

Experiment vs. modelling: what's the problem?

Bill Barnes

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Much of the material discussed here will soon be published as an article by the *Journal of Optics A: Pure and Applied Optics*.

The good

The good

The bad

The good

The bad

The ugly



experimentalist's perspective



The good: experiments (they are real!)

experimentalist's perspective



The good:

experiments (they are real!)

The bad:

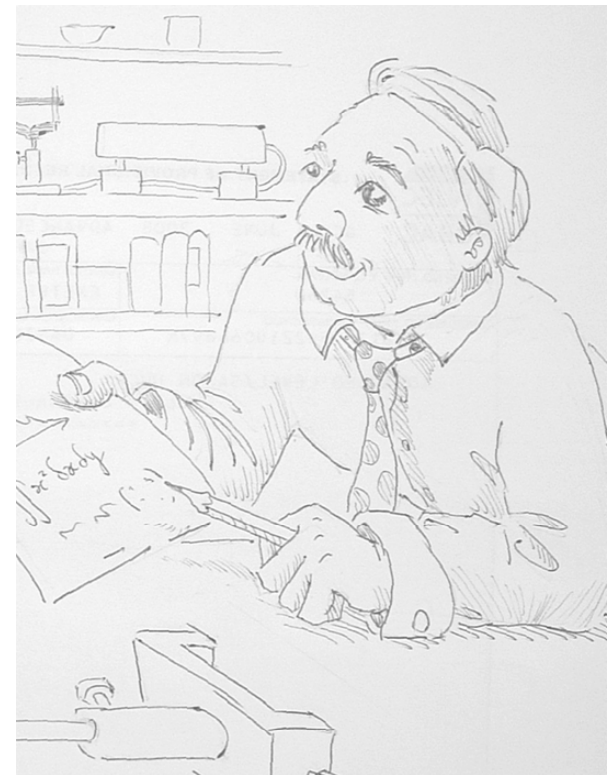
models (never match data)

experimentalist's perspective



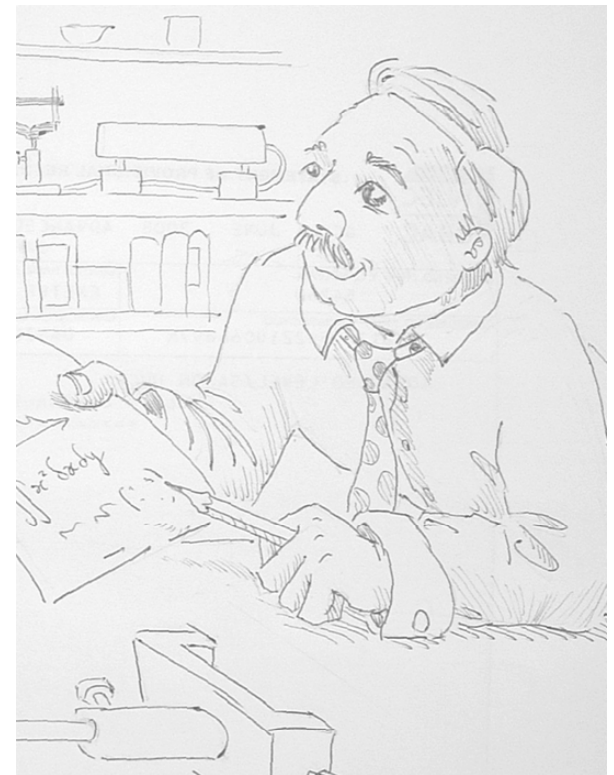
The good: experiments (they are real!)
The bad: models (never match data)
The ugly: theory (incomprehensible)

experimentalist's perspective



theorist's perspective

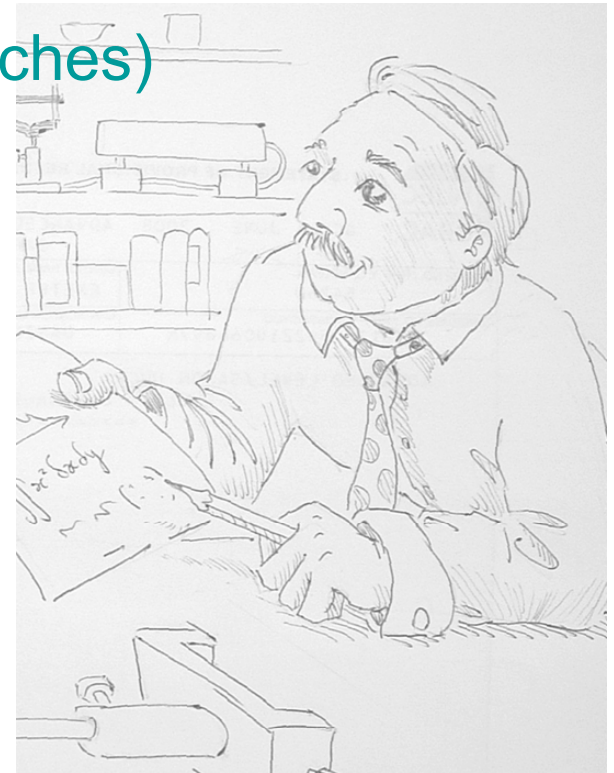
The good: theory (its pure!)



theorist's perspective

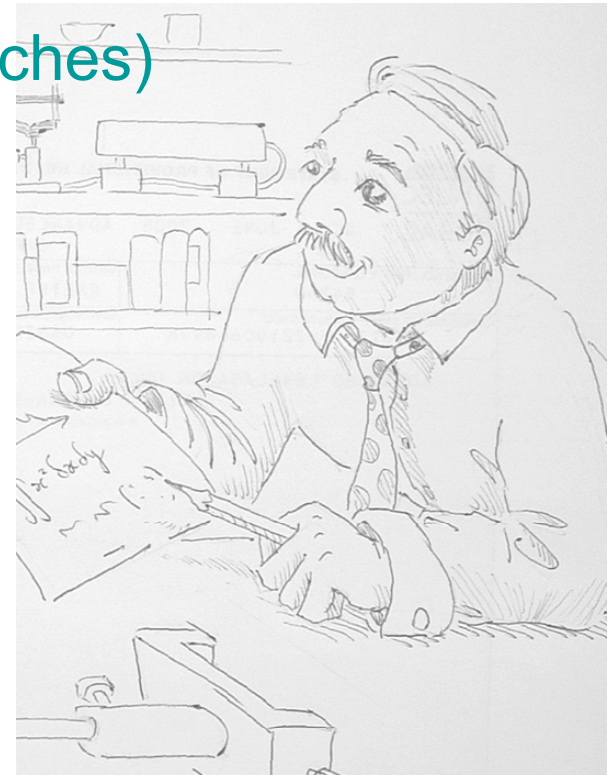
The good: theory (its pure!)

The bad: experiment (never matches)



theorist's perspective

The good: theory (its pure!)
The bad: experiment (never matches)
The ugly: fabrication details..



theorist's perspective

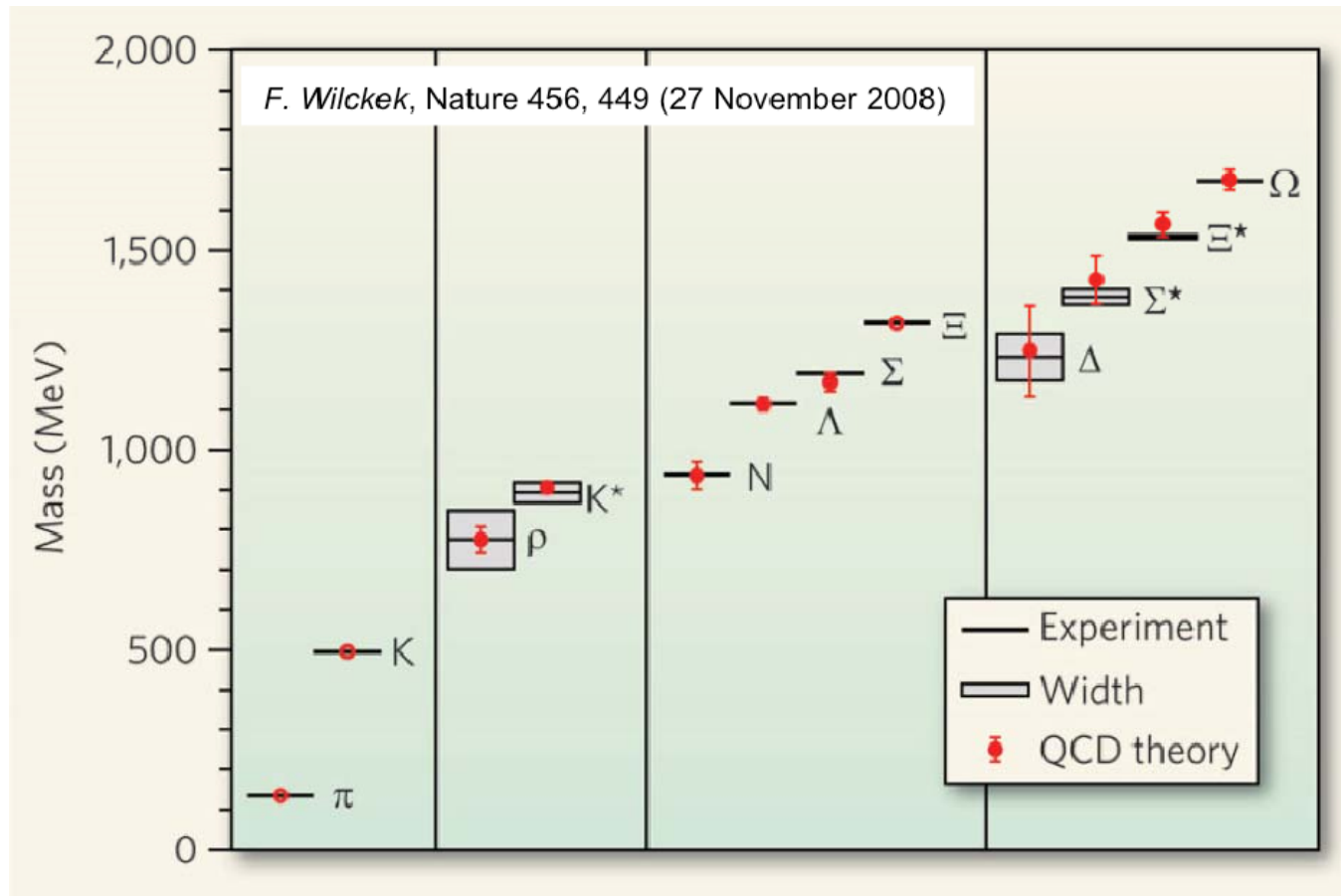
experiment vs. theory

..that looks incomprehensible...

..but its just a simple Green's function...

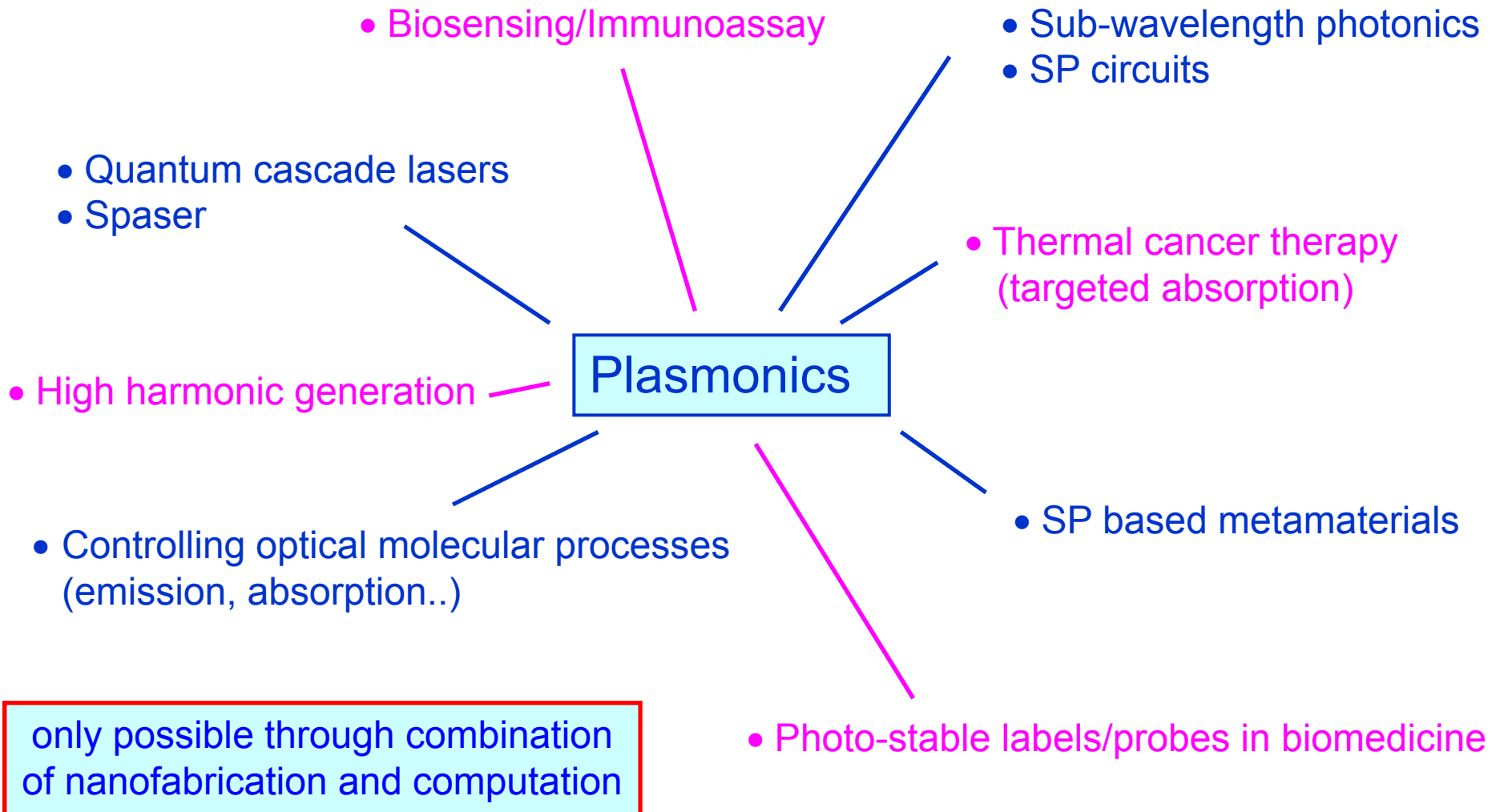


Dürr et al. Science **322** 1224 (Nov 21st 2008)



Science is a mixture of experiment and theory – that's the real beauty

plasmon modes – confinement and control of light in (deep) sub-wavelength regime

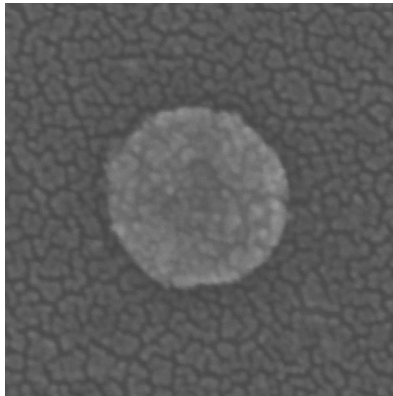


a simple problem



Chris Burrows

Scattering of light by a metallic disc. “I’ll even get rid of the substrate!”



