

**Struggling**

# **Experimentalists' Perspective**

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Department of Materials Science & Engineering

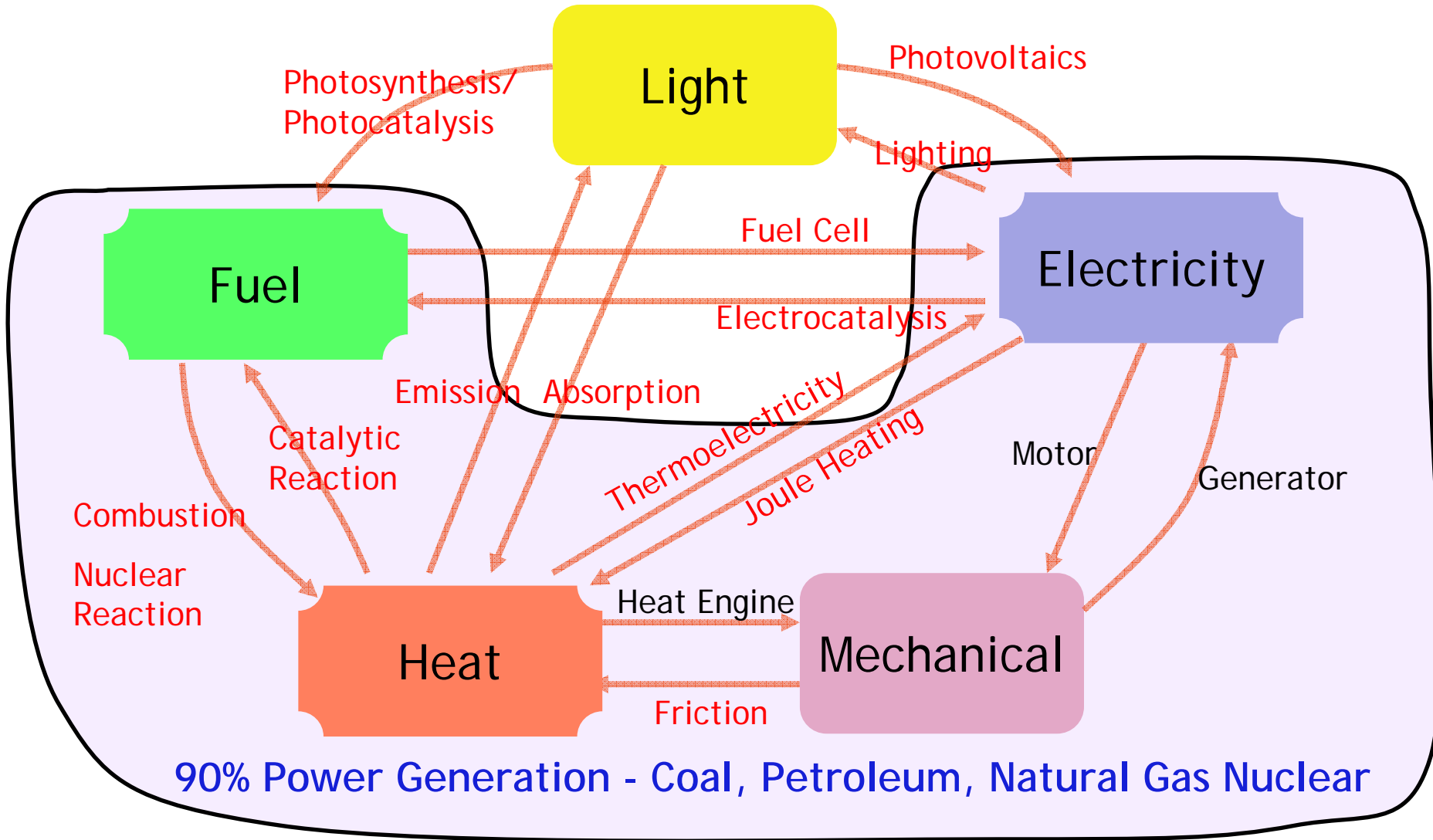
University of California, Berkeley

Faculty Scientist, Materials Sciences Division

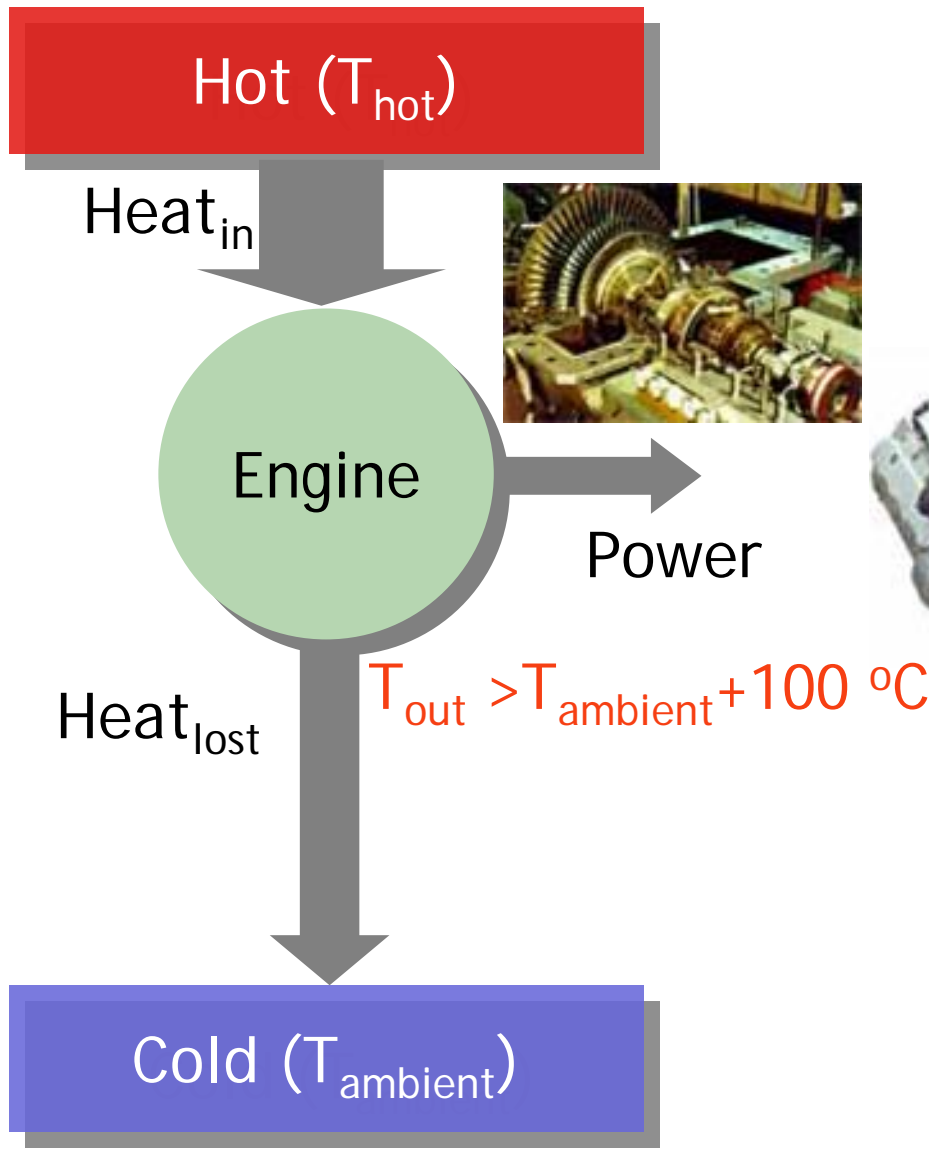
Director, Environmental Energy Technologies Division

Lawrence Berkeley National Laboratory

# Energy Conversion

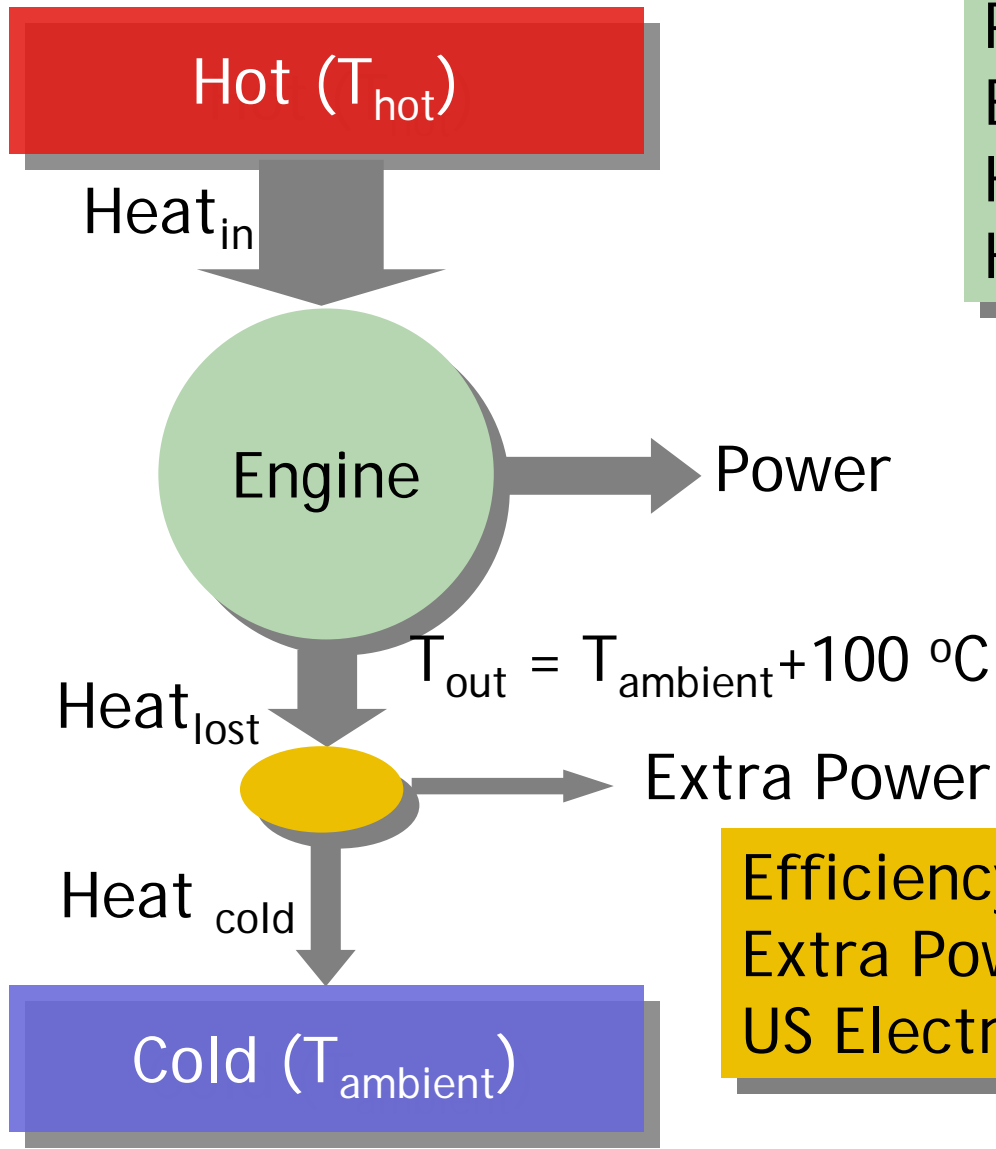


# Power Generation



Power = 10 TrillionWatts  
Efficiency = Power/Heat<sub>in</sub> ~ 40%  
Heat<sub>in</sub> = 25 TW  
Heat<sub>lost</sub> = 15 TW

