Useful Results

Basic equations of coherent transport

$$\Gamma_{1} = i[\Sigma_{1} - \Sigma_{1}^{+}], \Gamma_{2} = i[\Sigma_{2} - \Sigma_{2}^{+}]$$

$$G(E) = [EI - H - \Sigma_{1} - \Sigma_{2}]^{-1},$$

$$A(E) = i[G - G^{+}] = G\Gamma_{1}G^{+} + G\Gamma_{2}G^{+}$$

$$I(E) = [G\Gamma_{1}G^{+}] f_{1} + [G\Gamma_{2}G^{+}] f_{2}$$

$$Electron \ density$$

$$I_{i}(E) = (q/h) \ ((Trace[\Gamma_{i}A])f_{i} - Trace[\Gamma_{i}G^{*}]) \ Current/energy$$

$$I(E) = (q/h) \ Trace[\Gamma_{1}G\Gamma_{2}G^{+}](f_{1}(E) - f_{2}(E))$$

$$2-terminal \ current$$

Simpler version
$$n(E) = D(E) \frac{\gamma_1 f_1(E) + \gamma_2 f_2(E)}{\gamma_1 + \gamma_2}$$
 Electron density
 $I_i(E) = (q \gamma_i / \hbar) (D(E) f_i(E) - n(E))$ Current/energy
 $I(E) = \frac{q}{\hbar} \frac{\gamma_1 \gamma_2}{\gamma_1 + \gamma_2} D(E) (f_1(E) - f_2(E))$ 2-terminal current

Ballistic transport: $\gamma_1 = \gamma_2 = \hbar v_x/L$. In diffusive regime $dI^+/dx = dI^-/dx = -I/mfp$, leading to a reduction in the current $I = I^+ - I^-$ by a factor mfp/(mfp+L). In general H has to be replaced with H+U, and D(E) with D(E-U) where U has to be calculated self-consistently from an appropriate "Poisson"-like equation.

Other useful relations: $f(E) = \frac{1}{1 + \exp(E - \mu)/kT}$ Fermi function $P_{\alpha} = (1/Z) \exp(-(E_{\alpha} - \mu N_{\alpha})/kT)$ Law of equilibrium

$$[h(\vec{k})] = \sum_{m} [H_{sm}] \exp(i\vec{k}.(\vec{d}_{m} - \vec{d}_{s})) \quad Bandstructure$$
$$D(E) = \sum_{\vec{k}} \delta(E - \varepsilon(\vec{k})) \qquad Density \text{ of states}$$
$$M(E) = \sum_{\vec{k}} \delta(E - \varepsilon(\vec{k})) \frac{\pi \hbar \left| v_{s}(\vec{k}) \right|}{L} \quad Density \text{ of modes}$$