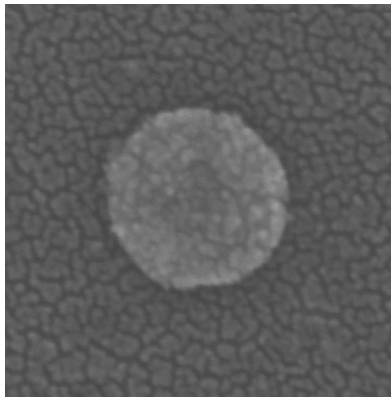
gold disc made by electron-beam lithography
immersed in index matching oil
120 nm dia, 30 nm thick

a simple problem



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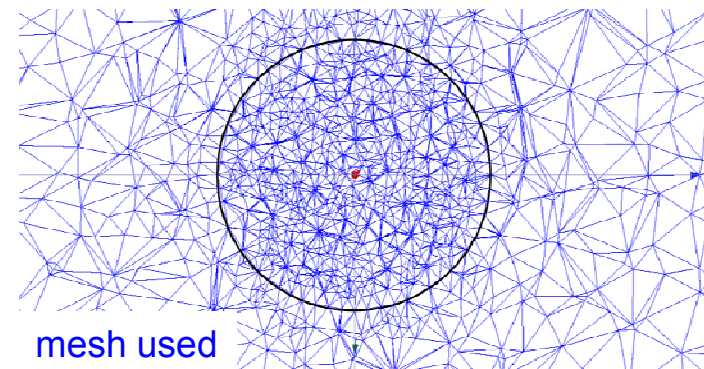
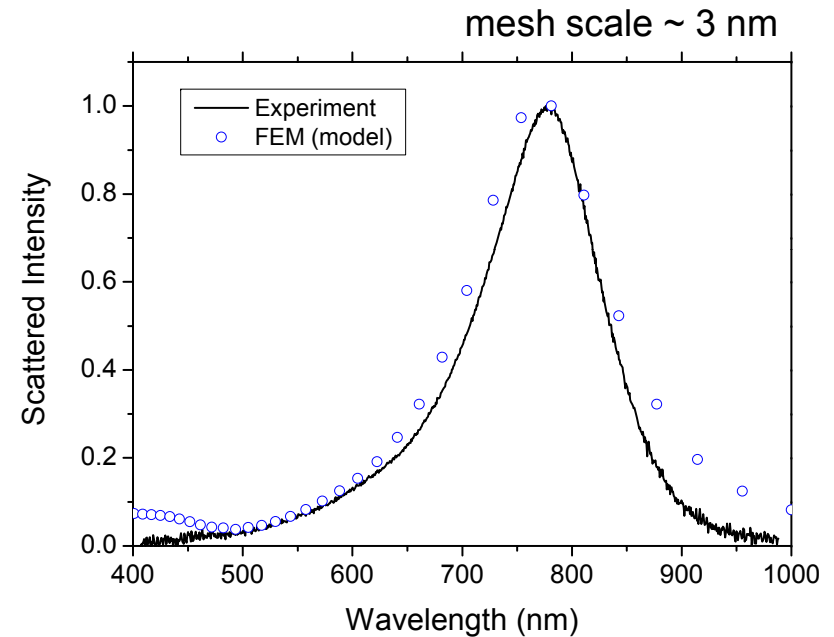
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exact shape? grains? surface contamination?..

....illumination and collection?

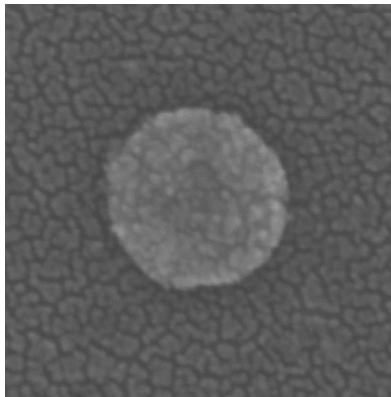


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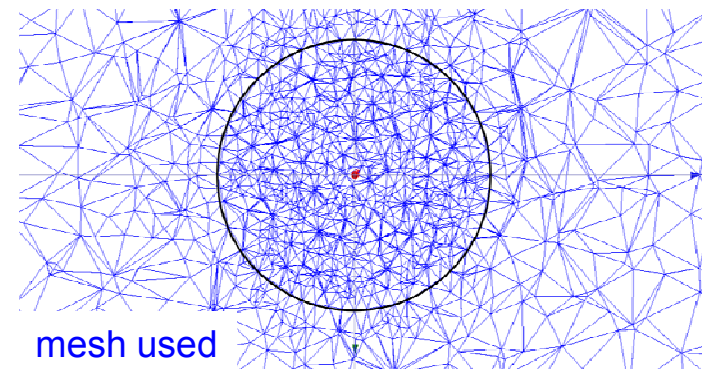
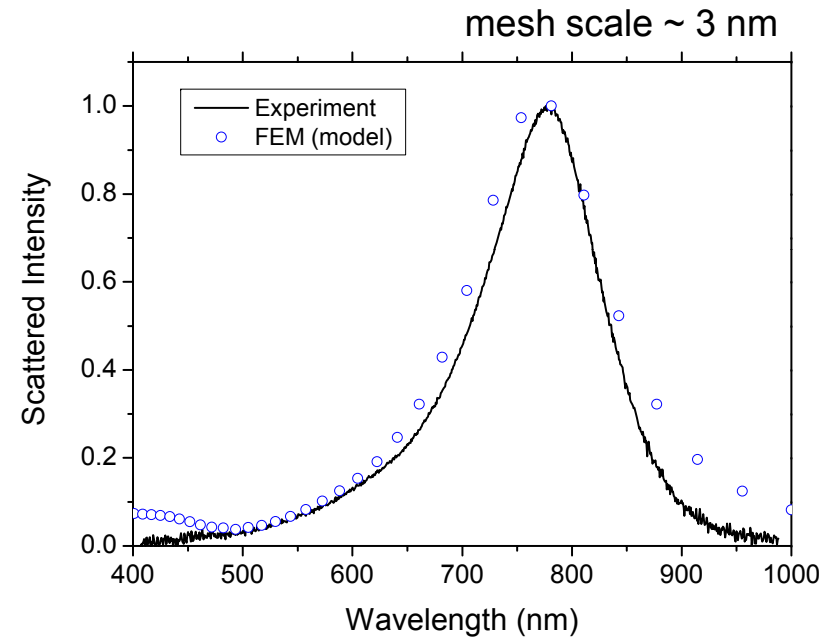
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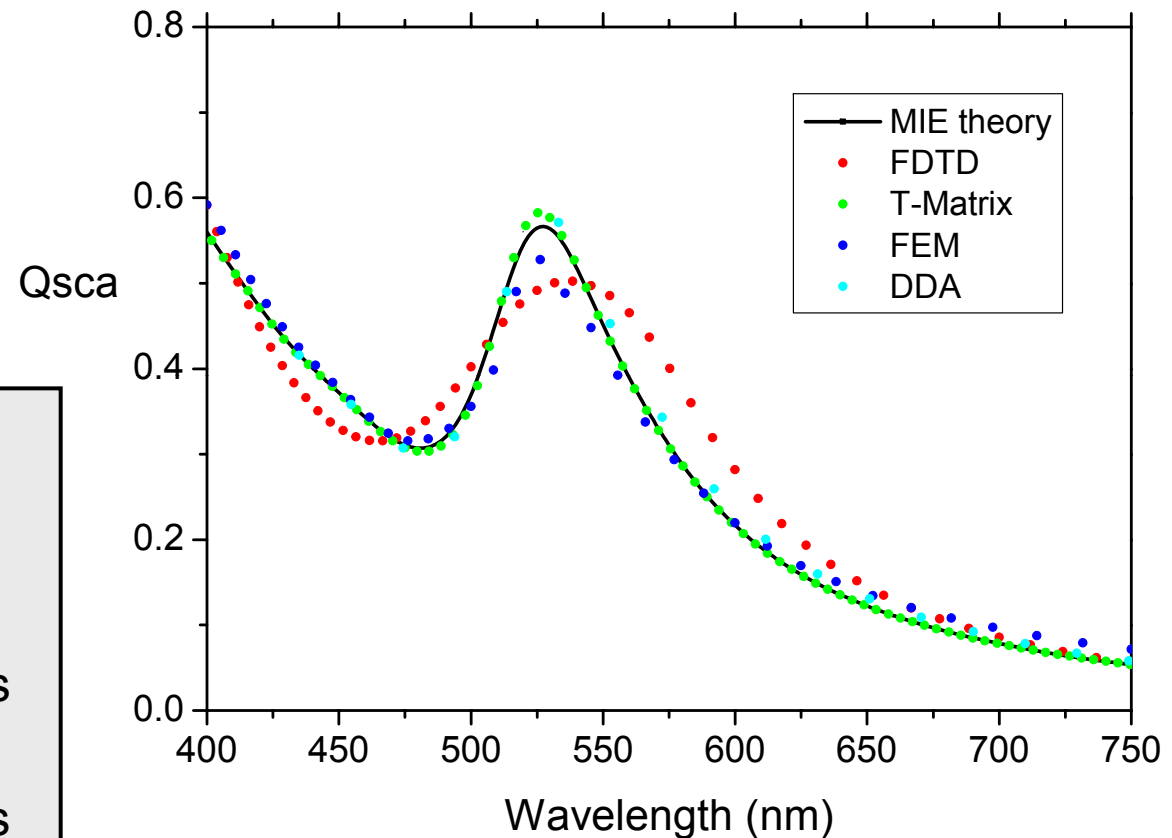


a simple problem

Scattering of light by a metallic sphere: comparison of techniques



James Parsons



80 nm gold sphere in vacuum

approach:	comp time
Mie theory (ϵ :J&C):	1 s
T-matrix (ϵ :J&C):	100 s
DDA: (ϵ :J&C)	1000 s
FDTD (Drude):	10000 s
FEM: (ϵ :J&C)	10000 s