# Power Co-Generation



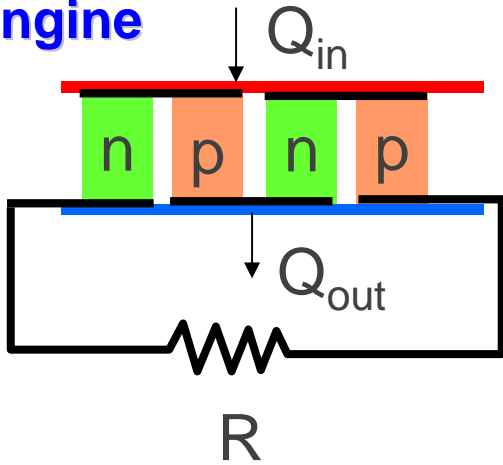
Power = 10 TrillionWatts  
Efficiency = Power/Heat<sub>in</sub> ~ 40%  
Heat<sub>in</sub> = 25 TW  
Heat<sub>lost</sub> = 15 TW

Efficiency ~ 3 %  
Extra Power = 0.45 TW  
US Electrical Capacity = 1 TW (2005)

# Thermoelectricity & Energy Conversion

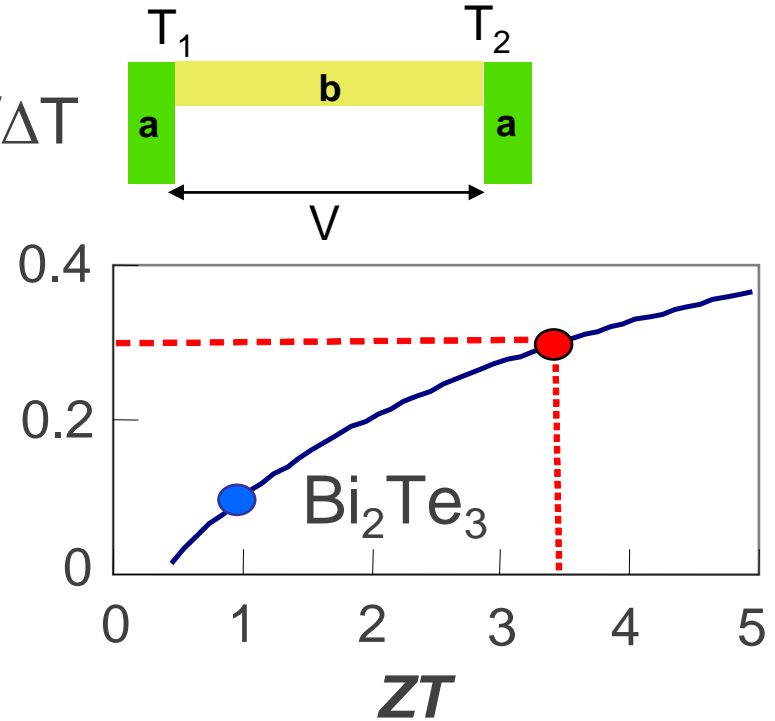
Seebeck Coefficient,  $S = V/\Delta T$

Engine

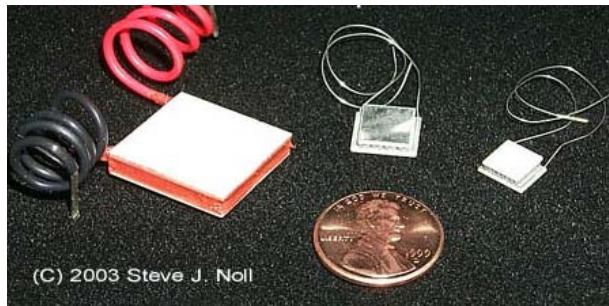
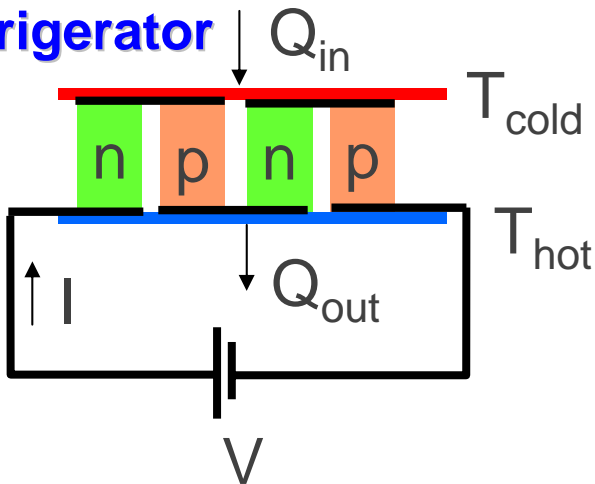


$$ZT = \frac{S^2 \sigma T}{k}$$

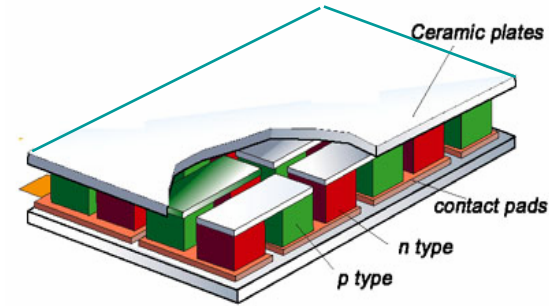
Fraction of Carnot



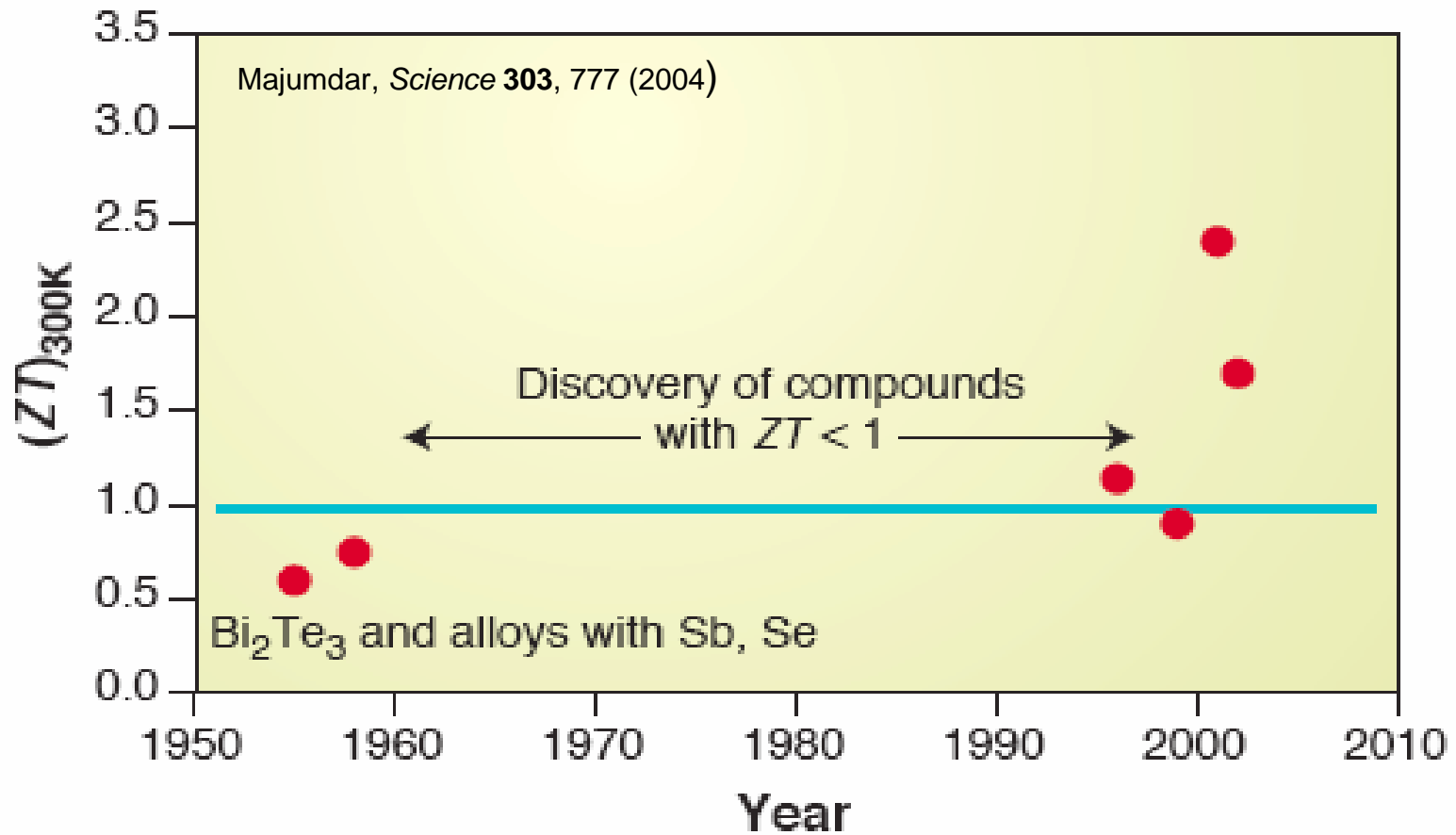
Refrigerator



Bismuth Telluride  
(low efficiency, expensive)

