

ECE 659 Quantum Transport: Atom to Transistor

Lecture 6: Hall Effect

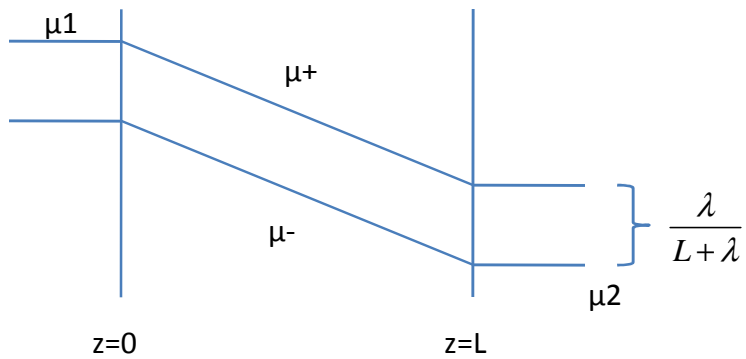
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Spring 2009

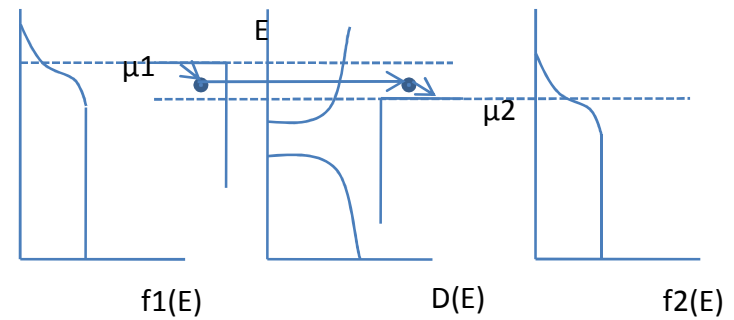
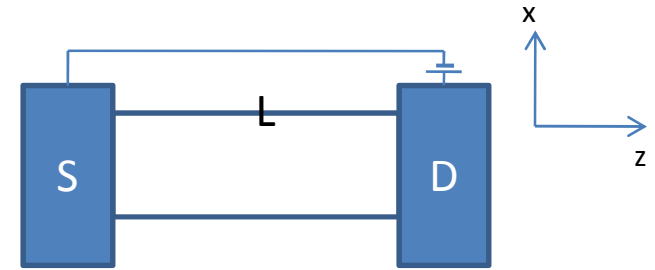
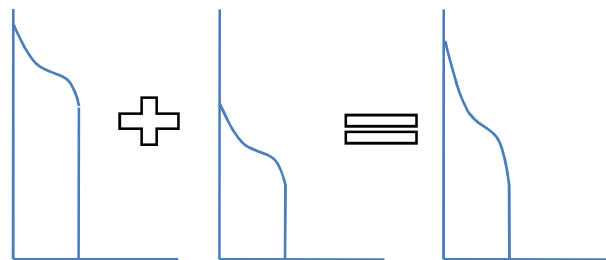
$$G = \sigma \frac{A}{L + \lambda}$$