First shot at using different approaches

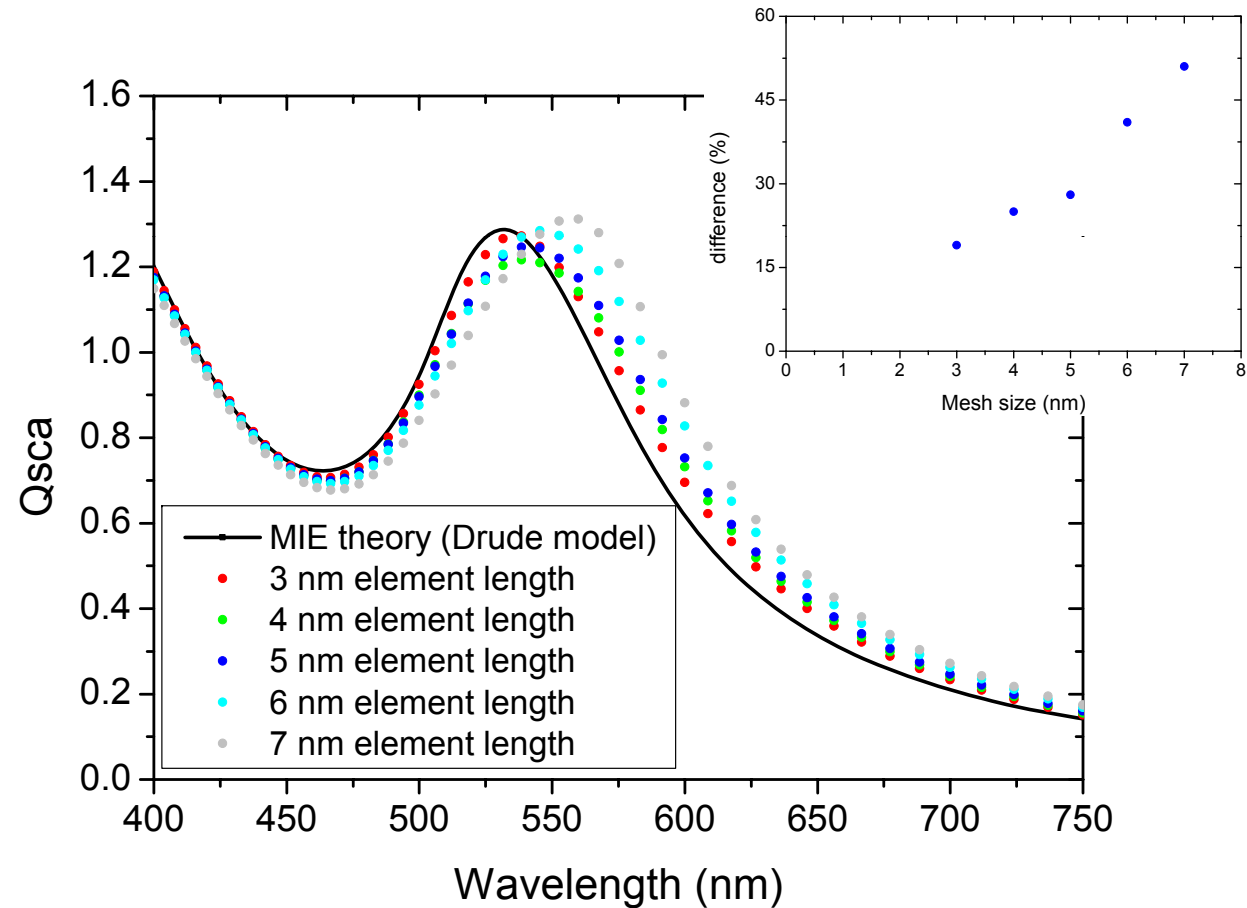
a simple problem



James Parsons

Scattering of light by a metallic sphere in vacuum: comparison of techniques

FDTD approach – effect of mesh size



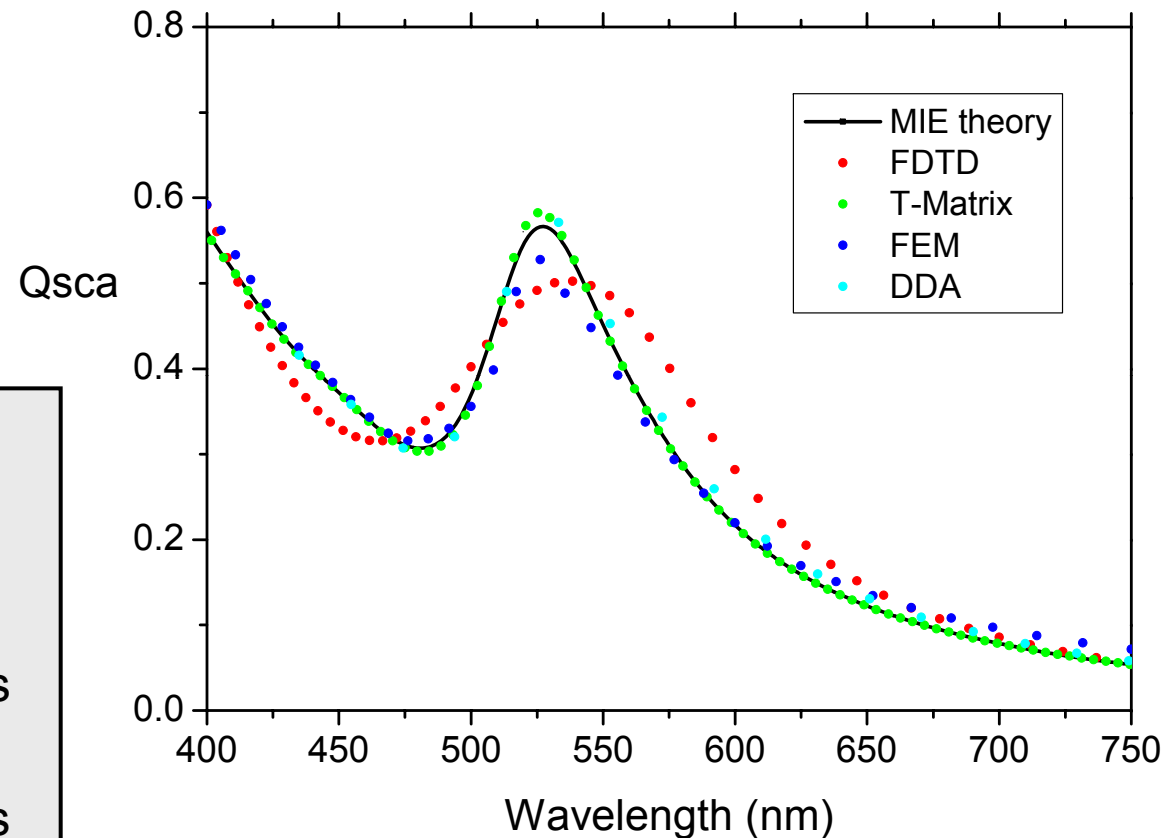
meshing needed at 1 nm level (\ll wavelength)

a simple problem

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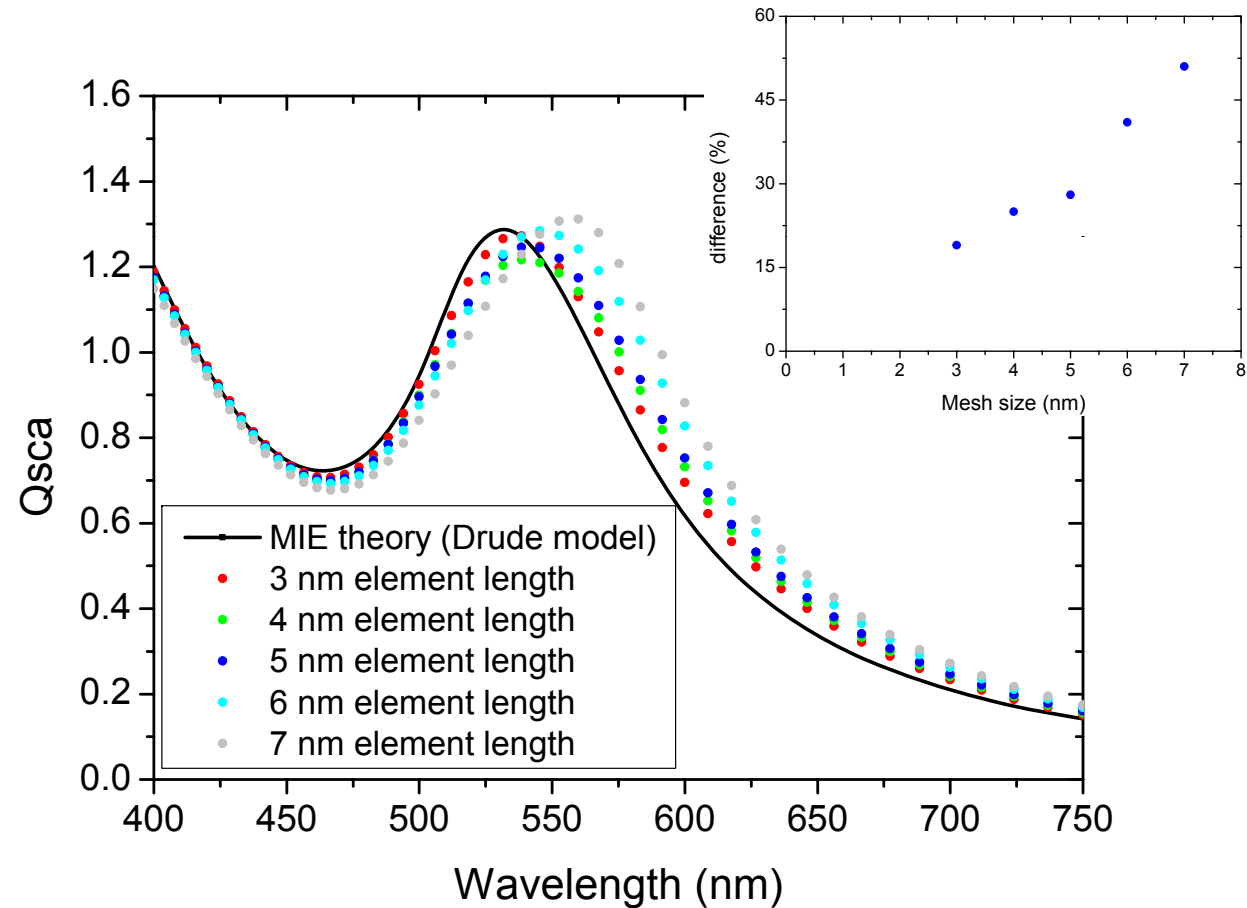
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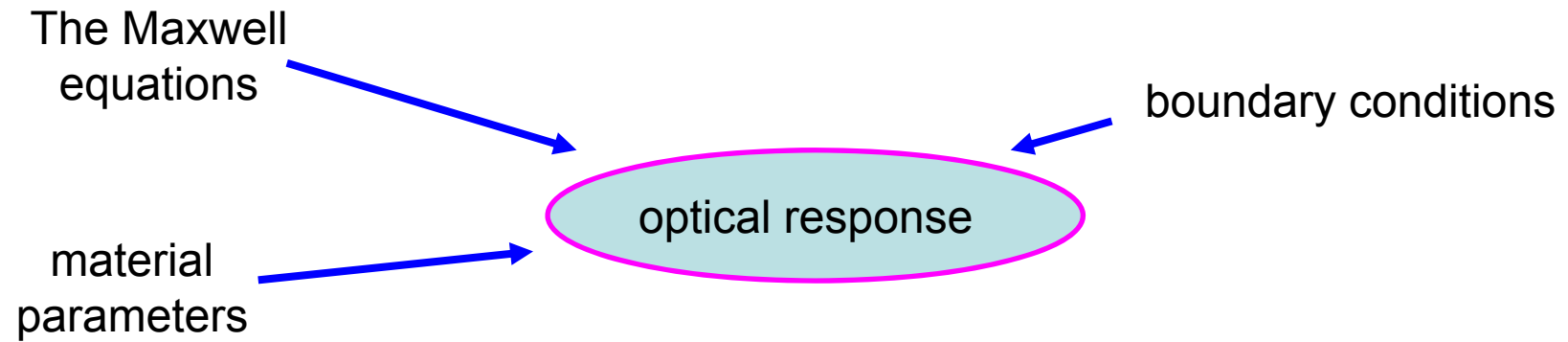
James Parsons

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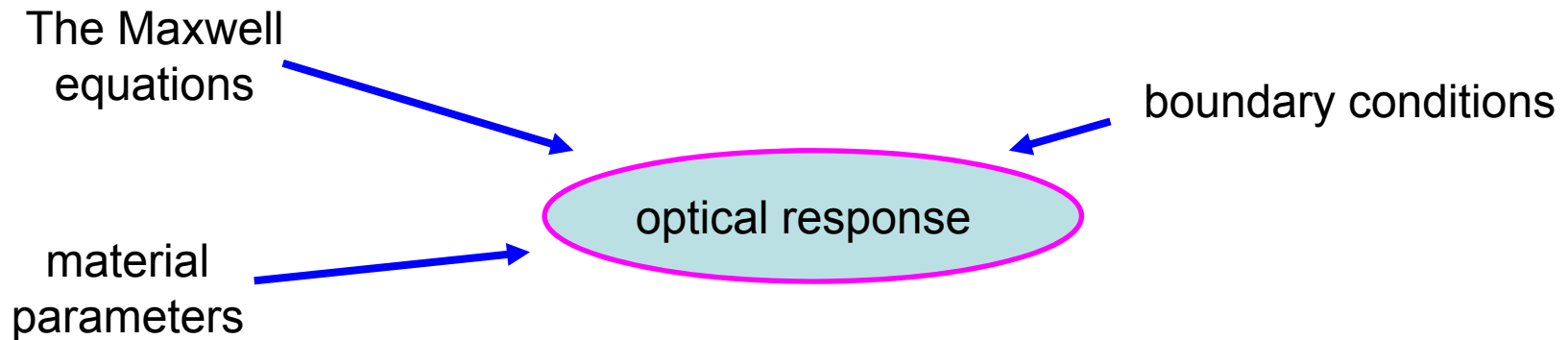


meshing needed at 1 nm level (\ll wavelength)

theory – EM & structured materials



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purpose of model

build understanding, explore physics.... design tools

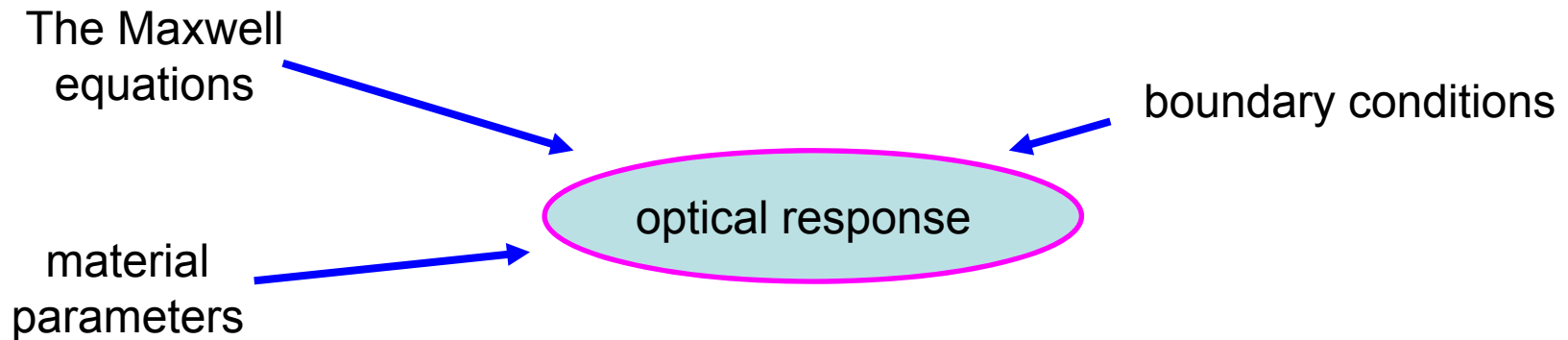
what do we require?

modes, field profiles, field enhancement, LDOS, cross-sections, polarization behaviour...

so what's the problem?

informal survey – (1) relative permittivity, $\epsilon(\omega)$, (2) meshing.

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so what's the problem?

informal survey – (1) relative permittivity, $\epsilon(\omega)$, (2) meshing.

experimental problems

not well enough controlled/specified, contamination, morphology, illumination, internal structure...

models

assumptions/and approximations too restrictive, perfectly periodic structures, bulk $\epsilon(\omega)$

computational approaches

- Mie theory
- Finite difference time domain (FDTD)
- Finite element method (FEM)
- Green's dyadic method
- Boundary element method (BEM)
- Dipole-dipole approximation (DDA)
- Multiple multi-poles (MMP)
- Rigorous coupled wave/Fourier modal method
- Coordinate transformation (Chandezon)
- Effective media
-I wish I could remember!!.....

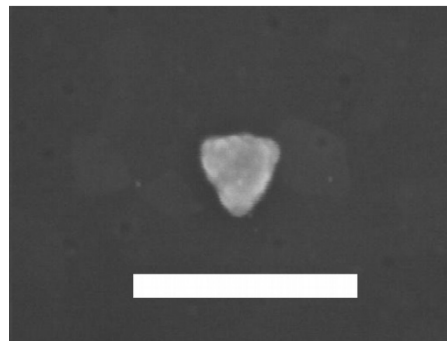
how well do they cope with,

- anisotropy?
- nonlinearity?
- transient behaviour?
- random structures?
-?

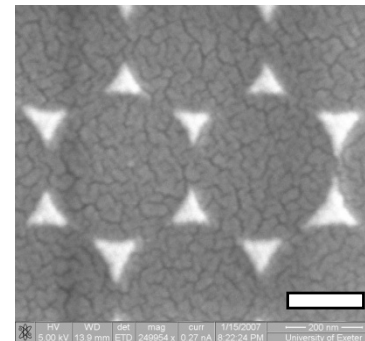
experimental details

fabrication !!!

electron-beam lithography vs. nanosphere lithography



scale bar 300 nm

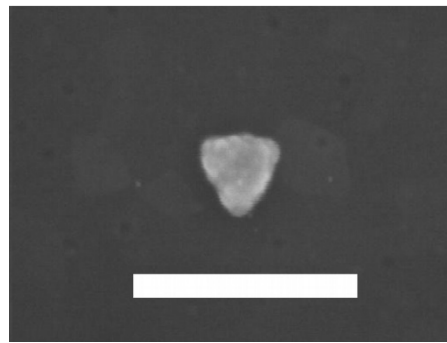


scale bar 200 nm

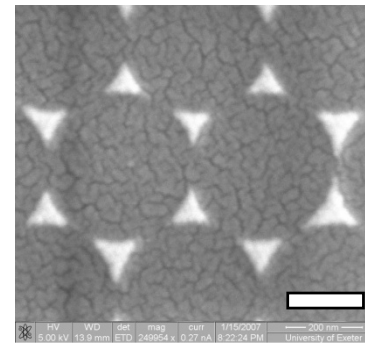
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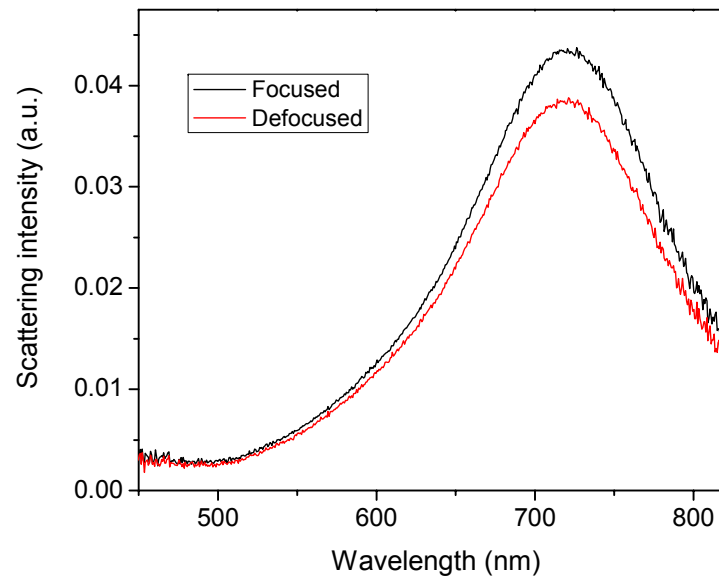


scale bar 300 nm



scale bar 200 nm

focussing!

