## **Physics of Nanoscale Transistors: Lecture 5:**

# Application to State-of-the-Art MOSFETS

## Changwook Jeong and Mark Lundstrom

Network for Computational Nanotechnology
Purdue University
West Lafayette, Indiana USA





#### outline

#### 1) Objectives

- 2) Measured I-V characteristics
- 3) Treatment of series resistance
- 4) Linear region analysis
- 5) Saturated region analysis
- 6) Comparison to ballistic limit
- 7) Discussion
- 8) Summary



## objectives

- To compare measured, device performance metrics to the values expected from ballistic theory.
- 2) To discuss and interpret the results.
- 3) To identify experimental uncertainties in extracting and interpreting parameters.

(Thanks to Shuji Ikeda of ATDF for supplying these devices in Dec. 2007)



#### outline

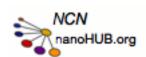
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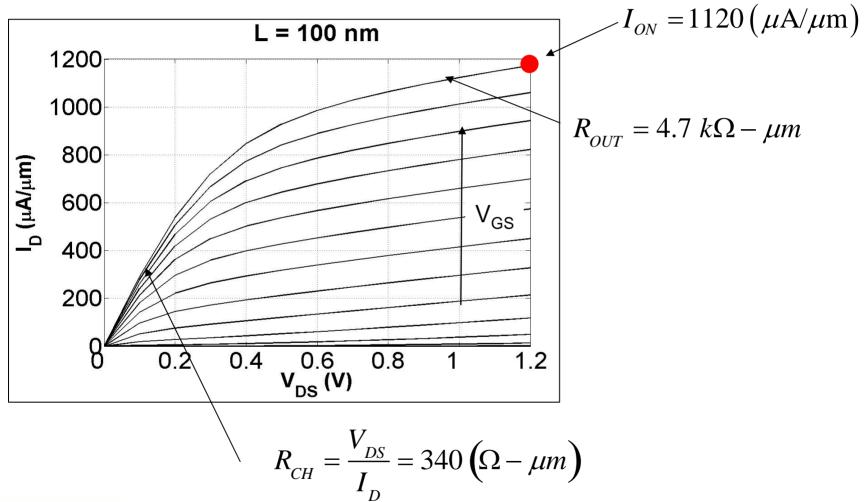
## technology parameters

- 1) Nitrided gate oxide (k = 5,  $t_{inv} = 2.2$  nm)
- 2) Polysilicon gate
- 3)  $V_{DD} = 1.2V$
- 4) Not intentionally strained
- 5) All measurements at  $T \sim 300$ K
- 6) Minimum mask channel length = 100 nm Minimum physical channel length (SEM) = 85 nm

(Thanks to Shuji Ikeda of ATDF for supplying these devices in Dec. 2007)

