

# Active Learning via Bayesian Optimization for Discovery of Energy Storage Materials



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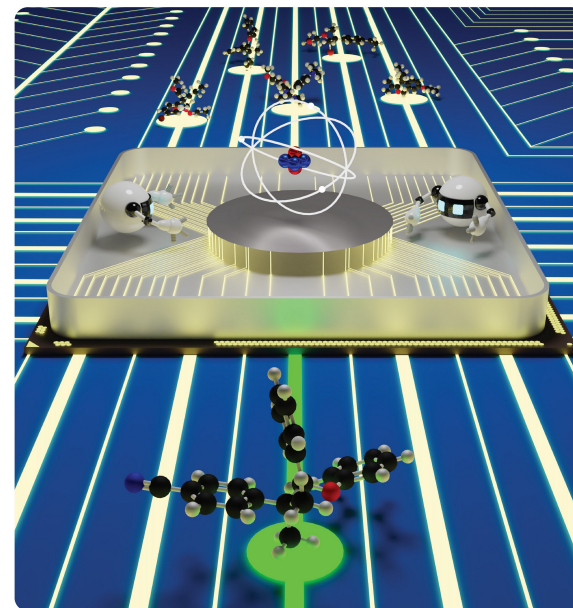
Molecular Materials Group  
Materials Science Division



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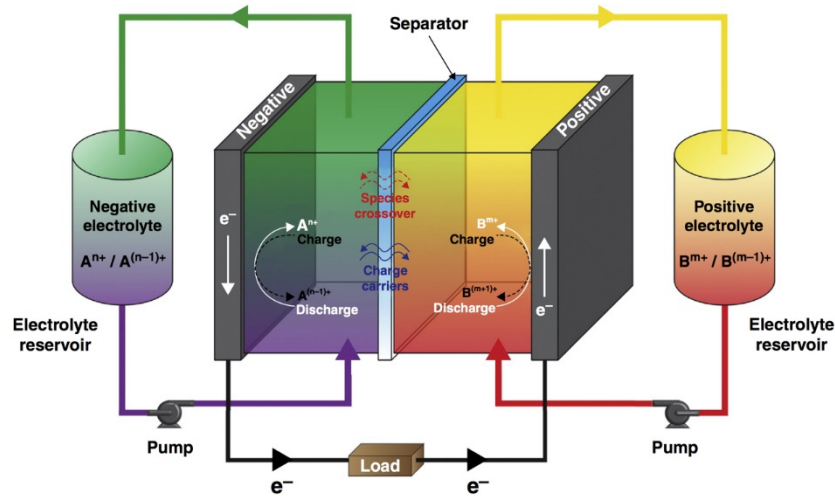
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Doan, Agarwal, Qian, Counihan, Rodríguez-López, Moore, & Assary.  
(2020). <https://doi.org/10.1021/acs.chemmater.0c00768>