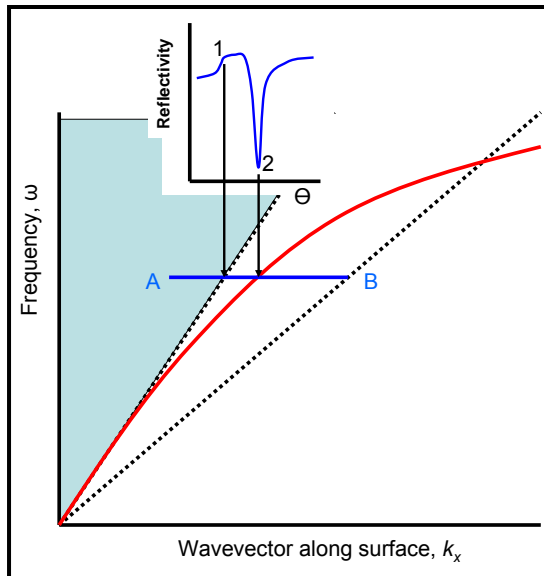
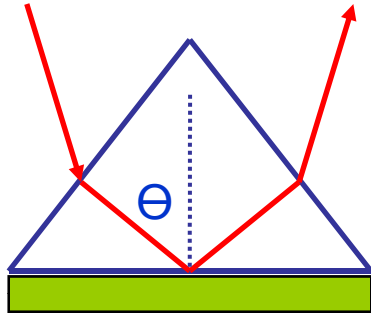


scattered light collected from single gold disc in dark-field

we would like to determine cross-section...

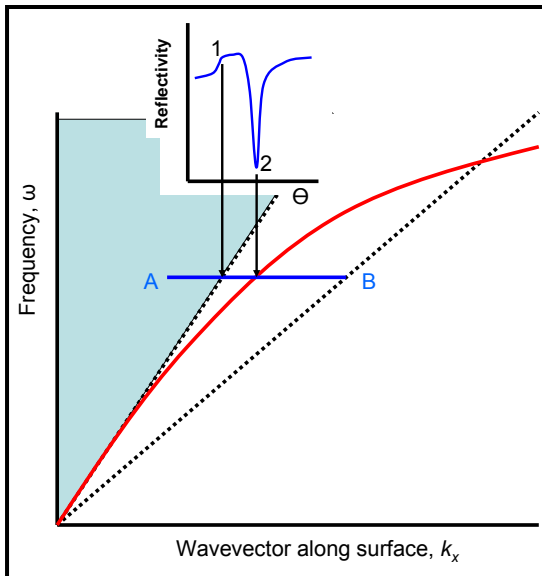
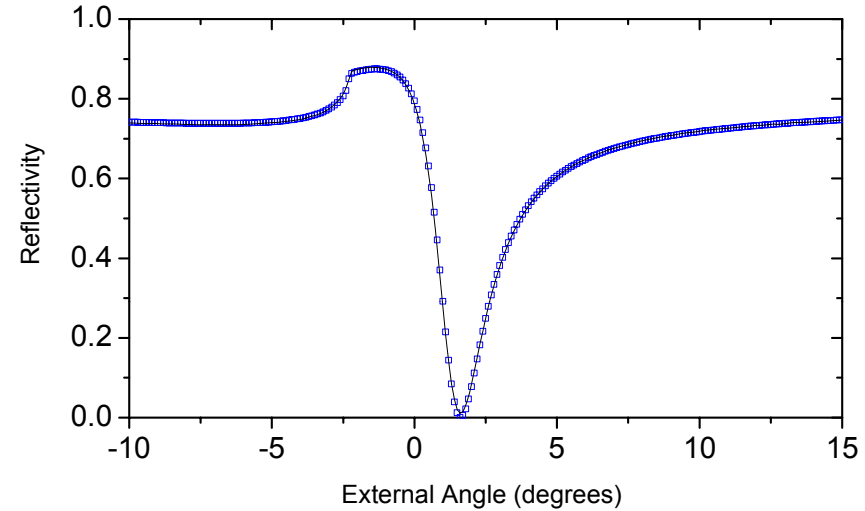
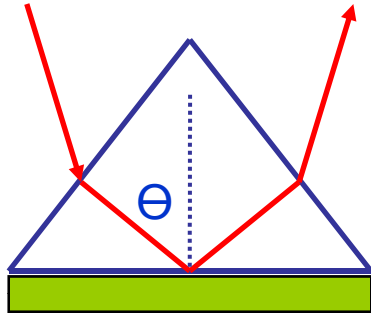
stepping back – planar metal film

surface plasmon-polariton on a planar metal film



stepping back – planar metal film

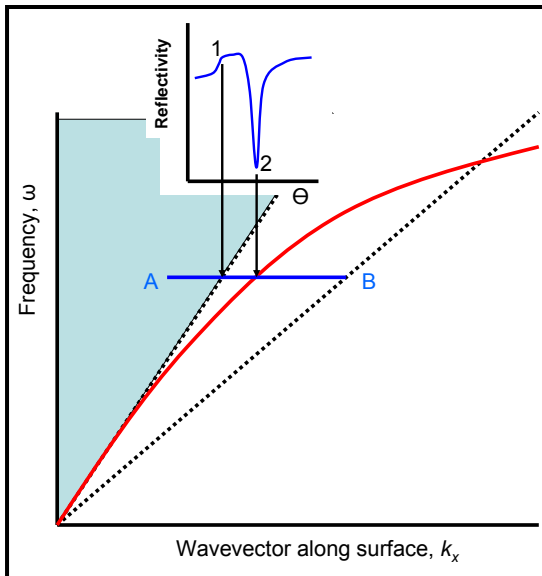
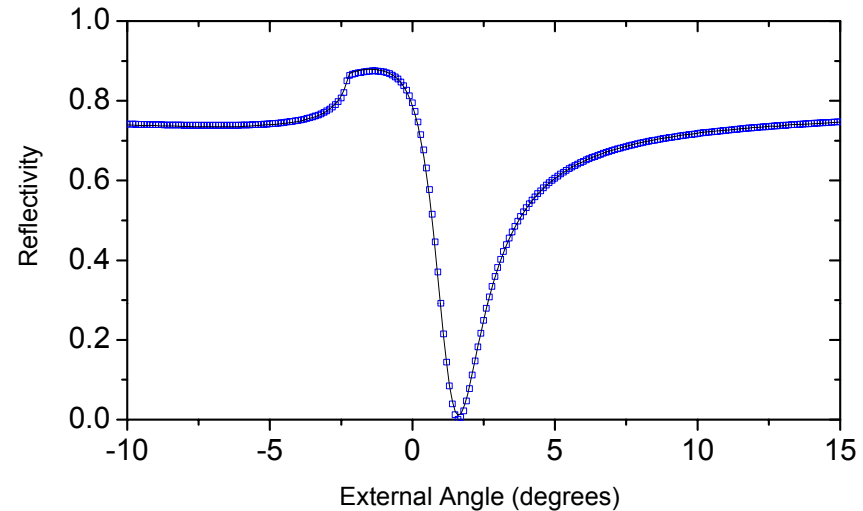
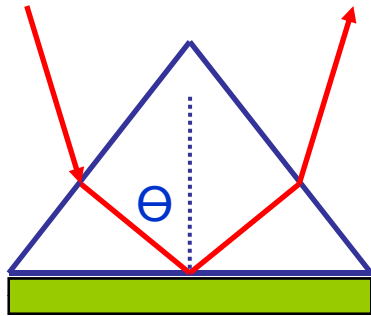
surface plasmon-polariton on a planar metal film



gold film parameters from fit of Fresnel's equations to data
permittivity, $\epsilon = -10.73 (\pm 0.02) + 1.279i (\pm 0.005)$, $d = 47.2 \text{ nm} \pm 0.1$

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gold film parameters from fit of Fresnel's equations to data
permittivity, $\epsilon = -10.73 (\pm 0.02) + 1.279i (\pm 0.005)$, $d = 47.2 \text{ nm} \pm 0.1$

but

Johnson and Christie (PRB 6 4370 (1972))

$\epsilon = -12.3 + \sim 1.2i$

and

Lynch and Huttner, "Handbook of Optical Constants of Solids", (1985), ed. Palik

$\epsilon = -10.4 + 1.4i$

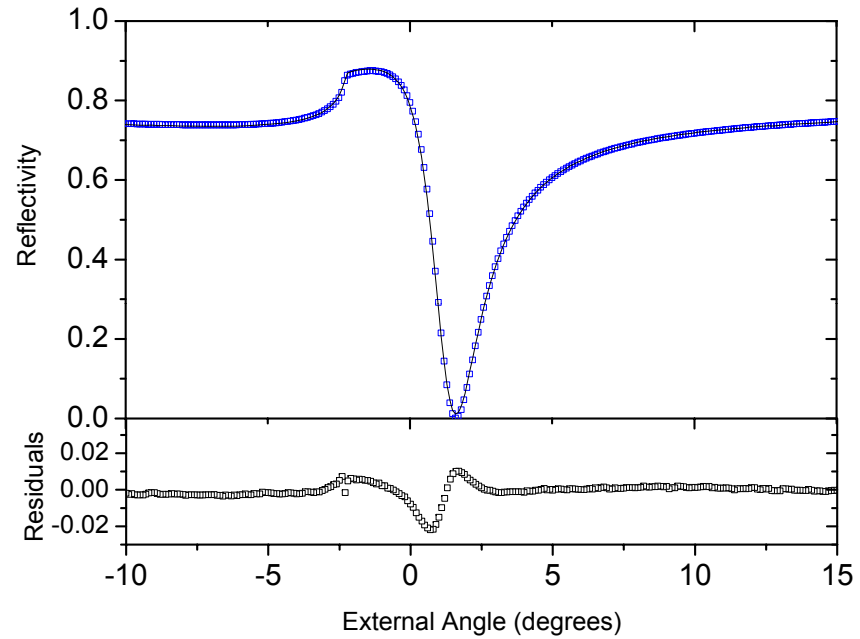
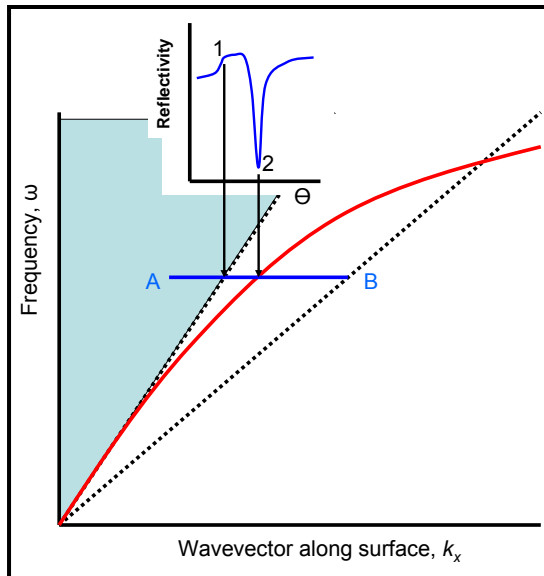
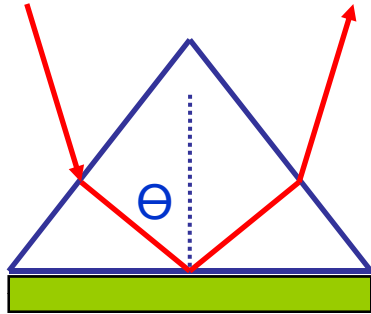
whilst

Innes and Sambles (J Phys F: Met 17 277 (1987))

$\epsilon = -11.8 + 1.36i$

stepping back – planar metal film

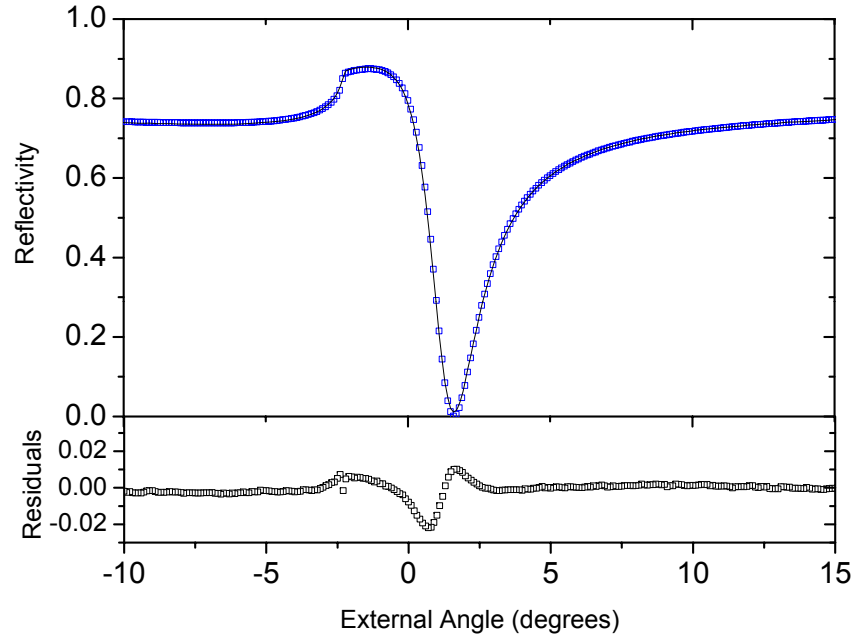
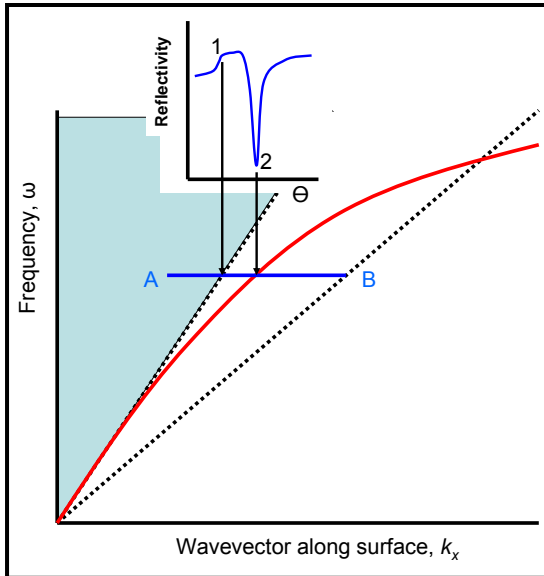
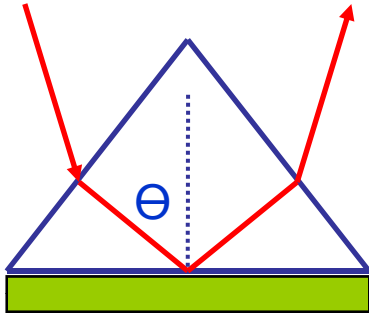
surface plasmon-polariton on a planar metal film