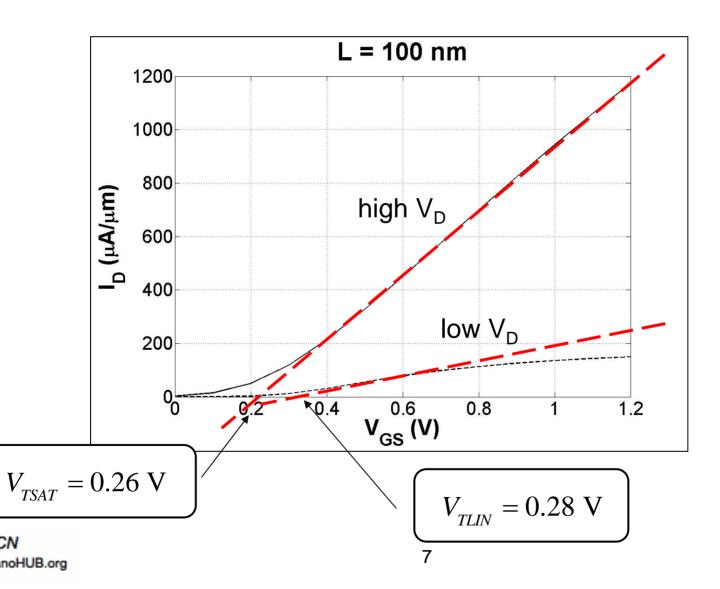


## NMOS common source characteristics



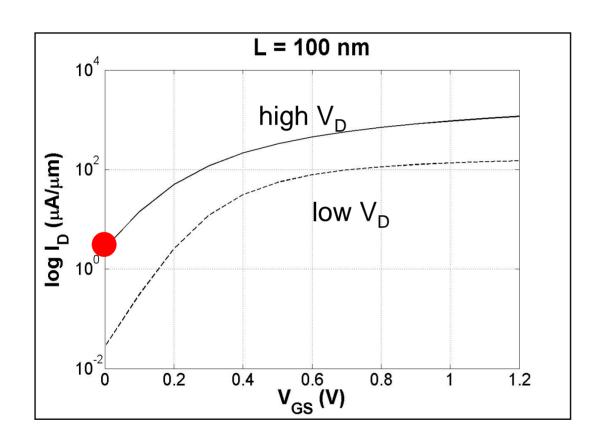


#### Transfer characteristics



NCN

# $Log_{10} I_D vs. V_{GS}$



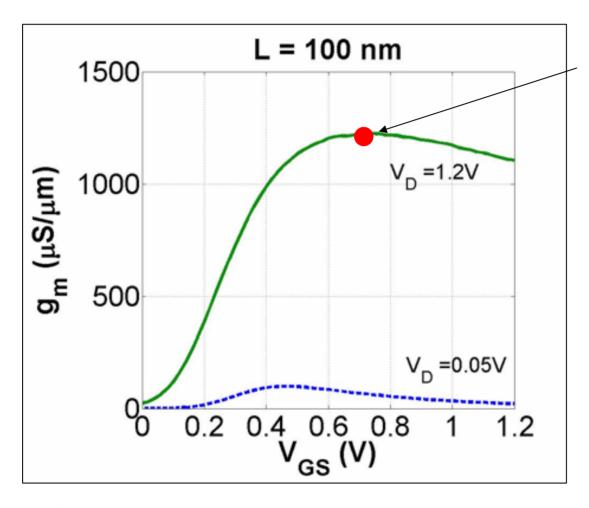
$$I_{OFF} = 0.95 (\mu \text{A}/\mu \text{m})$$
  
 $S = 110 (\text{mV/dec})$ 

$$S = 110 (\,\mathrm{mV/dec})$$

$$DIBL = 170 (mV/V)$$



### Transconductance



$$\ddot{\mathfrak{g}}_{m} = 1225 \left( \mu S / \mu m \right)$$

$$g_m \equiv \frac{\partial I_{DS}}{\partial V_{GS}}\bigg|_{V_{DS}}$$



## summary

parameter	value (extr.)
$V_{TSAT}\left( V ight)$	0.26
$V_{\scriptscriptstyle TLIN}\left(V ight)$	0.28
$I_{\mathit{ON}}\left(\mu\mathrm{A}/\mu\mathrm{m}\right)$	1120
$I_{OFF}\left(\mu\mathrm{A}/\mu\mathrm{m}\right)$	0.95
S(mV/dec)	110
DIBL(mV/V)	170
$R_{CH}\left(\Omega-\mu m\right)$	340
$R_{\scriptscriptstyle OUT}\left(\Omega-\mu m ight)$	4700
$g_{mMAX}(\mu S/\mu m)$	1225



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#### series resistance

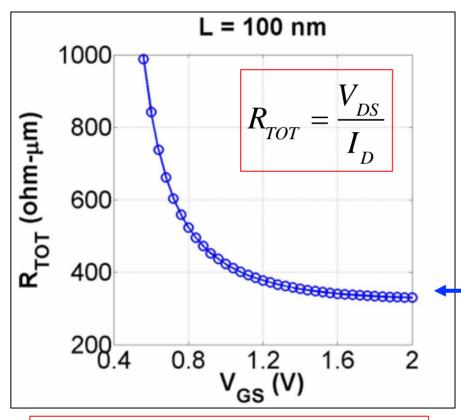
To analyze the device, we want to compare the **intrinsic device** to a hypothetical ballistic device. To do so, we must measure the series resistance so that we can deembed the intrinsic device.

There are many techniques to deduce the series resistance from measured IV data but it is **very difficult** for modern, short channel MOSFETs because of the underlying assumptions of these techniques are no longer well-satisfied.

Our analysis of the measured results will be limited by our uncertain knowledge of the value of the series resistance.



#### series resistance



$$R_{TOT} = R_{CH} \left( V_{GS} \right) + R_{BALL} \left( V_{GS} \right) + R_{SD}$$

From shift and ratio measurement:

$$R_{SD} \approx 100 \Omega - \mu m$$

$$R_{TOT} = R_{CH} + R_{BALL} + R_{SD}$$
$$= 320\Omega - \mu m$$

From BSIM simulator:

$$R_{SD} = 200 \Omega - \mu m$$



#### series resistance bounds

$$R_{BALL}\left(V_{GS} = 2 \text{ V}\right)W = \frac{\left(2k_BT/q\right)}{Q_I(0)\upsilon_T} \frac{\mathcal{F}_0\left(\eta_{F1}\right)}{\mathcal{F}_{-1/2}\left(\eta_{F1}\right)} \approx 40 \Omega - \mu m$$

For high  $V_G$ , we find that the ballistic channel resistance is approximately constant, and for Si parameters (100), single subband,  $m^* = 0.19$ , its value is about 40  $\Omega$ - $\mu$ m.

$$R_{CH}|_{V_{CS}=2} \cong R_{BALL} + R_{CH} + R_{SD} = 320 \rightarrow R_{SD} \le 280 \left(\Omega - \mu m\right)$$