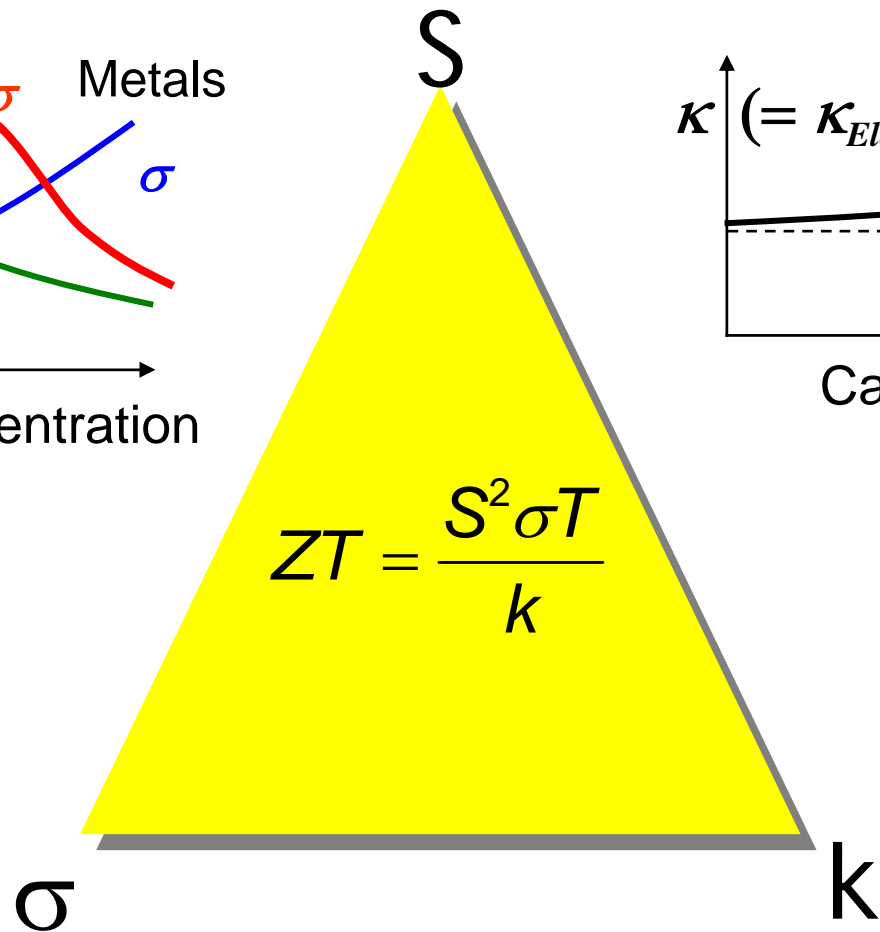
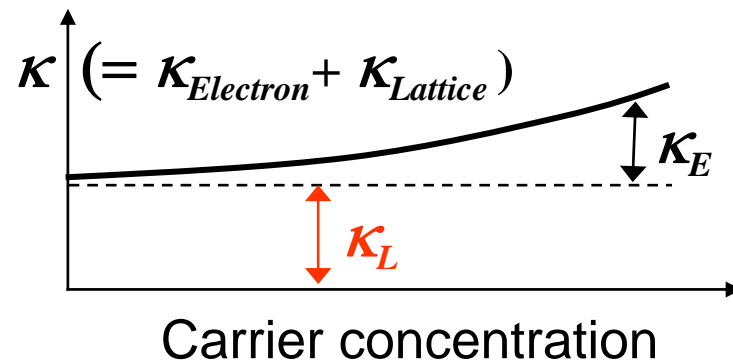
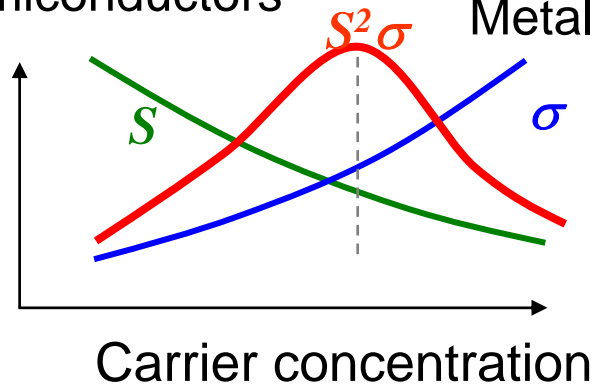


# History

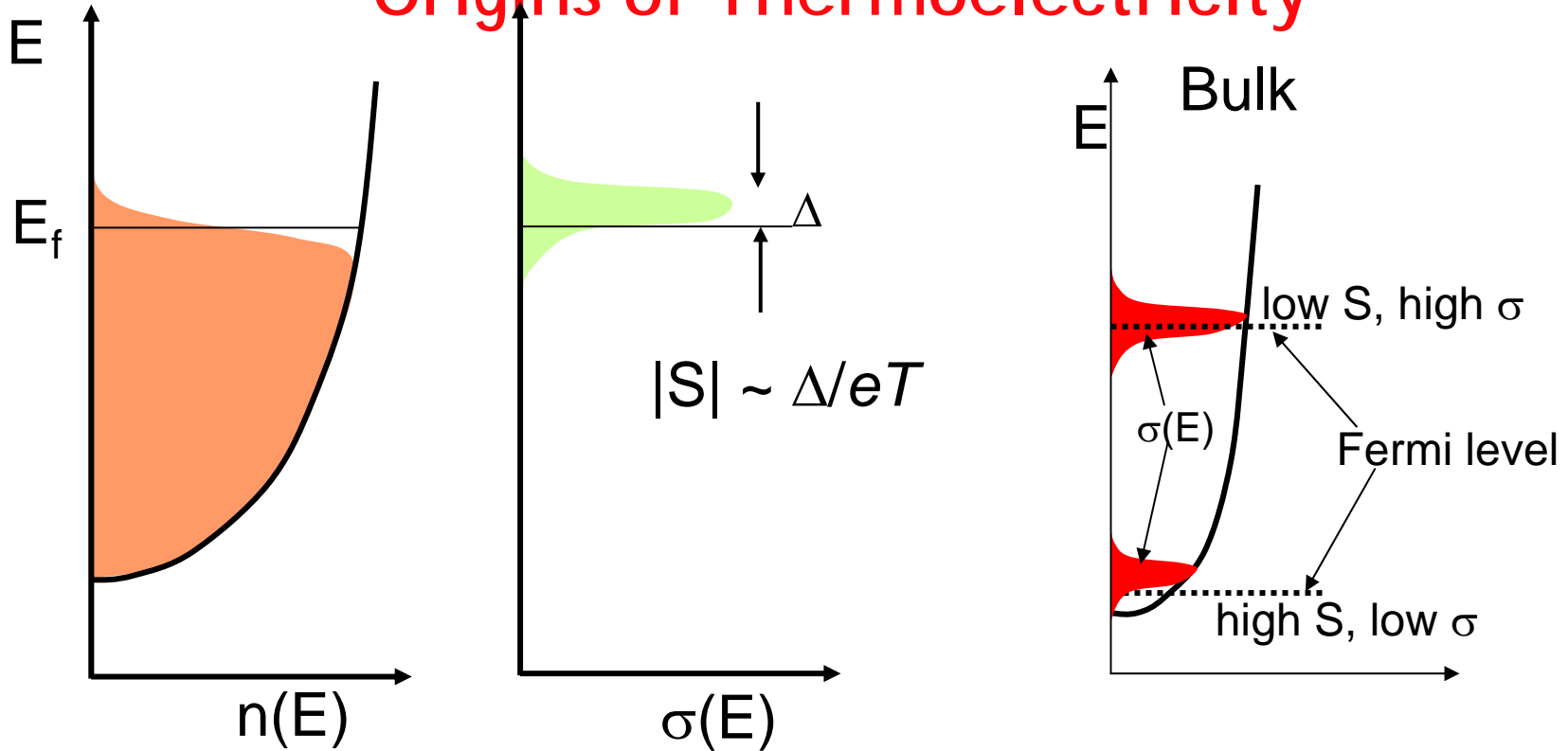


Semiconductors

Metals



# Origins of Thermoelectricity



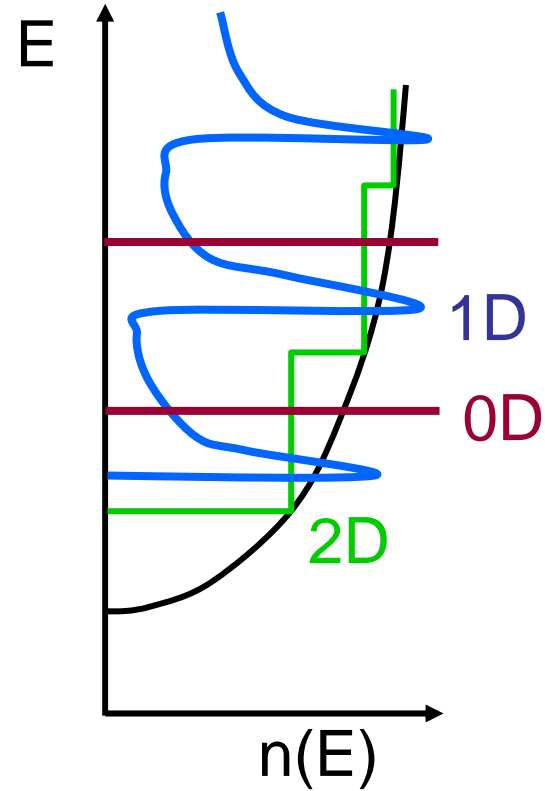
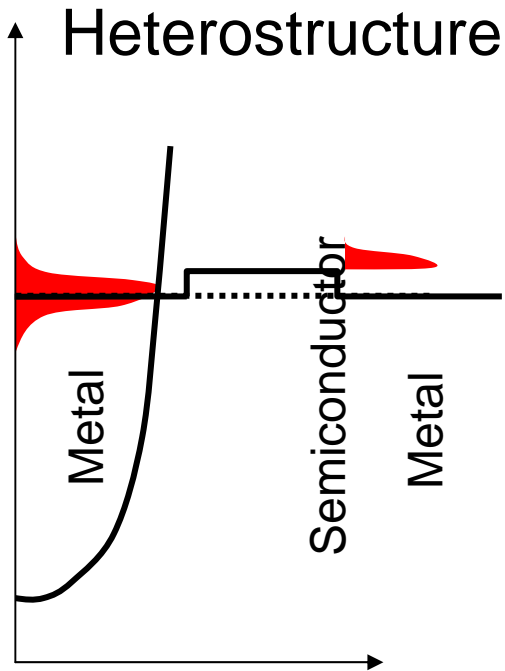
$$\sigma(E) = q^2 \tau(E) v^2(E) n(E) \left( -\frac{\partial f_{eq}}{\partial E} \right)$$