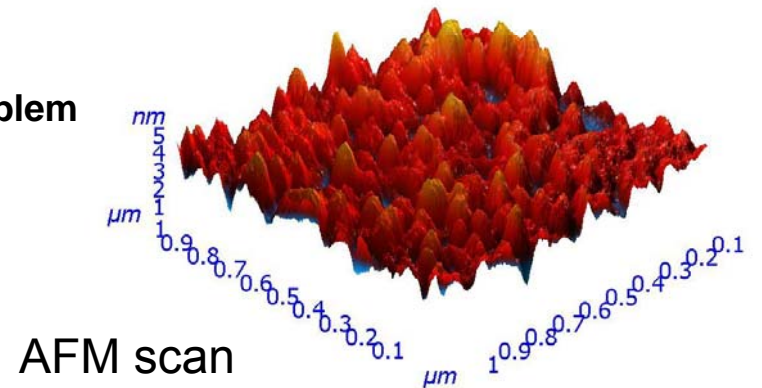
residuals show up a problem
surface roughness?
grain boundaries?

stepping back – planar metal film

surface plasmon-polariton on a planar gold film



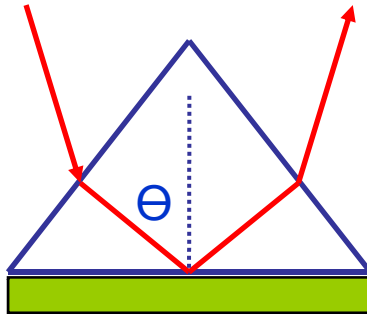
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AFM scan

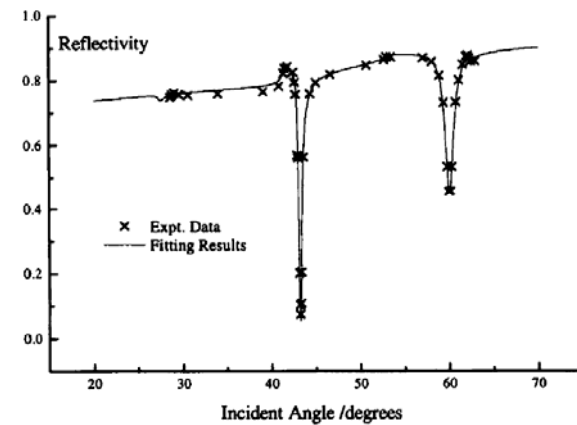
stepping back – planar metal film

...in fact there is an SPP supported by both metal surfaces...



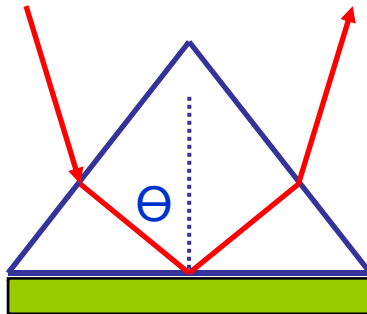
Corrugated film used so as to allow grating coupling to prism-silver SPP

Nash and Sambles (J Mod Opt **46** 1793 (1999))



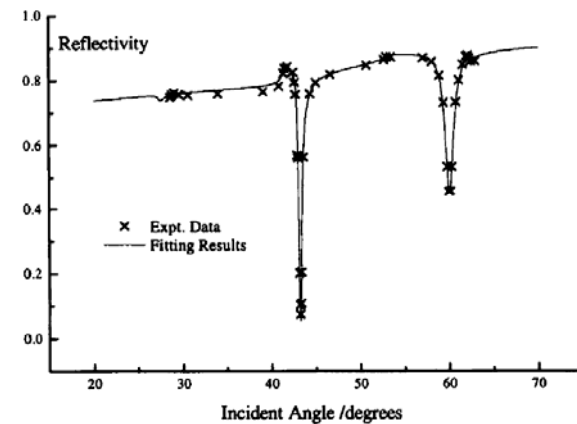
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wavelength 633 nm

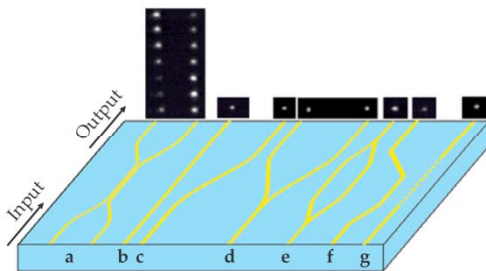
Silver film thickness/nm	Glass/Silver interface		Silver/Air interface		Uncertainties	
	ϵ_r	ϵ_i	ϵ_r	ϵ_i	$\Delta\epsilon_{r,i}$	thickness
31.1	-20.41	0.92	-14.74	0.69	± 0.1	± 1
50.1	-21.06	0.94	-13.85	0.90	± 0.1	± 2
58.6	-20.99	0.79	-15.56	0.58	± 0.1	± 2
76.2	-21.36	0.78	-14.50	0.43	± 0.1	± 4
86.2	-21.01	0.82	-17.02	0.49	± 0.1	± 5
125.3	-20.86	0.79	-17.92	0.49	± 0.1	± 5

even a simple planar film can not be described by just one $\epsilon(\omega)$,

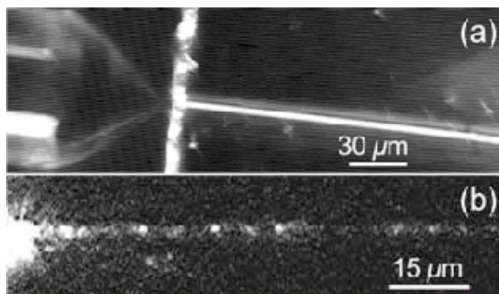
SPP waveguides and roughness



Ebbesen, Genet and Bozhevolnyi

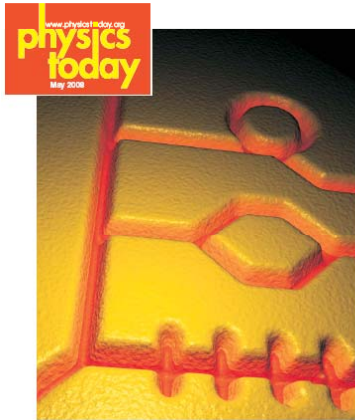


Charbonneau et al. Opt Exp **13** 977 2008



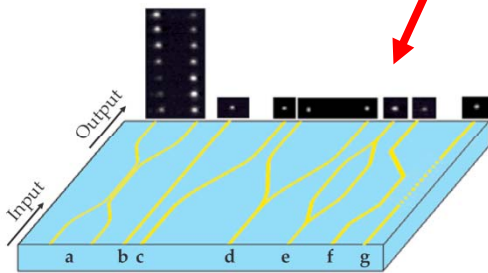
Nielsen et al. Opt Lett **33** 2800 2008

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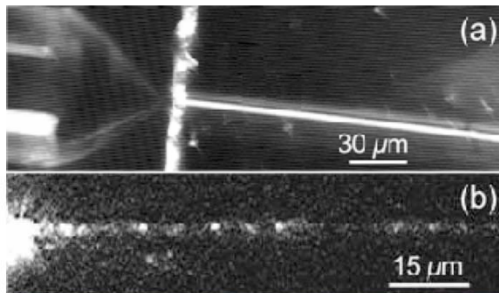


Elements of plasmonics

Ebbesen, Genet and Bozhevolnyi



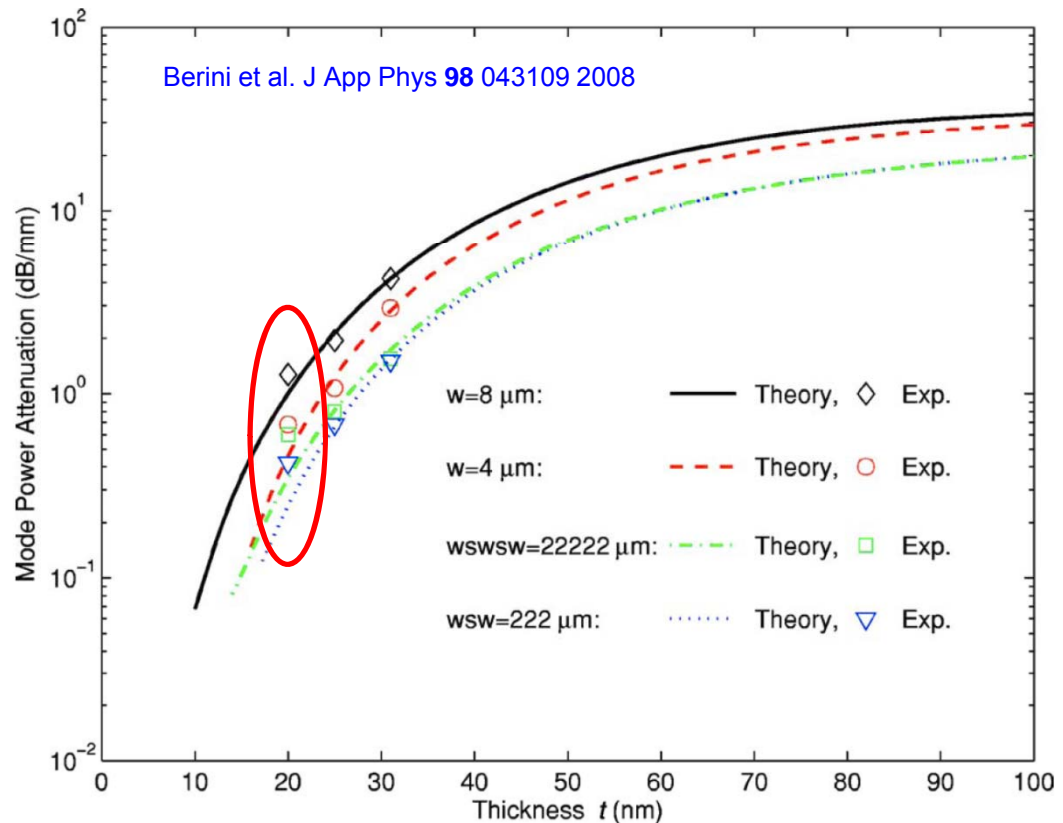
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Nielsen et al. Opt Lett 33 2800 2008

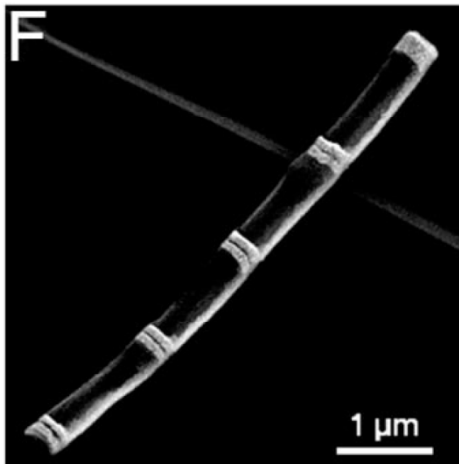
strip waveguides – coupled SPP mode (LRSPP)
loss should fall as thickness of metal reduced but...

roughness and grain boundaries influence attenuation
- not well understood



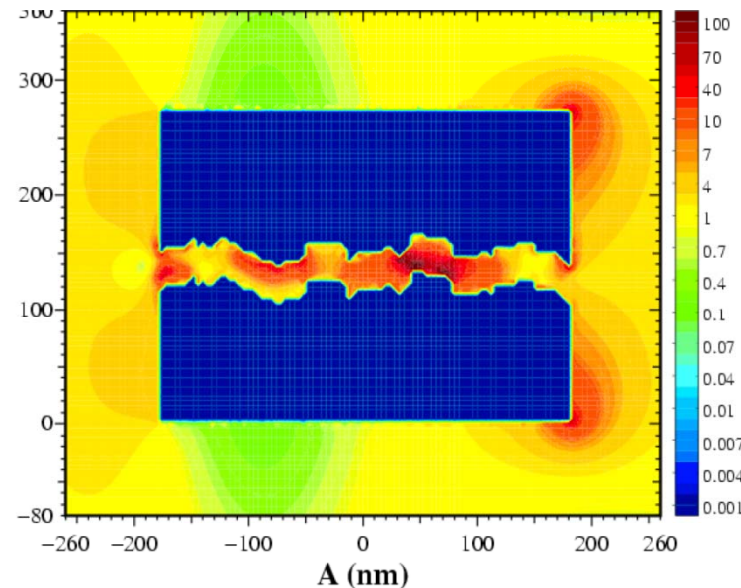
roughness and field enhancement

looking at Raman signal from double disc



Qin et al. (PNAS 103 13300 (2006))

optimum disc-disc spacing 10 nm from DDA calculations
but 30 nm from experiment



and Schatz (MRS Proceedings 2008)

including roughness
– hot spots

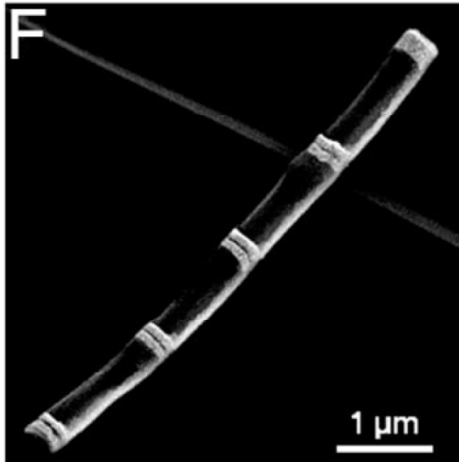
optimum separation is
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$|E|^2$ for gold dimer – 32 nm separation

hot spots may dominate system behaviour!