# Redox Flow Battery (RFB) as a Stationary Energy Storage System

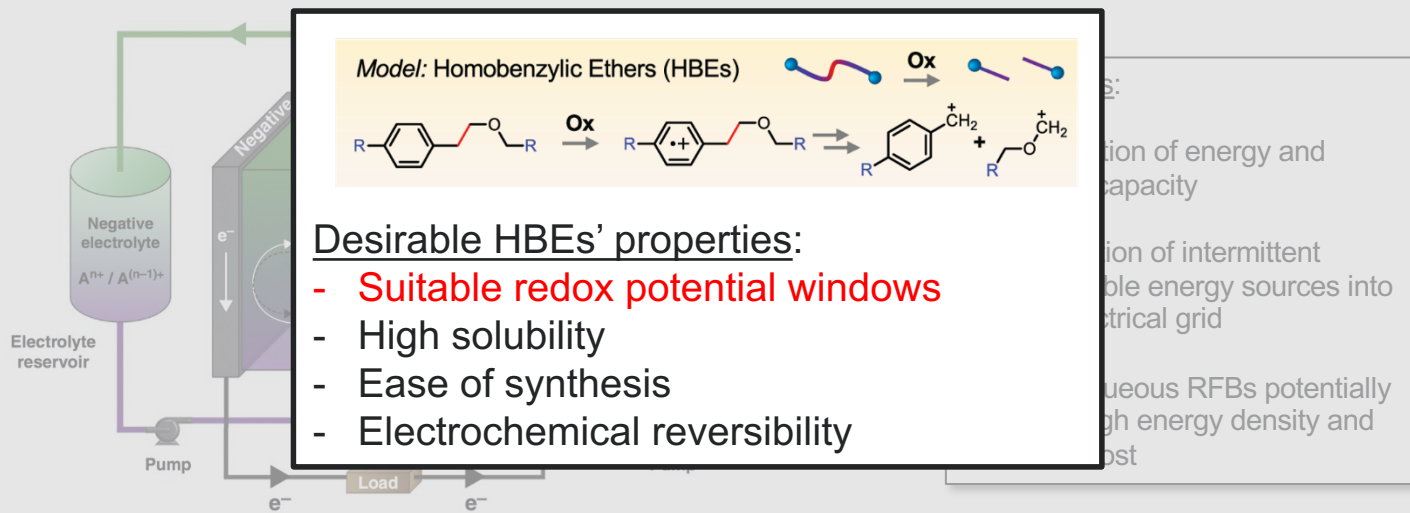


## Advantages:

- Separation of energy and power capacity
- Integration of intermittent renewable energy sources into the electrical grid
- Non-aqueous RFBs potentially yield high energy density and lower cost

Kowalski, Su, Milshtein, Brushett (2016) *Current Opinion in Chemical Engineering*

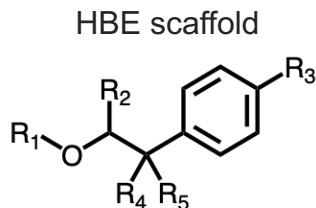
# Redox Flow Battery (RFB) as a Stationary Energy Storage System



Kowalski, Su, Milshtein, Brushett (2016) *Current Opinion in Chemical Engineering*

# The Challenges

## 1. Large space of molecular candidates



SMILES (Simplified Molecular-Input Line Entry System)

[R3]C1=CC=C(C([R4]))([R5])C([R2])-[O][R1])C=C1

$R_1$  = -Me, -Et, -Pr, -Ph, -CN, -Eth, -COMe, -C(Me)Me, -CCOMe

$R_2$  = -N(Me)<sub>3</sub><sup>+</sup>, -COMe, -Et, -OCMe, N(Me)<sub>2</sub>, -NO<sub>2</sub>, -C(=O), -Pr, -C(Me)Me, -CCOMe, -C(Me)OMe

$R_3$  = -N(Me)<sub>3</sub><sup>+</sup>, -Me, -COMe, -Br, -C(=O), -OEt, -Pr, -C(Me)Me, -C(COMe), -C(Me)(OMe)

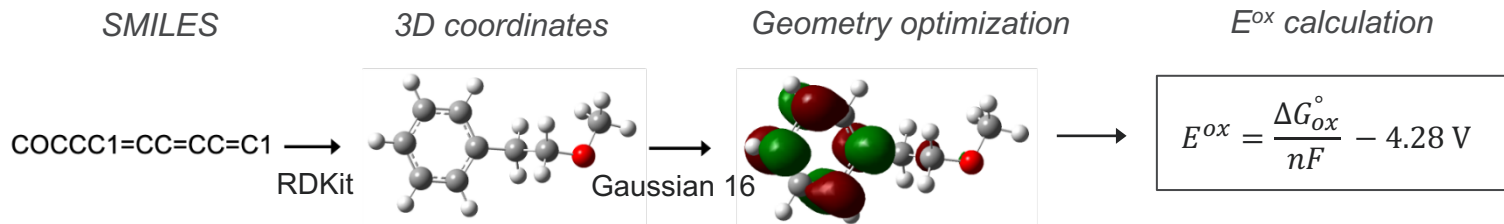
$R_4 - R_5$  = -N(Me)<sub>3</sub><sup>+</sup>, -OMe, -COMe, -Br, -N(Me)Me, -Et, -OEt, -NO<sub>2</sub>, -C(=O), -Pr, -C(Me)Me, -C(COMe), -C(Me)(OMe)