$$\sigma = \int \sigma(E) dE$$

$$S = \frac{1}{eT} \frac{\int \sigma(E) (E - E_f) dE}{\int \sigma(E) dE}$$



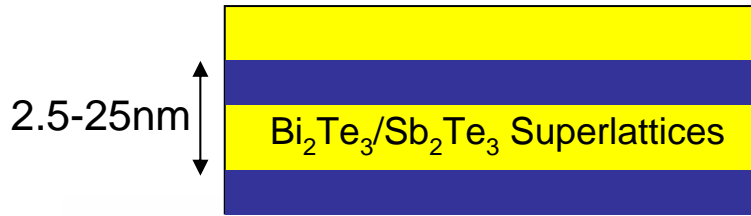
# How do we increase $S^2\sigma$



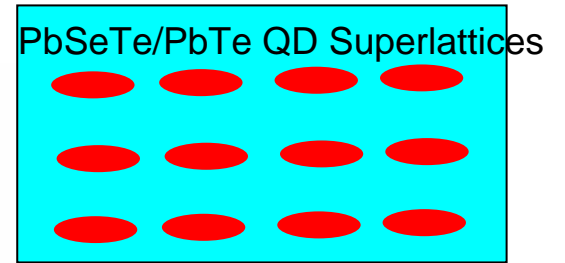
Quantum  
Confinement

# History

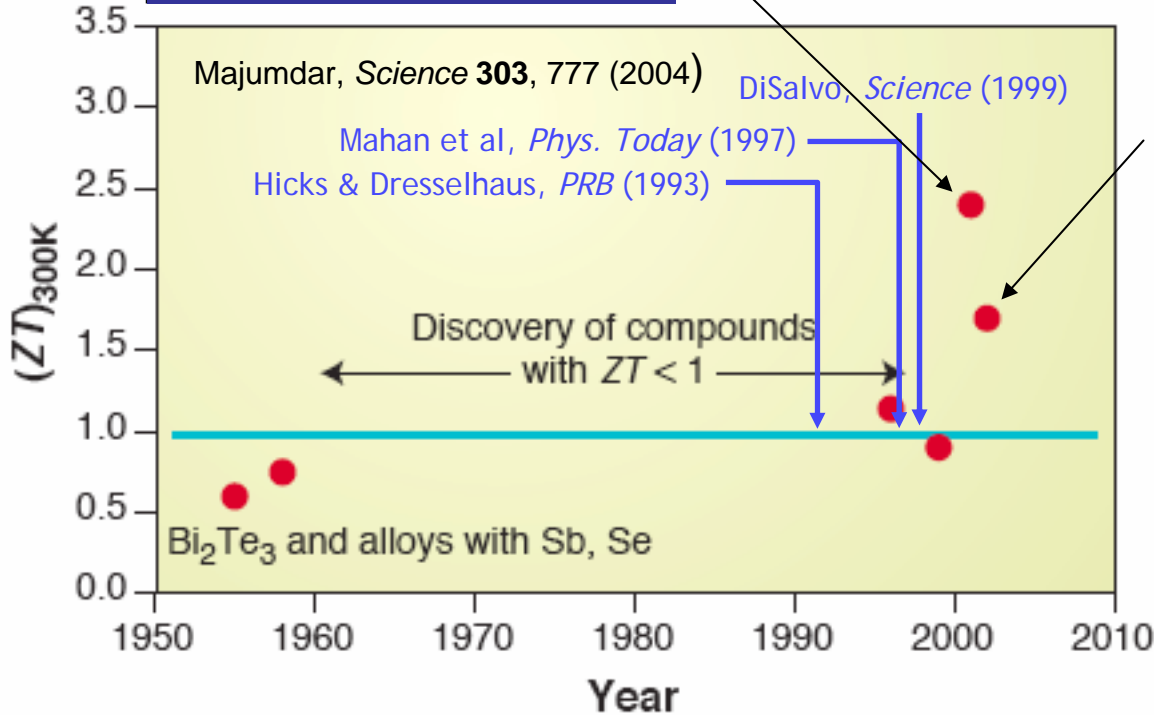
Venkatasubramanian et al. *Nature* **413**, 597 (2001)



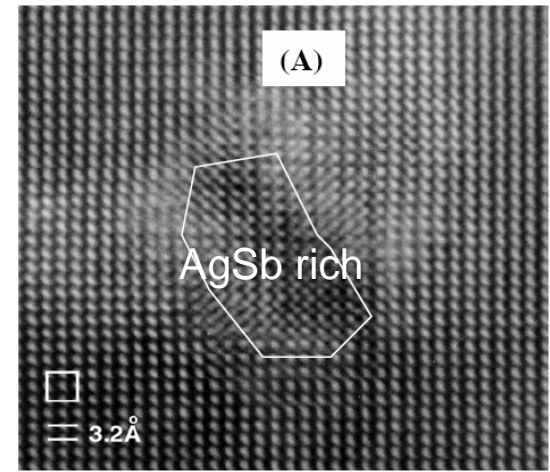
Harman et al., *Science* **297**, 2229 (2002)



$$ZT = \frac{S^2 \sigma T}{k}$$



Hsu et al., *Science* **303**, 818 (2004)



$\text{AgPb}_{18}\text{SbTe}_{20}$   
 $ZT = 2 @ 800K$

# Transport Length Scales for Si @ 300 K

Ju, Goodson (1999)

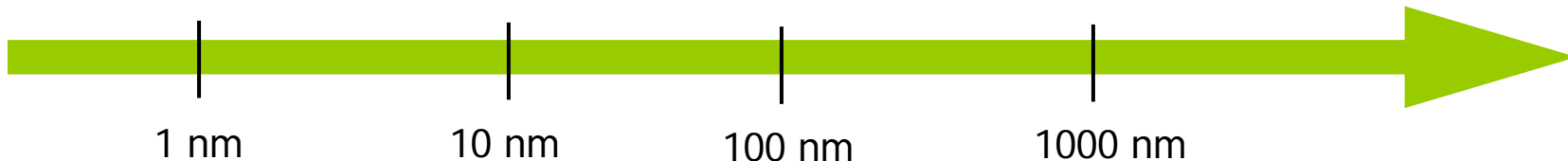
$$\sigma = \frac{\eta e^2 \ell_e}{m v_{therm}}$$

$$k = \frac{1}{3} C v_s \ell_{ph}$$

Mean Free Path

Electrons

Phonons



Wavelength

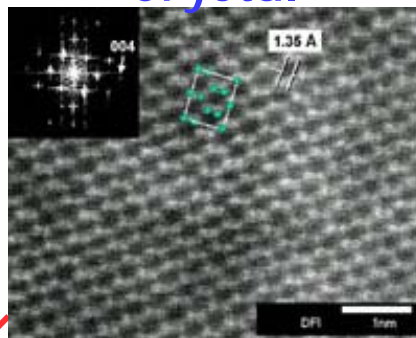
1 nm

10 nm

100 nm

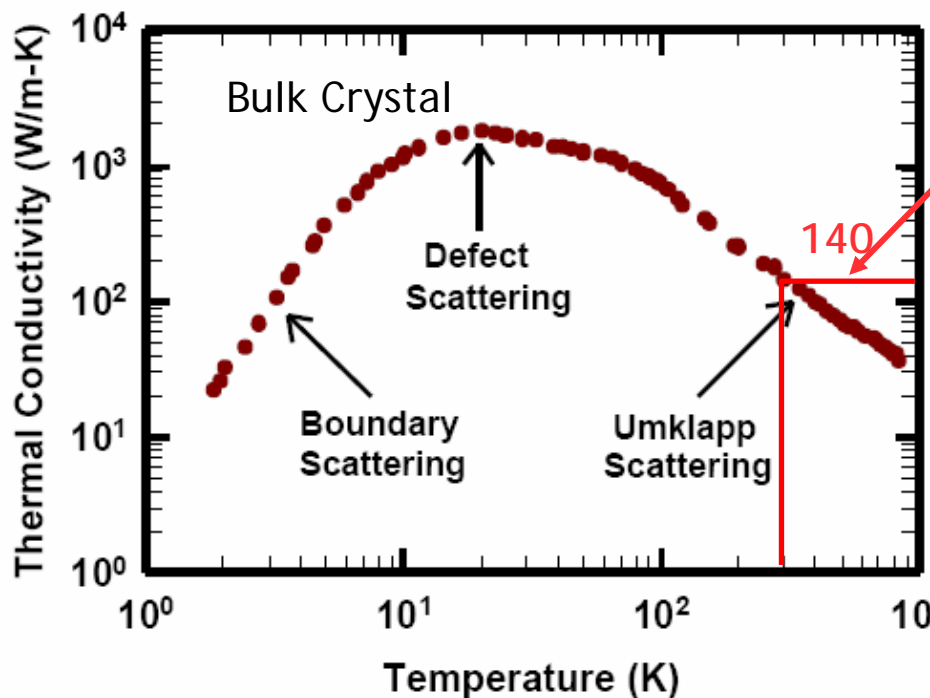
1000 nm

Crystal

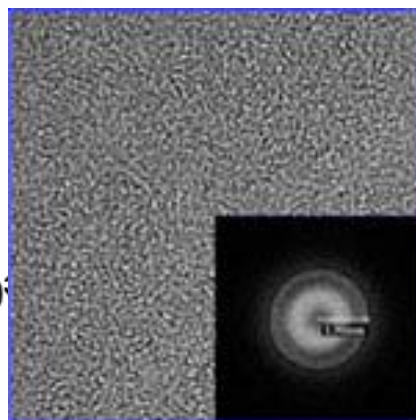


$$k_{max} = 140 \text{ W/m-K}$$

$$ZT_{Bulk,Crys} = \frac{S^2 \sigma T}{k} \approx 0.008$$



Amorphous



$$\ell_e, \ell_{ph} \leq 1 \text{ nm}$$

$$k_{min} = 1 \text{ W/m-K}$$

$\sigma$

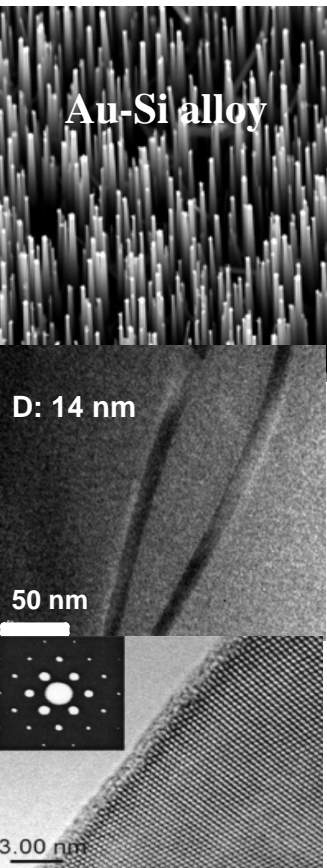
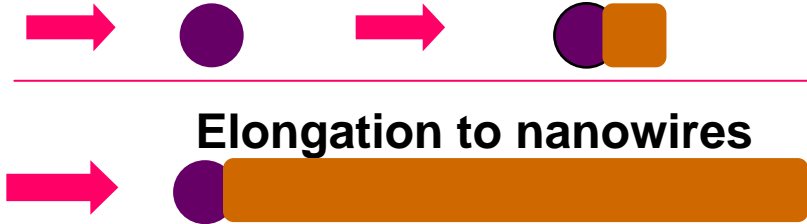
$$ZT_{Bulk,Amorp} \approx 0.08$$