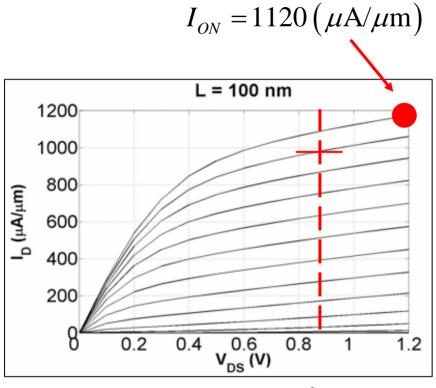
BSIM: 
$$R'_{SD} = 200 \rightarrow R_{SD} \approx 140 \left(\Omega - \mu m\right)$$

Given the approximations involved, we will assume:



$$R_{SD} = 200 \pm 50 \left(\Omega - \mu m\right)$$

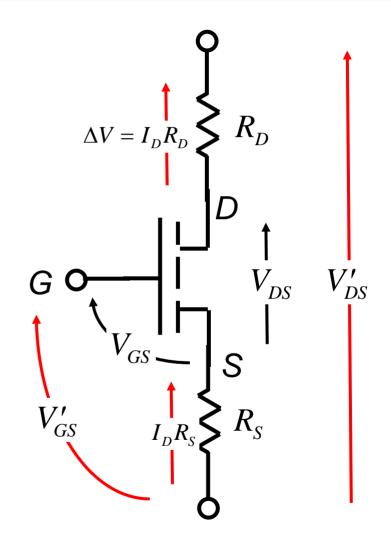
## Series resistance has a significant effect



$$\Delta V = 100 \times 1120 \times 10^{-6} = 0.11V$$

$$V_{DS} = 1.2 - 0.22 = 0.88V$$

$$V_{GS} = 1.2 - 0.11 = 1.09V$$



$$R_{\rm S} = R_{\rm D} \approx 100 \,\Omega - \mu m$$

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## channel resistance analysis ( $V_{GS} = 1.2V$ )

$$R_{CH} \left( V_{GS} \right) = R_{TOT} \left( V_{GS} \right) - R_{BAL} \left( V_{GS} \right) - R_{SD}$$

$$R_{SD} = 200 \pm 50 \left( \Omega - \mu m \right)$$

$$R_{CH} \left( V_{GS} = 1.2 \text{ V} \right) = 140 \pm 50 \left( \Omega - \mu m \right)$$

- 1) What is the inversion layer charge in the linear region?
- 2) What is the mobility?



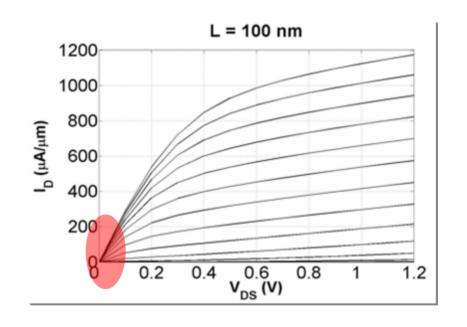
## inversion layer charge

$$Q_I(0) = C_{ox} \left( V_{GS} - V_T \right)$$

$$C_{ox} = \frac{\mathcal{E}_{ox}}{T_{inv}} = 1.544 \times 10^{-6} \text{ F/cm}^2$$

$$V_{GS} = V_{GS}' - I_D R_S \approx V_{GS}'$$

$$V_{T} = V_{T}(\text{lin}) = 0.28 \text{ V}$$



 $Q_I(0)/q$ ;  $8.9 \times 10^{12} \text{ cm}^{-2}$ 



How accurate is this estimate? (Will discuss in Sec. 7.)

## measuring mobility

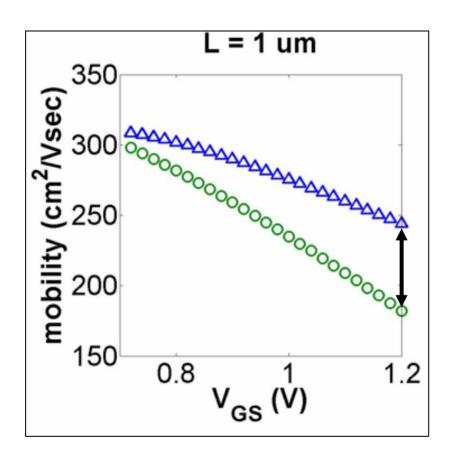
#### Two methods:

i) 
$$\mu_{eff} = \frac{L_{mask}}{W_{mask} \left(R_{TOT} - R_{BALL} - R_{SD}\right) C_{ox} (V_{GS} - V_T)}$$
 (Sensitive to  $R_{SD}$  and to the ballistic resistance.)

$$ii) \qquad \mu_{eff} = \frac{1}{W_{mask} \left( \partial R_{TOT} / \partial L_{mask} \right) C_{ox} (V_{GS} - V_T)}$$