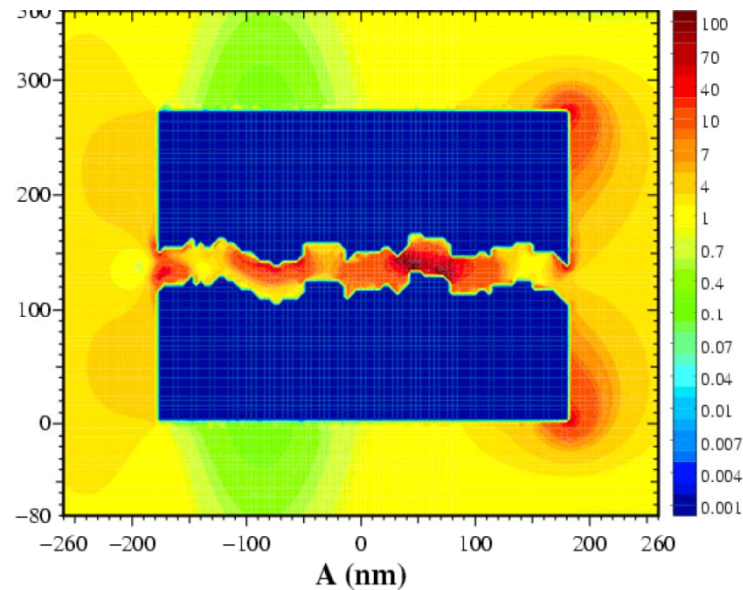
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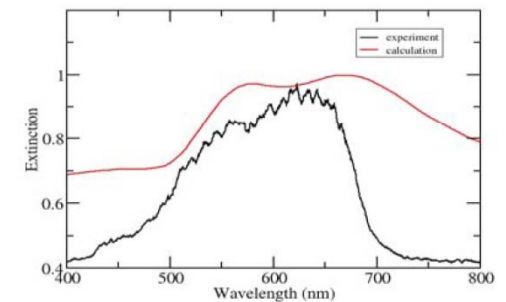
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but extinction spectrum!...



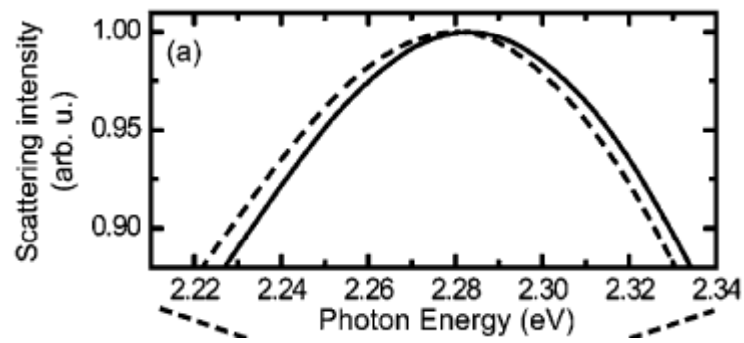
hot spots may dominate system behaviour!

contamination: basis of SPR sensing

Localised Surface Plasmon Resonance (LSPR) of gold and copper nano-triangles

Gold

- sensing presence of bound target molecules



Raschke et al., *Nano Lett.* , **3**, 935 (2003)

- able to detect just a few hundred molecules

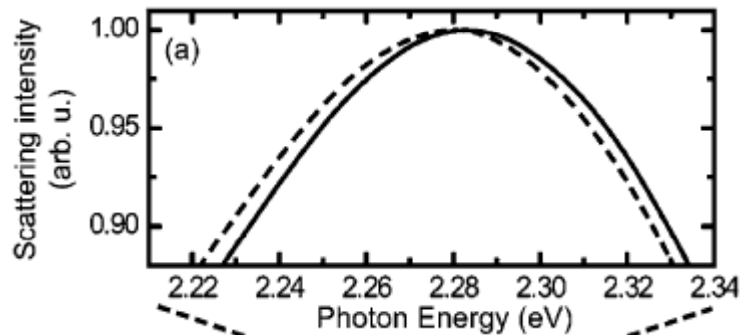
McFarland and van Duyne, *Nano Lett.* , **3**, 1057 (2003)

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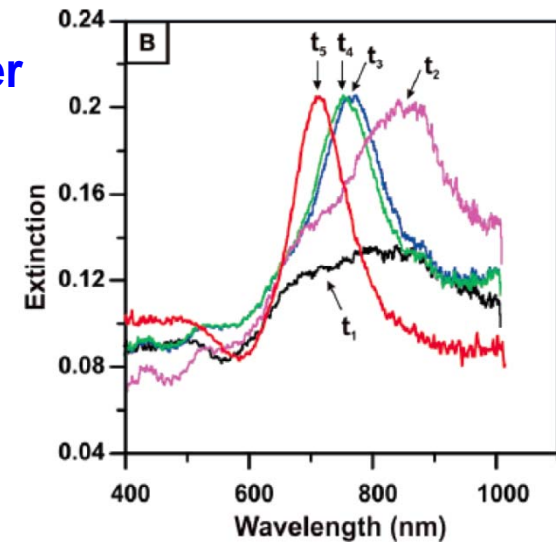
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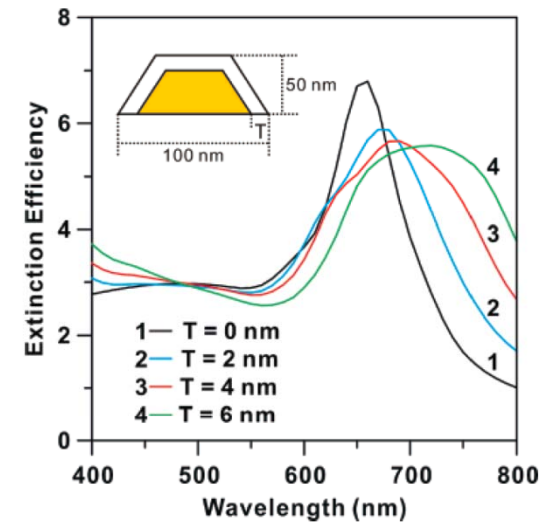
McFarland and van Duyne, Nano Lett. , 3, 1057 (2003)

chemical state of surface important

Copper



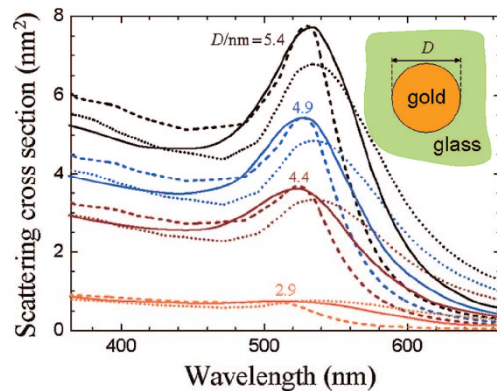
when surface oxide layer is removed,
copper shows good plasmon resonance



Chan et al. Nano Lett. , 7, 1947 (2007)

break down of bulk description

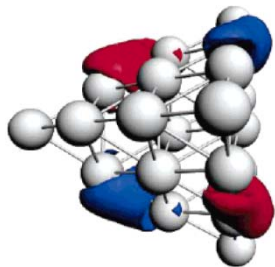
- roughness
- grain boundaries
- surface scattering
- non-local effects ..interface as a selvedge (J. Sipe, Phys Rev B **22**, 1589 (1980))
- down to what length scale can we ignore atomic nature of material?



García de Abajo J Phys Chem C **112** 17983 2008

solid lines: — experiment
analytical finite-size effect: dotted
non-local theory: - - - dashed

- do we need to combine atomic (QM) description and bulk (EM) description?



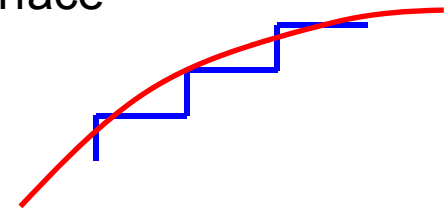
Zhao et al. J Am Chem Soc **128** 2911 2006



density-functional theory used to calculate Raman intensities for pyridine-Ag₂₀ cluster

problems with the mesh

- Optical regime – mesh is needed down to 1 nm scale
- Big mismatch between this mesh size and wavelength ($>10^2$)
- Fields at surface not well represented by staircase surface



....models might be flawed – but do we have experimental control at this level?

we don't have to go to the optical - problems exist at microwave frequencies!

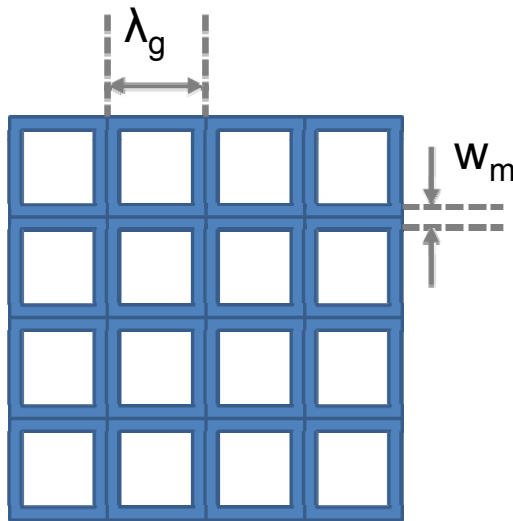
problems with the mesh



Celia Butler

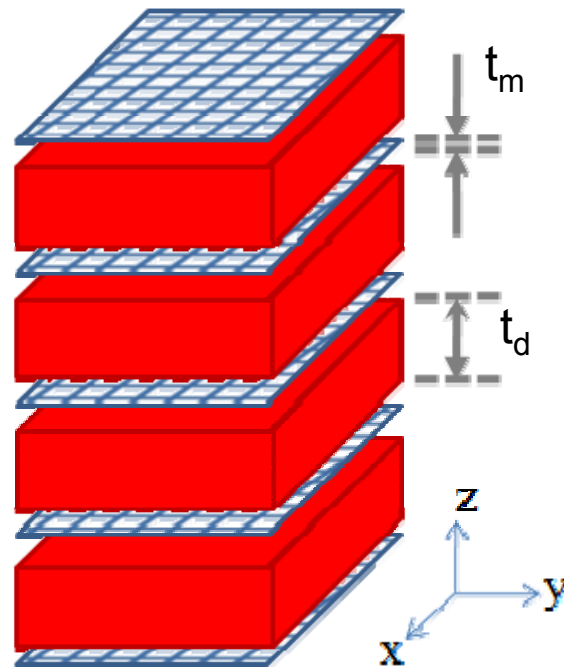
A metal-dielectric stack – the metal being a grid (hole array)

(Butler et al., submitted to PRL May 2009)



the air-filled hole array metamaterial, blue represents copper

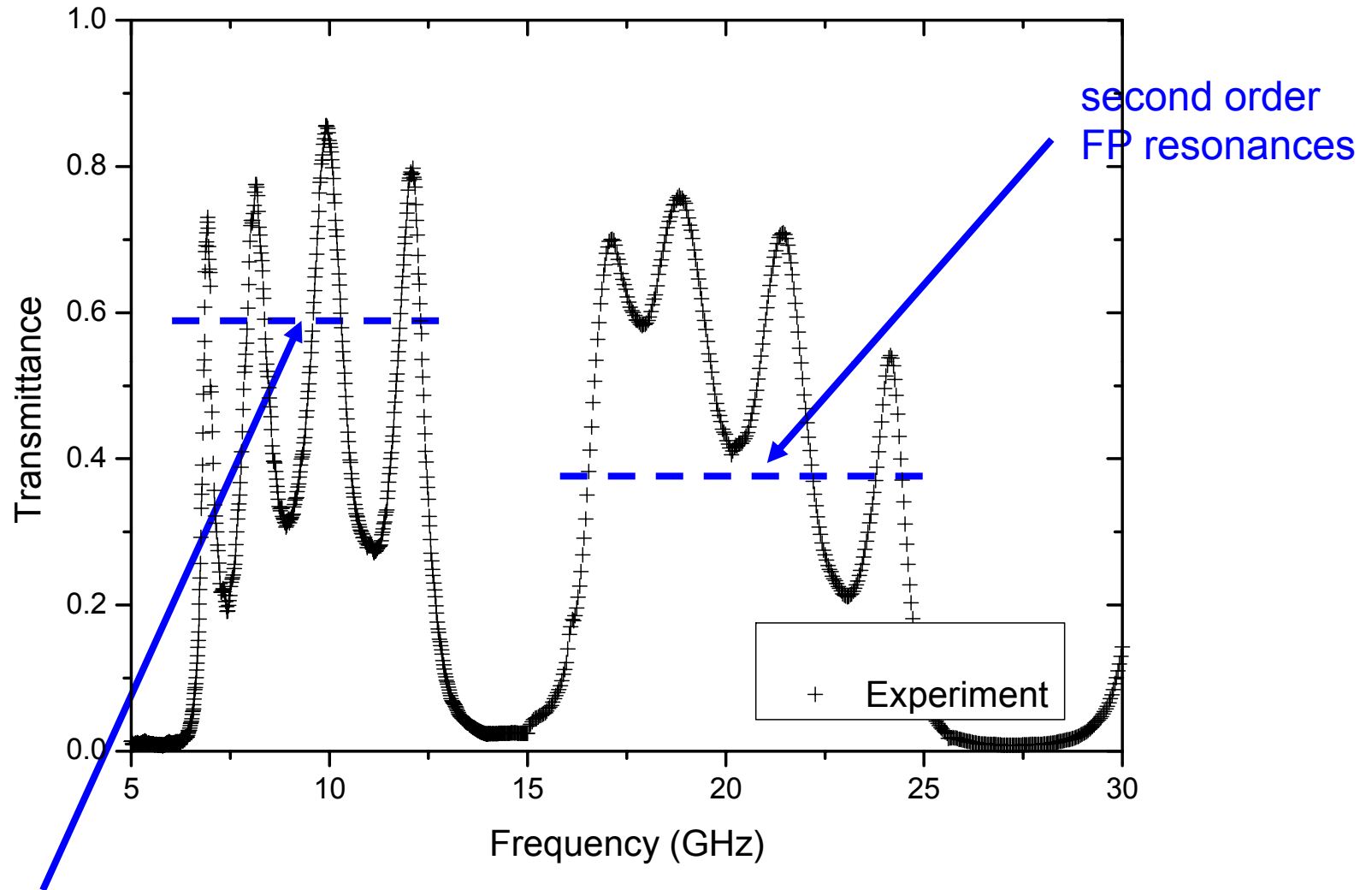
$t_m = 18\mu\text{m}$,
 $\lambda_g = 5\text{mm}$,
 $W_m = 0.2\text{mm}$.



the metamaterial/dielectric stack, where red regions represent the dielectric
 $t_d = 6.35\text{mm}$

- frequency range of interest is 5 GHz – 40 GHz
- equivalent wavelength range is 7.5 mm – 6 cm