# Vapor-Liquid-Solid (VLS) Si Nanowires

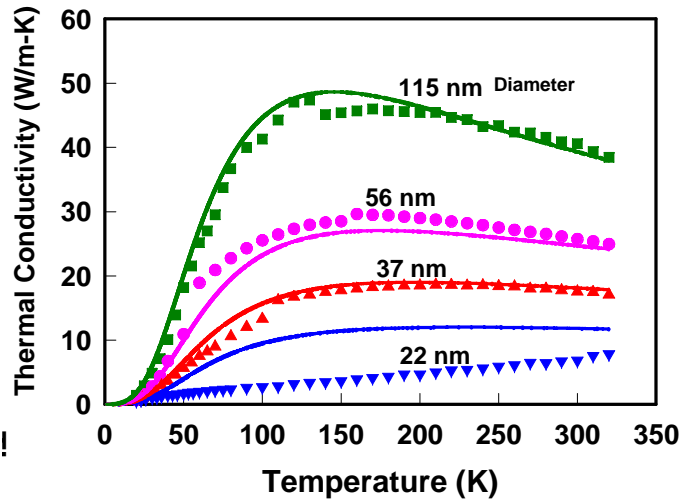
Vapor-Liquid-Solid (VLS) Technique

Si/Au alloy

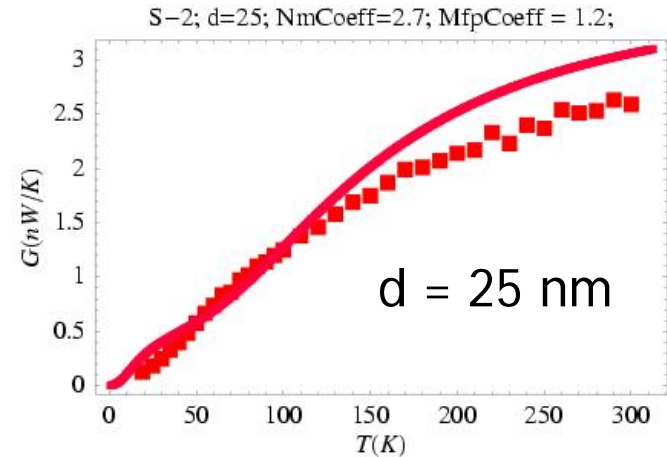
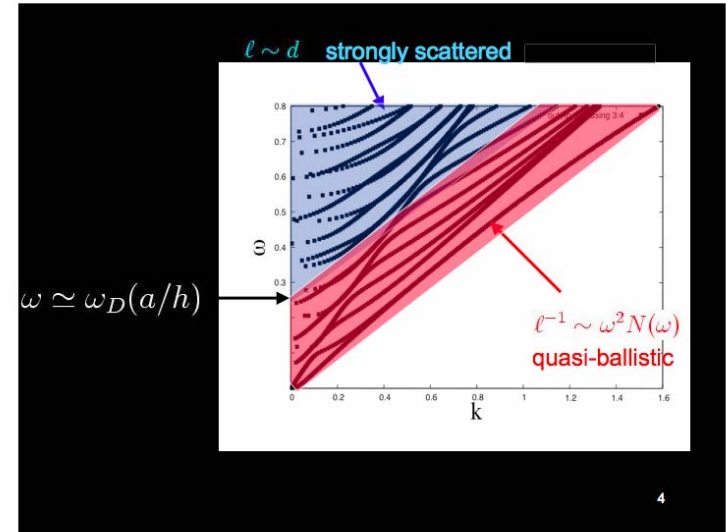
Phase Separation



Li, Wu, Kim, Shi, Yang, Majumdar, APL (2003)

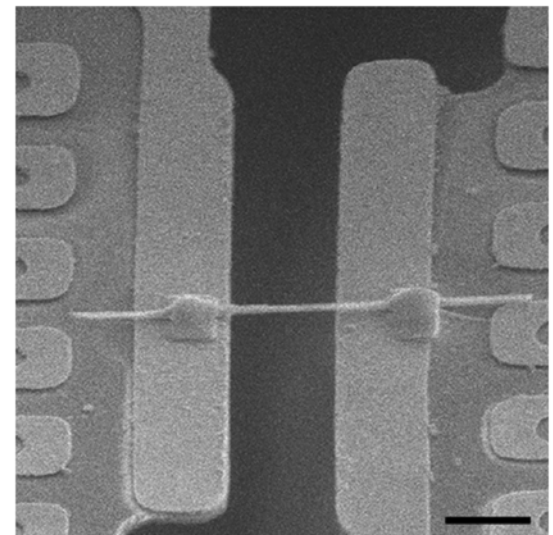
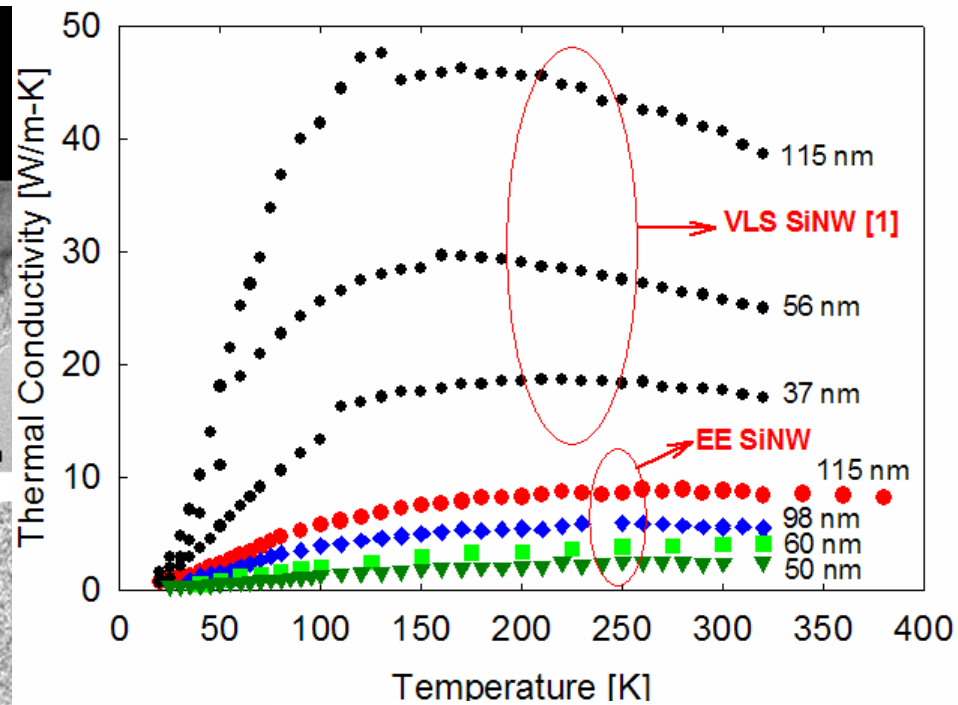
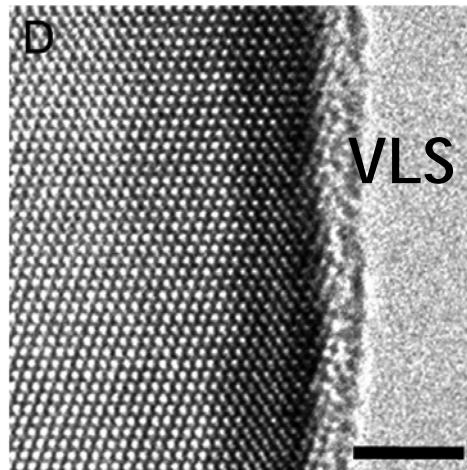
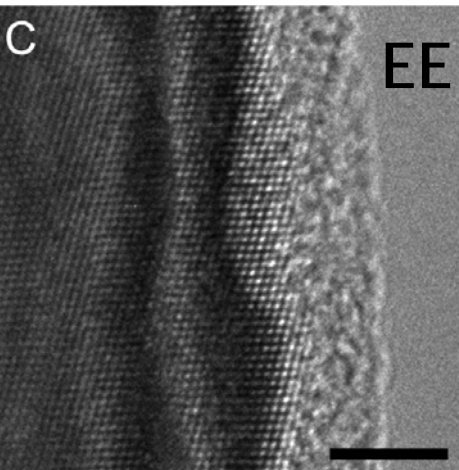
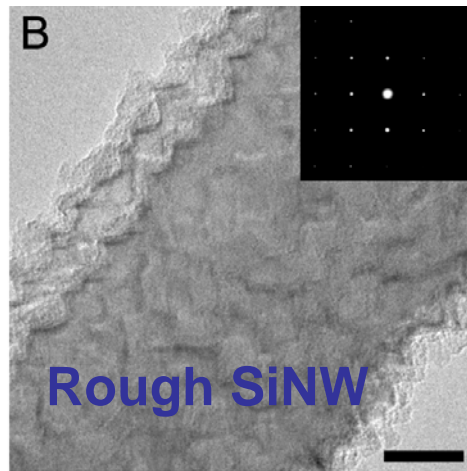
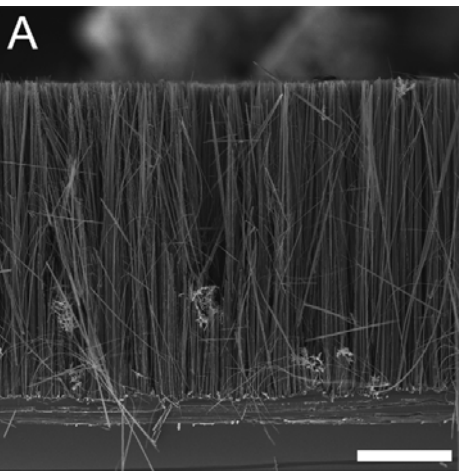


Peidong Yang (UCB)



Padraig Murphy, Joel Moore (UCB)

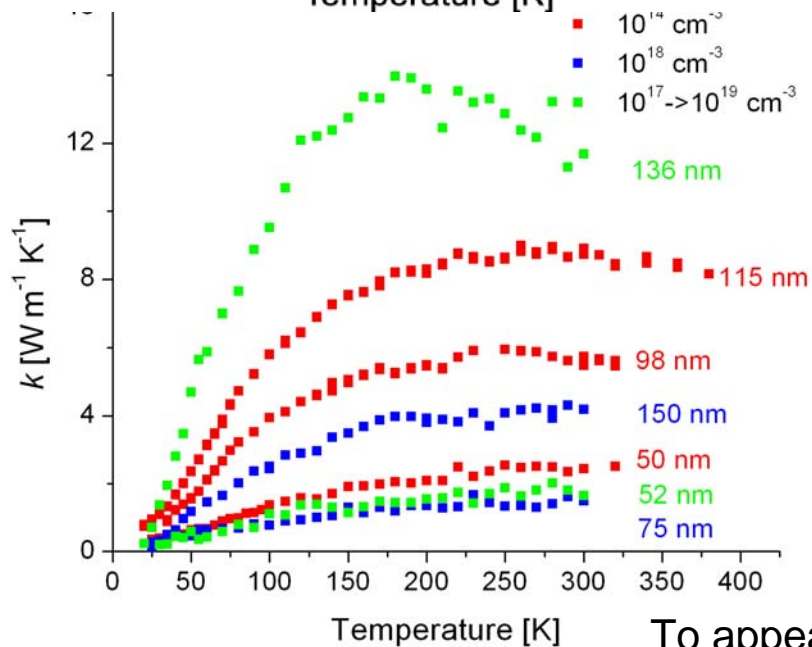
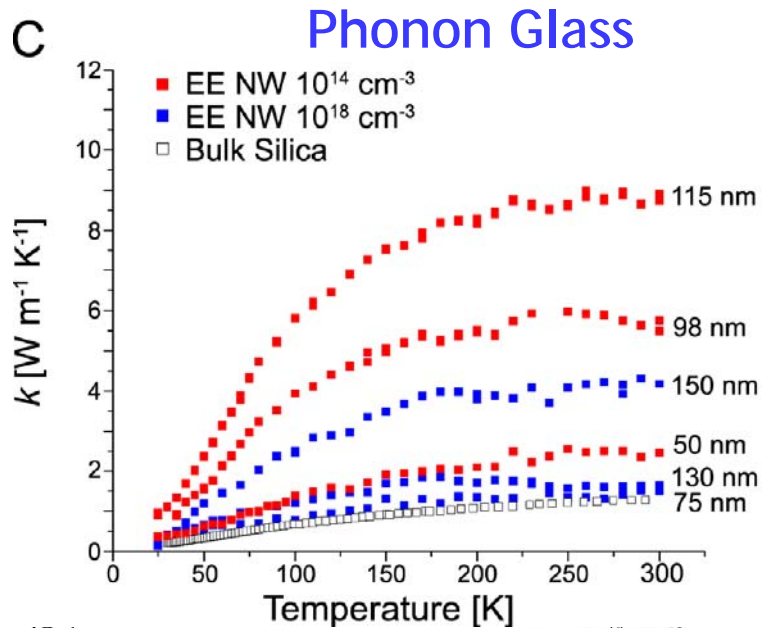
# Electroless Etched Si Nanowires