## measured mobility



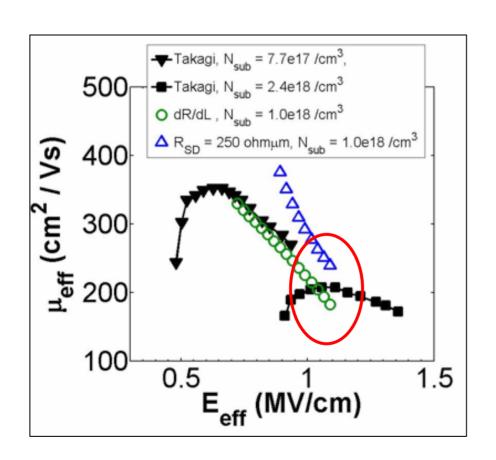
$$\mu_{eff} = \frac{L_{mask}}{W_{mask} \left( R_{TOT} - R_{SD} \right) C_{ox} (V_{GS} - V_T)}$$

$$\mu_{eff} = \frac{1}{W_{mask} \left( \partial R_{TOT} / \partial L_{mask} \right) C_{ox} (V_{GS} - V_T)}$$

Are these results consistent with the expected universal mobility curve?



## universal mobility



$$E_{eff} = \frac{q(N_{dep} + 0.5 \cdot N_{inv})}{\varepsilon_{si}}$$

where

$$qN_{inv} = \int_{0}^{V_{GS}} C_{GC} dV_{GS}$$

$$qN_{dep} = \sqrt{4q\varepsilon_{si}\Phi_{B}N_{sub}}$$

$$\Phi_{B} = (k_{B}T/q)\ln(N_{sub}/n_{i})$$

(Takagi et al, *IEEE TED* **41**, 2357-2362,1994)



## mobility and mean-free-path

The mobility inferred from measurements on a long channel transistor:

$$188 < \mu_{eff} < 248 \left( \text{cm}^2/\text{V-s} \right)$$

is consistent with the expected, universal mobility.

What mfp do we deduce from the mobility?

From Lecture 4:

$$\mu_n = \frac{\upsilon_T \lambda_0}{2 k_B T / q} \left[ \frac{\mathcal{F}_{-1/2} (\eta_{F1})}{\mathcal{F}_0 (\eta_{F1})} \right] \longrightarrow 15 < \lambda_0 < 19 \text{ nm}$$



# Linear region summary ( $V_{GS} = 1.2V$ )

1) Series resistance is a significant part of the total channel resistance.

$$R_{TOT} = 340 \left(\Omega - \mu m\right) R_{SD} \approx 200 \pm 50 \left(\Omega - \mu m\right)$$

$$R_{CH}$$
 (L=100 nm,  $V_{GS} = 2 \text{ V}$ )  $\approx 140 \pm 50 (\Omega - \mu m)$ 

2) The mobility inferred from the measurements is consistent with the expected, universal mobility.

$$188 < \mu_{eff} < 248 \left( \text{cm}^2/\text{V-s} \right)$$

3) The measured mobility implies a mfp of:



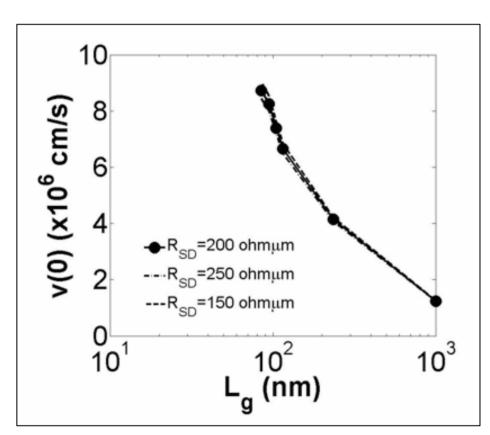
$$15 < \lambda_0 < 19 \text{ nm}$$

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## velocity at the beginning of the channel



## Under high drain bias = 1.2V

$$\langle \upsilon(0) \rangle = \frac{I_{ON}}{WQ_I(0)}$$

$$Q(0)/q \approx 7.9 \times 10^{12} \text{ cm}^{-2}$$

$$\langle \upsilon(0) \rangle = 8.7 \times 10^6 \,\text{cm/sec}$$
 at 100nm

$$\pm 25\%$$
 variation in  $R_{SD} \rightarrow \pm 4\%$  variation in  $\langle \upsilon(0) \rangle$ 



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# channel resistance analysis ( $V_{GS} = 1.2V$ )

$$R_{CH} = 140 \pm 50 \left(\Omega - \mu m\right)$$

- How significant is the ballistic resistance?
- 2) What is the transmission?
- 3) How does the mobility compare to the ballistic mobility?
- 4) How many modes conduct?