} > 10<sup>5</sup> molecules

## 2. Expensive/time-consuming synthesis and characterization

# The Opportunities

## 1. Density Functional Theory (DFT) calculations starting from SMILES



## 2. Train machine learning (ML) models using DFT-computed $E^{ox}$

Need ML models to not only make accurate predictions but also guide the selection of training data



Active learning/  
Bayesian optimization

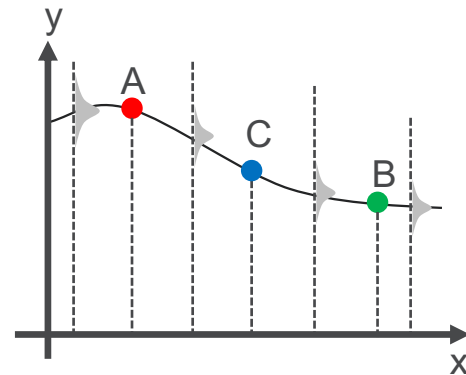
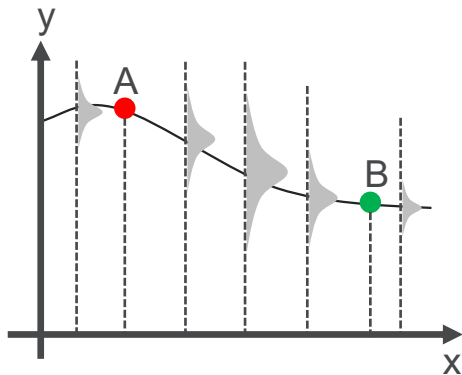
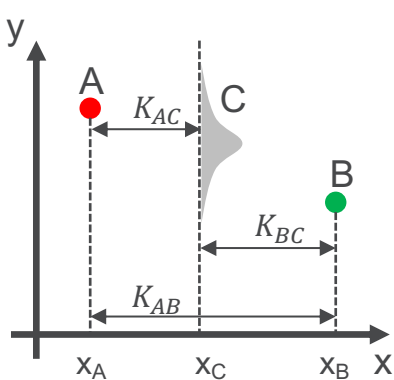
(Surrogate model + Acquisition function)

# Gaussian Process Regression (GPR) as a surrogate model

In a nutshell: Predict properties/outputs based on feature/input differences (distances)

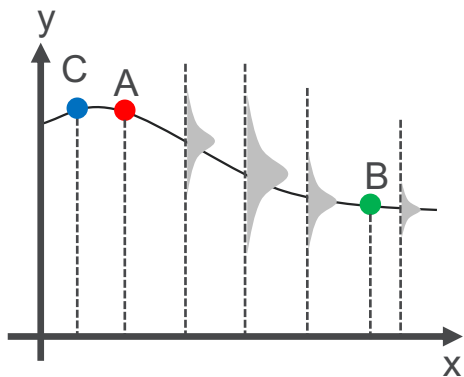
**Covariance** is calculated as a function of (feature) distances, e.g.