Allon Hochbaum, Renkun Chen,  
Peidong Yang (UCB)

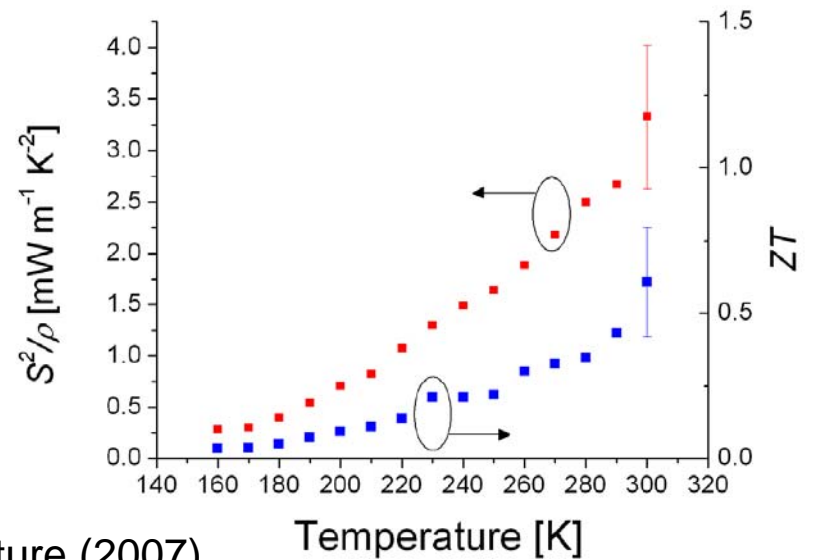
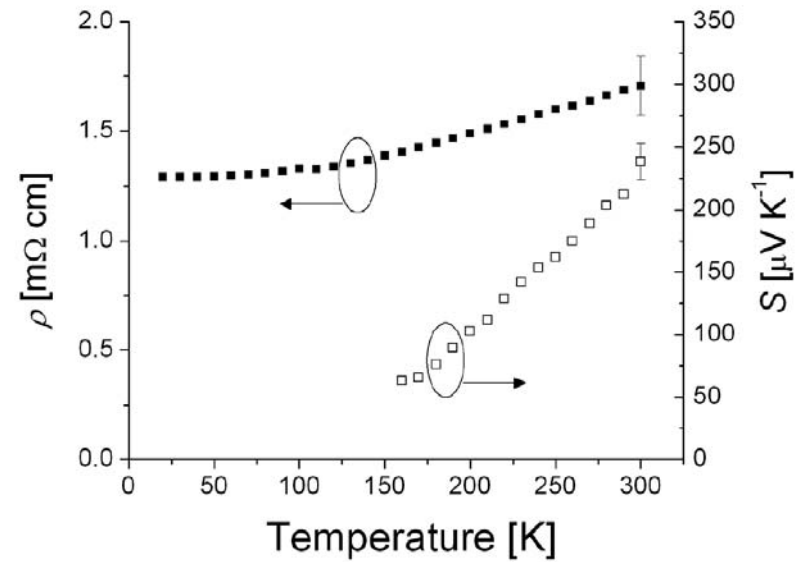


# Electroless Etched Si Nanowires



To appear in Nature (2007)

## Electronic Crystal



# Heat Flow in Solids

$$k = \frac{1}{3} C v l = \frac{1}{3} \int C(\varepsilon) v(\varepsilon)^2 \tau(\varepsilon) D(\varepsilon) d\varepsilon$$

We do not understand the wave effects in phonon transport and we don't have simple experimental tools to perform phonon spectroscopy.

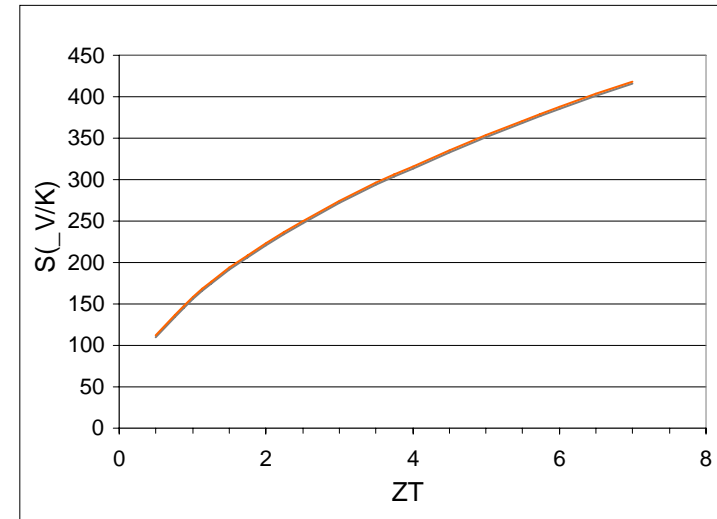
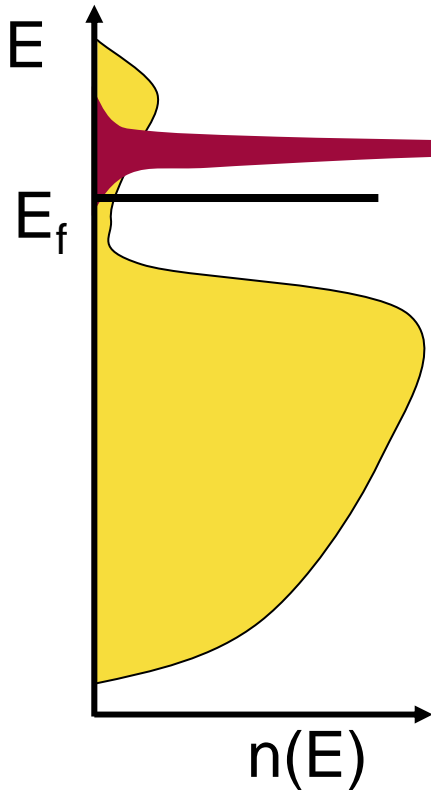
We need help from theory!

# Best Thermoelectric

$\delta$ -function/Lorentzian

YbAl<sub>3</sub> has highest  $S^2\sigma$  due to f-electron resonance state

$$ZT = \frac{S^2 \sigma T}{k} = S^2 \left( \frac{\sigma T}{k} \right) = \frac{S^2}{L_0} \approx 40 [S(mV)]^2$$



*Proc. Natl. Acad. Sci. USA*  
Vol. 93, pp. 7436–7439, July 1996  
Applied Physical Sciences

*This contribution is part of a special series of Inaugural Articles by members of the National Academy of Sciences elected on April 25, 1995.*

## The best thermoelectric

G. D. MAHAN\*† AND J. O. SOFO‡

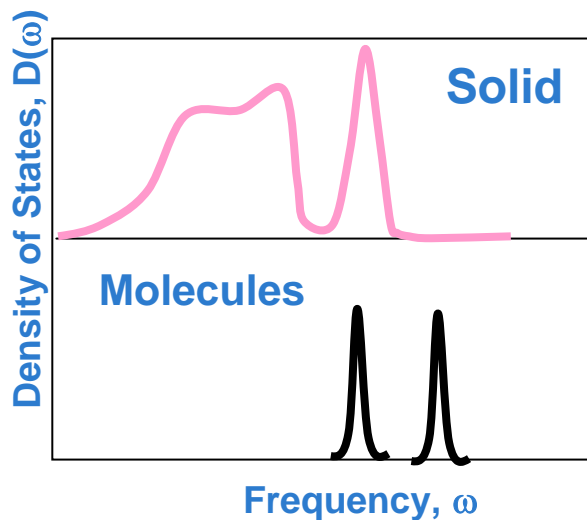
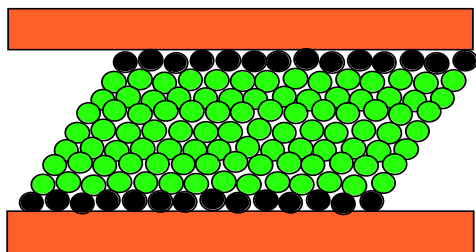
\*Department of Physics and Astronomy, The University of Tennessee, Knoxville, TN 37996-1200; †Solid State Division, Oak Ridge National Laboratory, P.O. Box 2008, Oak Ridge, TN 37831-6030; and ‡Instituto Balseiro, Centro Atomico Bariloche, (8400) Bariloche, Argentina



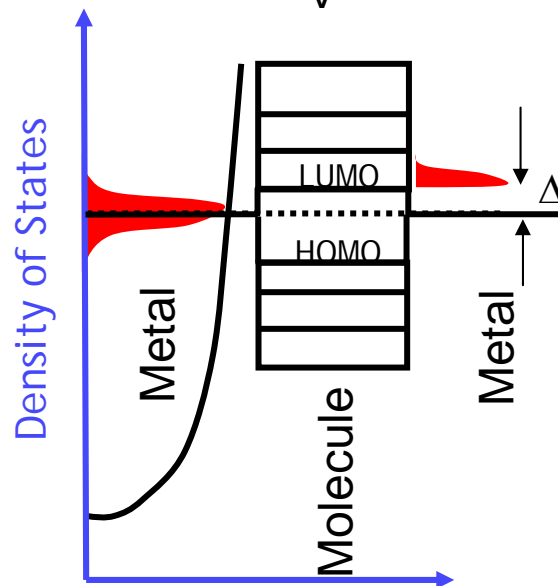
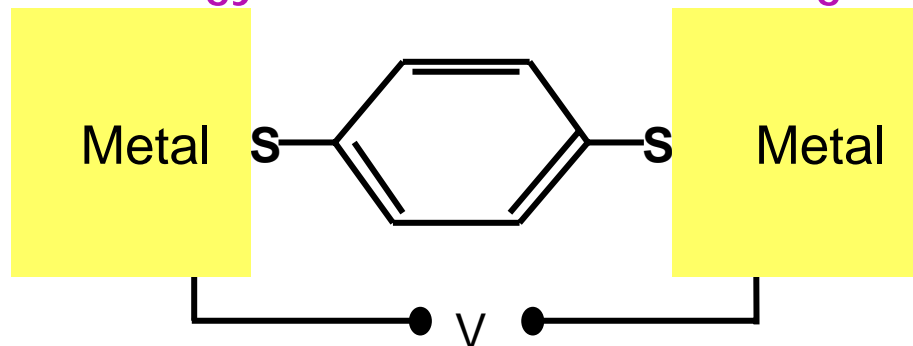
# Why Molecular Thermoelectrics?