#### ballistic resistance

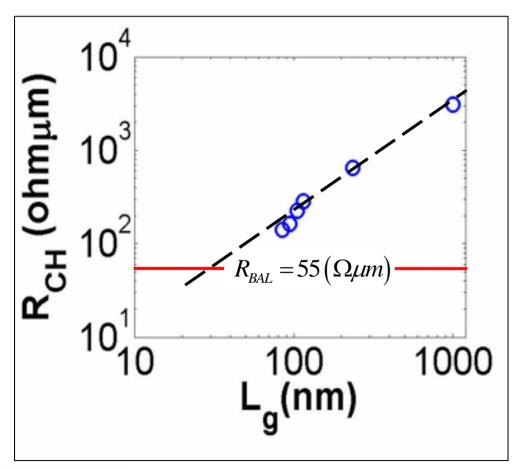
1) How significant is the ballistic resistance at  $V_{GS} = 1.2$ V?

$$R_{BALL}W = \frac{\left(2k_BT/q\right)}{Q_I(0)\upsilon_T} \frac{\mathcal{F}_0\left(\eta_{F1}\right)}{\mathcal{F}_{-1/2}\left(\eta_{F1}\right)} \approx 55\Omega - \mu m$$

$$R_{CH}$$
 (meas) = 140 ± 50  $\left(\Omega - \mu m\right) \approx 2 - 4 \times R_{CH}$  (ball)



# L<sub>g</sub> dependence of R<sub>ch</sub>

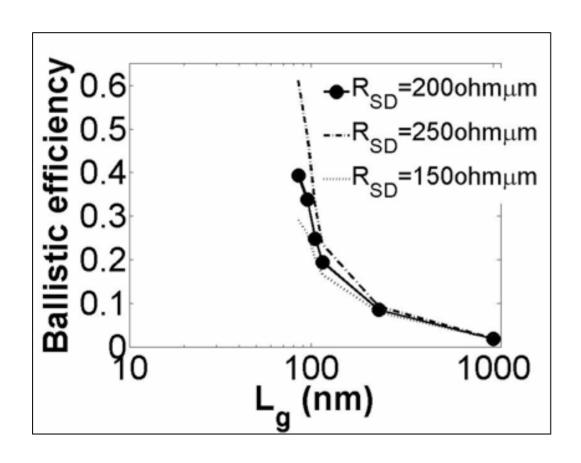


As L continues to decrease,  $R_{CH}$  will saturate at the ballistic resistance.

Because of the higher mobilities, this may be seen in III-V FETs before it is seen in Si MOSFETs.



## transmission vs. channel length

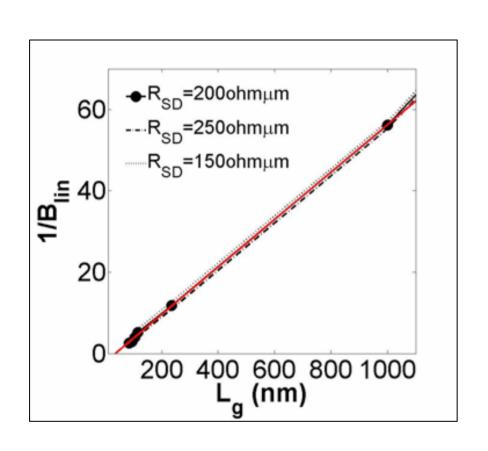


$$B_{lin} = \frac{I_{Dlin}(\text{meas})}{I_{Dlin}(\text{ball})} = T$$

$$0.3 < T_{lin} (100 \text{ nm}) < 0.6$$



## mfp from T vs. channel length



$$B_{lin} = T_{lin} = \frac{\lambda_0}{\lambda_0 + L}$$

$$\frac{1}{B_{lin}} = 1 + \frac{L}{\lambda_0}$$



$$\lambda_0 = 17nm$$

 $\lambda_0 = 17nm$ Independent of  $R_{SD}$ 

$$T_{lin} \approx \frac{\lambda_0}{\lambda_0 + L} = \frac{17}{17 + 85} = 0.17$$



## transmission recap

We can deduce *T* in the linear region three different ways:

1) From the linear region current:

$$T = I_{Dlin} \text{(meas)}/I_{Dlin} \text{(ball)} \rightarrow 0.3 < T < 0.6$$

2) From the mfp deduced from the mobilty:

$$T = \lambda_0 / (\lambda_0 + L)$$
 15 <  $\lambda_0$  < 19 nm  $\rightarrow 0.15 < T < 0.19$ 

3) From the mfp deduced from  $1/B_{lin}$  vs. L:

$$T = \lambda_0 / (\lambda_0 + L)$$
  $\lambda_0 \approx 17$  nm  $\rightarrow T \approx 0.17$ 



## channel resistance analysis

$$R_{CH} \left( V_{GS} = 1.2 \text{ V}, L = 100 \text{ nm} \right) = 140 \pm 50 \left( \Omega - \mu m \right)$$

- How significant is the ballistic resistance?
- 2) What is the transmission?
- 3) How does the mobility compare to the ballistic mobility?
- 4) How many modes conduct?