$$K(x_1, x_2) = \exp \left[ -\frac{1}{2} \frac{(x_1 - x_2)^2}{l^2} \right]$$

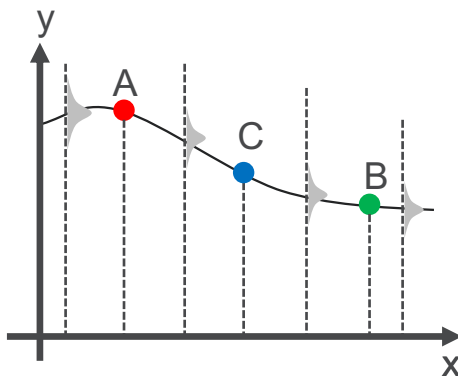
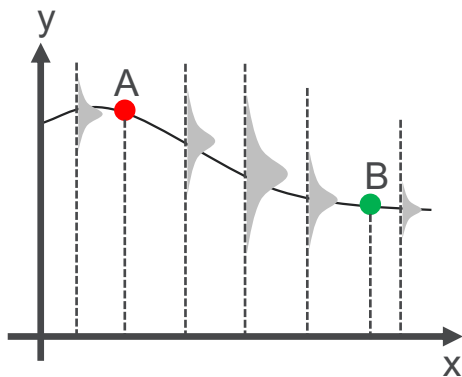


# Use of GPR in Active learning/Bayesian optimization

GPR-predicted  $\mu(x)$  and  $\sigma(x)$  enables **Active Learning/Bayesian optimization**



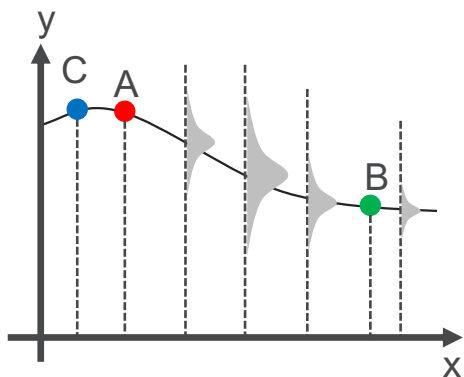
”Exploitation”: follow  $\mu(x)_{\max}$



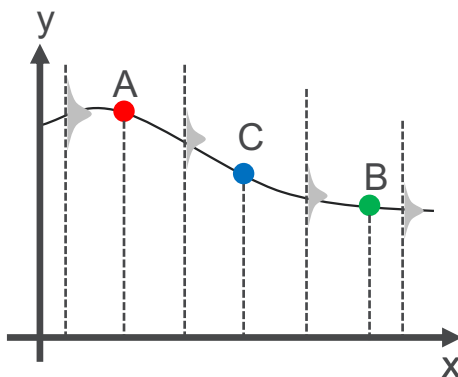
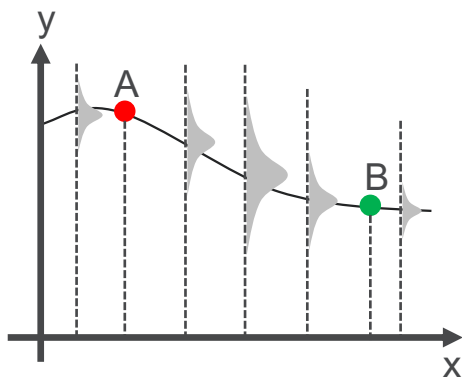
”Exploration”: follow  $\sigma(x)_{\max}$

# Acquisition function

Acquisition function formulates an optimal strategy toward an objective by guiding the next evaluation