Large Thermal Impedance  
By Phonon Filtering

Molecular Heterostructures



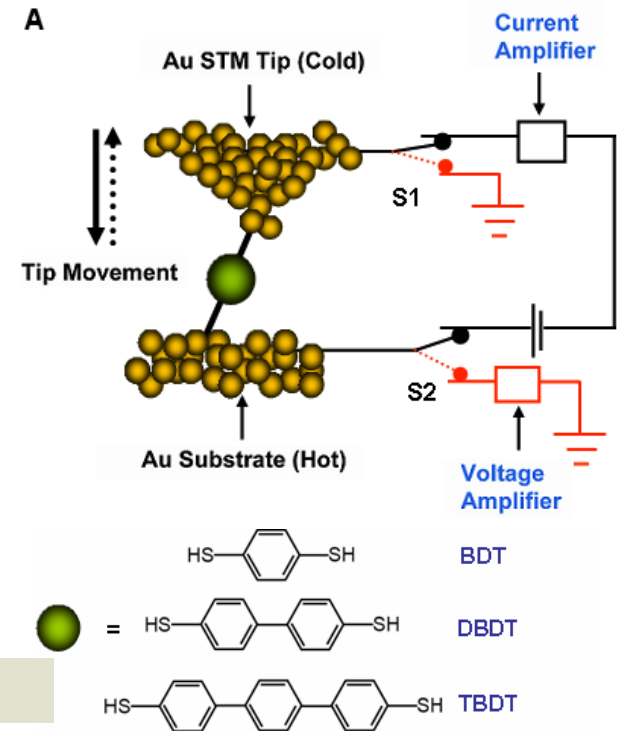
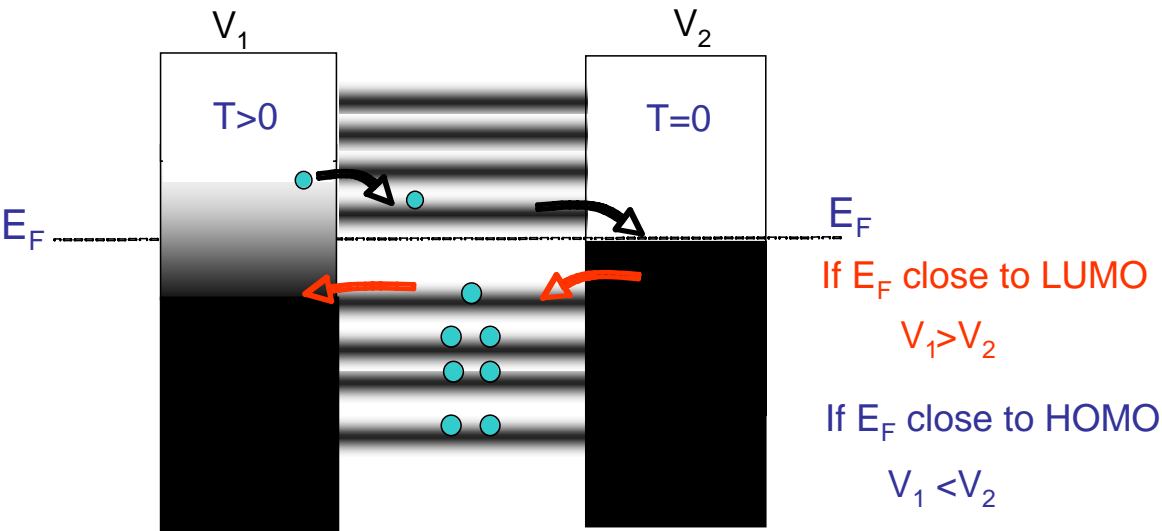
Potentially High Power Factor by  
Energy-Based Carrier Filtering



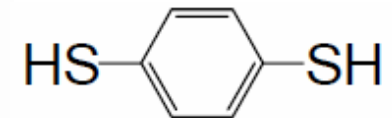
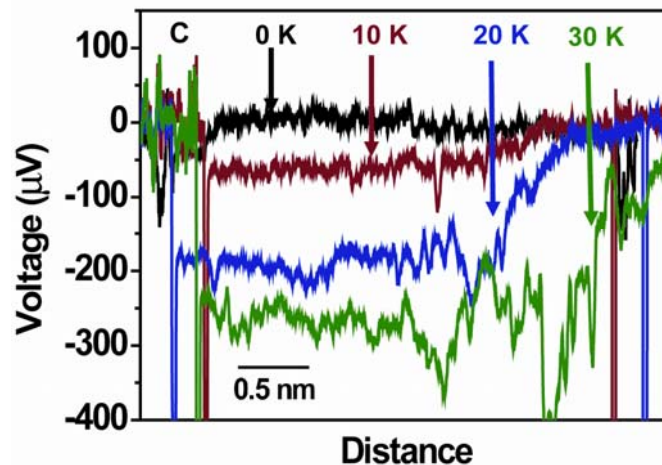
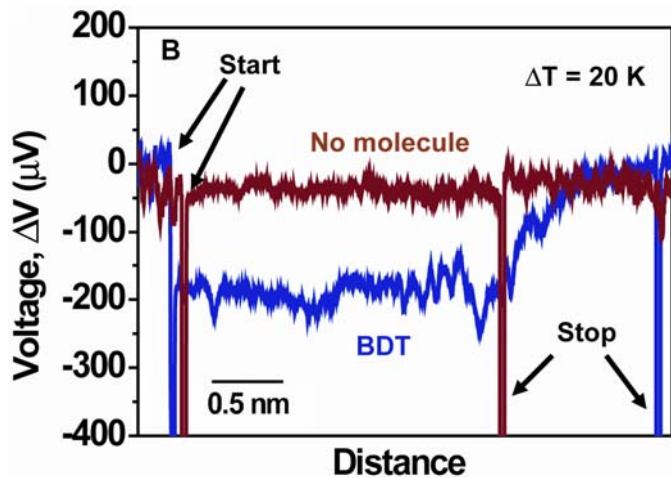
Pramod Reddy, Sung-Yeon Jang, Kaal Baheti,  
Jon Malen, Peter Doak, Don Tilley, Rachel Segalman

Jeff Neaton, Joel Moore

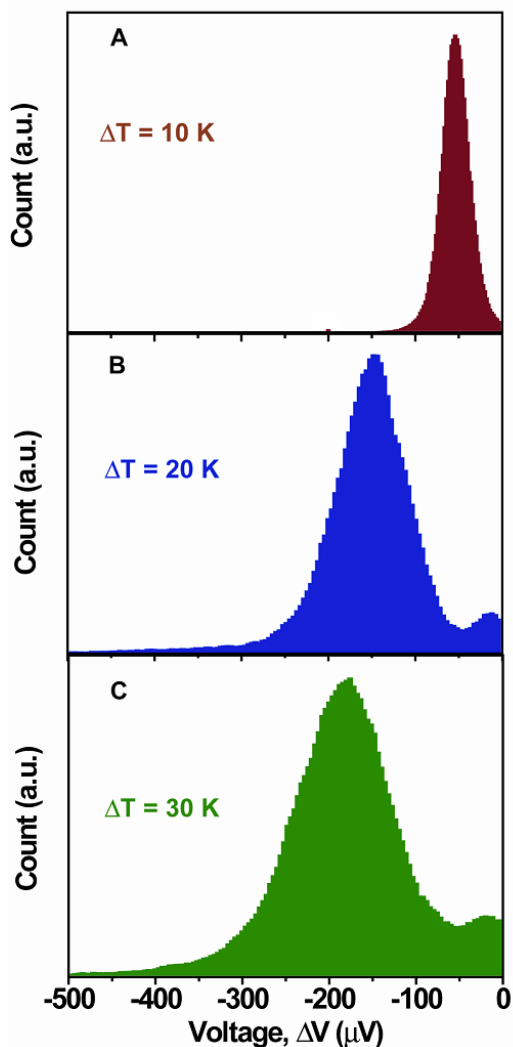
# Thermopower of Molecular Junctions



Reddy, Jang, Segalman, Majumdar, *Science* (2007)

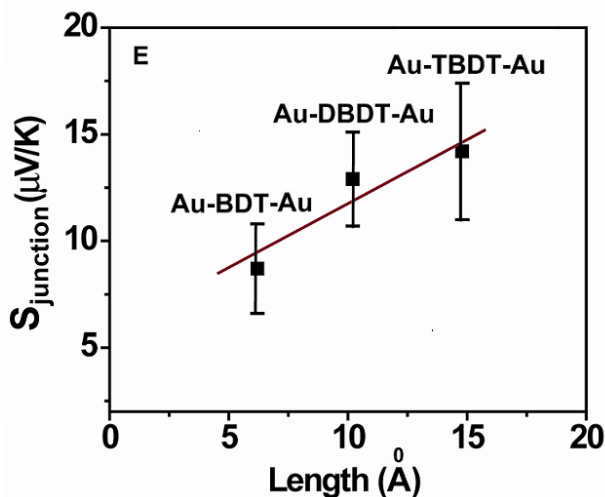
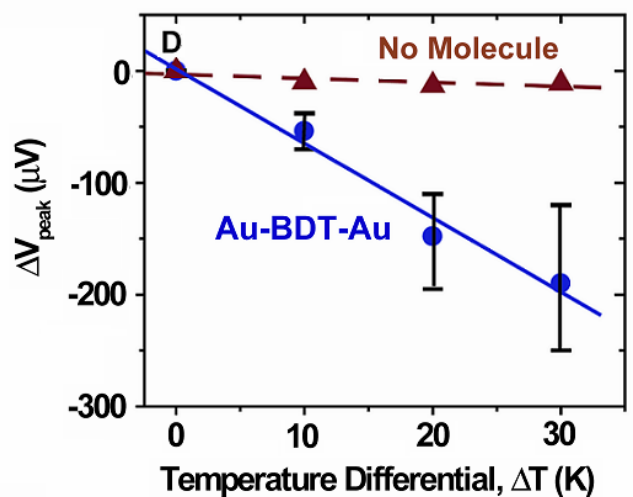


# Thermopower of Molecular Junctions

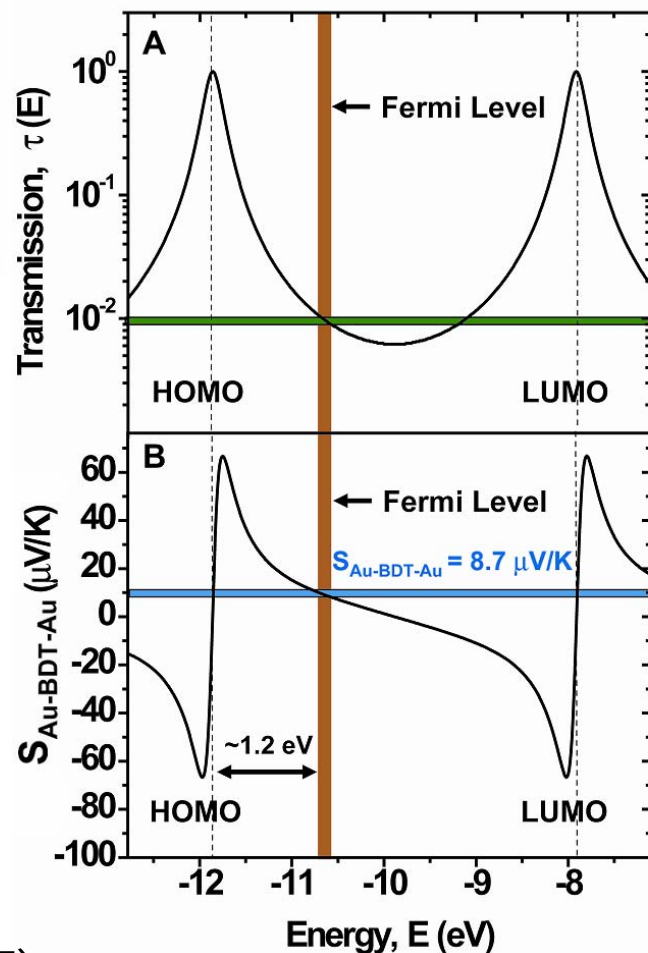


From >2000 consecutive measurements

Reddy, Jang, Segalman, Majumdar, *Science* (2007)