## mobility and ballistic mobility

The mobility inferred from measurements on a long channel transistor:

$$188 < \mu_{eff} < 248 \left( \text{cm}^2/\text{V-s} \right)$$

is consistent with the expected, universal mobility.

How does this compare to the ballistic mobility? From Lecture 4:

$$\mu_{B} = \frac{\upsilon_{T} L}{2 k_{B} T / q} \left[ \frac{\mathcal{F}_{-1/2} (\eta_{F1})}{\mathcal{F}_{0} (\eta_{F1})} \right]$$

for 
$$Q_I(0) = 8.9 \times 10^{12} \,\text{cm}^{-2}$$

for 
$$Q_I(0) = 8.9 \times 10^{12} \text{ cm}^{-2}$$
  $\mu_B \approx 3370 \text{ cm}^2/\text{V-s} >> \mu_{eff}$ 



# number of conducting channels at $V_{GS} = 1.2V$

$$G_{CH} = \frac{1}{R_{CH}} = \left[WQ_I(0)\frac{\upsilon_T}{\left(2k_BT/q\right)}\right] \left[\frac{\mathcal{F}_{-1/2}(\eta_{F1})}{\mathcal{F}_0(\eta_{F1})}\right] \equiv M_{eff} \frac{2q^2}{h}$$

$$M_{eff} = \frac{h}{2q^2} \left( \frac{WQ_I(0)\upsilon_T}{2k_B T/q} \right) \left[ \frac{\mathcal{F}_{-1/2}(\eta_{F1})}{\mathcal{F}_0(\eta_{F1})} \right]$$

For  $V_{GS} = 1.2V$ :

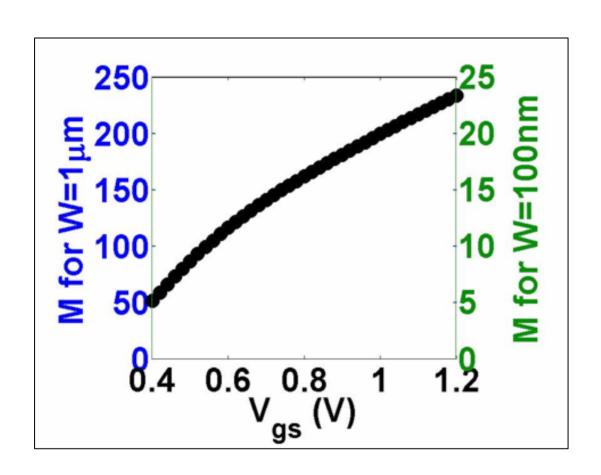
$$Q_{I}(0) = 8.9 \times 10^{12} \,\text{cm}^{-2}$$

$$\left[ \mathcal{F}_{-1/2}(\eta_{F1}) / \mathcal{F}_{0}(\eta_{F1}) \right] = 0.54$$

$$M_{eff} = 230 / \mu \text{m}$$



## number of conducting channels



Near threshold, a narrow width MOSFET has only a few conducting channels



# linear region summary ( $V_{GS} = 1.2V$ )

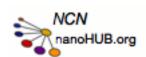
1) For this L = 85nm device, the ballistic mobility is much greater than the actual mobility:

$$\mu_{BALL} \approx 3370 \left( \text{cm}^2/\text{V-s} \right) >> \mu_{eff} \approx 248 \left( \text{cm}^2/\text{V-s} \right)$$

2) Because of the uncertainties in series resistance and mobility, it is best to deduce T from a plot of  $1/B_{lin}$  vs. L:

$$T(100 \text{ nm}) \approx 0.17$$

3) **But**, there are also uncertainties in interpretation (e.g. assumption that a single subband is occupied, parabolic bands, etc.)



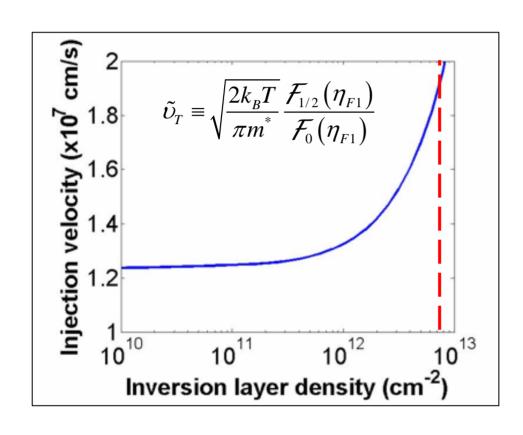
## saturation region analysis ( $V_{GS} = 1.2V$ )

At low 
$$V_{DS}$$
:  $T(100 \text{ nm}) \approx 0.17$ 

What is T at high  $V_{DS}$ ?



