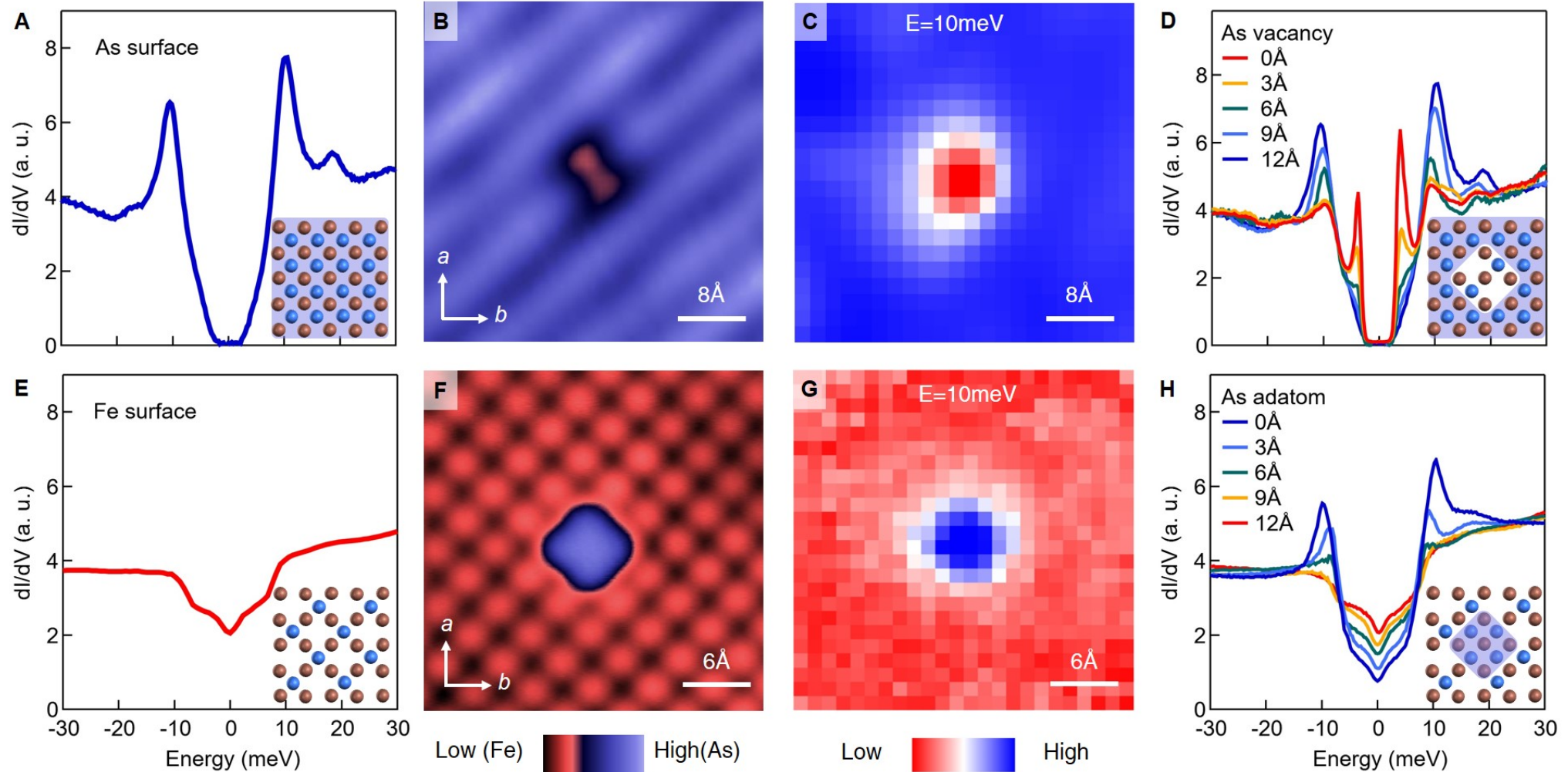
1% are Fe surfaces (six samples).

J.X. Yin, S. H. Pan et al. arXiv:2011.07701 (2020)



Atomic switch of superconducting electronic feature

Local pairing concept: P. W. Anderson Science (1987)