$$R = \frac{\rho}{A} (L + \lambda)$$

$$I = q \int dE \frac{Dv_z}{2L} (f^+ - f^-)$$

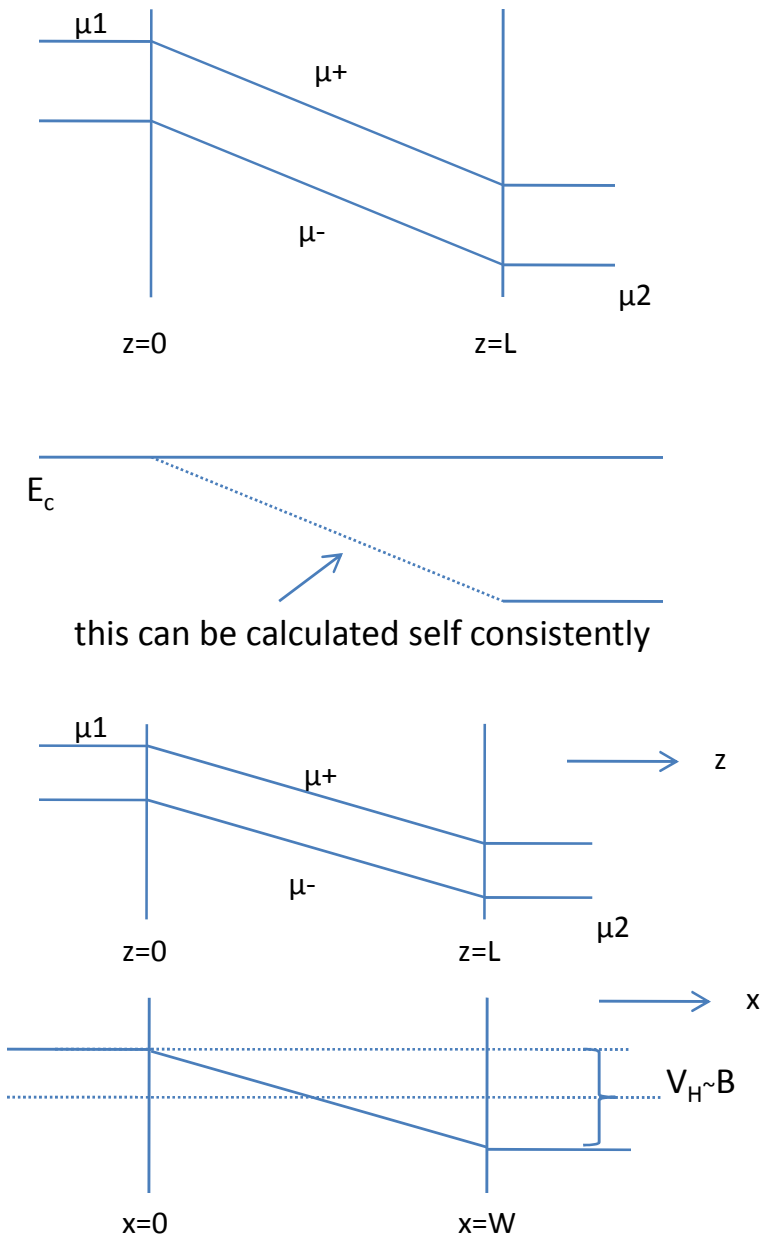


(at large T)



We can do Taylor series expansion of fermi function at large T

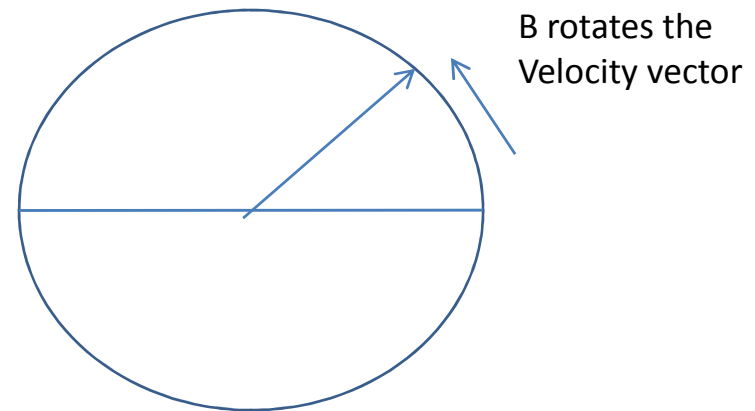
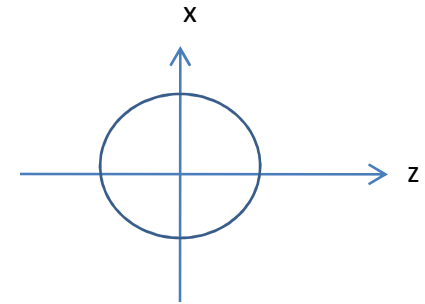
$$(f^+ - f^-) \sim \left(-\frac{df}{dE} \right) (\mu_1 - \mu_2)$$



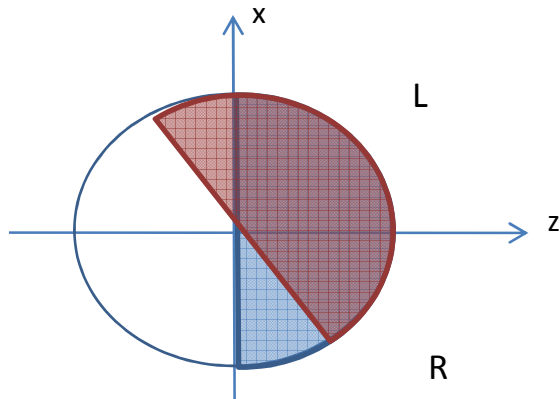
$$\frac{V_H}{I} = \frac{B}{qn}$$

$$\sigma = qn\mu_n$$

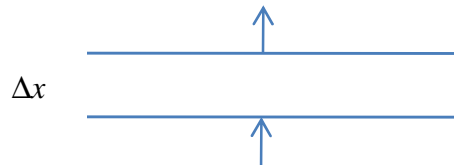
Electron velocity distribution



Cyclotron frequency $\omega_c = \frac{qB}{m}$

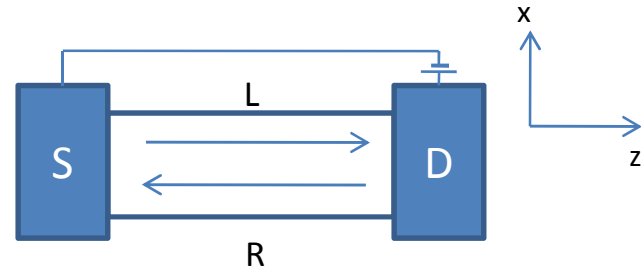


$$\frac{df^L}{dx} = \frac{df^R}{dx} = -\frac{(f^L - f^R)}{\lambda} + () B$$



$$\Delta f_L = \frac{\omega_c}{\pi/2} \left(\frac{\Delta x}{v} \right) f^+$$

$$\frac{\Delta f_L}{\Delta x} = \frac{\omega_c}{\pi/2} \frac{f^+}{v}$$



$$\frac{df_L}{dx} = \frac{df_R}{dx} = \frac{\omega_c}{\pi/2} (f^+ - f^-)$$

$$f_{L,R}(x=0) - f_{L,R}(x=W) = \frac{qBW}{(\pi/2)mv} (f^+ - f^-)$$

$$V_H = \frac{qBW}{(\pi/2)mv} \frac{\mu^+ - \mu^-}{q}$$

$$I = q^2 \frac{Dv_z}{2L} \frac{\mu^+ - \mu^-}{q}$$