### ballistic injection velocity



Since we know inversion layer density, we can just read off the ballistic injection velocity.

$$Q(0)/q \simeq 7.9 \times 10^{12} \text{ cm}^{-2}$$

$$\langle \tilde{\nu}_T \rangle = 1.9 \times 10^7 \text{ cm/sec}$$

Since we know actual velocity,

$$\langle \upsilon(0) \rangle = 8.7 \times 10^6 \,\text{cm/sec}$$
 at 100nm

we can estimate the ballistic ratio:

$$B_{sat} = \frac{I_{ON}}{I_{ON} \text{(ball)}} = \frac{\langle \upsilon(0) \rangle}{\vartheta_T^{\prime}}$$



## Ballistic ratio in saturation (L = 100nm)

$$\langle \tilde{\nu}_T \rangle = 1.9 \times 10^7 \, \text{cm/sec}$$

$$\langle \upsilon(0) \rangle = 8.7 \times 10^6 \,\text{cm/sec}$$
 at 100nm

$$B_{sat} = \frac{\left\langle \upsilon(0) \right\rangle}{\tilde{\upsilon}_T} \approx 0.45$$

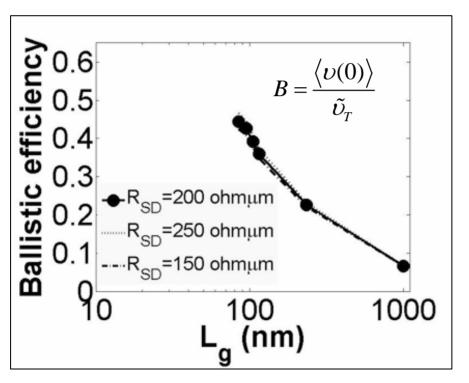
$$B_{sat} = \frac{T}{2 - T} \rightarrow T = 0.62$$

The L = 100nm transistor operates at about 45% of ballistic limit.

In saturation,  $T \sim 0.62$ 



### ballistic ratio in saturation vs. channel length

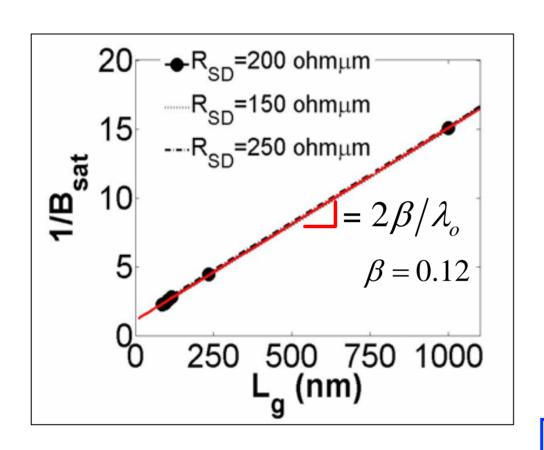


Under high drain bias = 1.2V

$$\begin{array}{c} \pm 25\% \ R_{SD} \\ \hline \\ \pm 4.7\% \ \left\langle \upsilon(0) \right\rangle \end{array}$$



### critical length analysis



$$B_{sat} = \frac{T}{2 - T} = \frac{\lambda_0}{\lambda_0 + 2I}$$

$$I = \beta L$$

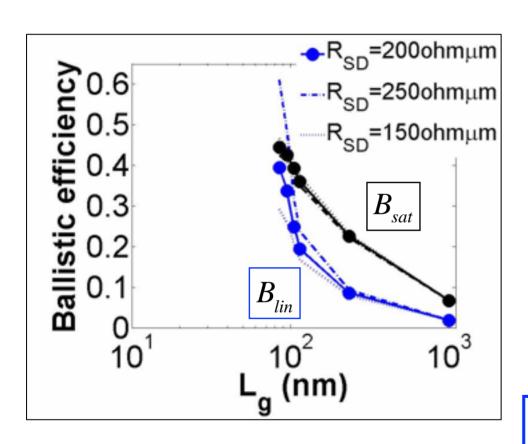
$$\frac{1}{B_{sat}} = 1 + \frac{2I}{\lambda_0} = 1 + \frac{2\beta}{\lambda_0} L$$

$$I = 0.12 \times L$$

The existence of a short, critical region of the channel is confirmed.



### channel length scaling: linear vs. saturation



$$B_{lin} = \frac{\lambda_o}{L + \lambda_o}$$

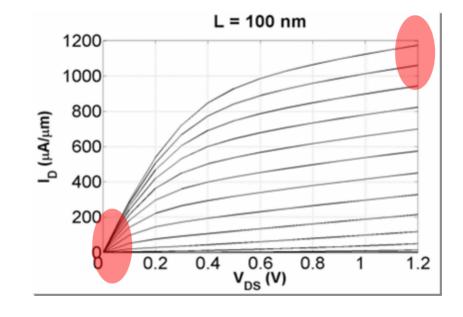
$$B_{sat} = \frac{\lambda_o}{\lambda_o + 2I} = \frac{\lambda_o}{\lambda_o + 2\beta L}$$

where  $\beta \sim 0.12$ 

 $B_{lin}$  drops off faster with increasing channel length than does  $B_{sat}$ .