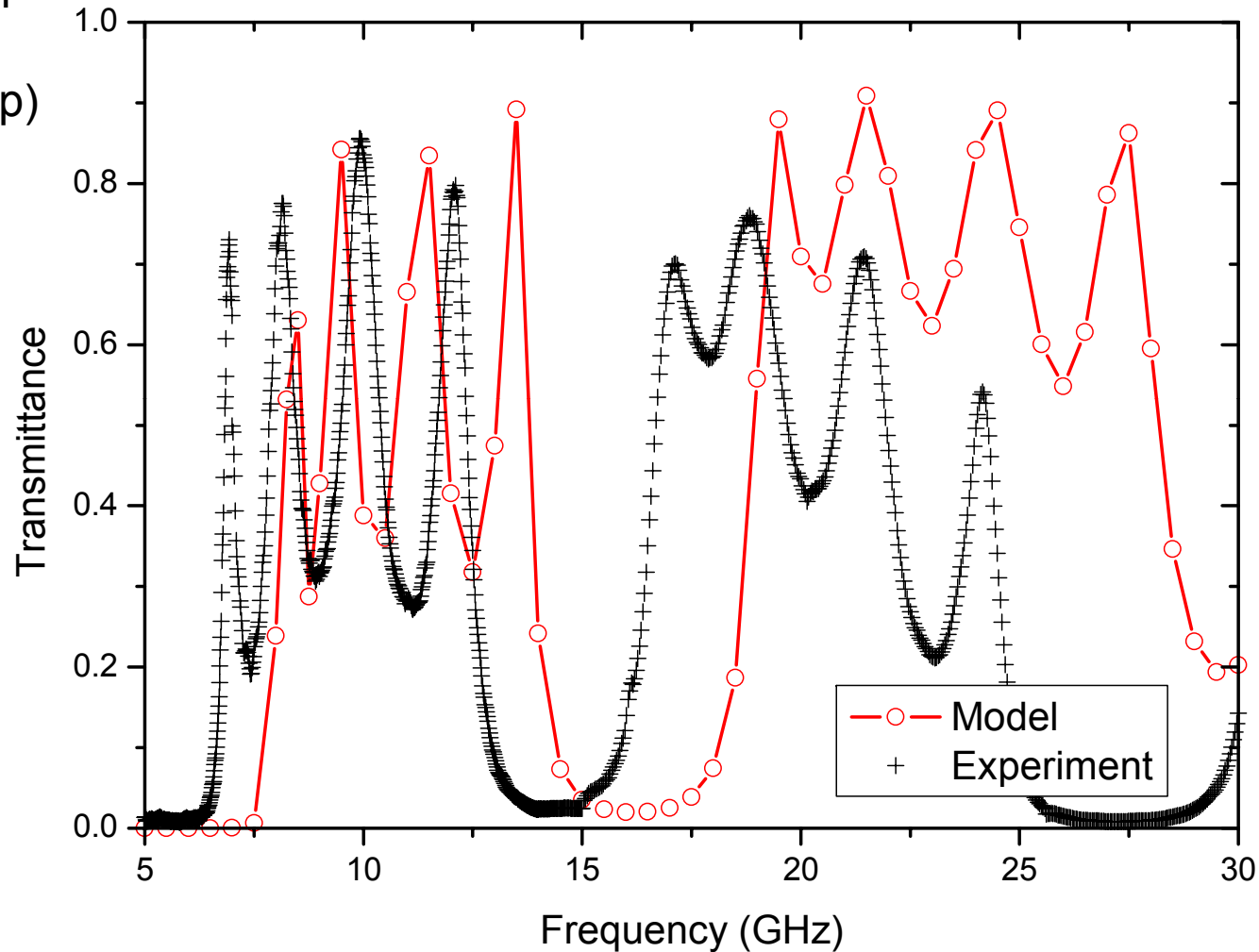
problems with the mesh



first order
FP resonances

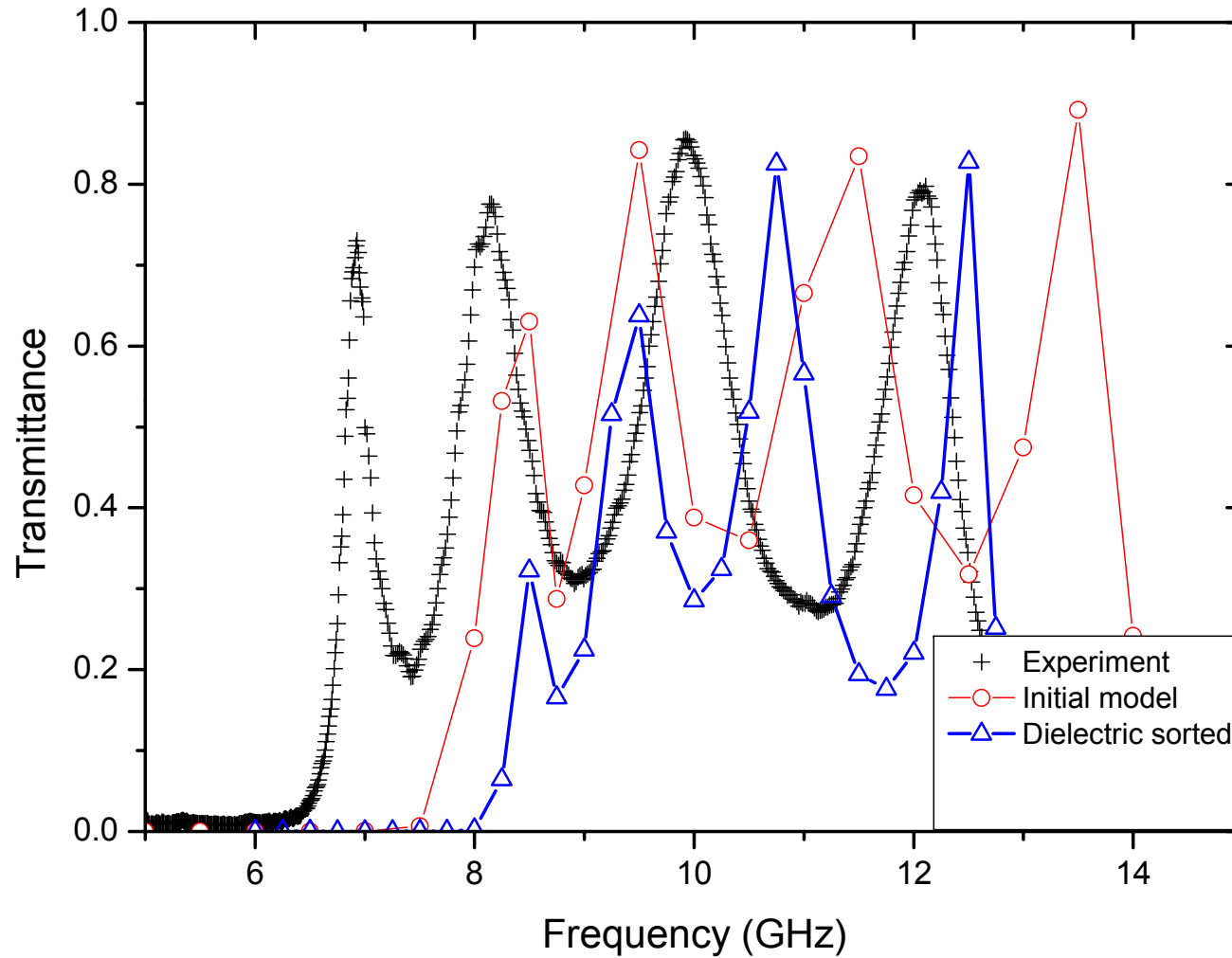
problems with the mesh

FEM model
HFSS
(Ansoft corp)



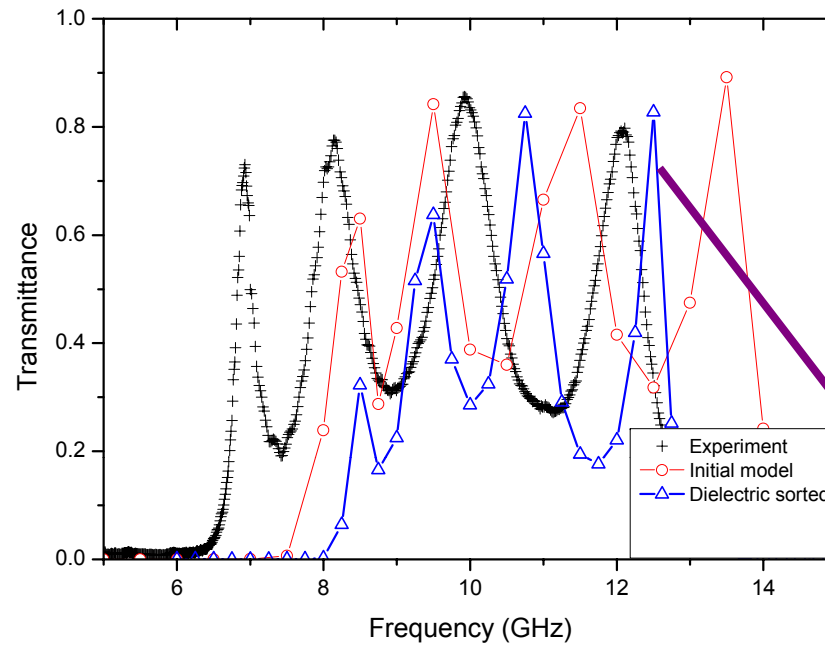
- 10% mismatch in frequency
- looks as though thickness and/or permittivity of spacer is wrong

problems with the mesh



measure permittivity independently $\epsilon = 2.55 + 0.0i \longrightarrow \epsilon = 3.00 + 0.004i$

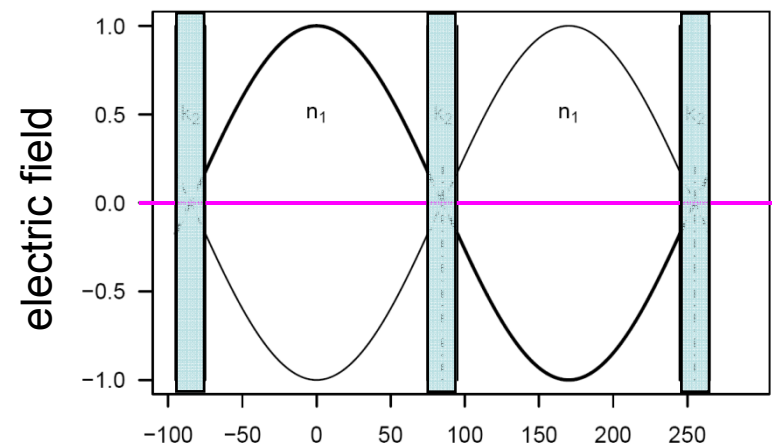
problems with the mesh



Martyn Gadsdon

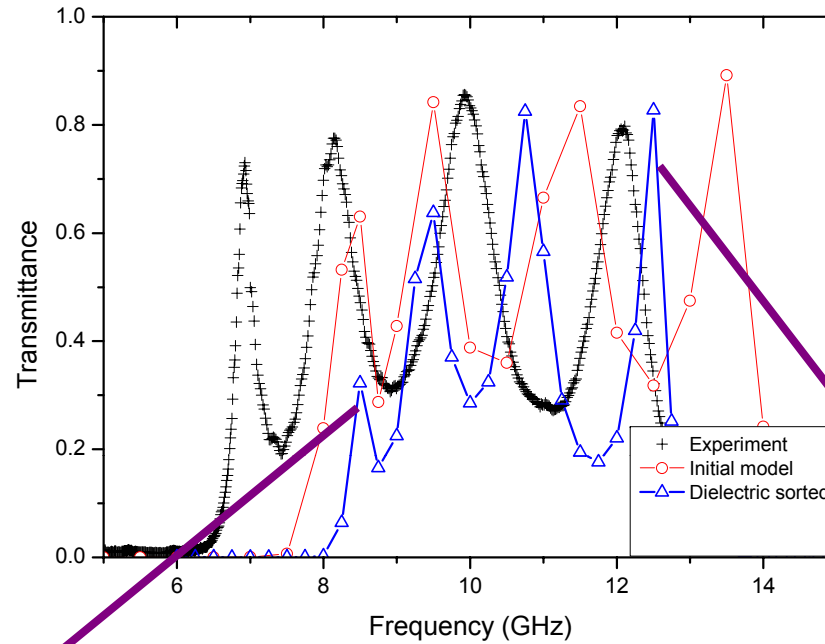
Gadsdon, Parsons and Sambles,
sub to JOSAB (2008)

high-freq solution



cos distribution – little field in metal

problems with the mesh

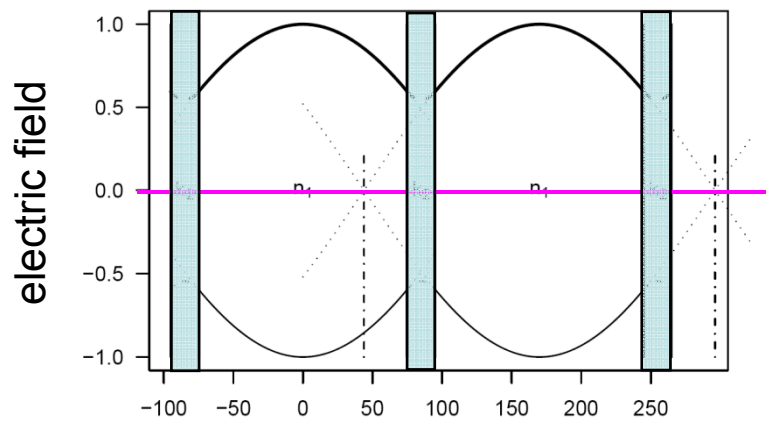


Martyn Gadsdon

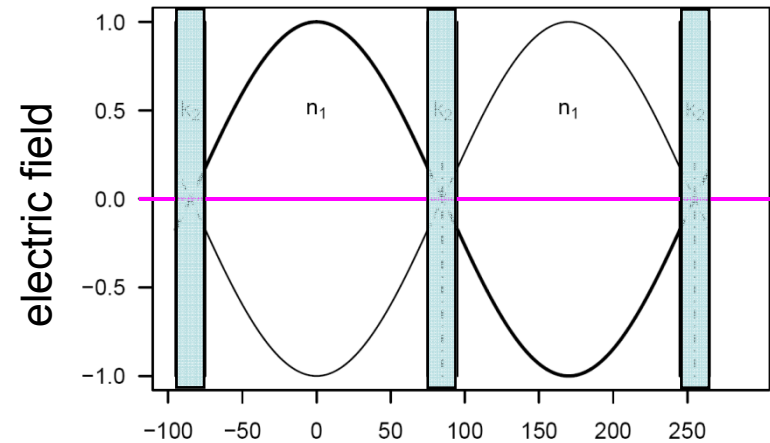
Gadsdon, Parsons and Sambles,
sub to JOSAB (2008)