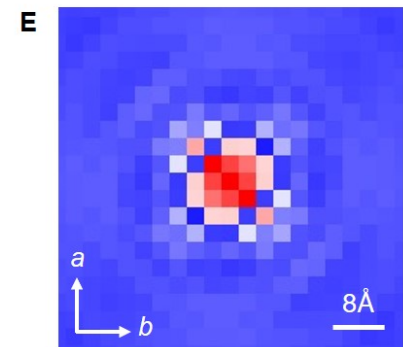
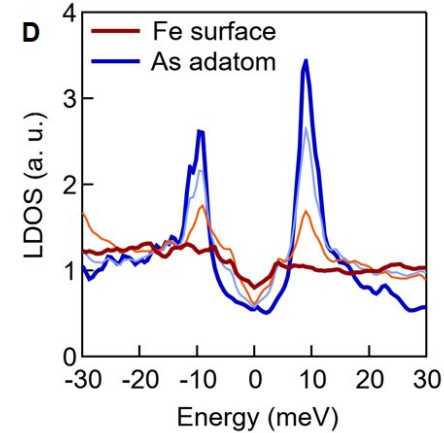
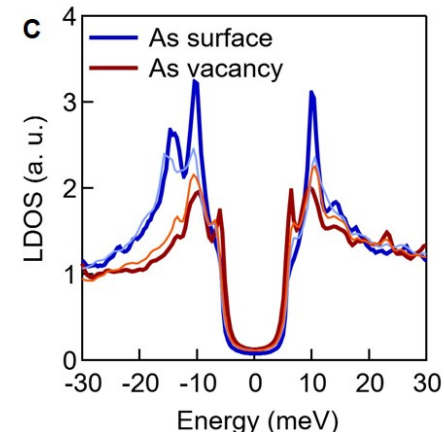
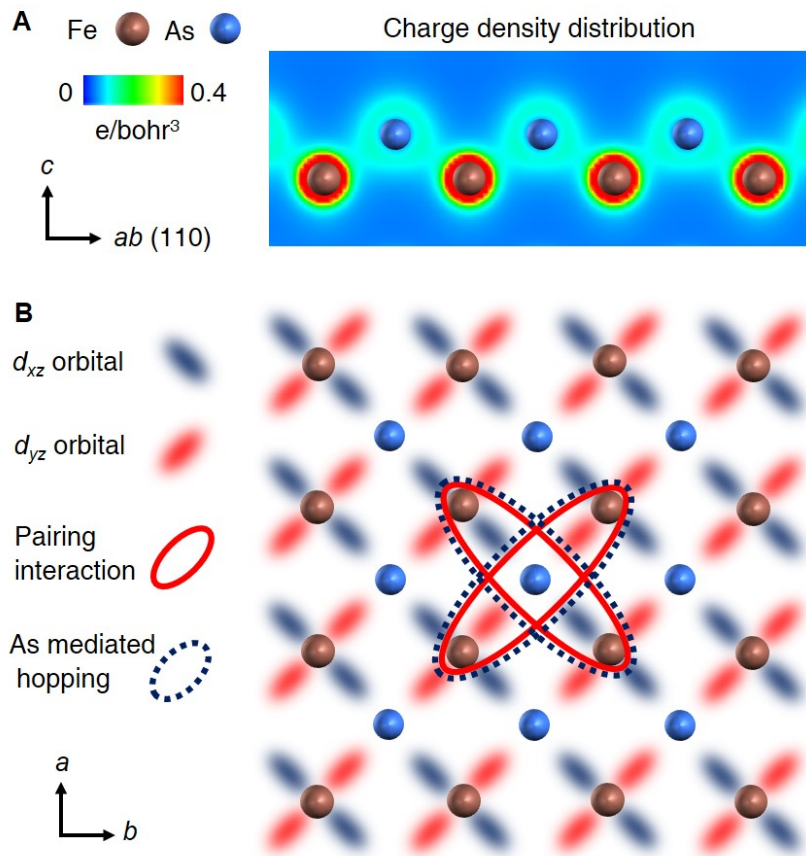
Local effects on pairing from geometry and interaction

Local pairing concept
P. W. Anderson Science (1987)

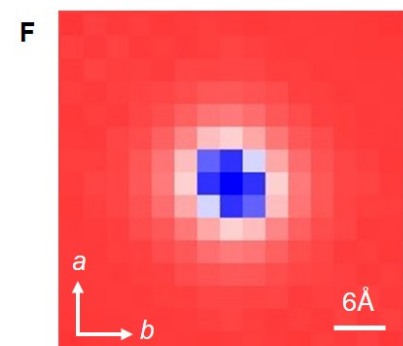
Calculations by C.S. Ting, Z. Wang, J.P. Hu, B.M. Andersen... (2011~2020)
 Self-consistent Bogoliubov-de Gennes calculation

Anion mediates
 hopping between
 neighboring Fe ions

Cooper pairing S_{\pm}
 $\Delta \sim \cos k_x \cos k_y$



Pairing strength 12  23meV



Pairing strength 2  17meV

More to discover

- **18T vector field**
- **Ramping mode map**
- **Vector electric field**



P. W. Anderson (1923-2020)

Vector field engineering of quantum materials
RMn₆Sn₆, CeAlGe, Co₂MnGa, UTe₂, BISSCO, Fe_{1+x}(Te,Se)
Wannier–Bloch correspondence visualization
Topological protection of quantum information

**Measurement of “new” :
how long it can be understood**

Ong: What is your best suggestion to young researchers when they encounter a new phenomenon?

Anderson: Patience, and it can take a lifetime long.

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