### comparison to ballistic limit summary



$$T \approx 0.62$$

$$I = 0.12 \times L$$

 $T \approx 0.17$ 

 $\lambda_0 \approx 17 \text{ nm}$ 

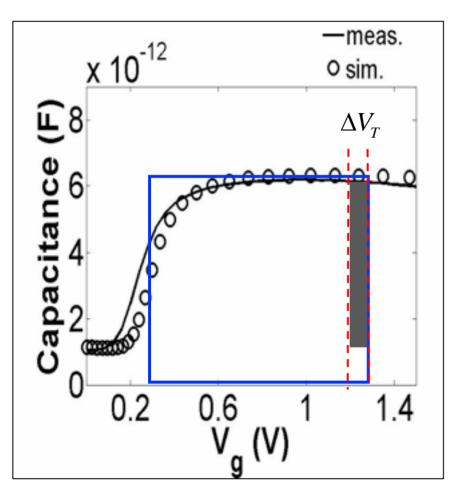


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# how accurate is $Q_I(0) = C_{ox}(V_{GS} - V_T)$ ?



$$Q(0) = \int_{0}^{V_{GS\_short}} C_{GC} / \left( L_{long} \times W_{long} \right) dV_{GS}$$

$$V_{GS\_short} = V_{GS\_long} + \Delta V_T (DIBL + SCE) - I_{ON} R_S$$

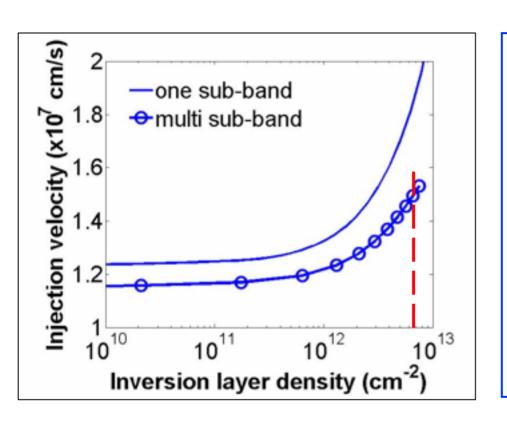
$$Q(0) = C_{ox} \left( V_{GS\_short} - V_T \right)$$

1.25 × 'exact'  

$$Q(0)/q$$
; 7.9 × 10<sup>12</sup> cm<sup>-2</sup>  $\Rightarrow$   
= 6.3 × 10<sup>12</sup> cm<sup>-2</sup>



### how good is the single sub-band approximation?



$$Q(0)/q = 6.3 \times 10^{12} \text{ cm}^{-3}$$

$$\theta_T$$
 = 1.9 × 10<sup>7</sup> cm/sec (single subband)

$$\theta_T = 1.5 \times 10^7 \,\text{cm/sec}$$
 (multi subband)



### implications

1)  $Q_I = C_{ox} (V_{GS} - V_T)$  over-estimates the inversion charge by ~25%

$$\langle \upsilon(0) \rangle = \frac{I_{ON}}{WQ_{I}(0)}$$
 8.7 × 10<sup>6</sup>  $\rightarrow$  1.1 × 10<sup>7</sup> cm/s

2) Single subband assumption over-estimates the ballistic injection velocity by ~27%

$$B_{sat} = \frac{\langle \upsilon(0) \rangle}{\delta_T^{\prime o}} = 0.45 \rightarrow 0.73$$
  $T = 0.62 \rightarrow T = 0.85$ 



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### linear region analysis

Extraction of *T* in the linear region is difficult because of uncertainties in the series resistance of short channel MOSFETs.

- 1) Improved  $R_{SD}$  measurement techniques would be useful.
- 2) Measurement techniques that eliminate  $R_{SD}$  (e.g. our  $1/B_{lin}$  v.s  $L_{mask}$  approach) are another possibility.



### saturated region analysis

Extraction of T in the **saturated region** is difficult because of uncertainties in the measured, average velocity,  $\langle v(0) \rangle$  and in the ballistic injection velocity,  $\mathscr{S}_{T}$ .

- 1) The inversion layer charge,  $Q_{l}(0)$ , of a short-channel MOSFET is difficult to measure.
- The ballistic injection velocity is affected by quantum confinement, bandstructure, strain, etc.



#### conclusions

- An analysis of modern MOSFET IV characteristics confirm the general features of the scattering model.
- 2) Extraction of precise numbers for transmission, ballistic efficiency, etc. is clouded by uncertainties in series resistance, physical channel length, mobility of short channel MOSFETs, inversion layer charge, etc.
- 3) Nevertheless, it is clear the modern MOSFETs deliver more than half of the ballistic on-current and much less than half of the ballistic linear current and that under high  $V_{DS}$ , a very short 'bottleneck' controls the on-current.