low-freq solution

high-freq solution

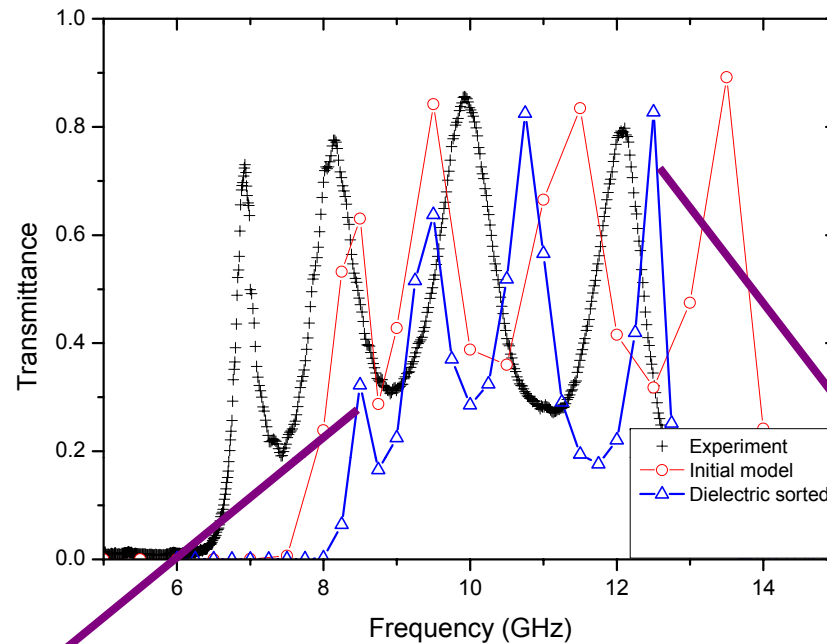


sinh distribution – considerable field in metal



cos distribution – little field in metal

problems with the mesh

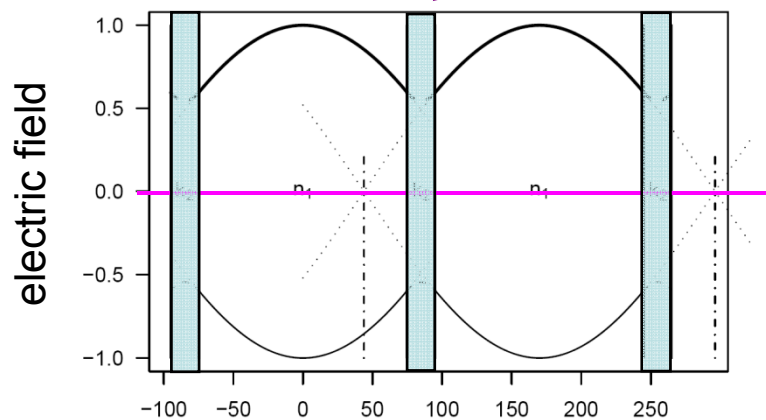


Martyn Gadsdon

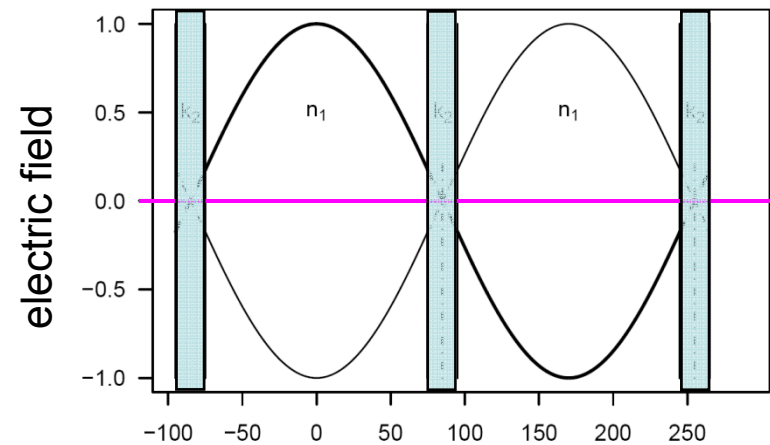
Gadsdon, Parsons and Sambles,
sub to JOSAB (2008)

low-freq solution

high-freq solution



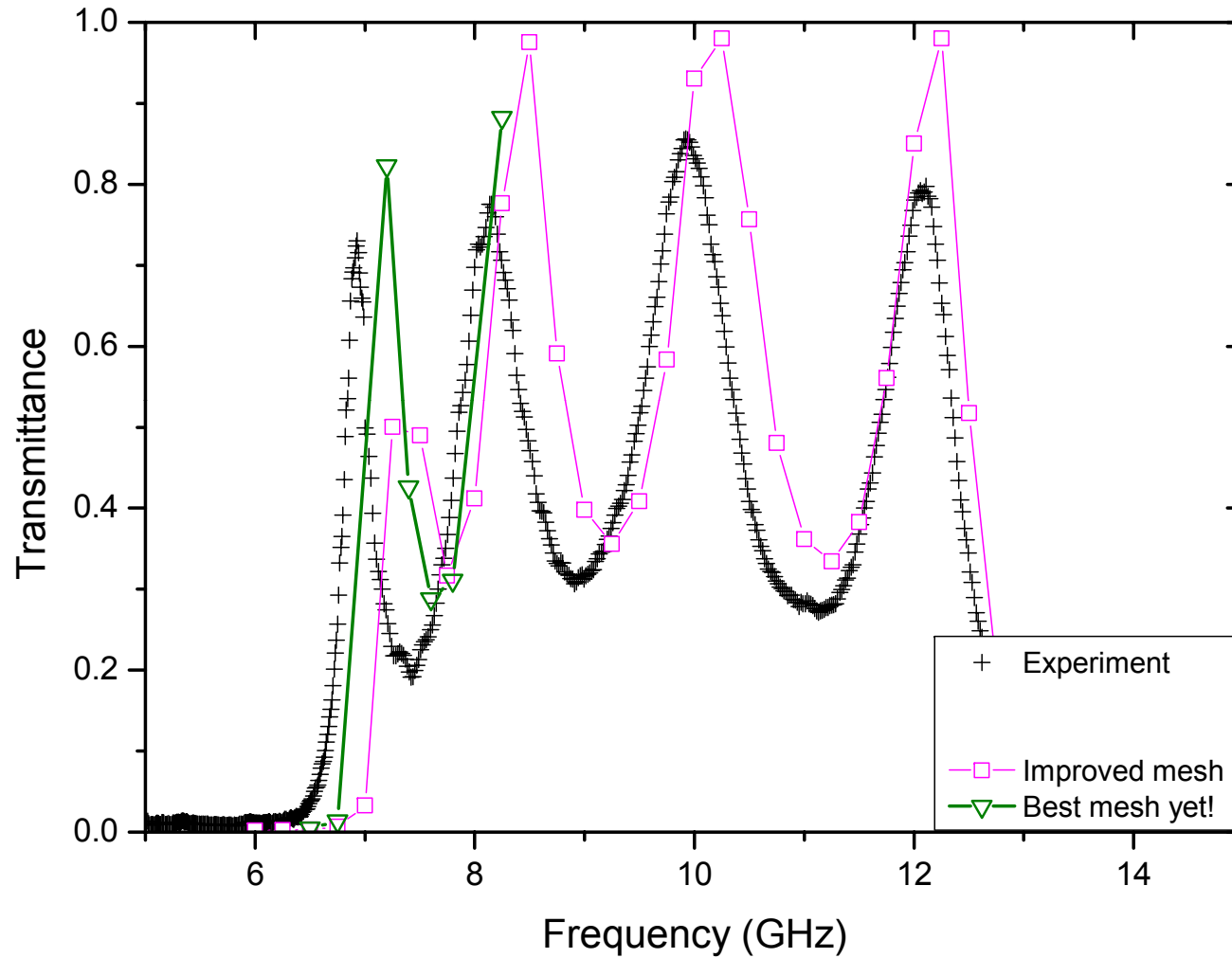
sinh distribution – considerable field in metal



cos distribution – little field in metal

meshing more important for low-freq modes

problems with the mesh



Skin depth in Copper at ~ GHz is 1 micron, $10^{-4} \times$ wavelength

where does this leave us?



- **experimental**: situation far from being well defined or under control
- mixture of **analytic and computational** approaches is essential – lots of good theory and models already available but.....
- **provided bulk description of matter valid**, equations are well known and problems are computational intensity and boundary conditions (morphology etc. – hard to specify problem well enough (random structures?))
- **validation** – quantitative agreement still difficult e.g. cross sections, range of validity

New Physics?

- **non-linearity** (esp. of metal) – CARS, TPL...
- **Atomic scale/quantum effects** (break down of bulk description)
- inclusion of **gain media**

Questions & Answers

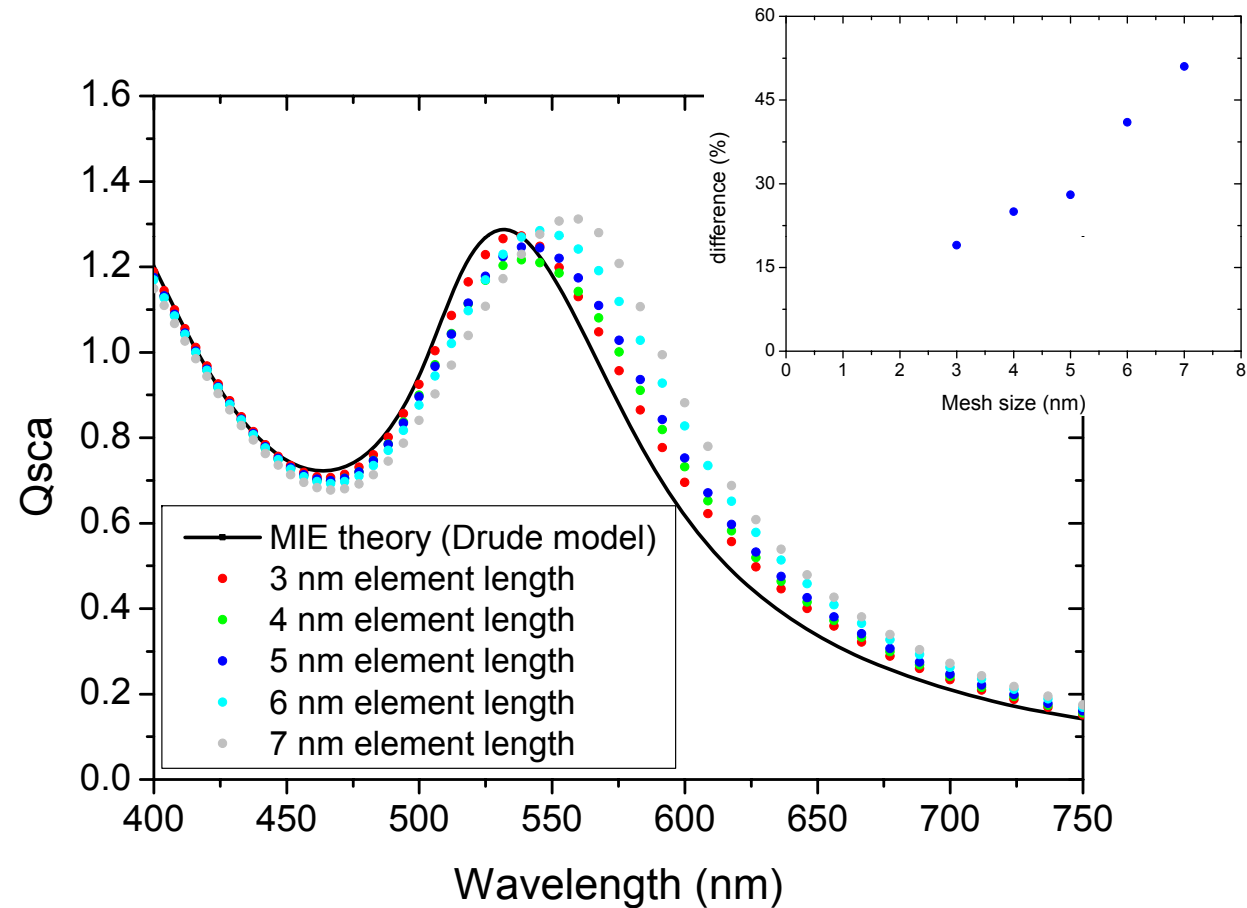
a simple problem



James Parsons

Scattering of light by a metallic sphere in vacuum: comparison of techniques

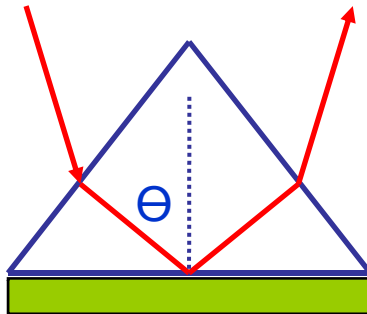
FDTD approach – effect of mesh size



meshing needed at 1 nm level (\ll wavelength)

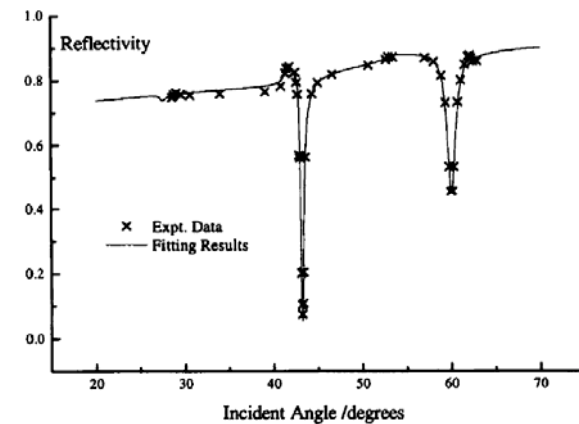
stepping back – planar metal film

...in fact there is an SPP supported by both metal surfaces...



Corrugated film used so as to allow grating coupling to prism-silver SPP

Nash and Sambles (J Mod Opt 46 1793 (1999))



wavelength 633 nm

Silver film thickness/nm	Glass/Silver interface		Silver/Air interface		Uncertainties	
	ϵ_r	ϵ_i	ϵ_r	ϵ_i	$\Delta\epsilon_{r,i}$	thickness
31.1	-20.41	0.92	-14.74	0.69	± 0.1	± 1
50.1	-21.06	0.94	-13.85	0.90	± 0.1	± 2
58.6	-20.99	0.79	-15.56	0.58	± 0.1	± 2
76.2	-21.36	0.78	-14.50	0.43	± 0.1	± 4
86.2	-21.01	0.82	-17.02	0.49	± 0.1	± 5
125.3	-20.86	0.79	-17.92	0.49	± 0.1	± 5

even a simple planar film can not be described by just one $\epsilon(\omega)$,