”Exploitation”: follow  $\mu(x)_{\max}$



”Exploration”: follow  $\sigma(x)_{\max}$



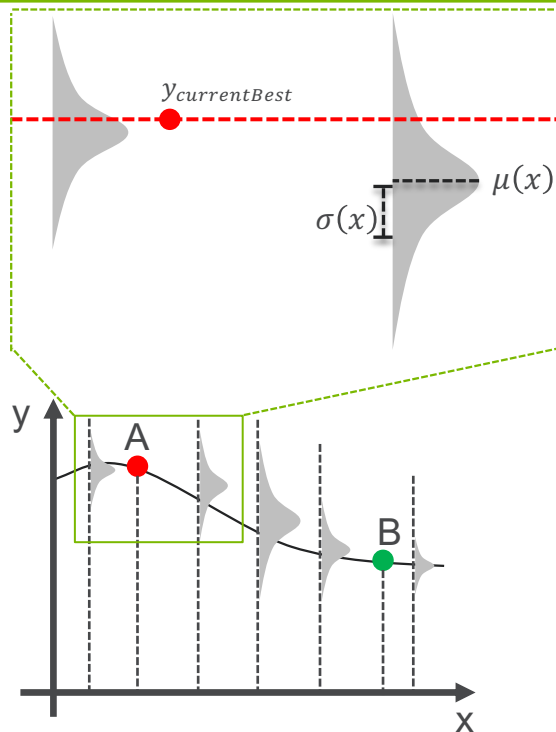


# Upper Confidence Bound (UCB)

Upper Confidence Bound (UCB)

$$UCB(x) = \mu(x) + \xi * \sigma(x)$$

$$x_{next} = \operatorname{argmax}(UCB(x))$$



$\mu(x)$ : Mean

$\sigma(x)$ : Standard deviation

# Probability of improvement (PI) and Expected improvement (EI)

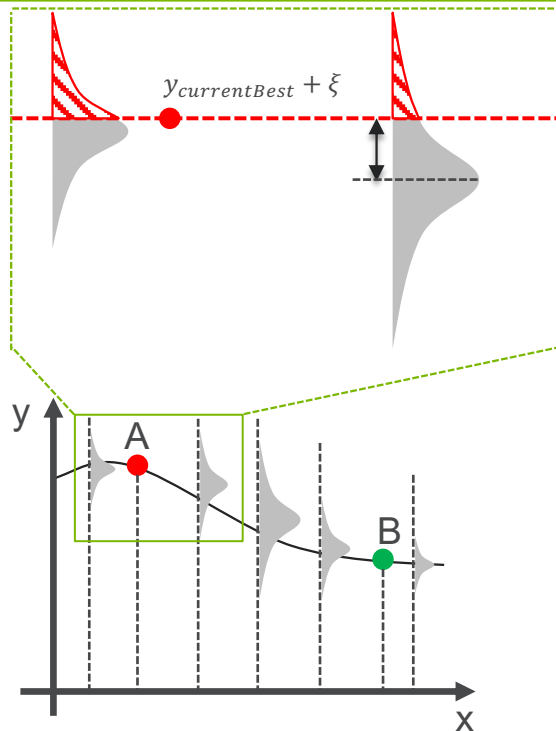
## Probability of Improvement (PI)

$$PI(x) = P(y'_x \geq y_{currentBest} + \xi)$$

$$= \Phi(Z)$$

$$Z = \frac{\mu(x) - y_{currentBest} - \xi}{\sigma(x)}$$

$$x_{next} = \operatorname{argmax}(PI(x))$$



## Expected Improvement (EI)

$$EI(x) = \begin{cases} (\mu(x) - y_{currentBest} - \xi)\Phi(Z) + \sigma(x)\phi(x), & \sigma(x) > 0 \\ 0, & \sigma(x) = 0 \end{cases}$$

$$x_{next} = \operatorname{argmax}(EI(x))$$

$\mu(x)$ : Mean  
 $\sigma(x)$ : Standard deviation

$\Phi$ : Cumulative Distribution Function  
 $\phi$ : Probability Density Function

# Problem definition for Bayesian optimization

Input

Molecule candidates  
(SMILES library)

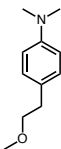
*“SMILES.csv”*



RDKit

Feature vectors

E.g.



MW	# of C	# of aromatic rings	...
179	11	1	...