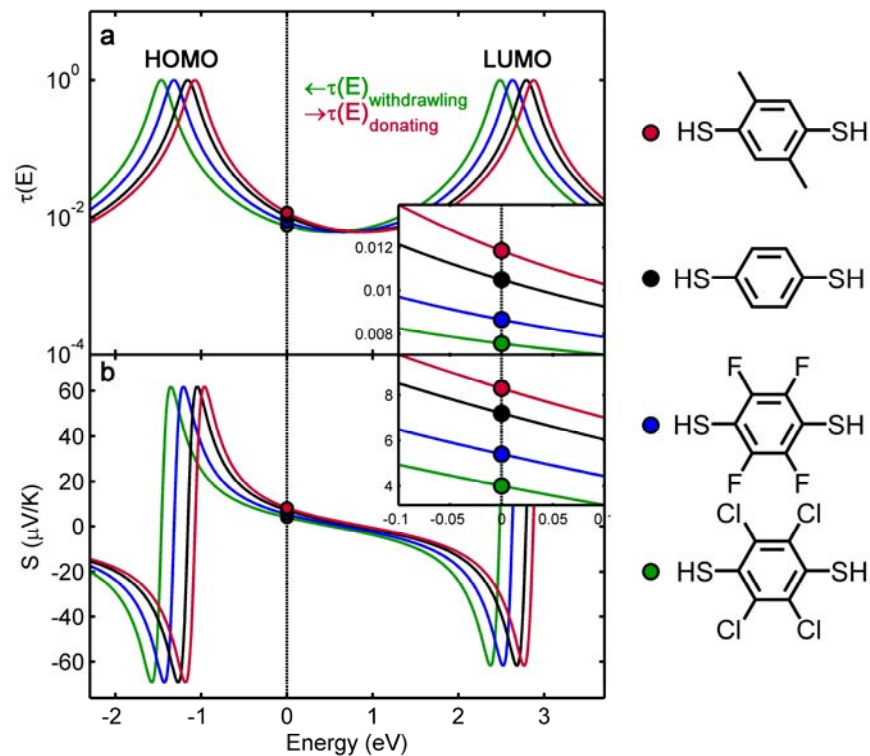
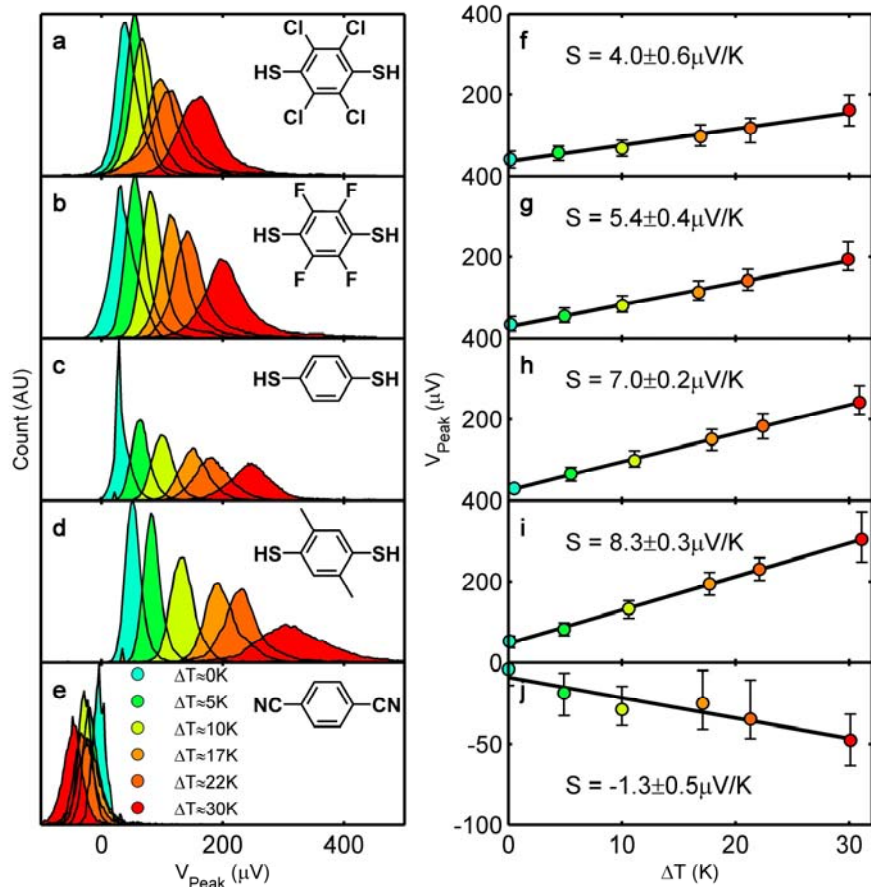


$$S = \frac{V}{\Delta T} = -\frac{\pi^2 \kappa_B^2 T}{3e} \left( \frac{1}{\tau(E)} \frac{\partial \tau(E)}{\partial E} \right)_{E=E_f}$$



Paulsson & Datta, *PRB* (2003)

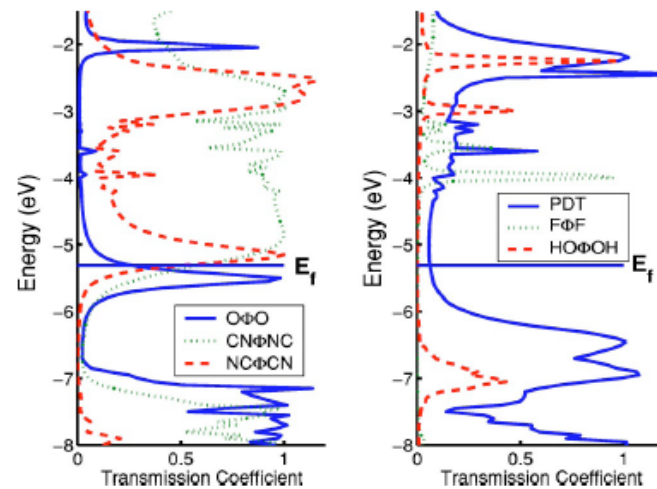
# Role of Chemistry



## Transmission for BDT (PDT) & BDCN (CN $\Phi$ CN) [2]

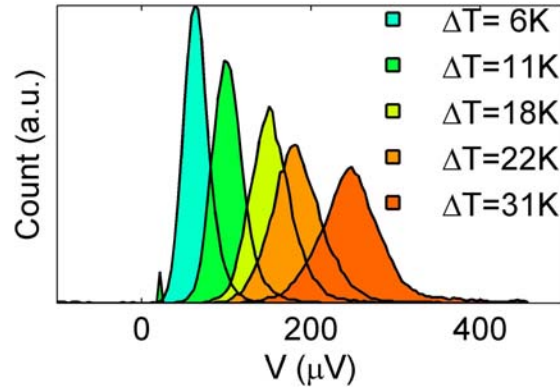
[1] Xue & Ratner PRB (2003)

[2] Xue & Ratner PRB (2004)

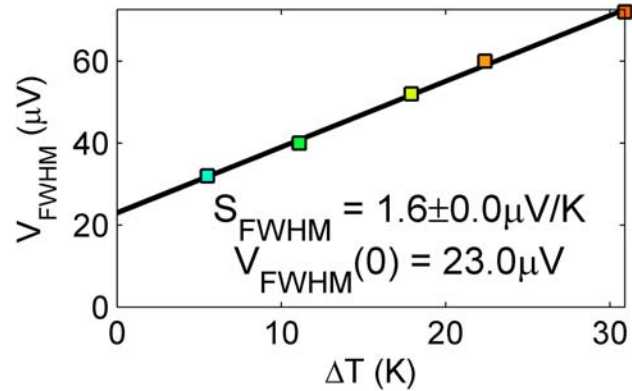


# Role of Fluctuations

Histograms of V for Several  $\Delta T$  for BDT



$V_{\text{FWHM}}$  vs  $\Delta T$  for BDT ( $S_{\text{FWHM}} = \text{slope}$ )



## Lorentzian

$$\tau(E) = \sum_{i=1}^2 \frac{\Gamma_1 \Gamma_2}{(E - E_i)^2 + (\Gamma_1 + \Gamma_2)^2 / 4}$$

$$\frac{\Delta E}{(E_F - E_{\text{HOMO}})} \approx 0.2 - 0.5!!$$

$$\frac{\Delta V_{1-2}}{(T_1 - T_2)} = \frac{\Delta E S_{\text{HOMO}}}{(E_f - E_{\text{HOMO}})}$$

# Transport in Molecular Heterojunctions

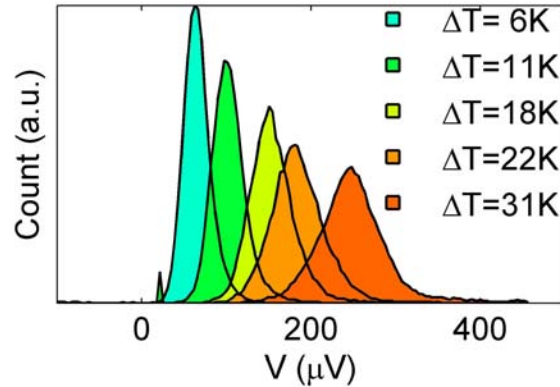
How do we design molecular junctions to obtain a property or combination of properties?

Role of:

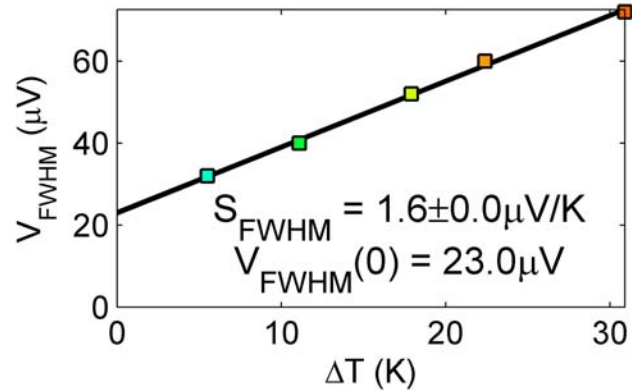
- Contacts
- Chemistry
- Fluctuations

# Role of Fluctuations

Histograms of V for Several  $\Delta T$  for BDT



$V_{FWHM}$  vs  $\Delta T$  for BDT ( $S_{FWHM}$  = slope)



## Lorentzian

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$$\frac{\Delta E}{(E_F - E_{HOMO})} \approx 0.2 - 0.5!!$$

$$\frac{\Delta V_{1-2}}{(T_1 - T_2)} = \frac{\Delta E S_{HOMO}}{(E_f - E_{HOMO})}$$

# Discussion