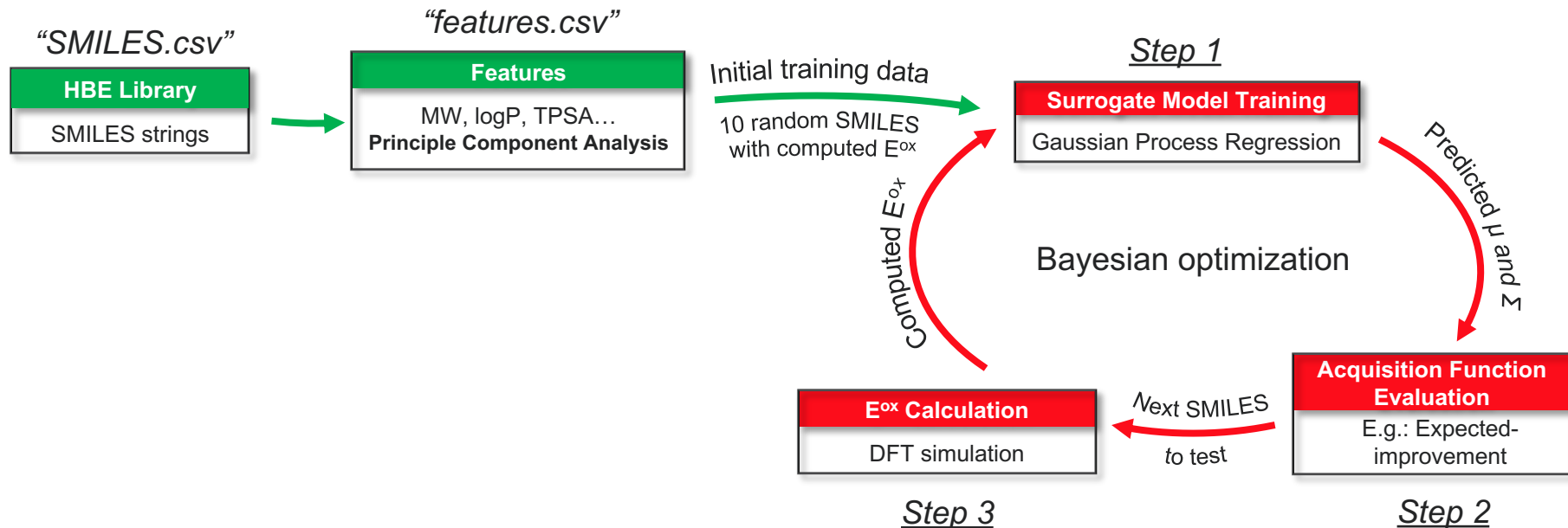
*“features.csv”* 125-component vectors

Output/Objective

Molecules w/ desired oxidation potential

# Bayesian optimization scheme

Objective: Given 1000 HBE molecules, find one with maximized  $E^{\text{ox}}$  within  $N$  evaluations



Code adapted from [https://github.com/rajak7/Bayesian\\_Optimization\\_Material\\_design](https://github.com/rajak7/Bayesian_Optimization_Material_design)

# Launch the nanoHUB tool

From your browser go to this link: <https://nanohub.org/resources/bayesopt>

The screenshot shows the nanoHUB interface for a tool titled "Bayesian optimization tutorial using Jupyter notebook". The header includes the nanoHUB logo and a "MENU" button. The main content area displays the author "By Hieu Doan, Garvit Agarwal" and a description: "Active learning via Bayesian optimization for materials discovery". A red box highlights the "Launch Tool" button, with a red arrow pointing to it from the text "Click to start the notebook". To the right of the "Launch Tool" button, there is a list of statistics: "0 users, detailed usage", "0 Citation(s)", "0 questions (Ask a question)", "0 review(s) (Review this)", and "0 wish(es) (New Wish)". At the bottom of the statistics, there is a "Share:" button with social media icons for Facebook, Twitter, and LinkedIn.

By Hieu Doan, Garvit Agarwal

Active learning via Bayesian optimization for materials discovery

**Launch Tool**

Version 1.0 - published on 11 Jun 2021

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